

# Classificação: Naive Bayes

$$P(C|x) = \frac{P(x|C) P(C)}{P(x)}$$

Likelihood  $\rightarrow$   $P(x|C)$   $\leftarrow$  Prior  $P(C)$   
 Posterior  $\rightarrow$   $P(C|x)$  Evidence  $\rightarrow$   $P(x)$

## Naive Bayes: Bayes Theorem.

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
8	0	0	1	yes
0	0	4	0	yes
8	0	4	0.7	no
0	0	0	1	yes
8	0	4	1	yes
5	0	2	1	yes
0	0	4	0.7	yes
0	0	2	0	no
0	5	2	1	yes
0	10	2	1	no
5	0	4	0.7	yes
8	5	4	0	yes
0	10	0	0.7	yes
0	0	2	0.7	yes
0	5	2	0	yes

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
8	0	0	1	yes ✓
0	0	4	0	yes
8	0	4	0.7	no
0	0	0	1	yes
8	0	4	1	yes
5	0	2	1	yes
0	0	4	0.7	yes
0	0	2	0	no
0	5	2	1	yes
0	10	2	1	no
5	0	4	0.7	yes
8	5	4	0	yes
0	10	0	0.7	yes
0	0	2	0.7	yes
0	5	2	0	yes

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
8	0	0	1	yes ✓
0	0	4	0	yes ✓
8	0	4	0.7	no
0	0	0	1	yes
8	0	4	1	yes
5	0	2	1	yes
0	0	4	0.7	yes
0	0	2	0	no
0	5	2	1	yes
0	10	2	1	no
5	0	4	0.7	yes
8	5	4	0	yes
0	10	0	0.7	yes
0	0	2	0.7	yes
0	5	2	0	yes

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
8	0	0	1	yes ✓
0	0	4	0	yes ✓
8	0	4	0.7	no
0	0	0	1	yes ✓
8	0	4	1	yes
5	0	2	1	yes
0	0	4	0.7	yes
0	0	2	0	no
0	5	2	1	yes
0	10	2	1	no
5	0	4	0.7	yes
8	5	4	0	yes
0	10	0	0.7	yes
0	0	2	0.7	yes
0	5	2	0	yes

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
8	0	0	1	yes ✓
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0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes
0	0	4	0.7	yes
0	0	2	0	no
0	5	2	1	yes
0	10	2	1	no
5	0	4	0.7	yes
8	5	4	0	yes
0	10	0	0.7	yes
0	0	2	0.7	yes
0	5	2	0	yes

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
8	0	0	1	yes ✓
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0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes
0	0	2	0	no
0	5	2	1	yes
0	10	2	1	no
5	0	4	0.7	yes
8	5	4	0	yes
0	10	0	0.7	yes
0	0	2	0.7	yes
0	5	2	0	yes



## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
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0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no
0	5	2	1	yes
0	10	2	1	no
5	0	4	0.7	yes
8	5	4	0	yes
0	10	0	0.7	yes
0	0	2	0.7	yes
0	5	2	0	yes

## ML: Classificação - Bayes

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0	0	0	1	yes ✓
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5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no
0	5	2	1	yes ✓
0	10	2	1	no
5	0	4	0.7	yes
8	5	4	0	yes
0	10	0	0.7	yes
0	0	2	0.7	yes
0	5	2	0	yes

## ML: Classificação - Bayes

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0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no
0	5	2	1	yes ✓
0	10	2	1	no
5	0	4	0.7	yes ✓
8	5	4	0	yes
0	10	0	0.7	yes
0	0	2	0.7	yes
0	5	2	0	yes

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
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0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no
0	5	2	1	yes ✓
0	10	2	1	no
5	0	4	0.7	yes ✓
8	5	4	0	yes ✓
0	10	0	0.7	yes
0	0	2	0.7	yes
0	5	2	0	yes

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
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0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no
0	5	2	1	yes ✓
0	10	2	1	no
5	0	4	0.7	yes ✓
8	5	4	0	yes ✓
0	10	0	0.7	yes ✓
0	0	2	0.7	yes
0	5	2	0	yes

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
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8	0	4	0.7	no
0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no
0	5	2	1	yes ✓
0	10	2	1	no
5	0	4	0.7	yes ✓
8	5	4	0	yes ✓
0	10	0	0.7	yes ✓
0	0	2	0.7	yes ✓
0	5	2	0	yes

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
8	0	0	1	yes ✓
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8	0	4	0.7	no
0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no
0	5	2	1	yes ✓
0	10	2	1	no
5	0	4	0.7	yes ✓
8	5	4	0	yes ✓
0	10	0	0.7	yes ✓
0	0	2	0.7	yes ✓
0	5	2	0	yes ✓

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
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0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no
0	5	2	1	yes ✓
0	10	2	1	no
5	0	4	0.7	yes ✓
8	5	4	0	yes ✓
0	10	0	0.7	yes ✓
0	0	2	0.7	yes ✓
0	5	2	0	yes ✓

12/15



## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
8	0	0	1	yes ✓
0	0	4	0	yes ✓
8	0	4	0.7	no ✗
0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no
0	5	2	1	yes ✓
0	10	2	1	no
5	0	4	0.7	yes ✓
8	5	4	0	yes ✓
0	10	0	0.7	yes ✓
0	0	2	0.7	yes ✓
0	5	2	0	yes ✓

12/15

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
8	0	0	1	yes ✓
0	0	4	0	yes ✓
8	0	4	0.7	no ✗
0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no ✗
0	5	2	1	yes ✓
0	10	2	1	no
5	0	4	0.7	yes ✓
8	5	4	0	yes ✓
0	10	0	0.7	yes ✓
0	0	2	0.7	yes ✓
0	5	2	0	yes ✓

12/15

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
8	0	0	1	yes ✓
0	0	4	0	yes ✓
8	0	4	0.7	no ✗
0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no ✗
0	5	2	1	yes ✓
0	10	2	1	no ✗
5	0	4	0.7	yes ✓
8	5	4	0	yes ✓
0	10	0	0.7	yes ✓
0	0	2	0.7	yes ✓
0	5	2	0	yes ✓

12/15

## ML: Classificação - Bayes

quake	flood	hurricane	wildfire	loss
8	0	0	1	yes ✓
0	0	4	0	yes ✓
8	0	4	0.7	no ✗
0	0	0	1	yes ✓
8	0	4	1	yes ✓
5	0	2	1	yes ✓
0	0	4	0.7	yes ✓
0	0	2	0	no ✗
0	5	2	1	yes ✓
0	10	2	1	no ✗
5	0	4	0.7	yes ✓
8	5	4	0	yes ✓
0	10	0	0.7	yes ✓
0	0	2	0.7	yes ✓
0	5	2	0	yes ✓

12/15

3/15

## ML: Classificação - Bayes

	quake		no	yes
no quake (0)	2	7	2/3	7/12
level 5	0	2	0/3	2/12
level 8	1	3	1/3	3/12

## ML: Classificação - Bayes

	quake		no	yes
<i>no quake (0)</i>	2	7	2/3	7/12
<i>level 5</i>	0	2	0/3	2/12
<i>level 8</i>	1	3	1/3	3/12

	flood		no	yes
<i>no flood (0)</i>	2	8	2/3	8/12
<i>mid level (5)</i>	0	3	0/3	3/12
<i>max level (10)</i>	1	1	1/3	1/12

## ML: Classificação - Bayes

	quake		no	yes
no quake (0)	2	7	2/3	7/12
level 5	0	2	0/3	2/12
level 8	1	3	1/3	3/12

	flood		no	yes
no flood (0)	2	8	2/3	8/12
mid level (5)	0	3	0/3	3/12
max level (10)	1	1	1/3	1/12

	hurricane		no	yes
no hurricane (0)	0	3	0/3	3/12
category 2	2	4	2/4	4/12
category 4	1	5	1/3	5/12

## ML: Classificação - Bayes

	quake		no	yes
no quake (0)	2	7	2/3	7/12
level 5	0	2	0/3	2/12
level 8	1	3	1/3	3/12

	flood		no	yes
no flood (0)	2	8	2/3	8/12
mid level (5)	0	3	0/3	3/12
max level (10)	1	1	1/3	1/12

	hurricane		no	yes
no hurricane (0)	0	3	0/3	3/12
category 2	2	4	2/4	4/12
category 4	1	5	1/3	5/12

	wildfire		no	yes
no fire (0)	1	3	1/3	3/12
high (0.7)	1	4	1/3	4/12
extreme (1.0)	1	5	1/3	5/12



## ML: Classificação - Bayes

	quake		no	yes
no quake (0)	2	7	2/3	7/12
level 5	0	2	0/3	2/12
level 8	1	3	1/3	3/12

	flood		no	yes
no flood (0)	2	8	2/3	8/12
mid level (5)	0	3	0/3	3/12
max level (10)	1	1	1/3	1/12

	hurricane		no	yes
no hurricane (0)	0	3	0/3	3/12
category 2	2	4	2/4	4/12
category 4	1	5	1/3	5/12

	wildfire		no	yes
no fire (0)	1	3	1/3	3/12
high (0.7)	1	4	1/3	4/12
extreme (1.0)	1	5	1/3	5/12

$$P(\text{Quake level 8} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Flood max-level} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Hurricane categ. 4} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Wildfire extreme} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{No sig. loss}) = \frac{3}{15}$$

## ML: Classificação - Bayes

	quake		no	yes
no quake (0)	2	7	2/3	7/12
level 5	0	2	0/3	2/12
level 8	1	3	1/3	3/12

	flood		no	yes
no flood (0)	2	8	2/3	8/12
mid level (5)	0	3	0/3	3/12
max level (10)	1	1	1/3	1/12

$$P(\text{Quake level 8} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Flood max-level} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Hurricane categ. 4} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Wildfire extreme} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{No sig. loss}) = \frac{3}{15}$$

	hurricane		no	yes
no hurricane (0)	0	3	0/3	3/12
category 2	2	4	2/4	4/12
category 4	1	5	1/3	5/12

	wildfire		no	yes
no fire (0)	1	3	1/3	3/12
high (0.7)	1	4	1/3	4/12
extreme (1.0)	1	5	1/3	5/12

$$P(\text{Quake level 8} \mid \text{yes}) = \frac{3}{12}$$

$$P(\text{Flood max-level} \mid \text{yes}) = \frac{1}{12}$$

$$P(\text{Hurricane categ. 4} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{Wildfire extreme} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{Yes sig. loss}) = \frac{12}{15}$$

## ML: Classificação - Bayes

$$P(\text{Quake level 8} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Flood max-level} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Hurricane categ. 4} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{wildfire extreme} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{No sig. loss}) = \frac{3}{15}$$

$$P(\text{Quake level 8} \mid \text{yes}) = \frac{3}{12}$$

$$P(\text{Flood max-level} \mid \text{yes}) = \frac{1}{12}$$

$$P(\text{Hurricane categ. 4} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{wildfire extreme} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{Yes sig. loss}) = \frac{12}{15}$$

$$P(Q \wedge F \wedge H \wedge W \mid \text{No}) \times P(\text{No}) = \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{3}{15} = 0.0025$$

## ML: Classificação - Bayes

$$P(\text{Quake level 8} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Flood max-level} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Hurricane categ. 4} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{wildfire extreme} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{No sig. loss}) = \frac{3}{15}$$

$$P(\text{Quake level 8} \mid \text{yes}) = \frac{3}{12}$$

$$P(\text{Flood max-level} \mid \text{yes}) = \frac{1}{12}$$

$$P(\text{Hurricane categ. 4} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{wildfire extreme} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{Yes sig. loss}) = \frac{12}{15}$$

$$P(Q \wedge F \wedge H \wedge W \mid \text{No}) \times P(\text{No}) = \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{3}{15} = 0.0025$$

$$P(Q \wedge F \wedge H \wedge W \mid \text{Yes}) \times P(\text{Yes}) = \frac{3}{12} \times \frac{1}{12} \times \frac{5}{12} \times \frac{5}{12} \times \frac{12}{15} = 0.0029$$

## ML: Classificação - Bayes

$$P(\text{Quake level 8} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Flood max-level} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Hurricane categ. 4} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{wildfire extreme} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{No sig. loss}) = \frac{3}{15}$$

$$P(\text{Quake level 8} \mid \text{yes}) = \frac{3}{12}$$

$$P(\text{Flood max-level} \mid \text{yes}) = \frac{1}{12}$$

$$P(\text{Hurricane categ. 4} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{wildfire extreme} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{Yes sig. loss}) = \frac{12}{15}$$

$$P(Q \wedge F \wedge H \wedge W \mid \text{No}) \times P(\text{No}) = \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{3}{15} = 0.0025$$

$$P(Q \wedge F \wedge H \wedge W \mid \text{Yes}) \times P(\text{Yes}) = \frac{3}{12} \times \frac{1}{12} \times \frac{5}{12} \times \frac{5}{12} \times \frac{12}{15} = 0.0029$$

$$\text{Normalizar por } P(Q \wedge F \wedge H \wedge W) = \frac{4}{15} \times \frac{2}{15} \times \frac{6}{15} \times \frac{6}{15} = 0.0057$$

## ML: Classificação - Bayes

$$P(\text{Quake level 8} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Flood max-level} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Hurricane categ. 4} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{wildfire extreme} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{No sig. loss}) = \frac{3}{15}$$

$$P(\text{Quake level 8} \mid \text{yes}) = \frac{3}{12}$$

$$P(\text{Flood max-level} \mid \text{yes}) = \frac{1}{12}$$

$$P(\text{Hurricane categ. 4} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{wildfire extreme} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{Yes sig. loss}) = \frac{12}{15}$$

$$P(Q \wedge F \wedge H \wedge W \mid \text{No}) \times P(\text{No}) = \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{3}{15} = 0.0025$$

$$P(Q \wedge F \wedge H \wedge W \mid \text{Yes}) \times P(\text{Yes}) = \frac{3}{12} \times \frac{1}{12} \times \frac{5}{12} \times \frac{5}{12} \times \frac{12}{15} = 0.0029$$

$$\text{Normalizar por } P(Q \wedge F \wedge H \wedge W) = \frac{4}{15} \times \frac{2}{15} \times \frac{6}{15} \times \frac{6}{15} = 0.0057$$

$$P(\text{No} \mid Q \wedge F \wedge H \wedge W) = \frac{0.0025}{0.0057} = 0.43$$

## ML: Classificação - Bayes

$$P(\text{Quake level 8} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Flood max-level} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Hurricane categ. 4} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{wildfire extreme} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{No sig. loss}) = \frac{3}{15}$$

$$P(\text{Quake level 8} \mid \text{yes}) = \frac{3}{12}$$

$$P(\text{Flood max-level} \mid \text{yes}) = \frac{1}{12}$$

$$P(\text{Hurricane categ. 4} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{wildfire extreme} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{Yes sig. loss}) = \frac{12}{15}$$

$$P(Q^A F^A H^A W \mid \text{No}) \times P(\text{No}) = \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{3}{15} = 0.0025$$

$$P(Q^A F^A H^A W \mid \text{Yes}) \times P(\text{Yes}) = \frac{3}{12} \times \frac{1}{12} \times \frac{5}{12} \times \frac{5}{12} \times \frac{12}{15} = 0.0029$$

$$\text{Normalizar por } P(Q^A F^A H^A W) = \frac{4}{15} \times \frac{2}{15} \times \frac{6}{15} \times \frac{6}{15} = 0.0057$$

$$P(\text{No} \mid Q^A F^A H^A W) = \frac{0.0025}{0.0057} = 0.43$$

$$P(\text{Yes} \mid Q^A F^A H^A W) = \frac{0.0029}{0.0057} = 0.51$$

## ML: Classificação - Bayes

$$P(\text{Quake level 8} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Flood max-level} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Hurricane categ. 4} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{wildfire extreme} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{No sig. loss}) = \frac{3}{15}$$

$$P(\text{Quake level 8} \mid \text{yes}) = \frac{3}{12}$$

$$P(\text{Flood max-level} \mid \text{yes}) = \frac{1}{12}$$

$$P(\text{Hurricane categ. 4} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{wildfire extreme} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{Yes sig. loss}) = \frac{12}{15}$$

$$P(Q^A F^A H^A W \mid \text{No}) \times P(\text{No}) = \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{3}{15} = 0.0025$$

$$P(Q^A F^A H^A W \mid \text{Yes}) \times P(\text{Yes}) = \frac{3}{12} \times \frac{1}{12} \times \frac{5}{12} \times \frac{5}{12} \times \frac{12}{15} = 0.0029$$

$$\text{Normalizar por } P(Q^A F^A H^A W) = \frac{4}{15} \times \frac{2}{15} \times \frac{6}{15} \times \frac{6}{15} = 0.0057$$

$$P(\text{No} \mid Q^A F^A H^A W) = \frac{0.0025}{0.0057} = 0.43$$

$$\underline{P(\text{Yes} \mid Q^A F^A H^A W) = \frac{0.0029}{0.0057} = 0.51}$$



## ML: Classificação - Bayes

$$P(\text{Quake level 8} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Flood max-level} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{Hurricane categ. 4} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{wildfire extreme} \mid \text{no}) = \frac{1}{3}$$

$$P(\text{No sig. loss}) = \frac{3}{15}$$

$$P(\text{Quake level 8} \mid \text{yes}) = \frac{3}{12}$$

$$P(\text{Flood max-level} \mid \text{yes}) = \frac{1}{12}$$

$$P(\text{Hurricane categ. 4} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{wildfire extreme} \mid \text{yes}) = \frac{5}{12}$$

$$P(\text{Yes sig. loss}) = \frac{12}{15}$$

$$P(Q \wedge F \wedge H \wedge W \mid \text{No}) \times P(\text{No}) = \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{3}{15} = 0.0025$$

$$P(Q \wedge F \wedge H \wedge W \mid \text{Yes}) \times P(\text{Yes}) = \frac{3}{12} \times \frac{1}{12} \times \frac{5}{12} \times \frac{5}{12} \times \frac{12}{15} = 0.0029$$

$$\text{Normalizar por } P(Q \wedge F \wedge H \wedge W) = \frac{4}{15} \times \frac{2}{15} \times \frac{6}{15} \times \frac{6}{15} = 0.0057$$

$$P(\text{No} \mid Q \wedge F \wedge H \wedge W) = \frac{0.0025}{0.0057} = 0.43$$

$$\underline{P(\text{Yes} \mid Q \wedge F \wedge H \wedge W) = \frac{0.0029}{0.0057} = 0.51}$$

**Se Quake level 8 e Flood max-level e Hurricane categ. 4 e Wildfire extreme => Yes Loss**

## ML: Classificação - Bayes

- Treinar com base nas features para prever o label.

```
from sklearn.naive_bayes import MultinomialNB
nb = MultinomialNB()
nb.fit(X_train, y_train)
acuracia_treino = nb.score(X_train, y_train)
acuracia_treino*100
```

73.75

## ML: Classificação - Bayes

- Vamos medir então o resultado das previsões com dados de teste: acurácia, matriz de confusão, precision e recall.

```
from sklearn.metrics import accuracy_score, confusion_matrix,
preds = nb.predict(X_test)
test_accuracy = accuracy_score(y_test,preds)*100
print(test_accuracy)
cm = confusion_matrix(y_test,preds)
print(cm)
print(classification_report(y_test,preds))
```

```
80.0
[[ 0  3]
 [ 1 16]]
```

	precision	recall	f1-score	support
0	0.00	0.00	0.00	3
1	0.84	0.94	0.89	17
accuracy			0.80	20
macro avg	0.42	0.47	0.44	20
weighted avg	0.72	0.80	0.76	20

## Exercício: Bayes

- Analise o Histórico de Crédito e verifique quais são as probabilidades de um cliente ter seu crédito aprovado ou não, utilizando o algoritmo de Bayes.
  - Compare com as classificações realizadas no exercícios anterior
  - Avalie o crédito para um novo conjunto de potenciais clientes.

treino: <https://raw.githubusercontent.com/lcbjrrr/data/main/RiscoCredito%20-%20okk.csv>

teste: <https://raw.githubusercontent.com/lcbjrrr/data/main/RiscoCredito%20-%20prever2.csv>



# MAD MEN

Intuición · Creatividad · Appeal



# MATH MEN

Analytics · Resultados · Lógica



## ATIVIDADE: Naive Bayes

- Escolha uma base de dados no <https://www.kaggle.com/datasets>, e se familiarize com sua base
- Procure realizar a previsão (inferência) de uma variável categórica através de um Naive Bayes. Se certifique de medir seus níveis de assertividade. Esteja a vontade a realizar mais um hiperparâmetro (número de vizinhos) de um e compará-los
- Não esqueça de junto com seus códigos realizar suas análises/conclusões (use o botão de +Texto).

## ML: Classificação - Bayes

1	previsao	temperatura	umidade	vento	jogar
2	ensolarado	quente	alta	nao_ventando	nao ✗
3	ensolarado	quente	alta	ventando	nao ✗
4	nublado	quente	alta	nao_ventando	sim ✓
5	chuvoso	brando	alta	nao_ventando	sim ✓
6	chuvoso	frio	normal	nao_ventando	sim ✓
7	chuvoso	frio	normal	ventando	nao ✗
8	nublado	frio	normal	ventando	sim ✓
9	ensolarado	brando	alta	nao_ventando	nao ✗
10	ensolarado	frio	normal	nao_ventando	sim ✓
11	chuvoso	brando	normal	nao_ventando	sim ✓
12	ensolarado	brando	normal	ventando	sim ✓
13	nublado	brando	alta	ventando	sim ✓
14	nublado	quente	normal	nao_ventando	sim ✓
15	chuvoso	brando	alta	ventando	nao