Math-42 Worksheet #14

Integer Representations and Algorithms

- 1. Convert decimal 1000 to:
 - (a) Binary
 - (b) Base 3
 - (c) Octal
 - (d) Hexadecimal
- 2. Convert to decimal:
 - (a) 101110110_2
 - (b) 12012021₃
 - (c) 17352_8
 - (d) $1CF3_{16}$
- 3. Complete the following table:

BINARY	OCTAL	DECIMAL	HEXADECIMAL
1011011110			
	175264		
		65536	
			F19A

- 4. Is 157834 a valid octal number? Why or why not?
- 5. Complete the following addition and multiplication tables using the base suggested by the number of digits—they will be helpful for the following exercise.

+	0	1
0		
1		

	0	1
0		
1		

+	0	1	2
0			
1			
2			

•	0	1	2
0			
1			
2			

+	0	1	2	3	4	5	6	7
0								
1								
2								
3								
4								
5								
6								
7								

•	0	1	2	3	4	5	6	7
0								
1								
3								
3								
4								
5								
6								
7								

+	0	1	2	3	4	5	6	7	8	A	B	C	D	E	F
0															
1															
2															
3															
4															
5															
6															
7															
8															
9															
A															
B															
C															
D															
$\mid E \mid$															
F															

•	0	1	2	3	4	5	6	7	8	A	B	C	D	E	F
0															
1															
2															
3															
4															
5															
6															
7															
8															
9															
A															
B															
C															
D															
E															
F															

6. Perform the following operations in the specified bases:

- (a) $11010101111_2 + 100010110_2$
- (b) $1101010111_2 \cdot 10110_2$
- (c) $2210120_3 + 1102_3$
- (d) $2210120_3 \cdot 1102_3$
- (e) $17534_8 + 61234_8$
- (f) $17534_8 \cdot 6102_8$
- (g) $F10A3_{16} + 1DC29_{16}$
- (h) $F10A3_{16} \cdot 20C_{16}$

7. Use fast exponentiation to calculate the following:

- (a) $7^{100} \mod 321$
- (b) $13^{300} \mod 209$