# Python Code for QSS Chapter 3: Measurement

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First Printing

In Chapter 2, we begin visualizing data. Python has a variety of excellent plotting libraries. This chapter uses seaborn, which is built on top of matplotlib. We occassionally leverage matplotlib to customize plots. In seaborn, we use three families of plotting functions, known as "figure-level" plots in seaborn terminology. Whenever we use one of these function families, we must specify a "kind" of plot, unless the kind we want to use is the default. The table below summarizes the families of plotting functions and the kinds of plots used in this chapter. Seaborn also has more specific, "axes-level," plotting functions, such as histplot and scatterplot. Axes-level plots are particularly useful for creating sub-plots.

Family	Kind
relplot	scatter (default), line
displot	hist (default), kde
catplot	bar, box

# Section 3.1: Measuring Civilian Victimization during Wartime

```
[]: # import libraries used in chapter with conventinal aliases
import pandas as pd
import seaborn as sns
import numpy as np
import matplotlib.pyplot as plt

# import data
afghan = pd.read_csv('afghan.csv')

# summarize variables of interest
afghan['age'].describe().round(2)
```

```
[]: count
               2754.00
                 32.39
     mean
                 12.29
     std
     min
                 15.00
     25%
                 22.00
     50%
                 30.00
     75%
                 40.00
                 80.00
     Name: age, dtype: float64
```

```
[]: afghan['educ.years'].describe().round(2)
[]: count
              2754.00
    mean
                 4.00
     std
                 4.75
                 0.00
    min
     25%
                 0.00
     50%
                 1.00
     75%
                 8.00
     max
                18.00
     Name: educ.years, dtype: float64
[]: afghan['employed'].describe().round(2)
[]: count
              2754.00
                 0.58
     mean
     std
                 0.49
    min
                 0.00
     25%
                 0.00
     50%
                 1.00
     75%
                 1.00
                 1.00
     max
     Name: employed, dtype: float64
[]: afghan['income'].describe()
[]: count
                       2600
     unique
                          5
     top
               2,001-10,000
                       1420
     freq
     Name: income, dtype: object
[]: afghan['income'].value_counts(sort=False, dropna=False)
[]: income
     2,001-10,000
                        1420
                         154
     10,001-20,000
                         616
     less than 2,000
                         457
     20,001-30,000
                          93
     over 30,000
                          14
     Name: count, dtype: int64
[]: # convert income to a categorical variable and specify levels
     afghan['income'] = afghan['income'].astype('category').cat.reorder_categories(
         ['less than 2,000', '2,001-10,000', '10,001-20,000', '20,001-30,000',
          'over 30,000']
```

```
afghan['income'].value_counts(sort=False, dropna=False)
[]: income
    less than 2,000
                         457
     2,001-10,000
                        1420
     10,001-20,000
                         616
     20,001-30,000
                          93
     over 30,000
                          14
     NaN
                         154
     Name: count, dtype: int64
[]: pd.crosstab(afghan['violent.exp.ISAF'], afghan['violent.exp.taliban'],
                 rownames=['ISAF'], colnames=['Taliban'], normalize=True)
[]: Taliban
                   0.0
                             1.0
     ISAF
     0.0
              0.495345 0.131844
     1.0
              0.176909 0.195903
    Section 3.2: Handling Missing Data in Pandas
[]: # print income data for first 10 respondents
     afghan['income'].head(10)
[]: 0
           2,001-10,000
           2,001-10,000
     1
           2,001-10,000
     2
           2,001-10,000
     3
     4
           2,001-10,000
     5
                    NaN
          10,001-20,000
     6
     7
           2,001-10,000
           2,001-10,000
     8
                    NaN
    Name: income, dtype: category
     Categories (5, object): ['less than 2,000', '2,001-10,000', '10,001-20,000',
     '20,001-30,000', 'over 30,000']
[]: # indicate whether respondents' income is missing
     afghan['income'].isnull().head(10)
[]:0
         False
         False
     1
         False
     2
         False
     3
         False
```

```
5
           True
     6
          False
     7
          False
     8
          False
           True
     Name: income, dtype: bool
[]: # count of missing values
     afghan['income'].isnull().sum()
[]: 154
[]: # proportion of missing values
     afghan['income'].isnull().mean()
[]: 0.05591866376180102
[]: x = pd.Series([1, 2, 3, np.nan])
     # pandas ignores missing values by default
     x.mean()
[]: 2.0
[]: # we can override the default behavior
     x.mean(skipna=False)
[]: nan
    The pandas crosstab method does not have an argument for including missing values in a contin-
    gency table. Instead, we can use the fillna method to supply a name for the missing values.
[]: pd.crosstab(afghan['violent.exp.ISAF'].fillna('Nonresponse'),
                 afghan['violent.exp.taliban'].fillna('Nonresponse'),
                 rownames=['ISAF'], colnames=['Taliban'], normalize=True)
[]: Taliban
                       0.0
                                  1.0 Nonresponse
     ISAF
     0.0
                  0.482934 0.128540
                                          0.007988
     1.0
                  0.172476 0.190995
                                          0.007988
     Nonresponse 0.002542 0.002905
                                          0.003631
[]: # listwise deletion
     afghan_sub = afghan.dropna()
     afghan_sub.shape[0]
```

[]: 2554

```
[]: afghan['income'].dropna().shape[0]
```

[]: 2600

# Section 3.3: Visualizing the Univariate Distribution

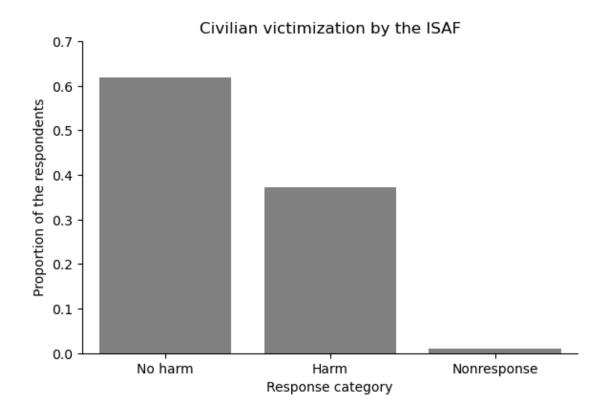
### Section 3.3.1: Bar Plot

```
[]: violent.exp.ISAF proportion
0 0.0 0.619463
1 1.0 0.371460
2 NaN 0.009078
```

```
[]: # add a response column for plotting convenience
ISAF_ptable['response'] = ['No harm', 'Harm', 'Nonresponse']

# plot using the catplot family and kind='bar'
sns.catplot(
    data=ISAF_ptable, x='response', y='proportion', color='gray',
    kind='bar', estimator=sum, height=4, aspect=1.5
).set(title='Civilian victimization by the ISAF',
    xlabel='Response category', ylabel='Proportion of the respondents',
    ylim=(0, 0.7))
```

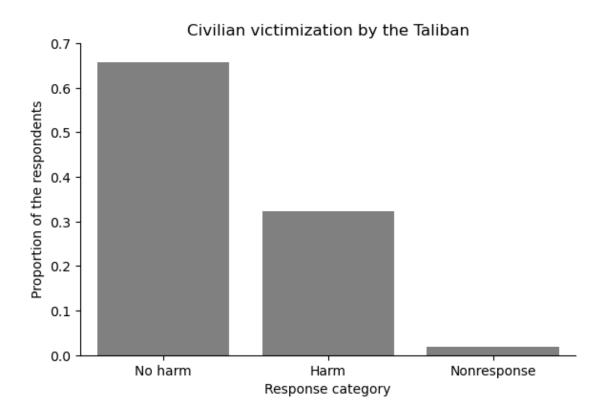
[]: <seaborn.axisgrid.FacetGrid at 0x1cf9dcc9e40>



Notice, we use estimator=sum because seaborn bar plots aggregate the data by a given function. The default aggregation function is mean. Since we have already calculated proportions, we can use sum to ensure there is no further aggregation. Another strategy for creating the bar plot is to use the mean aggregation directly on the original data frame categories.

Additionally, we set the height and aspect ratios directly. The default height is 5 inches for seaborn figure-level plots, and the default aspect ratio is 1. The aspect ratio is the ratio of the width to the height. Therefore, the default width is 5 inches.

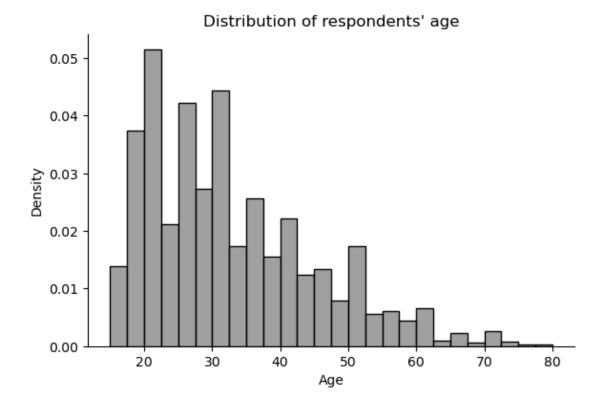
[]: <seaborn.axisgrid.FacetGrid at 0x1cf9df0f670>



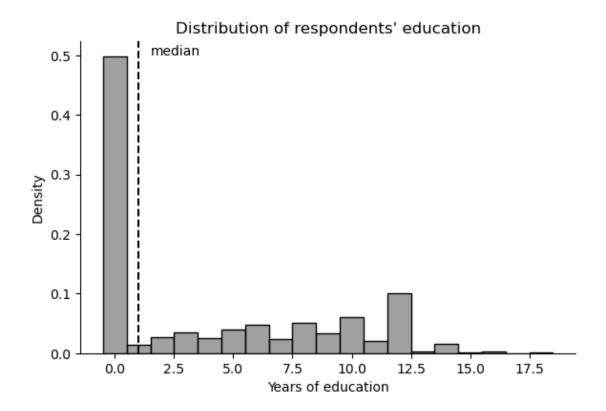
# Section 3.3.2: Histogram

```
[]: sns.displot(
    data=afghan, x='age', stat='density', color='gray',
    height=4, aspect=1.5
).set(title="Distribution of respondents' age", xlabel='Age')
```

[]: <seaborn.axisgrid.FacetGrid at 0x1cf9dec5ff0>



[]: Text(1.5, 0.5, 'median')

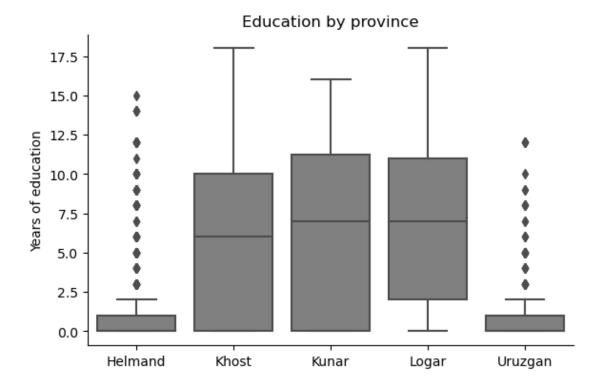


# Section 3.3.3: Box Plot

```
[]: # convert province to a categorical variable
# not necessary for plotting, but useful for other analyses
afghan['province'] = afghan['province'].astype('category')

sns.catplot(
    data=afghan, x='province', y='educ.years', kind='box', color='gray',
    height=4, aspect=1.5
).set(title='Education by province', xlabel='', ylabel='Years of education')
```

[]: <seaborn.axisgrid.FacetGrid at 0x1cf9e7a5690>



# []: afghan.groupby('province')['violent.exp.taliban'].mean()

## []: province

Helmand0.504222Khost0.233227Kunar0.303030Logar0.080247Uruzgan0.454545

Name: violent.exp.taliban, dtype: float64

# []: afghan.groupby('province')['violent.exp.ISAF'].mean()

# []: province

Helmand0.541023Khost0.242424Kunar0.398990Logar0.144033Uruzgan0.496042

Name: violent.exp.ISAF, dtype: float64

## Section 3.3.4: Saving Plots

```
[]: # Option 1: Save via point-and-click in IDE

# Option 2: Run plot code plus plt.savefig()

sns.catplot(
    data=afghan, x='province', y='educ.years', kind='box', color='gray',
    height=4, aspect=1.5
).set(title='Education by province', xlabel='', ylabel='Years of education')

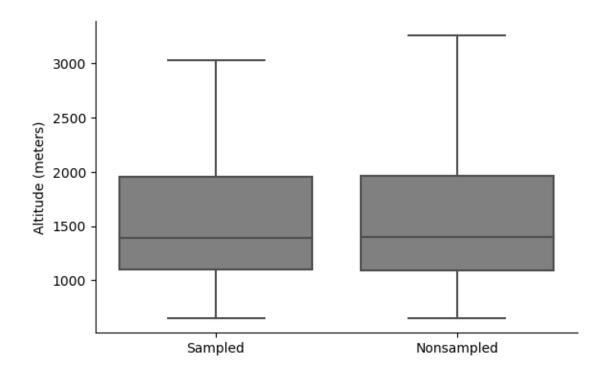
plt.savefig('education-by-province.png', bbox_inches='tight')

plt.close() # preventing plot from re-displaying
```

# Section 3.4: Survey Sampling

## Section 3.4.1: The Role of Randomization

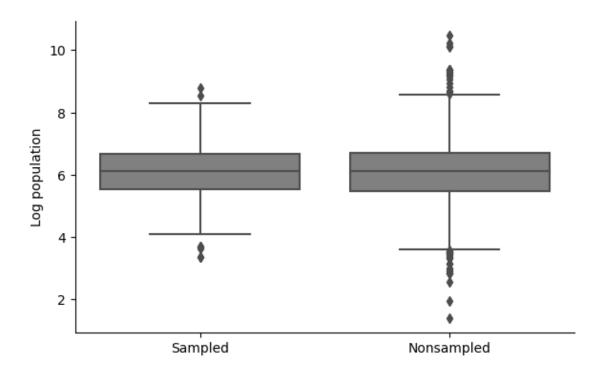
[]: <seaborn.axisgrid.FacetGrid at 0x1cf9e78fb20>



```
[]: # add the natural log of population to the data frame
afghan_village['log_pop'] = np.log(afghan_village['population'])

# boxplots for log population
sns.catplot(
    data=afghan_village, x='village_surveyed_desc', y='log_pop', kind='box',
    color='gray', height=4, aspect=1.5
).set(ylabel='Log population', xlabel='')
```

[]: <seaborn.axisgrid.FacetGrid at 0x1cf9f95b610>



# Section 3.4.2: Nonresponse and Other Sources of Bias

Logar

Uruzgan

0.000000

0.020672

```
[]: afghan.groupby('province')['violent.exp.taliban'].apply(
         lambda x: x.isnull().mean()
     )
[]: province
    Helmand
                0.030409
                0.006349
     Khost
    Kunar
                0.000000
    Logar
                0.000000
    Uruzgan
                0.062016
    Name: violent.exp.taliban, dtype: float64
[]: afghan.groupby('province')['violent.exp.ISAF'].apply(
         lambda x: x.isnull().mean()
     )
[]: province
    Helmand
                0.016374
    Khost
                0.004762
    Kunar
                0.000000
```

```
Name: violent.exp.ISAF, dtype: float64
```

```
[]: (afghan['list.response'][afghan['list.group'] == 'ISAF'].mean() -
    afghan['list.response'][afghan['list.group'] == 'control'].mean())
```

#### []: 0.0490196078431373

[]:	group	control	ISAF	taliban
	response			
	0	188	174	0
	1	265	278	433
	2	265	260	287
	3	200	182	198
	4	0	24	0

## Section 3.5: Measuring Political Polarization

## Section 3.6: Summarizing Bivariate Relationships

## Section 3.6.1: Scatter Plot

```
[]: congress = pd.read_csv('congress.csv')
congress.head()
```

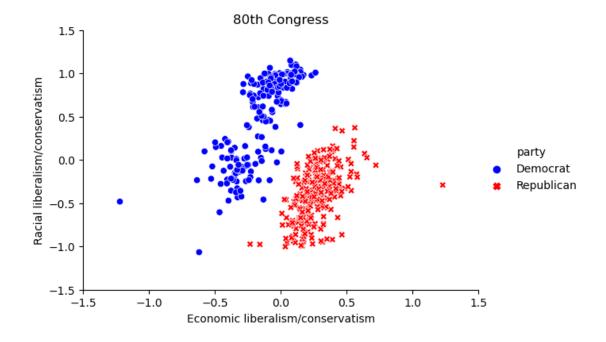
```
[]:
        congress
                 district
                              state
                                        party
                                                      name
                                                            dwnom1
                                                                    dwnom2
     0
                                                            -0.276
                                                                     0.016
              80
                         0
                                USA Democrat
                                                    TRUMAN
     1
              80
                         1 ALABAMA Democrat
                                                BOYKIN F.
                                                            -0.026
                                                                     0.796
     2
              80
                         2 ALABAMA
                                     Democrat
                                                 GRANT G.
                                                            -0.042
                                                                     0.999
     3
              80
                         3 ALABAMA Democrat ANDREWS G.
                                                            -0.008
                                                                     1.005
     4
              80
                         4 ALABAMA Democrat
                                                 HOBBS S.
                                                            -0.082
                                                                     1.066
```

# []: congress.dtypes

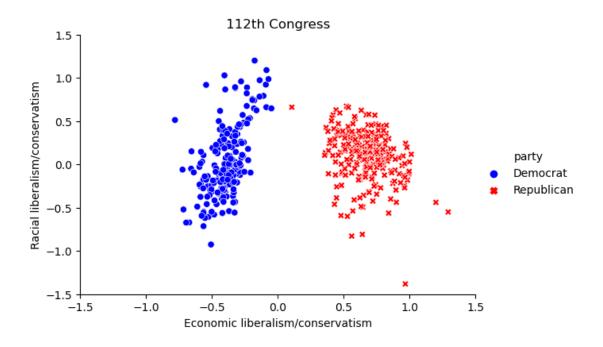
```
[]: congress int64
district int64
state object
party object
name object
dwnom1 float64
dwnom2 float64
```

dtype: object

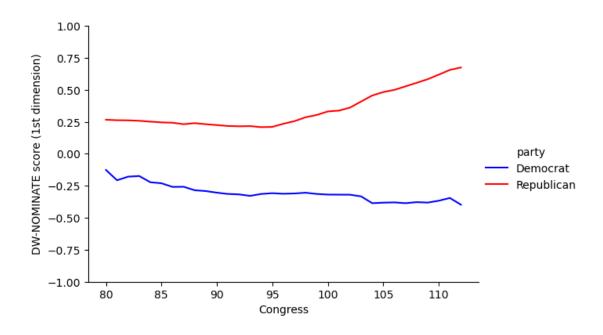
[]: <seaborn.axisgrid.FacetGrid at 0x1cf9faa7220>



[]: <seaborn.axisgrid.FacetGrid at 0x1cf9e6ffeb0>



[]: <seaborn.axisgrid.FacetGrid at 0x1cf9fbc3f10>



### Section 3.6.2: Correlation

```
[]: gini = pd.read_csv('USGini.csv')
     Calculate the difference between the Republican and Democratic medians.
     pandas will try to align indexes in conducting vector arithmetic. Therefore,
     it is best to reset the index and drop the old one so that the indexes are the
     same. An alternative is to use numpy arrays.
     111
     med_diff = (
         dwn1_med['dwnom1'][dwn1_med.party=='Republican'].reset_index(drop=True) -
         dwn1_med['dwnom1'][dwn1_med.party=='Democrat'].reset_index(drop=True)
     )
     # time series plot for partisan differences
     \# notice, we can feed x and y directly
     sns.relplot(
         x=np.arange(1947.5, 2012.5, step=2), y=med_diff, kind='line',
         color='black', height=4, aspect=1.5
     ).set(title='Political Polarization', xlabel='Year',
           ylabel='Republican median - Democratic median')
```

[]: <seaborn.axisgrid.FacetGrid at 0x1cf9fccbca0>



```
[]: # time-series plot for Gini coefficient
sns.relplot(
   data=gini, x='year', y='gini', kind='line', color='black',
   height=4, aspect=1.5
).set(title='Income Inequality', ylabel='Gini coefficient', xlabel='Year')
```

[]: <seaborn.axisgrid.FacetGrid at 0x1cf9fe59cc0>



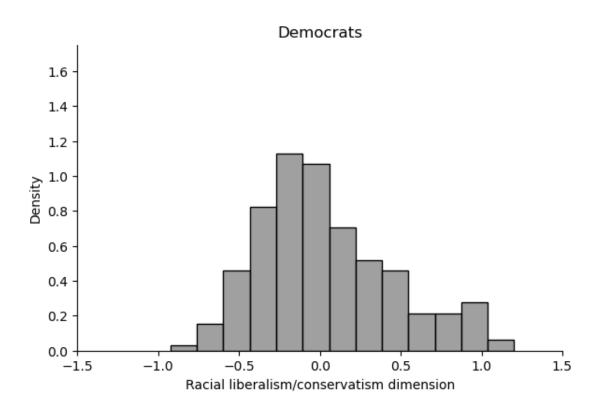
To correlate the partisan difference with the Gini coefficient, we need to select every other observation for the Gini starting with the second observation.

```
[]: (gini['gini'].iloc[np.arange(1, gini.shape[0], step=2)].
reset_index(drop=True).corr(med_diff))
```

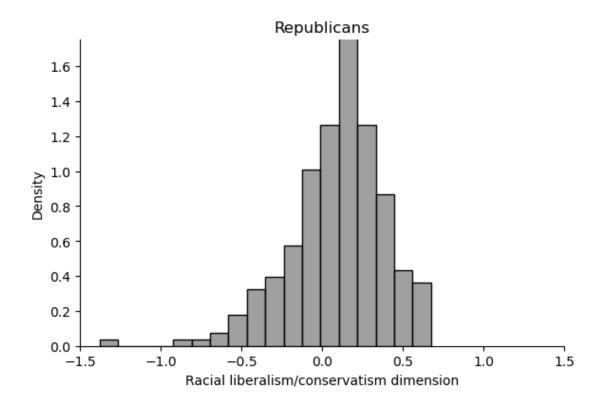
### []: 0.9418128160619333

# Section 3.6.3: Quantile-Quantile Plot

[]: <seaborn.axisgrid.FacetGrid at 0x1cf9ff0a440>

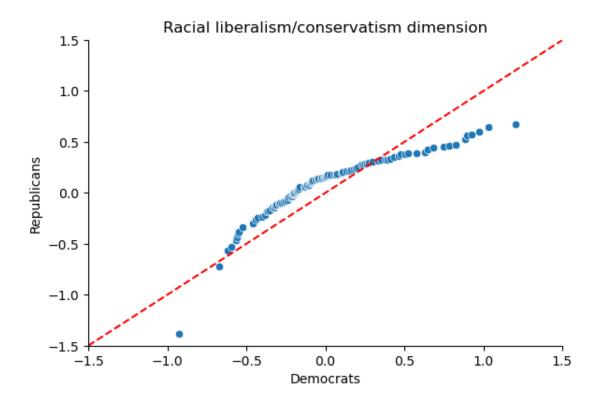


[]: <seaborn.axisgrid.FacetGrid at 0x1cfa10ac100>



Seaborn does not have a built-in function for Q-Q plots. However, we can create a scatterplot of the quantiles of two variables. The quantiles we plot need to be the same length. Below, we calculate and plot percentiles.

[]: <matplotlib.lines.\_AxLine at 0x1cfa16c7eb0>



## Section 3.7: Clustering

Before implementing clustering with the k-Means algorithm, we discuss numpy arrays and objects in Python, both of which are important for many Python modeling libraries.

## Section 3.7.1: Numpy Arrays

Thus far, we have used the numpy library for specific tasks, such as vectorized if-else statements using np.where() and log transformations using np.log(), but we have primarily relied on pandas for our analytical infrastructure. Having at least a high-level understanding of how numpy works is important for effective data analytics in Python. Indeed, pandas is built on top of numpy. While Python modeling libraries often work well with pandas, they occasionally work better with numpy, and many modeling outputs are numpy objects, as we will see in 3.7.3.

The fundamental numpy data structure is the N-dimensional array, known as the ndarray. For those coming from an R background, a one-dimensional numpy array is similar to a vector in R. There are a number of ways to create a numpy vector, depending on the analytical context.

```
[]: # One-dimensional arrays as vectors

# create a one-dimensional numpy array

## from a list
x = np.array([10, 20, 30, 40, 50])
```

```
Х
[]: array([10, 20, 30, 40, 50])
[]: ## from a sequence
     y = np.arange(10, 60, 10)
     У
[]: array([10, 20, 30, 40, 50])
[]: | ## from random draws from a uniform distribution between 50 and 100
     z = np.random.uniform(low=50, high=100, size=10)
     z
[]: array([80.42240937, 76.66056416, 82.79147704, 78.53086231, 59.40114555,
            59.46728769, 85.28013688, 88.64502818, 57.20413374, 96.81197204])
    Indexing and slicing numpy arrays is similar to indexing and slicing Python lists.
[]: # select the first observation from z
     ## recall, Python uses zero-based indexing
     z[0]
[]: 80.4224093715301
[]: # select the first five observations from z
     ## recall, Python uses "up to but not including" slicing semantics
     z[0:5]
[]: array([80.42240937, 76.66056416, 82.79147704, 78.53086231, 59.40114555])
[]: # select the fifth observation onward
     z[4:]
[]: array([59.40114555, 59.46728769, 85.28013688, 88.64502818, 57.20413374,
            96.81197204])
    In base Python, we need to use for loops to perform operations on each element of a list. Numpy,
    by contrast, enables vectorized computations.
[]: | # conduct vectorized arithmetic: multiply each element by .25
```

[]: array([20.10560234, 19.16514104, 20.69786926, 19.63271558, 14.85028639, 14.86682192, 21.32003422, 22.16125705, 14.30103343, 24.20299301])

z \* .25

```
[]: # conduct conditional vectorized arithmetic
     ## if an element is above 75, multiply by .25; otherwise, multiply by .75
     np.where(z > 75, z * .25, z * .75)
[]: array([20.10560234, 19.16514104, 20.69786926, 19.63271558, 44.55085916,
            44.60046577, 21.32003422, 22.16125705, 42.9031003 , 24.20299301])
[]: # calculate the sum of the elements
     z.sum()
[]: 765.2150169643911
[]: # calculate the mean of the elements
     z.mean()
[]: 76.52150169643912
    Two-dimensional numpy arrays can be thought of as matrices.
[]: # create a two-dimensional numpy array from a range
     mat = np.arange(0, 10).reshape(5, 2)
     mat
[]: array([[0, 1],
            [2, 3],
            [4, 5],
            [6, 7],
            [8, 9]])
[]: # select the first row
     mat[0]
[]: array([0, 1])
[]: # select the second column
     mat[:,1]
[]: array([1, 3, 5, 7, 9])
[]: # select the first two rows and the second column
     mat[0:2, 1]
[]: array([1, 3])
[]: # calculate the sum of the columns
     mat.sum(axis=0)
[]: array([20, 25])
```

```
[]: # calculate the mean of the rows
mat.mean(axis=1)

[]: array([0.5, 2.5, 4.5, 6.5, 8.5])
```

```
[]: # calculate the standard deviation of the columns mat.std(axis=0)
```

[]: array([2.82842712, 2.82842712])

A matrix generally must have the same data type for all elements. A data frame can have different data types for each column.

```
[]: df = pd.DataFrame({'x': ['a', 'b', 'c'], 'y': [1, 2, 3]})
    df.dtypes # contains a string and an integer

[]: x    object
    y    int64
    dtype: object
```

```
[]: np.array(df).dtype # produces a dtype 'O' for object; in other words, a string
```

[]: dtype('0')

#### Section 3.7.2: Objects in Python

In Python, it is said that "everything is an object." Python makes heavy use of object oriented programming (OOP), a programming paradigm that involves grouping code and data together into objects. In OOP, an object is created from a template called a "class." The data associated with objects are generally called attributes, and the functions are called methods. Libraries like pandas, numpy, and seaborn are designed so that we do not have to worry too much about OOP particulars. Still, it is important to recognize that we are working with objects of specific classes that have attributes and methods.

```
[]: # check the object class type(congress)
```

[]: pandas.core.frame.DataFrame

```
[]: # review an object's methods and attributes; print the first 15 dir(congress)[0:15]
```

```
'__add__',
      '__and__',
      '__annotations__',
      '__array__',
      '__array_priority__',
      '__array_ufunc__',
       __bool__',
      '__class__',
      '__contains__']
[]: # use a list comprehension to view the non-private attributes and methods
     [item for item in dir(congress) if not item.startswith('_')][0:15]
[]: ['T',
      'abs',
      'add',
      'add_prefix',
      'add_suffix',
      'agg',
      'aggregate',
      'align',
      'all',
      'any',
      'apply',
      'applymap',
      'asfreq',
      'asof',
      'assign']
[]: # use the data frame's value_counts "method"
     congress['party'].value_counts()
[]: party
    Democrat
                   8132
     Republican
                   6401
     Other
                     19
     Name: count, dtype: int64
[]: # review the data frame's shape "attribute"
     congress.shape
[]: (14552, 7)
```

As we will see in 3.7.3, some important modeling libraries in Python, such as scikit-learn, rely on a more conventional OOP workflow. In such a workflow, one generally follows a few key steps:

- Select a class.
- Instantiate an object of the class and set desired parameters.
- Use the object's methods to perform operations on data.

• Extract results from the object.

#### Section 3.7.3: The k-Means Algorithm

```
[]: from sklearn.cluster import KMeans
  dwnom80 = congress.loc[congress['congress']==80, ['dwnom1', 'dwnom2']].copy()
  dwnom112 = congress.loc[congress['congress']==112, ['dwnom1', 'dwnom2']].copy()
  # kmeans with two clusters

## instantiate the model with parameters
  k80two = KMeans(n_clusters=2, n_init=5)
  k112two = KMeans(n_clusters=2, n_init=5)
```

If you are working on Windows, you may get a warning about about memory leakage associated with using KMeans on Windows. The warning will likely recommend setting the environmental variable OPM\_NUM\_THREADS to a certain value. To do so, follow these steps:

- (1) Click on the Windows Search button
- (2) Type "Edit the system environment variables"
- (3) Select "Environment Variables"
- (4) Click "New" under "User variables for your\_username"
- (5) Enter "OMP\_NUM\_THREADS" for the variable name and '1' or the number recommended in the warning for the variable value
- (6) Click "OK" and close the windows

```
[]: ## fit the model to the data
k80two.fit(dwnom80)
k112two.fit(dwnom112)

## predict the clusters
k80two_labels = k80two.predict(dwnom80)
k112two_labels = k112two.predict(dwnom112)

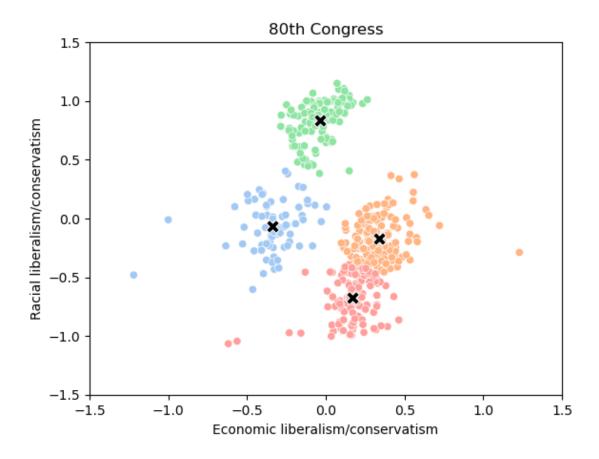
type(k80two_labels) # numpy.ndarray
```

[]: numpy.ndarray

```
[]: # Use a list comprehension to view the non-private methods and attributes [item for item in dir(k80two) if not item.startswith('_')]
```

```
'feature_names_in_',
      'fit',
      'fit_predict',
      'fit_transform',
      'get_feature_names_out',
      'get_params',
      'inertia_',
      'init',
      'labels_',
      'max_iter',
      'n_clusters',
      'n_features_in_',
      'n_init',
      'n_iter_',
      'predict',
      'random_state',
      'score',
      'set_output',
      'set_params',
      'tol',
      'transform',
      'verbose']
[]: # final centroids
     k80two.cluster_centers_
[]: array([[-0.04843704, 0.78272593],
            [ 0.14681029, -0.33892926]])
[]: k112two.cluster_centers_
[]: array([[ 0.67767355, 0.09061157],
            [-0.39126866, 0.03260696]])
[]: type(k112two.cluster_centers_) # numpy.ndarray
[]: numpy.ndarray
[]: # number of observations for each cluster by party
     pd.crosstab(congress['party'][congress.congress == 80],
                 k80two_labels, colnames=['cluster'])
[]: cluster
                   0
                        1
    party
    Democrat
                 132
                       62
     Other
                        2
                   0
    Republican
                   3 247
```

```
[]: pd.crosstab(congress['party'][congress.congress == 112],
                k112two_labels, colnames=['cluster'])
[]: cluster
                  0
    party
    Democrat
                  0 200
    Republican 242
[]: # k means with four clusters
     k80four = KMeans(n clusters=4, n init=5)
     k112four = KMeans(n_clusters=4, n_init=5)
     k80four.fit(dwnom80)
     k112four.fit(dwnom112)
     k80four_labels = k80four.predict(dwnom80)
    k112four_labels = k112four.predict(dwnom112)
[]: # plot the centroids over the clusters using subplots
     fix, ax = plt.subplots(1,1)
     sns.scatterplot(
        data=dwnom80, x='dwnom1', y='dwnom2', hue=k80four_labels, legend=False,
        palette='pastel', ax=ax,
        ).set(title='80th Congress', xlabel=xlab, ylabel=ylab, xlim=lim, ylim=lim)
     sns.scatterplot(
        x=k80four.cluster_centers_[:,0], y=k80four.cluster_centers_[:,1],
        legend=False, color='black', s=100, marker='X', ax=ax,
        )
[]: <Axes: title={'center': '80th Congress'}, xlabel='Economic
     liberalism/conservatism', ylabel='Racial liberalism/conservatism'>
```



```
[]: # repeat for 112th congress
fix, ax = plt.subplots(1,1)

sns.scatterplot(
    data=dwnom112, x='dwnom1', y='dwnom2', hue=k112four_labels, legend=False,
    palette='pastel', ax=ax,
    ).set(title='112th Congress', xlabel=xlab, ylabel=ylab, xlim=lim, ylim=lim)

sns.scatterplot(
    x=k112four.cluster_centers_[:,0], y=k112four.cluster_centers_[:,1],
    legend=False, color='black', s=100, marker='X', ax=ax,
    )
```

[]: <Axes: title={'center': '112th Congress'}, xlabel='Economic liberalism/conservatism', ylabel='Racial liberalism/conservatism'>

