## Getting Started With Haskell

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#### **Abstract**

The slides of today will hopefully convince you that learning Haskell is going to change your life for the better.

## **Keywords:**

Functional programming, executable specification.

## A Short History of Haskell

In the 1980s, efforts of researchers working on functional programming were scattered across many languages (Lisp, Scheme, SASL, KRC, Hope, Id, Miranda, ML,...).

In 1987 a dozen functional programmers decided to meet in order to reduce unnecessary diversity in functional programming languages by designing a common language [4]. The new language should be:

- based on ideas that enjoyed wide consensus;
- suitable for further language research as well as applications, including building large systems;
- freely available (in particular: anyone should be permitted to implement the language and distribute it to whomever they please).



The new language was called Haskell, after the logician and mathematician Haskell Brooks Curry (1900–1982). Curry is known for his work on the lambda calculus and on combinatory logic. The lambda calculus is the foundation of Haskell.



Haskell B. Curry

In 1990, the first Haskell specification was published.

Right now, Haskell has a flourishing (and very friendly) user community, and many enthousiastic supporters. If asked why learning Haskell is a good idea, they have things like this to say:

Haskell is a wide-spectrum language, suitable for a variety of applications. It is particularly suitable for programs which need to be highly modifiable and maintainable.

Much of a software product's life is spent in specification, design and maintenance, and not in programming. Functional languages are superb for writing specifications which can actually be executed (and hence tested and debugged). Such a specification then is the first prototype of the final program.

Functional programs are also relatively easy to maintain, because the code is shorter, clearer, and the rigorous control of side effects eliminates a huge class of unforeseen interactions.

From: http://www.haskell.org/haskellwiki/Introduction

## **Literate Programming**

We will use literate Haskell in this course. The Haskell code that we mention in these slides is collected into a so-called Haskell module. See [5] for the benefits of literate programming.

```
module Week1
where
import Data.List
```

You can find the module Week1. hs on the course website, at address http://www.homepages.cwi/~jve/courses/13/testing2013/.

### **How Haskell is Different**

Here is a quote from an interview with John Goerzen, one of the authors of Real World Haskell [6].

Question: One of Haskell's benefits is that you can use it as a purely functional language – but that's really different for people who've come up in the imperative or object-oriented worlds. What does it take to learn how to think in a pure fashion?

Goerzen: That's probably the single biggest mind-shift that you deal with coming from a different language; that and laziness. Both of those are both pretty big.

As for how to learn about it, it's a lot of relearning how to do some very basic things and then building upon that. For instance, in imperative languages, you have for loops and you have while loops. There's a lot of having a variable there and then incrementing it as you iterate over something. In Haskell, you tend to take a recursive approach rather than that. It can be a little bit scary at first because you might be thinking if you're using a language such as C, incrementing a variable is a pretty cheap operation.

http://broadcast.oreilly.com/2009/01/why-you-should-learn-haskell.
html

Haskell allows for abstract, high order programming. (Ideally, more thinking and less writing and debugging.)

Haskell is based on the lambda calculus, therefore the step from formal specification to implementation is very small.

Haskell offers you a new perspective on programming, it is powerful, and it is fun.

The type system behind Haskell is a great tool for writing specifications that catch many coding errors.

Your Haskell understanding will influence the way you look at programming: you will start to appreciate abstraction.

Haskell comes with great tools for automated test generation: a tool we will employ at some point is QuickCheck [1], which has served as inspiration for the development of similar tools for many other programming languages.

#### Haskell is functional

A Haskell program consists entirely of functions. Running a Haskell program consists in evaluating expressions (basically functions applied to arguments).

The main program itself is a function with the program's input as argument and the program's output as result.

Typically the main function is defined in terms of other functions, which in turn are defined in terms of still more functions, until at the bottom level the functions are language primitives.

This means that Haskell, like all functional languages, is extensible. If you need a certain programming construct that the language does not provide as a primitive, it is up to you to define it. We will use this feature a lot in this course.

Functions are first-class citizens, which means that they can be used as arguments to other (higher order) functions. This is extremely powerful and extremely useful.

## A shift in thinking

If you are an imperative thinker, you think mainly of:

- variables as pointers to storage locations whose value can be updated all the time
- sequences of commands telling the computer what to do (how to change certain memory locations) step by step.

#### Here are some examples:

- initialize a variable examplelist of type integer list, then add 1, then add 2, then add 3.
- in order to compute the factorial of n, initialize an integer variable f as 1, then for all i from 1 to n, set f to f×i

If you are a functional thinker, you view bound variables as place-holders for function arguments, and you view unbound variables as identifiers for immutable persistent values, or as names for functions.

Instead of telling the computer what actions to perform in what order, you prefer telling the computer what things are.

Running through the same examples again:

- examplelist is a list of integers containing the elements 1, 2, and 3
- the factorial of n is the product of all integers from 1 to n.

Here is the Haskell code for the factorial function:

```
factorial :: Integer -> Integer
factorial n = product [1..n]
```

All the same, this course will stress that functional programming is an inclusive paradigm, well capable of expressing the while loops, repeat loops and for loops that play such an important role in pseudo-code presentations of algorithms.

# Where Should I Begin?

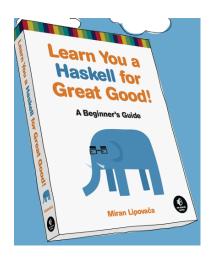
#### Resources

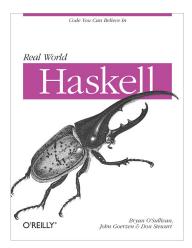
For everything Haskell-related, start at http://haskell.orghaskell.org.

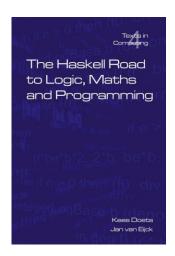
There are lots of free tutorials you may wish to consult:

- Chapter 1 of "The Haskell Road" [3], freely available from http://homepages.cwi.nl/~jve/HR/
- Real World Haskell [6], http://book.realworldhaskell.org/read/
- Learn you a Haskell for great good http://learnyouahaskell.comlearnyouahaskell.com
- A gentle introduction to Haskell http://haskell.org/tutorial.
- The Haskell Wikibook, secure.wikimedia.org/wikibooks/en/wiki/Haskell
- Hal Daume's Yet Another Haskell Tutorial [2] is also available as a Wikibook, from secure. wikimedia.org/wikibooks/en/wiki/Haskell/YAHT.

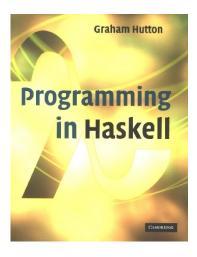
Some recommended books:

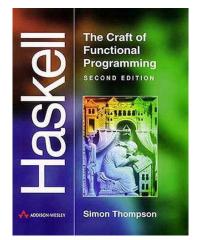


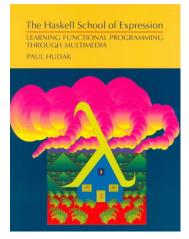




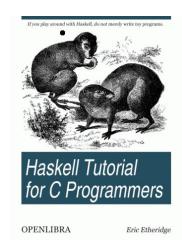
And some more:

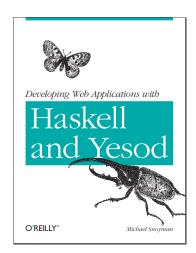


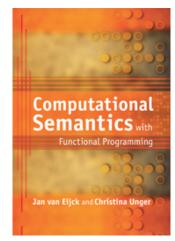




If you are coming to Haskell from elsewhere, or are into specific applications, one of the following might be for you:







## **Really Getting Started**

Get the Haskell Platform:

• http://hackage.haskell.org/platform/

This includes the Glasgow Haskell Compiler (GHC) together with standard libraries and the interactive environment GHCi. Follow the instructions to install the platform.

#### Haskell as a Calculator

#### Start the interpreter:

```
jve@vuur:~/courses/12/esslli12$ ghci
GHCi, version 7.0.3: http://www.haskell.org/ghc/ :? for help
Loading package ghc-prim ... linking ... done.
Loading package integer-gmp ... linking ... done.
Loading package base ... linking ... done.
Prelude>
```

The prompt Prelude> you are seeing indicates that the so-called Haskell Prelude, consisting of a list of useful predefined functions, is loaded.

GHCi can be used to interactively evaluate expressions.

```
Prelude> 2+3
Prelude> 2+3 * 4
Prelude> 2^10
Prelude> (42-10) / 2
Prelude> (+) 2 3
```

## Your first Haskell program

1. Write the following code to a text file and save it as first.hs:

```
double :: Int \rightarrow Int double n = 2 * n
```

- 2. Inside GHCi, you can load the program with :l first.hs (or by running ghci first.hs).
  With :r you can reload it if you change something.
- 3. Now you can evaluate expressions like double 5, double (2+3), and double (double 5).
- 4. With :t you can ask GHCi about the type of an expression.
- 5. Leave the interactive environment with :q.

## Some simple samples of lazy lists

"Sentences can go on and on and on (and on)\*"

Here is a so-called lazy list implementation:

```
sentence = "Sentences can go " ++ onAndOn
onAndOn = "on and " ++ onAndOn
```

This uses the operation ++ for list concatenation plus the double quote notation for character strings.

If you grab the module Week1.hs from http://www.homepages.cwi/~jve/courses/13/testing2013/ and load it, you will see the following:

```
jve@vuur:~/courses/13/testing2013/lectures$ ghci Week1.hs
GHCi, version 7.0.3: http://www.haskell.org/ghc/ :? for help
Loading package ghc-prim ... linking ... done.
Loading package integer-gmp ... linking ... done.
Loading package base ... linking ... done.
[1 of 1] Compiling Week1 (Week1.hs, interpreted)
Ok, modules loaded: Week1.
*Week1>
```

If you now type sentence and hit the return (enter) key, you will see that sentences can indeed go on and on and .... You can quit the infinite loop by hitting ^C (control-C). Next, check an initial segment:

```
*Week1> take 65 sentence
```

"Sentences can go on and on and on and on and on and on and on and" \*Week1>

Next, consider the following:

```
sentences = "Sentences can go on" :
    map (++ " and on") sentences
```

New ingredients here are: for putting a item in front of a list, and the function map that will be explained below.

The function sentences generates an infinite list of sentences. Here is the start of the list:

```
*Week1> take 10 sentences
```

["Sentences can go on", "Sentences can go on and on", "Sentences can go on and on and on", "Sentences can go on and on an

on and on and on and on", "Sentences can go on and on and

\*Week1>

#### Lambda Abstraction in Haskell

In Haskell,  $\setminus$  x expresses lambda abstraction over variable x.

```
sqr :: Int -> Int
sqr = \ x -> x * x
```

The standard mathematical notation for this is  $\lambda x \mapsto x * x$ . Haskell notation aims at remaining close to mathematical notation.

- The intention is that variabele x stands proxy for a number of type Int.
- The result, the squared number, also has type Int.
- The function sqr is a function that, when combined with an argument of type Int, yields a value of type Int.
- This is precisely what the type-indication Int -> Int expresses.

## **String Functions in Haskell**

```
Prelude> (\ x -> x ++ " emeritus") "professor" "professor emeritus"
```

This combines lambda abstraction and concatenation.

The types:

```
Prelude> :t (\ x -> x ++ " emeritus")
\x -> x ++ " emeritus" :: [Char] -> [Char]
Prelude> :t "professor"
"professor" :: String
Prelude> :t (\ x -> x ++ " emeritus") "professor"
  (\x -> x ++ " emeritus") "professor" :: [Char]
```

## **Concatenation**

The type of the concatenation function:

```
Prelude> :t (++)
(++) :: forall a. [a] -> [a] -> [a]
```

The type indicates that (++) not only concatenates strings. It works for lists in general.

## **More String Functions in Haskell**

## **Characters and Strings**

- The Haskell type of characters is Char. Strings of characters have type [Char].
- Similarly, lists of integers have type [Int].
- The empty string (or the empty list) is [].
- The type [Char] is abbreviated as String.
- Examples of characters are 'a', 'b' (note the single quotes).
- Examples of strings are "Turing" and "Chomsky" (note the double quotes).
- In fact, "Chomsky" can be seen as an abbreviation of the following character list:

```
['C','h','o','m','s','k','y'].
```

## **Properties of Strings**

- If strings have type [Char] (or String), properties of strings have type [Char] -> Bool.
- Here is a simple property:

```
aword :: [Char] -> Bool
aword [] = False
aword (x:xs) = (x == 'a') || (aword xs)
```

- This definition uses pattern matching: (x:xs) is the prototypical non-empty list.
- The head of (x:xs) is x, the tail is xs.
- The head and tail are glued together by means of the operation:, of type  $a \rightarrow [a] \rightarrow [a]$ .
- The operation combines an object of type a with a list of objects of the same type to a new list of objects, again of the same type.

#### **List Patterns**

- It is common Haskell practice to refer to non-empty lists as x:xs, y:ys, and so on, as a useful reminder of the facts that x is an element of a list of x's and that xs is a list.
- Note that the function aword is called again from the body of its own definition. We will encounter such **recursive** function definitions again and again.
- What the definition of aword says is that the empty string is not an aword, and a non-empty string is an aword if either the head of the string is the character a, or the tail of the sring is an aword.
- The list pattern [] matches only the empty list,
- the list pattern [x] matches any singleton list,
- the list pattern (x:xs) matches any non-empty list.

#### **List Reversal**

The reversal of the string "CHOMSKY" is the string "YKSMOHC". The reversal of the string "GNIRUT" is the string "TURING".

```
reversal :: [a] -> [a]
reversal [] = []
reversal (x:t) = reversal t ++ [x]
```

Reversal works for any list, not just for strings. This is indicated by the type specification [a] -> [a].

### **Haskell Basic Types**

- Int and Integer, to represent integers. Elements of Integer are unbounded (can be of any size).
- Float and Double represent floating point numbers. The elements of Double have higher precision.
- Bool is the type of Booleans.
- Char is the type of characters.

Note that the name of a type always starts with a capital letter.

To denote arbitrary types, Haskell allows the use of type variables. For these, a, b, ..., are used.

## **Haskell Derived Types**

Derived types can be constructed in the following way:

- By list-formation: if a is a type, [a] is the type of lists over a. Examples: [Int] is the type of lists of integers; [Char] is the type of lists of characters, or strings.
- By pair- or tuple-formation: if a and b are types, then (a,b) is the type of pairs with an object of type a as their first component, and an object of type b as their second component. If a, b and c are types, then (a,b,c) is the type of triples with an object of type a as their first component, an object of type b as their second component, and an object of type c as their third component...
- By function definition: a -> b is the type of a function that takes arguments of type a and returns values of type b.
- By defining your own datatype from scratch, with a data type declaration. More about this in due course.

## **Mapping**

If you use the Hugs command: t to find the types of the predefined function map, you get the following:

```
Prelude> :t map
map :: forall a b. (a -> b) -> [a] -> [b]
```

The function map takes a function and a list and returns a list containing the results of applying the function to the individual list members.

This is an example of higher order functional programming, of a function taking another function as an argument.

If f is a function of type  $a \rightarrow b$  and xs is a list of type [a], then map f xs will return a list of type [b]. E.g., map (^2) [1..9] will produce the list of squares

```
[1, 4, 9, 16, 25, 36, 49, 64, 81]
```

### **Sections**

But let us first explain the notation  $(^2)$ .

- In general, if op is an infix operator, (op x) is the operation resulting from applying op to its righthand side argument.
- (x op) is the operation resulting from applying op to its lefthand side argument.
- (op) is the prefix version of the operator.
- Thus (2<sup>^</sup>) is the operation that computes powers of 2, and map (2<sup>^</sup>) [1..10] will yield [2, 4, 8, 16, 32, 64, 128, 256, 512, 1024]
- Similarly, (>3) denotes the property of being greater than 3, and (3>) the property of being smaller than 3.
- (++ " and on") denotes the operation of appending " and on" to a string.

## Map again

If p is a property (an operation of type a  $\rightarrow$  Bool) and 1 is a list of type [a], then map p 1 will produce a list of type Bool (a list of truth values), like this:

```
Prelude> map (>3) [1..6]
[False, False, False, True, True]
Prelude>
```

Here is a definition of map, including a type declaration.

```
map :: (a -> b) -> [a] -> [b]
map f [] = []
map f (x:xs) = (f x) : map f xs
```

The code is in light grey. This indicates that this definition will not be added to the chapter module. Adding it to the chapter module would result in a compiler error, for map is already defined.

#### **Filter**

A function for filtering out the elements from a list that satisfy a given property:

```
Prelude> filter (>3) [1..10] [4,5,6,7,8,9,10]
```

The type declaration and the function definition:

## **List comprehension**

List comprehension is defining lists by the following method:

```
[ x \mid x \leftarrow xs, property x ]
```

This defines the sublist of xs of all items satisfying property. It is equivalent to:

```
filter property xs
```

Here are some examples:

```
someEvens = [ x | x <- [1..1000], even x ]
evensUntil n = [ x | x <- [1..n], even x ]
allEvens = [ x | x <- [1..], even x ]</pre>
```

Equivalently:

```
someEvens = filter even [1..1000]
evensUntil n = filter even [1..n]
allEvens = filter even [1..]
```

### Nub

The function nub removes duplicates, as follows:

```
nub :: Eq a => [a] -> [a]
nub [] = []
nub (x:xs) = x : nub (filter (/= x) xs)
```

Note the indication  $Eq = \infty$  in the type declaration. This is to indicate that the type a has to satisfy some special properties, to ensure that (/=), the operation for non-equality, is defined on it.

## **Function Composition**

The composition of two functions f and g, pronounced 'f after g' is the function that results from first applying g and next f.

Standard notation for this:  $f \cdot g$ . This is pronounced as "f after g".

Haskell implementation:

```
(.) :: (a \rightarrow b) \rightarrow (c \rightarrow a) \rightarrow (c \rightarrow b)
f . g = \ x \rightarrow f (g x)
```

Note the types!

### Elem, all, and

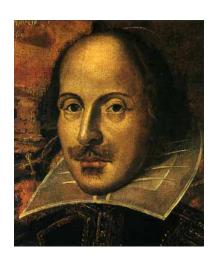
```
elem :: Eq a => a -> [a] -> Bool
elem x [] = False
elem x (y:ys) = x == y || elem x ys
```

```
all :: Eq a => (a -> Bool) -> [a] -> Bool
all p = and . map p
```

Note the use of . for function composition.

```
and :: [Bool] -> Bool
and [] = True
and (x:xs) = x && and xs
```

# **Shakespeare's Sonnet 73**



```
"That time of year thou mayst in me behold\n"
++ "When yellow leaves, or none, or few, do hang\n"
++ "Upon those boughs which shake against the cold,\n"
++ "Bare ruin'd choirs, where late the sweet birds sang.\n"
++ "In me thou seest the twilight of such day\n"
++ "As after sunset fadeth in the west,\n"
++ "Which by and by black night doth take away,\n"
++ "Death's second self, that seals up all in rest.\n"
++ "In me thou see'st the glowing of such fire\n"
++ "That on the ashes of his youth doth lie,\n"
++ "As the death-bed whereon it must expire\n"
++ "Consumed with that which it was nourish'd by.\n"
++ "This thou perceivest, which makes thy love more strong,\n"
++ "To love that well which thou must leave ere long."
```

### **Counting**

```
average :: [Int] -> Rational
average [] = error "empty list"
average xs = toRational (sum xs) / toRational (length xs)
```

Here length is a built-in function that computes the length of a list.

**Exercise 1** Give your own definition of length.

### Some commands to try out

- putStrLn sonnet73
- map toLower sonnet73
- map toUpper sonnet73
- filter ('elem' "aeiou") sonnet73
- count 't' sonnet73
- count 't' (map toLower sonnet73)
- count "thou" (words sonnet73)
- count "thou" (words (map toLower sonnet73))

Next, attempt the programming exercises from Chapter 1 and 2 of "The Haskell Road" [3].

### **Expressing the Essence of Recursion over Lists with Fold**

The pattern of recursive definitions over lists consists of matching the empty list [] for the base case, and matching the non-empty list (x:xs) for the recursive case. Witness:

```
and :: [Bool] -> Bool
and [] = True
and (x:xs) = x && and xs
```

This occurs so often that Haskell provides a standard higher-order function that captures the essence of what goes on in this kind of definition:

```
foldr:: (a -> b -> b) -> b -> [a] -> b

foldr f b [] = b

foldr f b (x:xs) = f x (foldr f b xs)
```

Here is what happens if you call foldr with a function f, and identity element z, and a list  $[x_1, x_2, x_3, \ldots, x_n]$ :

foldr 
$$f z [x_1, x_2, ..., x_n] = (f x_1 (f x_2 (f x_3 ... (f x_n z)...).$$

And the same thing using infix notation:

foldr 
$$f z [x_1, x_2, ..., x_n] = (x_1 'f' (x_2 'f' (x_3 'f' (... (x_n 'f' z)...).$$

For instance, the and function can be defined using foldr as follows:

and = foldr (&&) True

#### **Exercise 2**

- 1. Define length in terms of foldr.
- 2. Define elem x in terms of foldr.
- 3. Find out what or does, and next define your own version of or in terms of foldr.
- 4. Define map f in terms of foldr.
- 5. Define filter p in terms of foldr.
- 6. Define (++) in terms of foldr.
- 7. Define reversal in terms of foldr.

While foldr folds to the right, the following built-in function folds to the left.

#### Official definition:

#### Equivalent definition:

```
foldl :: (a -> b -> a) -> a -> [b] -> a
foldl f z [] = z
foldl f z (x:xs) = foldl f (f z x) xs
```

If you apply fold1 to a function  $f :: \alpha \to \beta \to \alpha$ , a left identity element  $z :: \alpha$  for the function, and a list of arguments of type  $\beta$ , then we get:

foldl 
$$f z [x_1, x_2, ..., x_n] = (f ... (f(f(f z x_1) x_2) x_3) ... x_n)$$

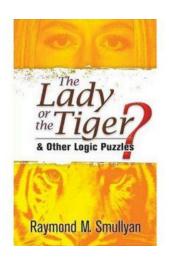
Or, if you write f as an infix operator:

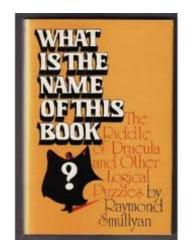
foldl 
$$f z [x_1, x_2, ..., x_n] = (...(((z 'f' x_1) 'f' x_2) 'f' x_3) ... 'f' x_n)$$

Exercise 3 Give an alternative definition of reverse, in terms of foldl.

# **Solving Logic Puzzles with Haskell**

We can use Haskell to solve logical puzzles such as the famous Lady or Tiger puzzles by Raymond Smullyan [7].





Here is the first puzzle. There are two rooms, and a prisoner has to choose between them. Each room contains either a lady or a tiger. In the first test the prisoner has to choose between a door with the sign "In this room there is a lady, and in the other room there is a tiger", and a second door with the sign "In one of these rooms there is a lady and in the other room there is a tiger." A final given

is that one of the two signs tells the truth and the other does not. Here is a Haskell implementation that states the puzzle:

```
data Creature = Lady | Tiger deriving (Eq,Show)
sign1, sign2 :: (Creature,Creature) -> Bool
sign1 (x,y) = x == Lady && y == Tiger
sign2 (x,y) = x /= y
```

#### And here is the Haskell solution:

Running this reveals that the first room has a tiger in it, and the second room a lady:

```
*Week1> solution1 [(Tiger, Lady)]
```

**Exercise 4** The second puzzle of the book runs as follows. Again there are two signs. The sign on the first door says: "At least one of these rooms contains a lady." The sign on the second door says: "A tiger is in the other room." This time either the statements are both true or both false. Give a Haskell implementation of solution2 that solves the puzzle. You will also have to write functions for the new signs, of course.

On the island of knights and knaves made famous in another logic puzzle book by Raymond Smullyan [8], there are two kinds of people. Knights always tell the truth, and knaves always lie. Of course, if you ask inhabitants of the island whether they are knights, they will always say "yes."

Suppose John and Bill are residents of the island. They are standing next to each other, with John left and Bill right. John says: "We are both knaves." Who is what? Here is a Haskell solution:

This reveals that John is a knave and Bill a knight:

```
*Week1> solution3 [(Knave, Knight)]
```

**Exercise 5** In this puzzle, again John is on the left, Bill on the right. John says: "We are both of the same kind." Bill says: "We are both of different kinds." Who is what? Implement a Haskell solution.

### **A Puzzling Program**

Use a minute or so to analyze the following program.

```
main = putStrLn (s ++ show s)
  where s = "main = putStrLn (s ++ show s) \n where s = "
```

This has the following ingredients that may still be unfamiliar to you:

- show for displaying an item as a string (if the item to be displayed is already a string, then this string is quoted);
- \n for the newline character.

Now that this was explained to you, reflect again, and tackle the exercises below.

Exercise 6 Predict what will happen when the function main is executed. Next write down your prediction, and check it by executing the function.

**Exercise 7** (Only for those who know some logic.) What does this have to do with logic? Hint: think of Kurt Gödel's famous proof of the incompleteness of the first order theory of arithmetic.

# **Summary**

If this was your first acquaintance with Haskell, make sure to actually play around and do some exercises. You will find that you will be up and running in no time.

If you already have some Haskell experience, this first chapter should have been plain sailing for you.

In the rest of this course we will focus on a particular aspect of functional programming: the use of executable specifications for programs.

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