

Cubic Extensions

Theorem

Let K/\mathbb{Q} be a finite extension of fields. K/\mathbb{Q} is Galois iff K is the splitting field of some (monic) irreducible $f(x) \in F[x]$. Furthermore, all of the roots of $f(x)$ are distinct and thus $f(x)$ is separable.