

故凸向原點

$$q = 10L = 10K$$

(E) TC, AC, MC

(F) 產10單位 最低 cost

$$TC = 20q$$

$$TC(10) = 2 \times 10 = 20$$

$$AC = 2$$

$$MC = 2$$

隨9 $A \Rightarrow q = \min\{\frac{1}{2}, \frac{K}{4}\}$ $w=1, r=2$

權利金=40

$B \Rightarrow q = \min\{\frac{1}{4}, \frac{K}{2}\}$

權利金=100

$TC = \text{生產成本} + \text{權利金成本}$

生產成本 = $LTC = wL + rK = L + 2K$

成本極小化

(A) ① $q = \frac{1}{2} = \frac{K}{4} \Rightarrow L^* = 2q, K^* = 4q$

$$C = 1 \times 2q + 2 \times 4q = 10q, LTC_A = 10q + 40$$

② $q = \frac{1}{4} = \frac{K}{2} \Rightarrow L^* = 4q, K^* = 2q$

$$C = 1 \times 4q + 2 \times 2q = 8q, LTC_B = 8q + 100$$

(B) 生產20, $q=20, TC_A=240, TC_B=260$ (A)

(C) 生產40, $q=40, TC_A=440, TC_B=420$ (B)

(D) 產量低於? buy A

$$TC_A < LTC_B, 10q + 40 < 8q + 100 \Rightarrow q < 30$$

隨 11 $Q = 10L^{\frac{1}{2}}K^{\frac{1}{2}}$ $w=r=10$, K 固定 K_0

$$*STC = wL + rK$$

成本極小化

(A) STC, AC, MC

$$Q = 10L^{\frac{1}{2}}K^{\frac{1}{2}} \Rightarrow L^* = \frac{Q^2}{100K_0}$$

$$STC = 10 \times \frac{Q^2}{100K_0} + 10K_0 = \frac{Q^2}{10K_0} + 10K_0 \#$$

$$SAC = \frac{Q}{10K_0} + \frac{10K_0}{Q} \#$$

$$SMC = \frac{dSTC}{dQ} = \frac{2Q}{10K_0} \#$$

(B) 求極小 STC

$$\frac{dSTC}{dK} = \frac{-Q^2}{10K^2} + 10 = 0 \Rightarrow K = \frac{Q}{10} \quad (\text{求 } K \text{ 最小, 所以做微分})$$

$$STC = 8 + 8 = 16$$

隨 12 $Q=20$, AC & AVC 差 10, $Q=40$ 差?

$$Q=20, AC = AFC + AVC, AFC = 10$$

$$AFC = \frac{FC}{Q} = \frac{rk}{Q}, FC = 200$$

$$Q=40, AFC' = 5 \#$$

隨 13 $MC = 10Q$, $FC = 100$, $Q = 10$, $TC = ?$

$$TC = FC + VC = 100 + VC$$

$$MC = \frac{dVC}{dQ} = 10Q$$

$$VC = \int MC dQ = \int_0^{10} 10Q dQ = 5Q^2 \Big|_0^{10} = 500$$

$$TC = 100 + 500$$

$$= 600 \#$$