

## Math-19 Section 1

### Homework #1

**Due: 6/10/2019 9:00am**

#### Reading

Sections 1.1–1.5

#### Problems

1. We have stated in class that there may be multiple syntaxes to represent each point on the real number line. For example, we saw how to convert finite decimal and infinite repeating decimal forms to rational numbers in integer ratio form.

- (a) Convert the rational number  $0.\overline{1}$  to integer ratio form using the process that we learned in class.
- (b) Without repeating the process, fill in the following table:

$0.\overline{1}$	
$0.\overline{2}$	
$0.\overline{3}$	
$0.\overline{4}$	
$0.\overline{5}$	
$0.\overline{6}$	
$0.\overline{7}$	
$0.\overline{8}$	

- (c) Based on this pattern, predict what  $0.\overline{9}$  equals. Prove this by repeating the process to convert it to an integer ration.
- (d) Explain why the answer you got in the previous problem is valid.
- (e) Without repeating the process, what do you think  $25.\overline{39}$  equals?

2. Consider the following two sets:

$$A = \{x \in \mathbb{R} \mid -1 < x \leq 3\}$$

$$B = \{x \in \mathbb{R} \mid x > 2\}$$

Show the graph and the interval notation for each of the following:

(a)  $A$

(b)  $B$

(c)  $A \cap B$

(d)  $A \cup B$

(e)  $A - B$

3. Simplify the following expression. Your answer should contain no radicals and no negative exponents. You may assume that  $a, b, c > 0$ . Hint: convert all the ugly radicals to rational exponents and be care with parentheses: note that there is a radical within a radical.

$$\frac{a^2 b^{-3} \sqrt{abc^3}}{\sqrt[3]{a^{-2} \sqrt{b^3 c}}}$$

4. Determine whether each of the following statements is either correct, incorrect, or misleading. Explain why incorrect and misleading statements are incorrect or misleading are fix them so that they are correct.

(a)  $\sqrt{9} = \pm 3$

(b)  $\left(x^{\frac{1}{2}}\right)^2 = |x|$

(c)  $(x^2)^{\frac{1}{2}} = x$

(d)  $(x^3)^{\frac{1}{3}} = |x|$