Notation

Let
$$f(z) = f(x + iy) = u(x, y) + iv(x, y)$$
:

•
$$f(\bar{z}) = f(x - iy) = u(x, -y) + iv(x, -y)$$

•
$$\overline{f(z)} = u(x,y) - iv(x,y) = \overline{f}(\overline{z})$$

•
$$\bar{f}(z) = u(x, -y) - iv(x, -y) = \overline{f(\bar{z})}$$

Example

$$f(z) = iz^3$$

$$f(\bar{z}) = i\bar{z}^3$$

$$\overline{f(z)} = \overline{iz^3} = \overline{i}\,\overline{z^3} = -i\overline{z}^3$$

$$\bar{f}(z) = \overline{f(\bar{z})} = \overline{i\bar{z}^3} = -iz^3$$