

DAA WEEK-DYNAMIC PROGRAMMING

1)

Question 1 | Correct Mark 10.00 out of 10.00 Flag question

Playing with Numbers:

Ram and Sita are playing with numbers by giving puzzles to each other. Now it was Ram's turn, so he gave Sita a positive integer 'n' and two numbers 1 and 3. He asked her to find the possible ways by which the number n can be represented using 1 and 3. Write any efficient algorithm to find the possible ways.

Example 1:

Input: 6

Output: 6

Explanation: There are 6 ways to represent the number with 1 and 3.

```
f+f+f+f+f+f  
3+3  
f+f+3+f  
f+f+f+3  
f+3+f+f  
3+f+f+f
```

Input Format

First Line contains the number n

Output Format

Print: The number of possible ways 'n' can be represented using 1 and 3

Sample Input

6

Sample Output

6

Answer: (penalty regime: 0 %)

```
1 #include<stdio.h>  
2 #include<stdint.h>  
3 uint64_t countryWays(int n){  
4     uint64_t dp[n+1];  
5     dp[0]=1;  
6     for(int i=1;i<=n;i++){  
7         dp[i]=0;  
8         if(i>1){  
9             dp[i]=dp[i-1];  
10            if(i>3){  
11                dp[i]+=dp[i-3];  
12            }  
13        }  
14    }  
15    return dp[n];  
16}  
17 int main(){  
18     int n;  
19     scanf("%d",&n);  
20     uint64_t result=countryWays(n);  
21     printf("%lu\n",result);  
22 }
```

OUTPUT:

| | Input | Expected | Got | |
|---|-------|-------------------|-------------------|---|
| ✓ | 6 | 6 | 6 | ✓ |
| ✓ | 25 | 8641 | 8641 | ✓ |
| ✓ | 100 | 24382819596721629 | 24382819596721629 | ✓ |

Passed all tests! ✓

Correct

Marks for this submission: 10.00/10.00.

2)

Question 1 | Correct Mark 10.00 out of 10.00 [Flag question](#)

Playing with Chessboard:

Ram is given with an $n \times n$ chessboard with each cell with a monetary value. Ram stands at the $(0,0)$, that the position of the top left white rook. He is been given a task to reach the bottom right black rook position $(n-1, n-1)$ constrained that he needs to reach the position by traveling the maximum monetary path under the condition that he can only travel one step right or one step down the board. Help ram to achieve it by providing an efficient DP algorithm.

Example:

Input

3

1 2 4

2 3 4

8 7 1

Output:

19

Explanation:

Totally there will be 6 paths among that the optimal is

Optimal path value: $1+2+8+7+1=19$

Input Format

First Line contains the integer n

The next n lines contain the $n \times n$ chessboard values

Output Format

Print Maximum monetary value of the path

Answer: (penalty regime: 0 %)

```
1 #include<stdio.h>
2 #define MAX 100
3 int max(int a,int b){
4     return (a>b)?a:b;
5 }
6 int main(){
7     int n;
8     int board[MAX][MAX],dp[MAX][MAX];
9     scanf("%d",&n);
10    for(int i=0;i<n;i++){
11        for(int j=0;j<n;j++){
12            scanf("%d",&board[i][j]);
13        }
14    }
15    dp[0][0]=board[0][0];
16    for(int j=1;j<n;j++){
17        dp[0][j]=dp[0][j-1]+board[0][j];
18    }
19    for(int i=1;i<n;i++){
20        dp[i][0]=dp[i-1][0]+board[i][0];
21    }
22    for(int i=1;i<n;i++){
23        for(int j=1;j<n;j++){
24            dp[i][j]=board[i][j]+max(dp[i-1][j],dp[i][j-1]);
25        }
26    }
27    printf("%d\n",dp[n-1][n-1]);
28    return 0;
29 }
```

OUTPUT:

| | Input | Expected | Got | |
|---|---|----------|-----|---|
| ✓ | 3 1 2 4 2 3 4 8 7 1 | 19 | 19 | ✓ |
| ✓ | 3 1 3 1 1 5 1 4 2 1 | 12 | 12 | ✓ |
| ✓ | 4 1 1 3 4 1 5 7 8 2 3 4 6 1 6 9 8 | 28 | 28 | ✓ |

Passed all tests! ✓

Correct

Marks for this submission: 10.00/10.00.

3)

Question 1 | Correct Mark 1.00 out of 1.00 Flag question

Given two strings find the length of the common longest subsequence(need not be contiguous) between the two.

Example:

s1: ggtaabe
s2: tgatasb

| | | | | | | | |
|----|---|---|---|---|---|---|---|
| s1 | a | g | g | t | a | b | |
| s2 | g | x | t | x | a | y | b |

The length is 4

Solving it using Dynamic Programming

For example:

| Input | Result |
|-------|--------|
| aab | 2 |
| azb | |

Answer: (penalty regime: 0 %)

```
1 #include<stdio.h>
2 #include<string.h>
3 # define MAX 100
4 int max(int a,int b){
5     return (a>b)? a:b;
6 }
7 int lcs(char *s1,char *s2){
8     int n=strlen(s1);
9     int m=strlen(s2);
10    int dp[MAX][MAX];
11
12    for(int i=0;i<n;i++){
13        for(int j=0;j<m;j++){
14            if(i==0 || j==0)
15                dp[i][j]=0;
16            else if(s1[i]==s2[j-1])
17                dp[i][j]=i+dp[i-1][j-1];
18            else
19                dp[i][j]=max(dp[i-1][j],dp[i][j-1]);
20        }
21    }
22    return dp[n][n];
23 }
24 int main(){
25     char s1[MAX],s2[MAX];
26     scanf("%s", s1);
27     scanf("%s", s2);
28     printf("%d\n",lcs(s1,s2));
29     return 0;
30 }
```

OUTPUT:

| | Input | Expected | Got | |
|---|--------------|----------|-----|---|
| ✓ | aab azb | 2 | 2 | ✓ |
| ✓ | ABCD ABCD | 4 | 4 | ✓ |

Passed all tests! ✓

Correct

Marks for this submission: 1.00/1.00.

5)

Question 1 | Correct Mark 1.00 out of 1.00 [Flag question](#)

Problem statement:

Find the length of the Longest Non-decreasing Subsequence in a given Sequence.

Eg:

Input:9

Sequence: [-1,3,4,5,2,2,2,2,3]

the subsequence is [-1,2,2,2,2,3]

Output:6

Answer: (penalty regime: 0 %)

```
1 #include<stdio.h>
2 #define MAX 100
3 int max(int a,int b){
4     return (a>b)? a:b;
5 }
6 int longNonDecreasingSubsequence(int arr[],int n){
7     int dp[MAX];
8     int maxlen=1;
9     for(int i=0;i<n;i++){
10         dp[i]=1;
11         for(int j=0;j<i;j++){
12             if(arr[j]<arr[i]){
13                 dp[i]=max(dp[i],dp[j]+1);
14             }
15         }
16         if(dp[i]>maxLen){
17             maxlen=dp[i];
18         }
19     }
20     return maxlen;
21 }
22 int main(){
23     int n;
24     scanf("%d",&n);
25     int arr[MAX];
26     for(int i=0;i<n;i++){
27         scanf("%d",&arr[i]);
28     }
29     int result=longNonDecreasingSubsequence(arr,n);
30     printf("%d\n",result);
31     return 0;
32 }
```

OUTPUT:

| | Input | Expected | Got | |
|---|-------------------------|----------|-----|---|
| ✓ | 9 -1 3 4 5 2 2 2 2 3 | 6 | 6 | ✓ |
| ✓ | 7 1 2 2 4 5 7 6 | 6 | 6 | ✓ |

Passed all tests! ✓

Correct

Marks for this submission: 1.00/1.00.