

# Analysis and Prediction of COVID-19 Pandemic in India

Narayana Darapaneni

*Director - AIML**Great Learning/Northwestern**University**Illinois, USA**darapaneni@gmail.com*

Praphul Jain

*Student - AIML**Great Learning**Gurgoan, India**praphuljain.iitd@gmail.com*

Rohit Khattar

*Student - AIML**Great Learning**Gurgoan, India**rkhattar@gmail.com*

Manish Chawla

*Student - AIML**Great Learning**Gurgoan, India**manish.k.chawla@gmail.com*

Rijy Vaish

*Student - AIML**Great Learning**Gurgoan, India**rijuvaish@gmail.com*

Anwesh Reddy Paduri

*Research Assistant - AIML**Great Learning**Gurgoan, India**anwesh@greatlearning.in*

**Abstract:** In this paper, we have analysed the COVID-19 progression in India and the three most affected Indian states (viz. Maharashtra, Tamil Nadu and Andhra Pradesh) as of 29-Aug-20 and developed a prediction model to forecast the behaviour of COVID-19 spread in the future months. We used time series data for India and applied the Susceptible-Infective-Removed (SIR) model and the FbProphet model to predict the peak infectives and peak infective date for India and the three most affected states. In this paper, we further performed the comparative analysis of the prediction results from SIR and FbProphet models. From this study, we concluded that with the assumption that a total 5% of India's population might be infected by the pandemic, the countrywide spread is forecasted to reach its peak by the end of Nov-20. And till the time there is no vaccination, for the states that have already reached their peak and with festivals around the corner, there are high chances of resurgence in the number of cases if the social distancing and other control measures are not followed diligently in the coming months.

**Keywords —** COVID-19, SARS-CoV-2, Coronavirus, SIR model, FbProphet model, India

## I. INTRODUCTION

The Coronavirus disease 2019 (COVID-19) was declared as a global pandemic by World Health Organization (WHO) on 11-Mar-20. [1] The disease has severely impacted globally across 188 countries and territories, with the confirmed cases count reaching 24.7 million. [2] The disease was first detected in India on 30-Jan-20 and currently it has third highest number of confirmed cases globally after the United States and Brazil. As of 29-Aug-20, the total (cumulative) count of confirmed infected population is 3,463,972 across India. [3] A total of 62,550 deaths have been reported while 2,648,998 people have recovered. Active cases stand at 752,424.

In the SIR model,  $R_0$  is the basic reproduction number. It is the expected count of secondary cases produced by a single infection in an entirely susceptible population.  $R_0$  helps in determining if an emerging disease can spread in a population. Bhoomika and Vishesh [4] built the SIR model to predict the endpoint of the pandemic in India and three states - Maharashtra, Gujarat and Delhi. The results show that the endpoint in India will be reached on 12-Sep-20, while endpoints in Delhi, Gujarat and Maharashtra will be reached on 20-Aug-20, 30-Jul-20 and 9-Sep-20 respectively. Liu et al. [5] performed studies and calculated the  $R_0$  of COVID-19 in China and came up

with a  $R_0$  value of 4.2 from studies using mathematical modelling, and a  $R_0$  value of 2.67 from studies using statistical methods. The values from both these studies were higher than the one predicted by the WHO (1.95). Zhao et al. [6] estimated the  $R_0$  at 2.1 for the Diamond Princess cruise ship using the Poisson process approach. Tindale et al. [7] estimated 1.97 as the value for  $R_0$  for Singapore and 1.87 for Tianjin, China.

Pandey et al. [8] used the SEIR and regression models for studying the COVID-19 growth in India over a two weeks' period. They observed that the results for the regression model were higher by 15.7% as compared to the SEIR model. Dhanwant and Ramanathan [9] and Sardar et al. [10] predicted the progress of COVID-19 using the SIR model during the first 21-day lockdown, and concluded that only social distancing will not help to contain the spread of COVID-19 if the lockdown were to be lifted after 21 days. Poonia and Azad [11] analyzed the state wise growth of COVID-19 in India and identified the regions where relaxation of the restrictions might be possible post-April-20. Peipei et al. [12] applied the Logistic model to predict the epidemic trend, and then used the predicted values into FbProphet model to derive the epidemic curve. As per their estimations, the disease will peak in Oct-20 with an infected population of 14.12 million.

## II. MATERIALS AND METHODS

We have used two different models

### A. The Susceptible-Infective-Removed (SIR) Model

The SIR model divides the total population( $N$ ) into three compartments: Susceptibles ( $S$ ): The potential population having the disease, Infectives( $I$ ): The population currently having the disease and could infect the others, and Removed( $R$ ): The people who have already caught the disease and either have recovered from it or have died.

Like all mathematical models, here we have to make various assumptions to simplify the real-world phenomenon. First, the epidemic is sufficiently short and does not last that long and the total population( $N$ ) remains constant. The births and deaths (excluding the COVID-19 deaths) can be ignored. Second, the rate of increase in the Infectives( $I$ ) is proportional to the contact between Susceptible( $S$ ) and Infectives( $I$ ). And third, the rate of increase in the Removed ( $R$ ) is proportional to the number of infectives( $I$ ).

Hence,  $S + I + R = S_0 + I_0 + R_0$ .

#### *Equations which govern the model:*

New infections arise due to the contact between susceptible and infective population. As per the second assumption,  $\beta SI$  is the rate of occurrence of new infections for some positive constant  $\beta$ . With the occurrence of new infection, the infected individual moves from the susceptible compartment to infective compartment. Therefore,

$$dS/dt = -\beta SI \quad (1)$$

The other scenario is when infective individuals enter the removed compartment. The assumption is that  $\gamma I$  is the rate of change of Infectives (I) for some positive constant  $\gamma$  which gives us other differential equations.

$$dI/dt = \beta SI - \gamma I \quad (2)$$

$$dR/dt = \gamma I \quad (3)$$

We need some initial data to solve these sets of differential equations. We assume  $S = S_0$  and  $I = I_0$  and  $R = R_0$  initially.

As per the first assumption  $dN/dt = 0$ . However,  $N = S + I + R$ , therefore,  $d(S + I + R)/dt = 0$ .

Knowing the maximum number of infectives i.e. the peak of active cases will be very helpful in planning how to distribute health resources. Now dividing the equation (2) by equation (1) and rearranging, we get:

$$dI/dS = \gamma/\beta S - 1 = (1/qS) - 1 \quad (6)$$

Solving this differential equation, we get:

$$I + S - (1/q)\ln S = I_0 + S_0 - (1/q)\ln S_0 \quad (7)$$

Infectives(I) will be maximum when  $dI/dS = 0$  i.e. when  $S = 1/q$ . Substituting  $S = 1/q$  and rearranging,

$$I_{max} = I_0 + S_0 - (1/q)(1 + \ln(qS_0)) \quad (8)$$

The parameters  $\beta$  and  $\gamma$  are estimated by minimizing the difference between actual and predicted values of C.  $C \in (S, I, R)$

$$\min ||C_t - C_t^*(\beta, \gamma, S_0)||^2 \quad (9)$$

where  $C_t = (C_1, C_2, \dots, C_n)$  represents the actual values and  $C_t^* = C_1^*, C_2^*, \dots, C_n^*$  represents the predictions calculated by the model at time  $t_i, i \in 1, \dots, n$  respectively.

#### *B. FbProphet (Facebook Prophet) Model*

FbProphet is for time-series forecasting based on an additive model which was made open source by Facebook in 2017. [13], [14] The non-linear trends of the FbProphet are fitted with yearly, weekly, and daily seasonality, plus

SIR model tries to answer some critical questions related to the epidemic.

#### *Question 1: Will the disease spread?*

We have an initial number of infective people  $I_0$ . But we want to know whether this number will grow. Now since,  $dS/dt$  is negative, we expect S to decrease with time. Therefore

$$\begin{aligned} S &\leq S_0 \\ dI/dt &< I(\beta S_0 - \gamma) \end{aligned} \quad (4)$$

Now, the disease will spread if,

$$dI/dt > 0 \text{ ie if } S_0 > \gamma/\beta = 1/q \quad (5)$$

$q$  is called the contact ratio: the fraction of the population that comes in a contact with an infective individual during the period when they are infectious. As introduced earlier in this paper, we define here the parameter  $R = \beta S_0 / \gamma$ .  $R_0$  is called basic reproductive ratio and it represents the number of secondary infections in the population caused by one initial primary infection. So, the disease will spread if  $R > 1$ .

#### *Question 2: What is the maximum number of infectives at any day i.e. the peak?*

holiday effects. The ideal FbProphet model not only does future prediction, but also helps in filling the missing values and detecting the anomalies. The FbProphet model can be described by the below equation,

$$y(t) = g(t) + s(t) + h(t) + \epsilon_t \quad (10)$$

Here,  $g(t)$  is a function used for the analysis of non-periodic time-series changes.  $s(t)$  reflects the periodic change, such as the weekly or a yearly periodicity.  $h(t)$  refers to the impact of an occasional day(s), such as a holiday.  $\epsilon_t$  refers to the error term due to any unobserved factors not being captured by the model. In this paper, we have only considered the time-series changes which are non-periodic in nature.

#### *Our Analysis*

We have considered the time duration from 01-Jun-20 to 30-Jul-20 for training the models. We have done our analysis on the data gathered from the official website of the Ministry of Health and Family Welfare, Government of India. Also, for the sake of our analysis, considering the huge population of our country, we have assumed that not the whole population is likely to be infected with this disease. Therefore, we have considered three scenarios that only - (i) 2%, (ii) 5% and (iii) 10% of the total population is susceptible to this disease.

The SIR model estimates the optimal values of parameters  $\beta$  and  $\gamma$ . It uses minimizing the RMSE (Root Mean Square Error) metric for actual and predicted values of S, I and R as the criterion for optimal values of  $\beta$  and  $\gamma$ . Further, the MAPE (Mean Absolute Percentage Error) metric has been used as a measure of the performance of the model.

The  $\beta$  and  $\gamma$  were estimated for different periods of time. Minimum RMSE (S, I, R) was considered to derive the

optimum values of  $\beta$  and  $\gamma$ . MAPE was targeted to be kept within 30% for the acceptable  $\beta$  and  $\gamma$  values.

In FbProphet forecasting, we started with the creation of a Prophet instance. Its fit and predict functions were then called for training and prediction respectively. The input to FbProphet model is always a time-series data with two features: date  $ds$  and value  $y$ . Here in our study,  $ds$  is the date of day, and  $y$  is the accumulated cases for the Confirmed, Deaths and Cured cases in India, Maharashtra, Tamil Nadu and Andhra Pradesh.

### III. RESULTS

In this section, we have presented the results from the SIR and FbProphet model.

TABLE 1 : POPULATION CONSIDERED

| Country/States | Population    |
|----------------|---------------|
| India          | 1,380,004,385 |
| Maharashtra    | 128,466,921   |
| Tamil Nadu     | 83,704,074    |
| Andhra Pradesh | 90,959,737    |

Both the models are trained on time-series data from 01-Jun-20 to 30-Jul-20 and the prediction starts from *Day 0* i.e. 31-Jul-20

#### A. SIR Model Prediction Results

TABLE 2: FORECASTING WITH THE SIR MODEL – INDIA

| Scenario        | 2%         | 5%         | 10%         |
|-----------------|------------|------------|-------------|
| N               | 27,600,088 | 69,000,219 | 138,000,439 |
| S <sub>0</sub>  | 27,565,115 | 68,809,684 | 137,809,903 |
| R <sub>0</sub>  | 1.51       | 1.48       | 1.48        |
| $\beta$         | 0.0924     | 0.0926     | 0.0914      |
| $\gamma$        | 0.061      | 0.0625     | 0.0616      |
| RMSE            | 28,200     | 25,576     | 24,287      |
| MAPE(S)         | 0.04%      | 0.02%      | 0.01%       |
| MAPE(I)         | 2.88%      | 2.52%      | 2.65%       |
| MAPE(R)         | 2.51%      | 2.92%      | 2.47%       |
| Peak Infectives | 1,830,144  | 4,136,872  | 8,342,276   |
| Peak Date       | 21-Oct-20  | 24-Nov-20  | 20-Dec-20   |

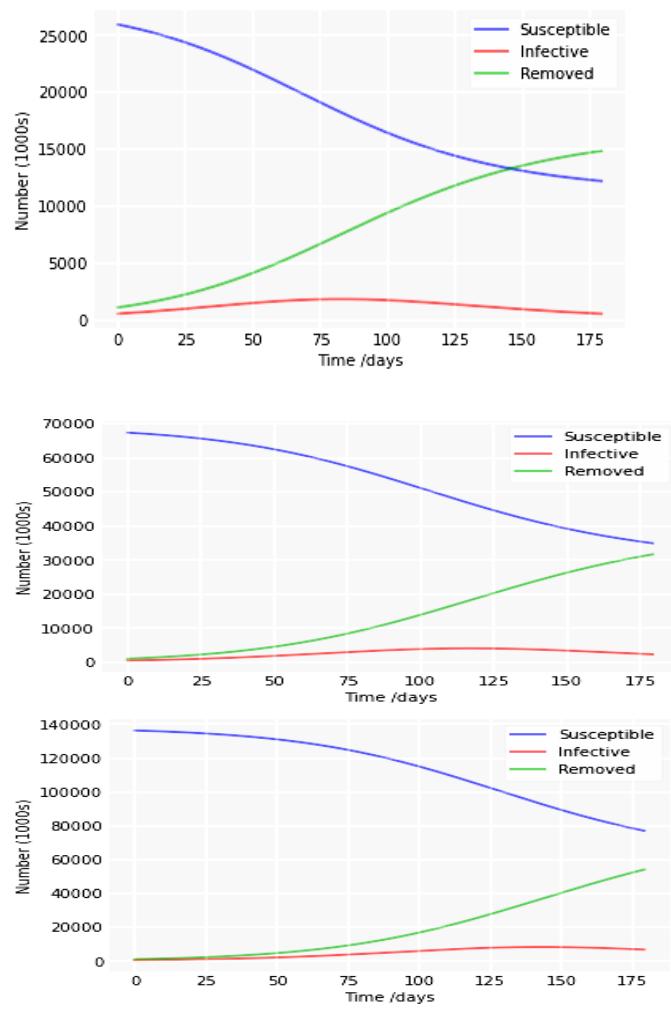


Figure 1: India forecasting with SIR model for 2%, 5% and 10% scenarios

TABLE 3: MAHARASHTRA FORCASTING WITH SIT MODEL

| Scenario        | 2%        | 5%        | 10%        |
|-----------------|-----------|-----------|------------|
| N               | 2,569,338 | 6,423,346 | 12,846,692 |
| S <sub>0</sub>  | 2,501,683 | 6,355,691 | 12,779,037 |
| R <sub>0</sub>  | 1.66      | 1.6       | 1.61       |
| $\beta$         | 0.0726    | 0.0912    | 0.0702     |
| $\gamma$        | 0.0427    | 0.0565    | 0.0433     |
| RMSE            | 7324      | 5701      | 5281       |
| MAPE(S)         | 0.13%     | 0.03%     | 0.01%      |
| MAPE(I)         | 3.00%     | 2.09%     | 1.89%      |
| MAPE(R)         | 1.40%     | 1.39%     | 1.41%      |
| Peak Infectives | 262,501   | 545,523   | 1,027,685  |
| Peak Date       | 26-Sep-20 | 09-Nov-20 | 11-Dec-20  |

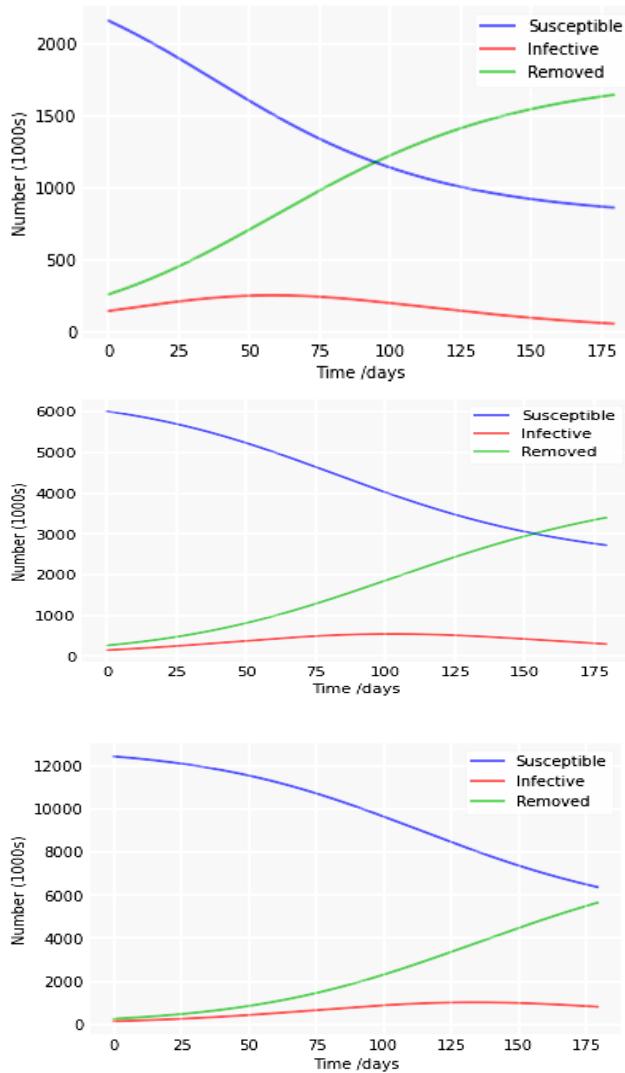


Figure 2: Maharashtra forecasting with SIR model for 2%, 5% and 10% scenarios

TABLE 4: TAMILNADU FORECASTING WITH SIR MODEL

| Scenario        | 2%        | 5%        | 10%       |
|-----------------|-----------|-----------|-----------|
| $N$             | 1,674,081 | 4,185,204 | 8,370,407 |
| $S_0$           | 1,651,748 | 4,162,870 | 8,348,074 |
| $R_0$           | 1.47      | 1.42      | 1.41      |
| $\beta$         | 0.1244    | 0.1242    | 0.1227    |
| $\gamma$        | 0.0837    | 0.0873    | 0.0868    |
| RMSE            | 8022      | 9240      | 9754      |
| MAPE(S)         | 0.10%     | 0.05%     | 0.03%     |
| MAPE(I)         | 10.16%    | 11.62%    | 12.09%    |
| MAPE(R)         | 4.82%     | 5.09%     | 4.82%     |
| Peak Infectives | 93,871    | 197,839   | 388,680   |
| Peak Date       | 08-Sep-20 | 10-Oct-20 | 02-Nov-20 |

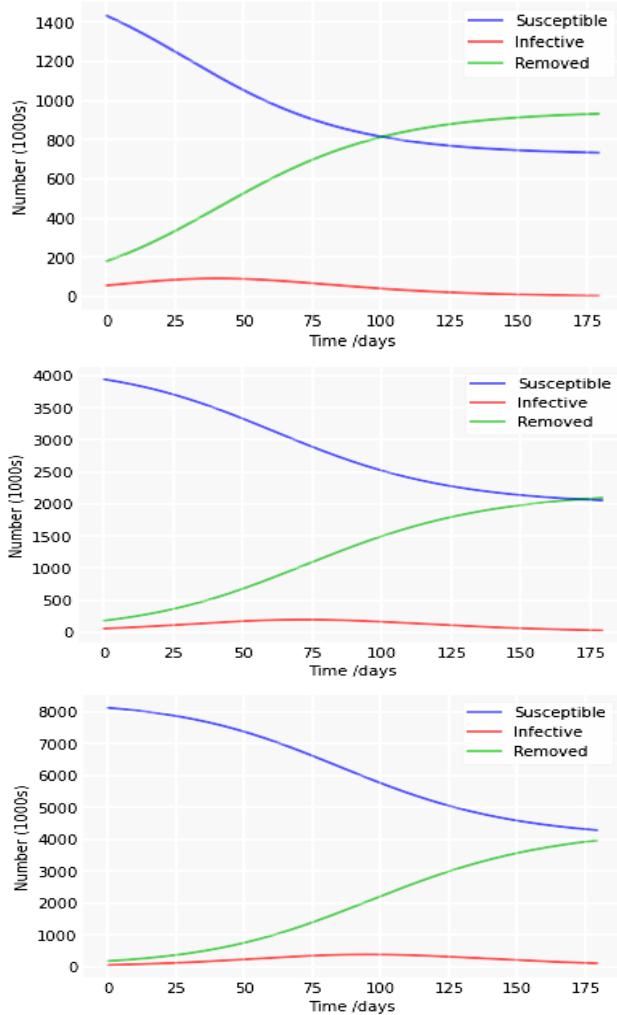


Figure 3: Tamil Nadu forecasting with SIR model for 2%, 5% and 10% scenarios

TABLE 5: ANDHRA PRADESH FORECASTING WITH SIR MODEL

| Scenario        | 2%        | 5%        | 10%       |
|-----------------|-----------|-----------|-----------|
| $N$             | 1,819,195 | 4,547,987 | 9,095,974 |
| $S_0$           | 1,815,515 | 4,544,307 | 9,092,294 |
| $R_0$           | 2.07      | 2.06      | 2.06      |
| $\beta$         | 0.1254    | 0.1246    | 0.1245    |
| $\gamma$        | 0.0604    | 0.0604    | 0.0604    |
| RMSE            | 7068      | 6717      | 6614      |
| MAPE (S)        | 0.16%     | 0.06%     | 0.03%     |
| MAPE (I)        | 9.25%     | 8.54%     | 8.57%     |
| MAPE (R)        | 15.43%    | 15.01%    | 14.99%    |
| Peak Infectives | 307,155   | 749,938   | 149,385   |
| Peak Date       | 15-Sep-20 | 01-Oct-20 | 13-Oct-20 |

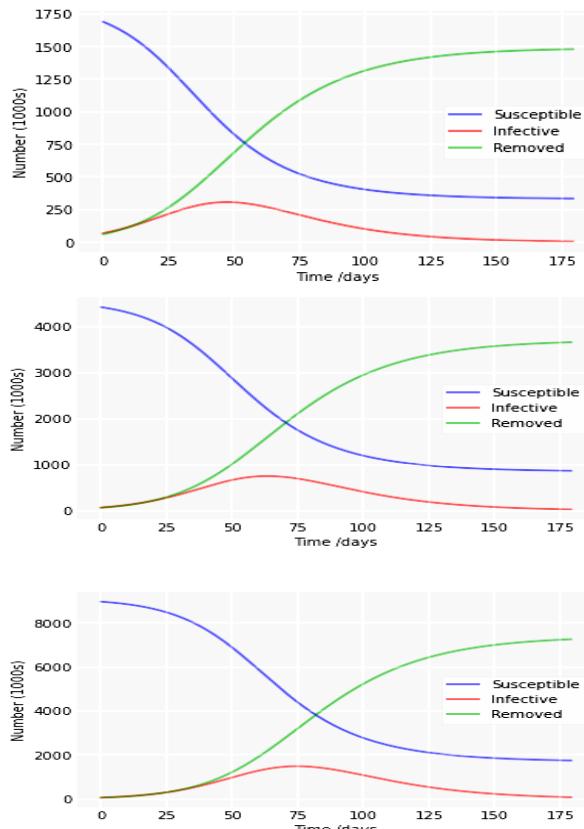


Figure 4: Andhra Pradesh forecasting with SIR model for 2%, 5% and 10% scenarios

### B. FbProphet Model Prediction Results

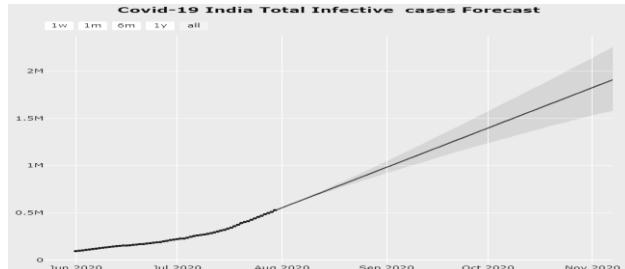


Figure 5: India Infective cases forecasting with FbProphet model

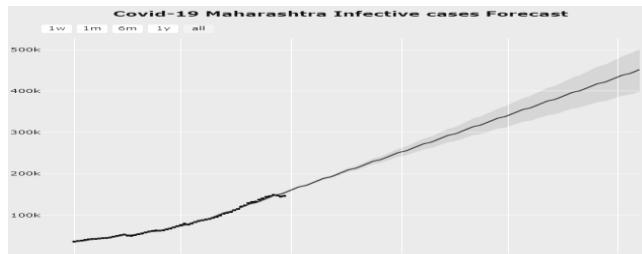


Figure 6: Maharashtra Infective cases forecasting with FbProphet model

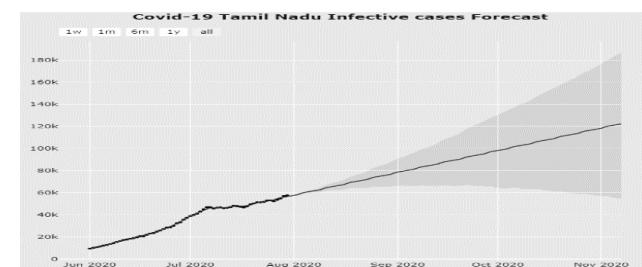


Fig 7: Tamil Nadu Infective cases forecasting with FbProphet Model

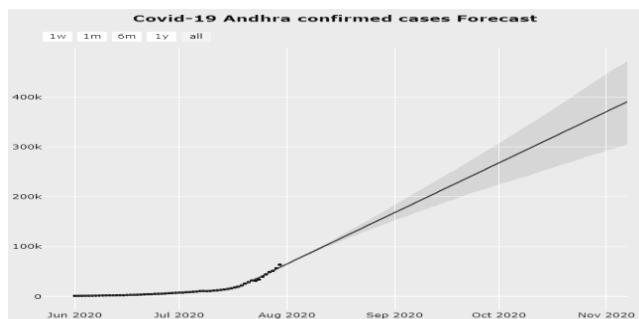


Figure 8: Andhra Infective cases forecasting with FbProphet model

### C. Results Comparison Between SIR and FbProphet Models:

TABLE 6: SIR AND FBPROPHET MODELS COMPARISION FOR INDIA

| Scenario                   | 2%        | 5%        | 10%       |
|----------------------------|-----------|-----------|-----------|
| <b>SIR Peak</b>            | 21-Oct-20 | 24-Nov-20 | 20-Dec-20 |
| <b>Infective (SIR)</b>     | 1,830,144 | 4,136,872 | 8,342,276 |
| <b>Infective_Min (FbP)</b> | 1,394,162 | 1,687,145 | 2,505,180 |
| <b>Infective (FbP)</b>     | 1,673,524 | 2,145,754 | 2,505,180 |
| <b>Infective_Max(FbP)</b>  | 1,933,592 | 2,553,789 | 3,066,819 |

TABLE 7: : SIR AND FBPROPHET MODELS COMPARISION FOR MAHARASHTRA

| Scenario                   | 2%        | 5%       | 10%       |
|----------------------------|-----------|----------|-----------|
| <b>SIR Peak</b>            | 26-Sep-20 | 9-Nov-20 | 11-Dec-20 |
| <b>Infective (SIR)</b>     | 262,501   | 5,45,523 | 1,027,685 |
| <b>Infective_Min (FbP)</b> | 306,227   | 408,707  | 477,247   |
| <b>Infective (FbP)</b>     | 327,390   | 458,859  | 552,390   |
| <b>Infective_Max(FbP)</b>  | 349,080   | 514,227  | 635,467   |

TABLE 8: : SIR AND FBPROPHET MODELS COMPARISION FOR TAMILNADU

| Scenario                   | 2%       | 5%        | 10%      |
|----------------------------|----------|-----------|----------|
| <b>SIR Peak</b>            | 8-Sep-20 | 10-Oct-20 | 2-Nov-20 |
| <b>Infective (SIR)</b>     | 93,871   | 197,839   | 388,680  |
| <b>Infective_Min (FbP)</b> | 66,298   | 64,344    | 57,957   |
| <b>Infective (FbP)</b>     | 83,330   | 103,807   | 125,949  |
| <b>Infective_Max(FbP)</b>  | 99,792   | 144,152   | 180,228  |

TABLE 9: : SIR AND FBPROPHET MODELS COMPARISION FOR ANDHRA PRADESH

| Scenario               | 2%        | 5%        | 10%       |
|------------------------|-----------|-----------|-----------|
| <b>SIR Peak</b>        | 15-Sep-20 | 01-Oct-20 | 13-Oct-20 |
| <b>Infective (SIR)</b> | 307,155   | 749,938   | 149,385   |

|                           |         |         |         |
|---------------------------|---------|---------|---------|
| <b>Infected_Min (FbP)</b> | 187,018 | 225,130 | 250,525 |
| <b>Infected (FbP)</b>     | 214,566 | 267,760 | 307,528 |
| <b>Infected_Max (FbP)</b> | 249,753 | 306,752 | 358,524 |

#### IV. DISCUSSION AND CONCLUSION

The SIR model and FbProphet models seem to be giving similar forecast results when we consider the susceptible population as 2% of the overall population which can be seen in Tables 6, 7, 8 and 9. For SIR model prediction, in the best-case scenario (2%), India seems to peak at an active infected population of 1.83 Million, while in the worst-case scenario (10%), it could peak at 8.34 Million. We noticed a significant difference in the forecast from the two models when susceptible population is taken as 5% or 10% of the overall population. This could be due to various reasons like the FbProphet model couldn't catch interactions between the external features, which we think could improve the model's forecasting power. The FbProphet might not be suitable for the time-series with an unstable variance [15]. Moreover, the FbProphet model is still under development and might not be completely stable. [16] On the other side, it should be noted that the SIR model also takes into account some simplifying assumptions about the population. It assumes homogeneous mixing of the population which might not be the case in the real scenario. The SIR model also assumes a constant population with no births, or deaths from other than this disease.

For 5% scenario, India seems to be attaining the peak in Nov-20 while the different states are seen to be attaining the peak at different times. This could possibly be due to the difference in the scale of measures implemented by the respective state governments at different times and if these measures were adhered to by the population as expected in order to control the pandemic. Overall, the peak for India is predicted to be a result of the strict implementation of the measures taken by the central government, like compulsory face mask, social distancing, washing hands frequently, halting public transport completely during the lockdown period, limiting interstate and intrastate movements to only essential travels, etc.

TABLE 10: ACTUAL [3] vs PREDICTED INFECTIONS AS ON 29-AUG-2020

| State / Country | Actual  | Predicted (2%) SIR | Predicted (5%) SIR | FbProphet |
|-----------------|---------|--------------------|--------------------|-----------|
| India           | 752,424 | 106,1728           | 117,950            | 940,137   |
| Maharashtra     | 185,131 | 223,803            | 268,934            | 244,243   |
| Tamil Nadu      | 52,726  | 90,277             | 123,060            | 76,037    |
| Andhra Pradesh  | 97,681  | 243,508            | 336,928            | 157,912   |

While some of the states (like Delhi) have already attained the peak, other states are expected to attain the peak within next few weeks (in Oct-20), while some other states are expected to be attaining it further in Nov-20 and Dec-20. This could be due to the commencement of the

unlock period wherein the movement of people has been allowed. While the pandemic until now was limited to certain areas, it seems to be spreading in the other areas due the movement of the population in these areas. We feel that the magnitude of spread in these areas will primarily depend on the readiness of the governments to tackle the infected population, strict implementation of the control measures and the adherence of the same by the population. Table 10 presents the actual and predicted numbers for infective cases as on 29-Aug-20. The possible reason for the variation in the numbers might lie in the nature and novelty of this pandemic. Patterns have changed quickly in this pandemic. Also, modelling the result with precision becomes difficult as still we know very little about the disease at this point of time. Different aspects such as the modes of transmission, life of virus on different surfaces and virus mutation are still being researched.

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