

# Fractal Causality: Mathematical Skeleton (v2)

This document provides the cleaned mathematical framework for Fractal Causality (FC), focusing solely on the testable equations without philosophical narrative.

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## 1. Power Spectrum Template

The core testable prediction is a log-periodically modulated power spectrum:

$$P(k) = P_{\text{LCDM}}(k) * [1 + \varepsilon \cos(\omega \ln(k/k_0) + \phi)]$$

where:

$\varepsilon$  = echo amplitude (strength of modulation)

$\omega$  = log-frequency of oscillation

$k_0$  = pivot scale

$\phi$  = phase

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## 2. Parameter Priors (for testing)

$$\varepsilon \in [-0.1, 0.1]$$

$$\omega \in [1, 50]$$

$$\phi \in [0, 2\pi)$$

$k_0$  chosen within survey's  $k$ -range (e.g., 0.01–0.2 h/Mpc)

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## 3. Predictions

- Residuals  $\Delta P(k) = P_{\text{data}}(k) - P_{\text{LCDM}}(k)$  should show oscillations matching the template.
- Bispectrum  $B(k_1, k_2, k_3)$  should exhibit phase-coherent oscillations with the same  $\omega, \phi$ .
- Cross-dataset consistency: true signals must persist across independent surveys.

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## 4. Extensions

Beyond cosmology, FC suggests that log-periodic echoes may appear in:

- Stochastic gravitational wave background spectra  $\Omega_{\text{GW}}(f)$ .
- Correlated optical clock fluctuations across large baselines.

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## Conclusion

This skeleton is meant for direct testing: fit the above template to cosmological and physical datasets, compare Bayesian evidence ( $Z_{\text{FC}}$  vs  $Z_{\text{null}}$ ), and assess support for or against FC.