

Math-71 Sections 9, 11, 12

Homework #1

Due: 2/5/2019 5:45pm

Reading

- Read section 7.1 very carefully, keeping in mind our discussion of *arbitrarily close*.
- Read section 7.2.
- Review section 0.4, paying careful attention to rationalizing with the conjugate.
- Review section 3.7 (and the relevant previous sections in chapter 3) so that you can sketch polynomials and rational functions.

Special Office Hours

On Friday, 2/1, I am going to hold special office hours from 9am to noon for an *optional* review of sketching polynomials and rational functions (chapter 3). I think that we can just review section 0.4 in class. I will hold two sessions:

- 9–10:30
- 10:30–noon

I will take an informal count of who wants to attend which session in class on Tuesday. This is entirely optional, so you can attend zero, one, or both sessions.

Problem

You are a business analyst for the city of Lakeside, California. Lakeside is famous for its huge lake, which unfortunately has become polluted with carbon compounds over the years by a nearby factory. The factory is now closed, so the city council wants to clean up the lake. They have made you the head of the project. You contact the EPA and find out three important things:

1. The lake can be cleaned up to what is considered to be a naturally-occurring level of the carbon pollutants by removing 80% of the pollutants.
2. The cost, in *millions* of dollars, to reduce the pollutants in the lake to a given percentage p is estimated by the following formula (function):

$$C(p) = \frac{10p}{100 - p}$$

3. EPA standards say that cleaning up 75% of the pollutants is good enough, because the extra 5% doesn't do any significant harm.

You decide that the best way to raise the money for this project is to hold a special election for a local ballot initiative to assess a special charge on next year's property tax bill. You know that the population of Lakeside is 100,000 people, of which 80% are property owners.

- (a) Assuming that the property tax burden is to be distributed equally, what will be the resulting assessment on each property tax bill under the federal requirements?
- (b) Governor Newsom visits the lake with a state EPA representative. They tell you that California leads the nation in environmental policy, so he says that the state requirement is to bring the pollutant level all the way to the natural level. What is the resulting property tax bill assessment now?
- (c) Some members from the group *Save the Fish!* protest outside your office. They claim that the lake is home to a rare species of fish that is being harmed by the pollutants. They demand that you decrease the pollutant level by 95% and if you don't then they are going to sue you in federal court under the endangered species act. What would be the resulting property bill assessment for that level of cleanup?
- (d) What does the formula tell you about removing *all* of the pollutants from the lake and why do you think this might be so?
- (e) Over what values of percentage p , expressed in interval notation, is the function represented by the formula continuous?