

Affine Cipher

Substitution Cipher

①

Encryption process

$$E(x) = (ax + b) \bmod m$$

$E(x)$ → Encrypted letter

x → position of plaintext letter in alphabet

a → Key₁ and b → Key₂

m → size of Alphabet.

HELLO → message ; Key → $a=5, b=8$

H → 7 → $(5(7) + 8) \bmod 26 \rightarrow 43 \bmod 26 \rightarrow 17 \rightarrow R$

E → 4 → $(5(4) + 8) \bmod 26 \rightarrow 28 \bmod 26 \rightarrow 2 \rightarrow C$

L → 11 → $(5(11) + 8) \bmod 26 \rightarrow 63 \bmod 26 \rightarrow 11 \rightarrow L$

L → 11 → $(5(11) + 8) \bmod 26 \rightarrow 63 \bmod 26 \rightarrow 11 \rightarrow L$

O → 14 → $(5(14) + 8) \bmod 26 \rightarrow 78 \bmod 26 \rightarrow 0 \rightarrow A$

RCLLA → Encrypted message

Decryption Process: (Affine cipher)

②

$$D(x) = a^{-1}(x-b) \bmod 26$$

$a^{-1} \rightarrow$ Multiplicative inverse of $a \bmod 26$

$RCLLA \rightarrow$ Message Key $\rightarrow a=5, b=8$

Multiplicative inverse of 5 mod 26 is 21

$$R \rightarrow 17 \rightarrow 21(17-8) \bmod 26 \rightarrow 21(9) \bmod 26 \rightarrow 7$$

$$C \rightarrow 2 \rightarrow 21(2-8) \bmod 26 \rightarrow 21(-6) \bmod 26 \rightarrow 4$$

$$L \rightarrow 11 \rightarrow 21(11-8) \bmod 26 \rightarrow 21(3) \bmod 26 \rightarrow 11$$

$$L \rightarrow 11 \rightarrow 21(11-8) \bmod 26 \rightarrow 21(3) \bmod 26 \rightarrow 11$$

$$A \rightarrow 0 \rightarrow 21(0-8) \bmod 26 \rightarrow 21(-8) \bmod 26 \rightarrow 14$$

$$7 \rightarrow H$$

$$4 \rightarrow E$$

$$11 \rightarrow L$$

$$11 \rightarrow L$$

$$14 \rightarrow O$$

HELLO \rightarrow Decrypted Message