

國立中興大學

109 學年度

碩士班考試入學招生

試 題

學系：資訊科學與工程學系

甲組

科目名稱：基礎數學 A

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本科目不得使用計算機

本科目試題共 2 頁

1. If  $A$  is an  $n \times n$  matrix, derive the characteristic polynomial of  $A$ . (7%)

2. Let  $W \subset \mathbb{R}^4$  be the subspace of vectors  $(x_1, x_2, x_3, x_4)$  satisfying  $2x_1 - x_3 + 4x_4 = 0$ . Find an orthonormal basis for  $W$ . (10%)

3. Solve the differential equations, where  $x(0) = 1$  and  $y(0) = 0$ . (7%)

$$\frac{dx}{dt} = 3x - 4y, \quad \frac{dy}{dt} = 2x - 3y.$$

4. Please explain the reason if there is an orthogonal transformation  $T$  from  $\mathbb{R}^3$  to  $\mathbb{R}^3$ . (5%)

$$T \begin{bmatrix} 2 \\ 5 \\ 0 \end{bmatrix} = \begin{bmatrix} 5 \\ 0 \\ 2 \end{bmatrix} \quad \text{and} \quad T \begin{bmatrix} -5 \\ 2 \\ 0 \end{bmatrix} = \begin{bmatrix} 2 \\ -5 \\ 0 \end{bmatrix}$$

5. Given a matrix  $A$ , find (a) the reduced row echelon form  $R$  and the rank of  $A$ , (b) a low triangular matrix  $L$  and an upper triangular matrix  $U$  so that  $A = LU$ , and (c) the null space of  $A$ . (15%)

$$A = \begin{bmatrix} 2 & 4 & -2 & 2 & 4 \\ 5 & 10 & -4 & 5 & 9 \\ 3 & 6 & -2 & 1 & 9 \\ 1 & 2 & -1 & 2 & 0 \end{bmatrix}.$$

6. Let  $A = \begin{bmatrix} 0 & 1 \\ 2 & 3 \end{bmatrix}$ . Show that  $A^2 = \begin{bmatrix} 5 & 3 \\ 6 & 14 \end{bmatrix}$  is linear combination of  $A$  and  $I_2$ . (6%)

7. Please calculate  $4^{532} \pmod{11}$ . (10%)

8. Let  $A = \{7, 8, 9\}$ . Please list all the subsets of  $A$ . (10%)

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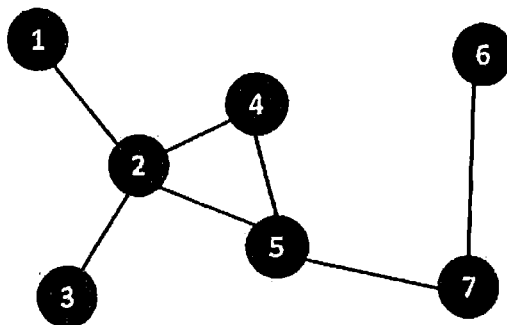
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9. Please identify the minimum dominating set of the graph below. (15%)



10. Given a group  $G$  with  $|G| = p$ , where  $p$  is a prime number. How many different sizes of subgroups can  $G$  have? (15%)