

CHEM / BCMB 4190/6190/8189

Introductory NMR

Lecture 12

The INEPT Experiment

Sensitivity problem in NMR:

\mathcal{E} = electromagnetic induction force in detection coil

$$\varepsilon \propto N \gamma^3 \hbar^2 B_0^2 I(I+1) / (3k_B T)$$

Small S/N in spectra of insensitive nuclei with low natural abundance (e.g. ^{13}C , ^{15}N) is a main problem in NMR spectroscopy of organic molecules. Example

$$\frac{\varepsilon(^{13}\text{C})}{\varepsilon(^1\text{H})} = \frac{1.1\% * 1}{100\% * 4^3} = \frac{1}{5818}$$

One would need to record ~33 million (5818^2) more scans in a 1D ^{13}C spectrum to get equal signal intensity than in a 1D ^1H spectrum!

Solutions to this problem are:

- 1) Get more sample
- 2) Isotope labeling (may be expensive and not practical)
- 3) Record spectrum at higher field (B_0)
- 4) Record spectrum at lower temperature (not significant effect)
- 5) Special NMR experiments

Selective Population Inversion (SPI) Experiment:

- **Advantage of SPI:** Very useful to explain the principle of Selective Population Transfer that provides a means to "recover" one of the γ factor.
- **Disadvantage of SPI:** Not very practical because selective pulses are used.

Lets consider the two-spin AX system ($^{13}\text{CHCl}_3$)

with $\text{A} = ^1\text{H}$ = sensitive nuclei

and $\text{X} = ^{13}\text{C}$ = insensitive nuclei

A) At equilibrium:

$$\text{N4} = \text{N}$$

$$\text{N3} = \text{N} + \Delta\text{C}$$

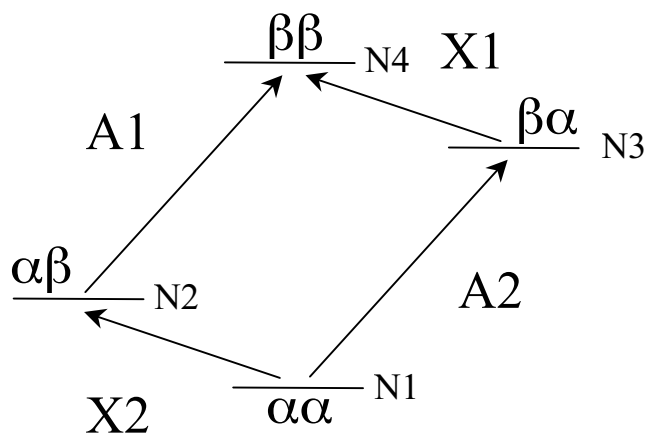
$$\text{N2} = \text{N} + \Delta\text{H}$$

$$\text{N1} = \text{N} + \Delta\text{C} + \Delta\text{H}$$

$$\text{N2} - \text{N4} \approx \text{N1} - \text{N3} = \Delta\text{H}$$

$$\text{N3} - \text{N4} \approx \text{N1} - \text{N2} = \Delta\text{C}$$

$$\Delta\text{H} = 4 * \Delta\text{C}$$



For ^{13}C spectrum:

$$\text{X1 transition: } \text{N3} - \text{N4} = \Delta\text{C}$$

$$\text{X2 transition: } \text{N1} - \text{N2} = \Delta\text{C}$$



B) After a selective 180° pulse exciting the A2 transition:

The populations of N1 and N3

are inverted:

$$N4 = N$$

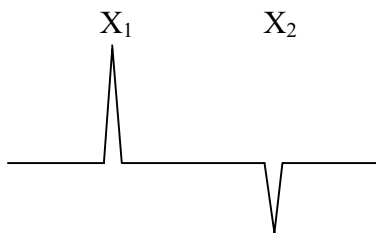
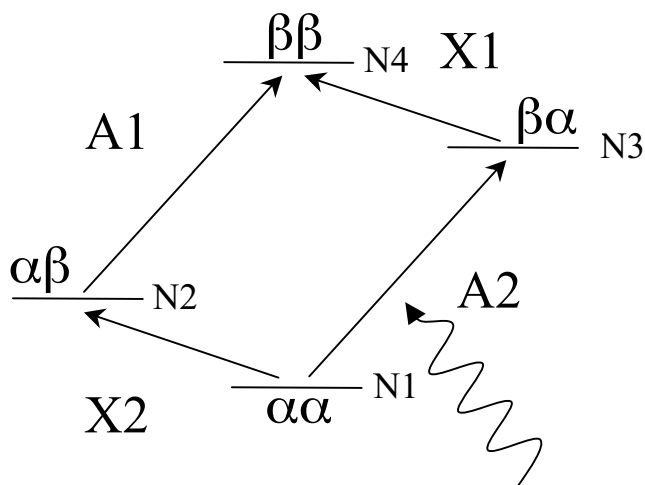
$$N3 = N + \Delta C + \Delta H$$

$$N2 = N + \Delta H$$

$$N1 = N + \Delta C$$

$$\text{X1 transition: } N3 - N4 = \Delta C + \Delta H = 5\Delta C$$

$$\text{X2 transition: } N1 - N2 = \Delta C - \Delta H = -3\Delta C$$



C) After a selective 180° pulse exciting the A1 transition:

The populations of N2 and N4

are inverted:

$$N4 = N + \Delta H$$

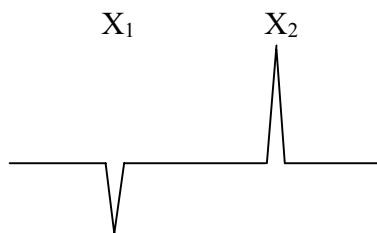
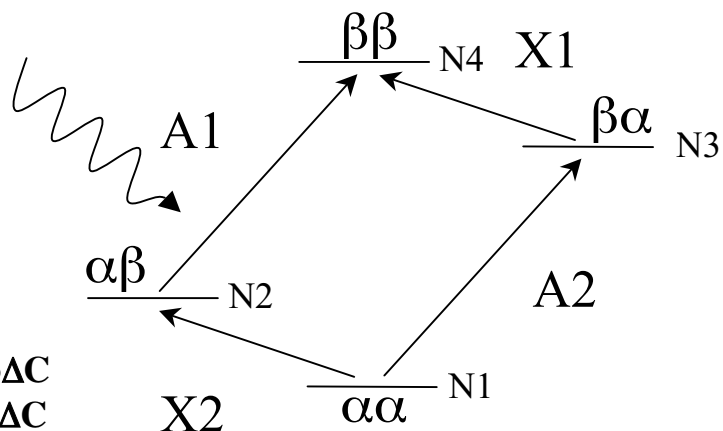
$$N3 = N + \Delta C$$

$$N2 = N$$

$$N1 = N + \Delta C + \Delta H$$

$$\text{X1 transition: } N3 - N4 = \Delta C - \Delta H = -3\Delta C$$

$$\text{X2 transition: } N1 - N2 = \Delta C + \Delta H = 5\Delta C$$



After selective inversion of the A1 or A2 transition, the signal amplification factors for the spectra of X are given by:

$$1 + \gamma_A / \gamma_X \text{ and } 1 - \gamma_A / \gamma_X$$

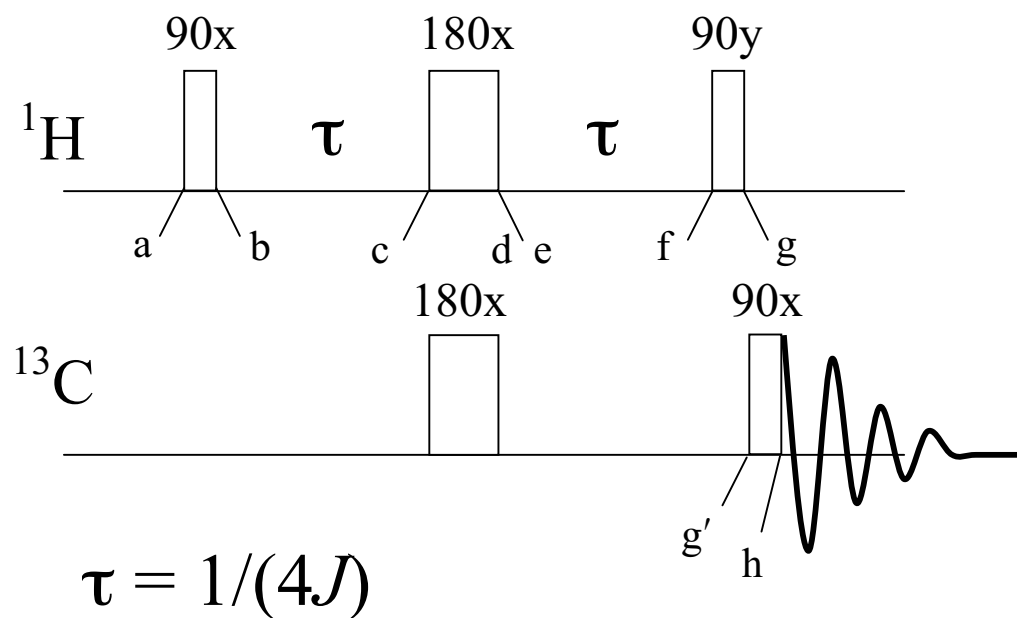
The INEPT experiment:

INEPT: Insensitive Nuclei Enhanced by Polarization Transfer
Polarization transfer achieved using non-selective pulses

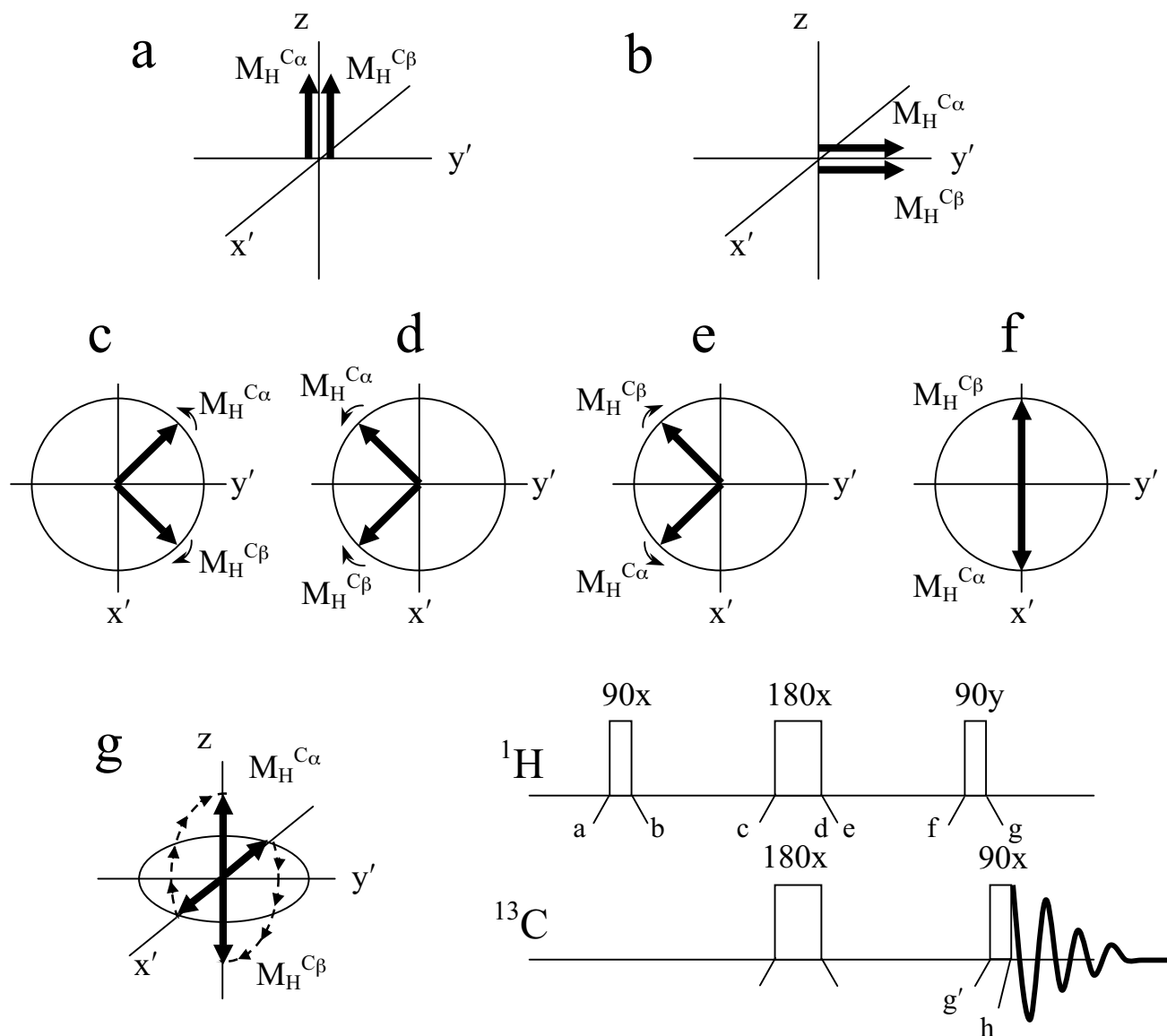
Example: $^{13}\text{CHCl}_3$

A) Pulse sequence in the ^1H and ^{13}C channels

(Note: without carbon pulses, this is a spin-echo experiment on ^1H)



B) Vector diagrams showing the ^1H magnetization vectors



a: $M_H^{C\alpha}$ and $M_H^{C\beta}$ are of approximately equal populations

b: $\nu(^{13}\text{C}_\alpha\text{HCl3}) = \nu_H - J_{\text{CH}}/2$ and $\nu(^{13}\text{C}_\beta\text{HCl3}) = \nu_H + J_{\text{CH}}/2$

c- d: until then just like beginning of a spin-echo experiment on ^1H

e: Effect of ^{13}C 180° :

- phase of 180° doesn't matter (x or y), M_C from z to $-z$
- inverts population between N1 and N2 and between N3 and N4
- $M_H^{C\alpha}$ becomes $M_H^{C\beta}$ and $M_H^{C\beta}$ becomes $M_H^{C\alpha}$

f: JCH continue to evolve instead of being refocused during the next τ delay

g: ^1H 90° pulse rotates $M_H^{C\alpha}$ to $+z$ and $M_H^{C\beta}$ to $-z$

Same effect as the SPI experiment, but without selective excitation!

The populations of N2 and N4

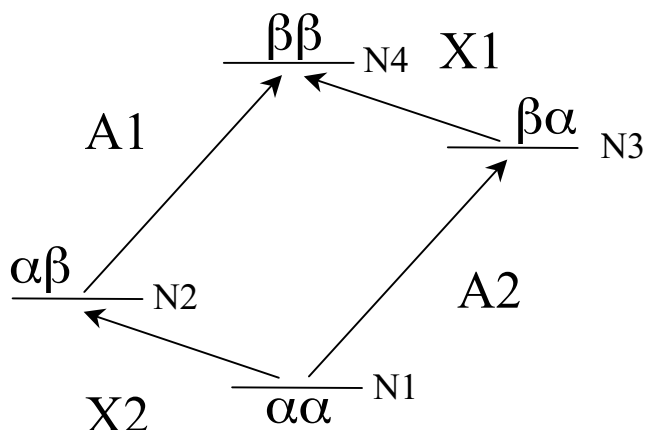
are inverted:

$$N4 = N + \Delta H$$

$$N3 = N + \Delta C$$

$$N2 = N$$

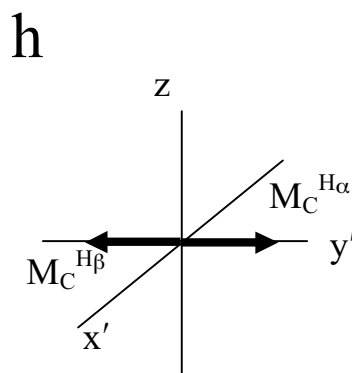
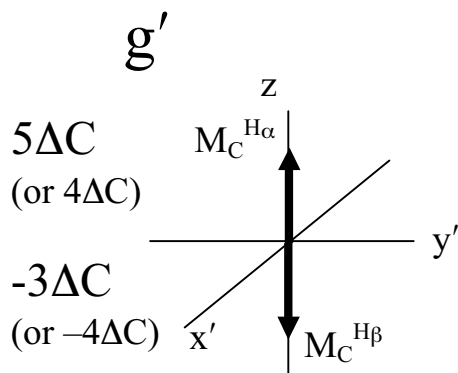
$$N1 = N + \Delta C + \Delta H$$



$$\text{X1 transition: } N3 - N4 = \Delta C - \Delta H = -3\Delta C$$

$$\text{X2 transition: } N1 - N2 = \Delta C + \Delta H = 5\Delta C$$

C) Vector diagrams showing the ^{13}C magnetization vectors



g': Note that $M_C^{H\alpha}$ is in its original position, but that $M_C^{H\beta}$ is inverted

h: The 90°_x pulse on ^{13}C create transverse magnetization components which are observable

The natural I spin magnetization in the INEPT experiment

In many applications of polarization transfer, the contribution from the natural ^{13}C magnetization (ΔC) is unwanted. There are multiple ways to remove it:

1) Presaturate ^{13}C at the start of the pulse sequence

2) Apply a 90° ^{13}C pulse followed by a gradient pulse at the start of the pulse sequence

In cases 1) and 2) the populations at point a are:

$$\mathbf{N4 = N + \Delta C/2}$$

$$\mathbf{N3 = N + \Delta C/2}$$

$$\mathbf{N2 = N + \Delta C/2 + \Delta H}$$

$$\mathbf{N1 = N + \Delta C/2 + \Delta H}$$

The populations at point g are (N2 and N4 inverted):

$$\mathbf{N4 = N + \Delta C/2 + \Delta H}$$

$$\mathbf{N3 = N + \Delta C/2}$$

$$\mathbf{N2 = N + \Delta C/2}$$

$$\mathbf{N1 = N + \Delta C/2 + \Delta H}$$

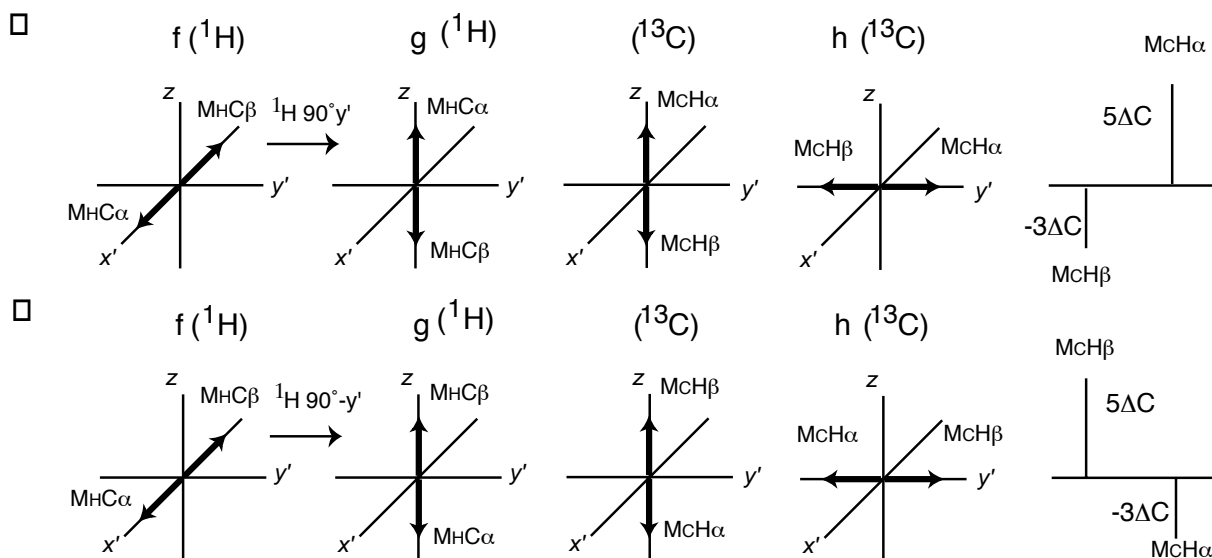
$$\mathbf{X1 \text{ transition: } N3 - N4 = -\Delta H = -4\Delta C}$$

$$\mathbf{X2 \text{ transition: } N1 - N2 = \Delta H = 4\Delta C}$$

3) By phase cycling

Collect 2 experiments, the phase of the last 90° pulse on ^1H changes between y and $-y$.

Lets analyze the effect of the 90° - y pulse.



At point g: ^1H 90° - y pulse rotates $M_{\text{H}}^{\text{C}\alpha}$ to $-z$ and $M_{\text{H}}^{\text{C}\beta}$ to $+z$
 Same effect as the SPI experiment, but without selective excitation!
 The populations of N1 and N3 are inverted:

$$N4 = N$$

$$N3 = N + \Delta C + \Delta H$$

$$N2 = N + \Delta H$$

$$N1 = N + \Delta C$$

$$\text{X1 transition: } N3 - N4 = \Delta C + \Delta H = 5\Delta C$$

$$\text{X2 transition: } N1 - N2 = \Delta C - \Delta H = -3\Delta C$$

We have seen the effect of the 90° - y pulse already.

$$\text{X1 transition: } N3 - N4 = \Delta C - \Delta H = -3\Delta C$$

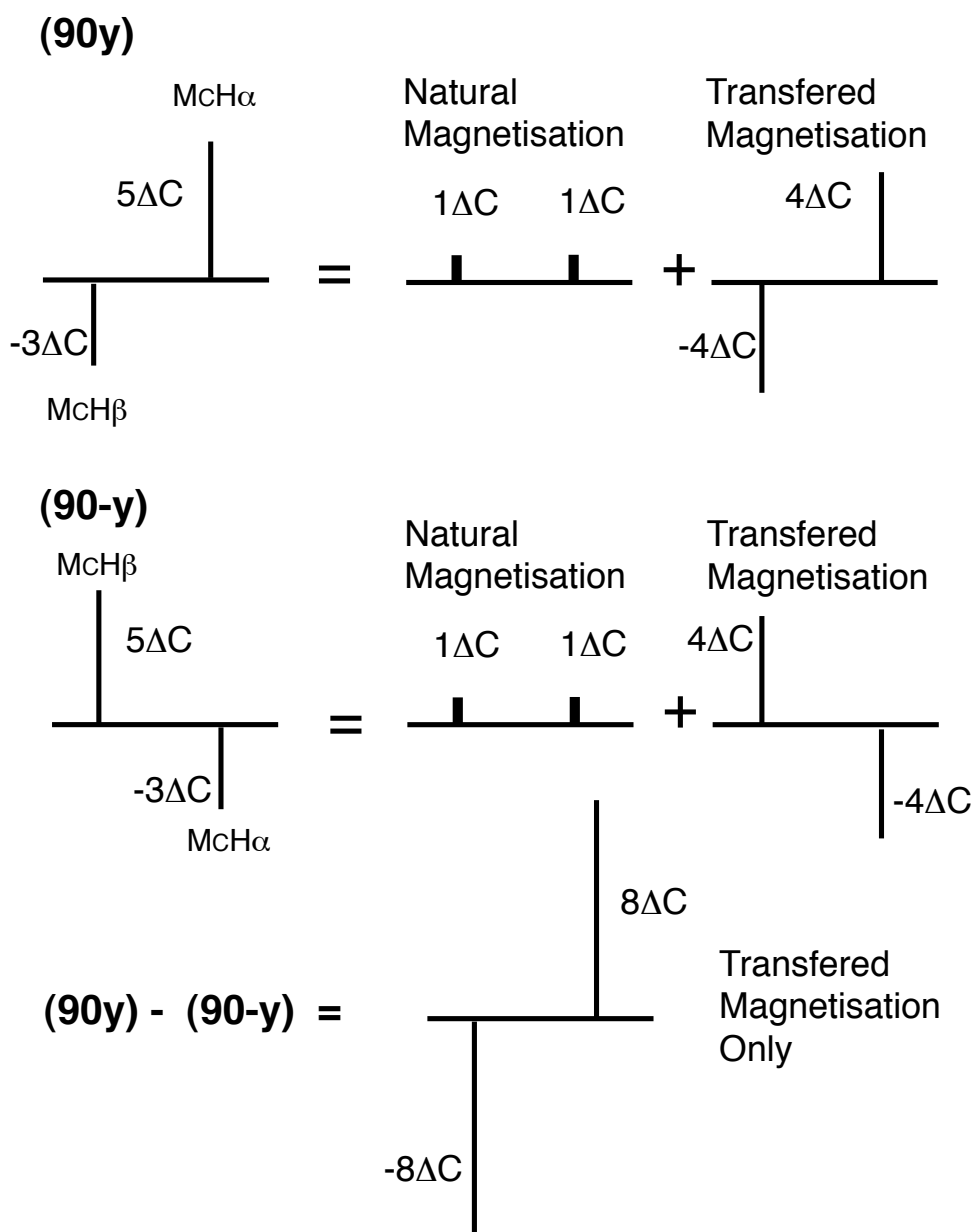
$$\text{X2 transition: } N1 - N2 = \Delta C + \Delta H = 5\Delta C$$

The first FID (with 90°_y) and the second FID (with 90°_{-y}) will be recorded with phases of 0° and 180° for the receiver. The net effect is subtraction of the first spectrum to the second spectrum.

For X1 transition: $-3\Delta C - (5\Delta C) = -8\Delta C$

For X2 transition: $5\Delta C - (-3\Delta C) = +8\Delta C$

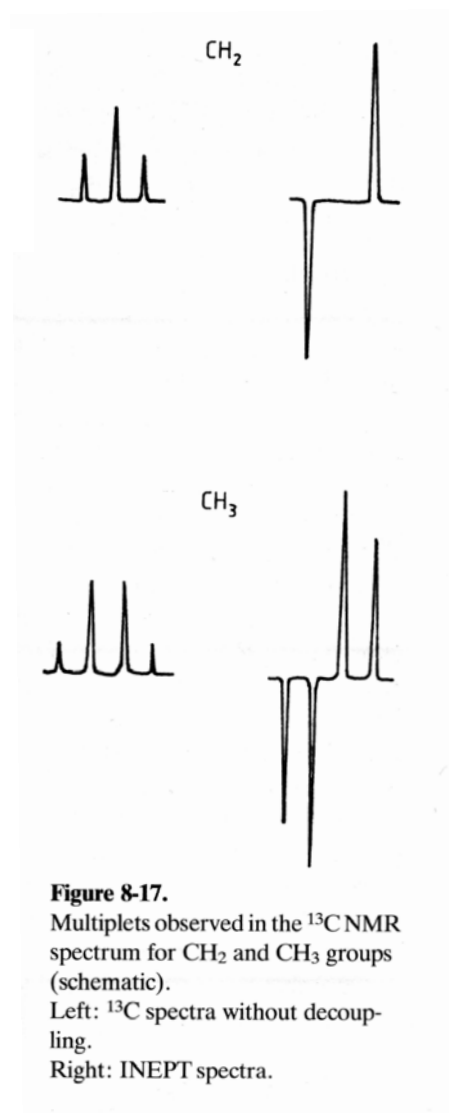
The trick here is that in these two experiments, the natural ^{13}C magnetization gives rise to a signal with a constant phase and the change in receiver phase will eliminate it.



INEPT pulse sequence applied to CH₂ and CH₃ groups

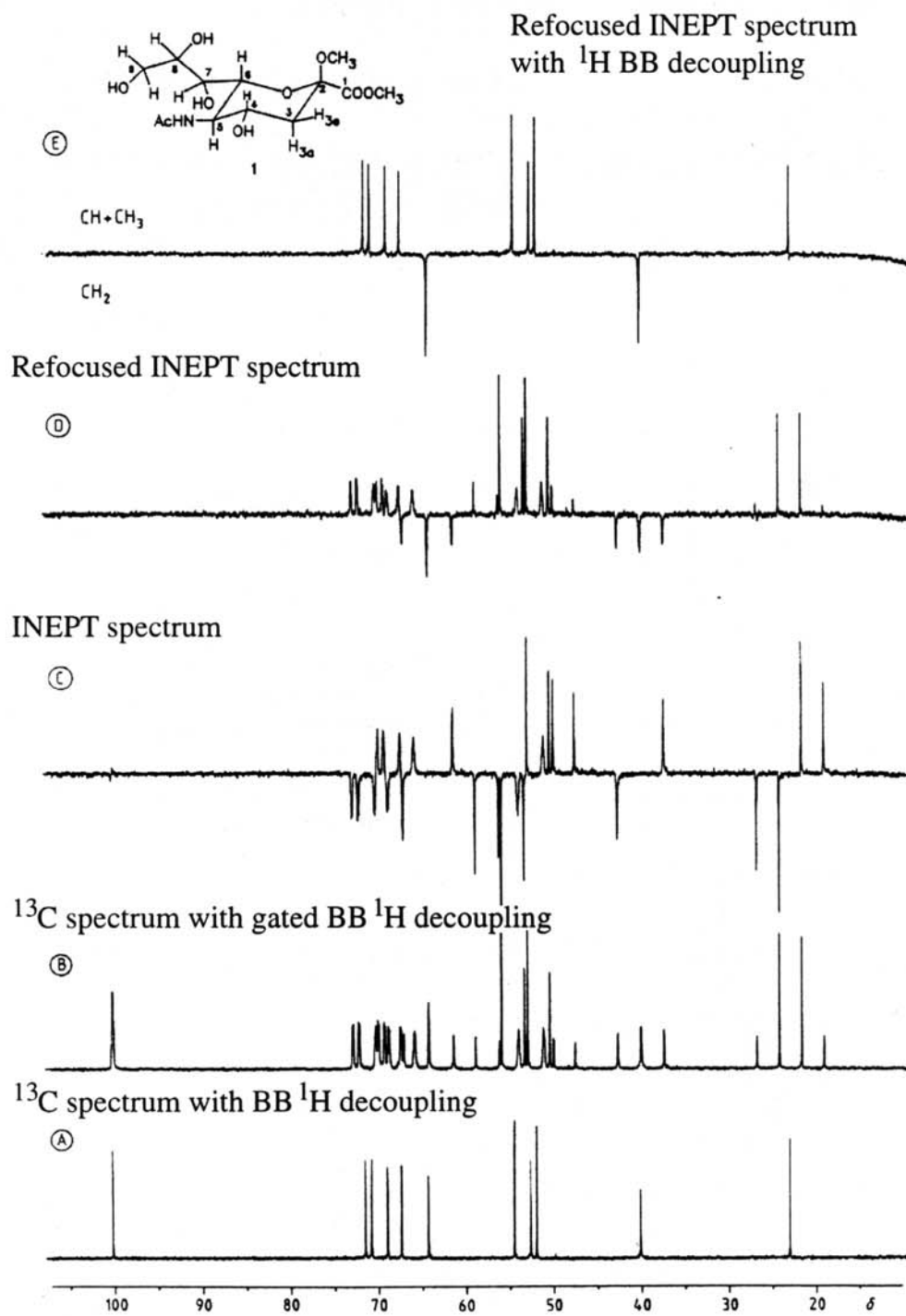
Use average value for τ ($J_{\text{CH}} = 125\text{-}150\text{ Hz}$)

	1D ¹³ C spectrum	INEPT spectrum
CH ₂ :	1:2:1	$-2\gamma(^1\text{H})/\gamma(^{13}\text{C}):0:2\gamma(^1\text{H})/\gamma(^{13}\text{C})$
CH ₃ :	1:3:3:1	approx.: $3\gamma(^1\text{H})/\gamma(^{13}\text{C}):3\gamma(^1\text{H})/\gamma(^{13}\text{C}):$ $-3\gamma(^1\text{H})/\gamma(^{13}\text{C}): -3\gamma(^1\text{H})/\gamma(^{13}\text{C})$



Examples of INEPT experiments:

(Note: Experiments recorded for different times, S/N should not be compared)



The refocused INEPT experiment:

- Provides additional delay (2Δ) to refocus J_{CH} coupling.
- The additional 180° pulse refocuses chemical shift evolution during that delay.
- Allows application of ^1H BB decoupling during acquisition.

Optimal delays:

- For CH groups, the optimal delay Δ is $1 / [4 * J_{\text{CH}}]$ (~ 1.79 ms)
- For CH₂ groups, the optimal delay Δ is $1 / [8 * J_{\text{CH}}]$ (~ 0.89 ms)
- For CH₃ groups, only two of the four vectors can be refocused, the optimal delay Δ is around $1/[8 * J_{\text{CH}}]$
- Need to find a compromise! In practice, a value of $3 / [8 * J_{\text{CH}}]$ (2.68 ms) is usually chosen.

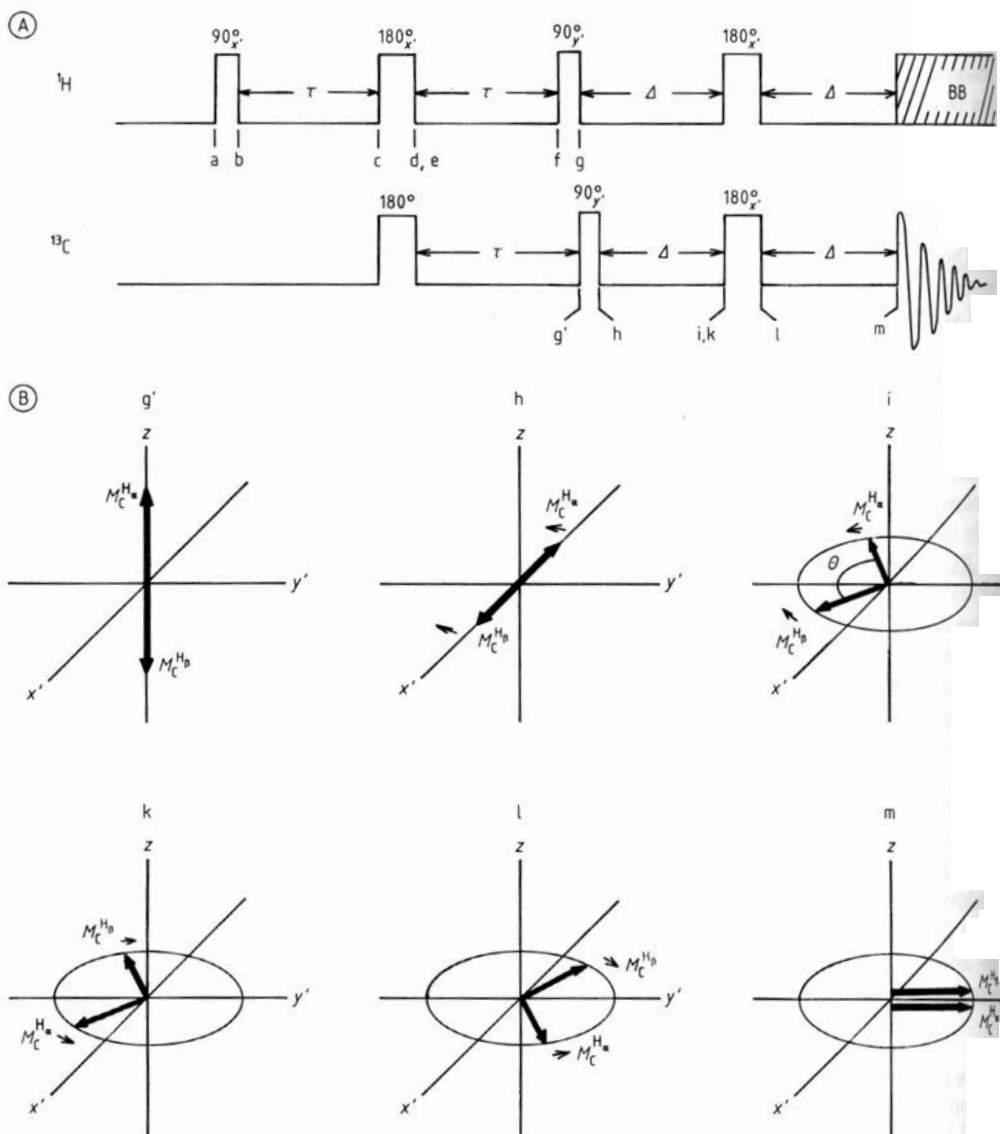


Figure 8-19.

The refocused INEPT experiment.

A: Pulse sequences in the ^1H and ^{13}C channels.

B: Vector diagrams for a two-spin AX system with A = ^1H and X = ^{13}C (example: $^{13}\text{CHCl}_3$). The evolution of the ^1H and ^{13}C magnetization vectors up to the instant g' is as in Figure 8-15 B, and diagram g' here is identical to the previous g'. Diagrams h to m show the evolution of the vectors $M_C^{H_a}$ and $M_C^{H_b}$ during the remainder of the pulse sequence A up to the instant m immediately before data acquisition.

Signal intensity enhancement of INEPT spectra

Table 6.1 A comparison of signal strength available by direct observation in the presence of the full nOe from protons, against that resulting from polarisation transfer from protons to the heteronucleus. The figures are *intensities* relative to direct observation of the nucleus without nOe.

<i>Nucleus</i>	<i>Maximum nOe</i>	<i>Polarisation Transfer</i>
^{31}P	2.24	2.47
^{13}C	2.99	3.98
^{29}Si	-1.52	5.03
^{15}N	-3.94	9.87
^{57}Fe	16.48	30.95
^{103}Rh	-14.89	31.78

CHEM / BCMB 4190/6190/8189

Introductory NMR

Lecture 13

The DEPT Experiment

Interpreting ^{13}C NMR spectra:

- Very useful to know which signals belong to quaternary carbons, CH, CH₂, and CH₃
- J-modulated spin-echo experiment and refocused INEPT are useful but don't provide all the necessary information
- The DEPT experiment (Distorsionless Enhancement by Polarization Transfer) is now one of the most important techniques available for interpreting 1D ^{13}C NMR spectra

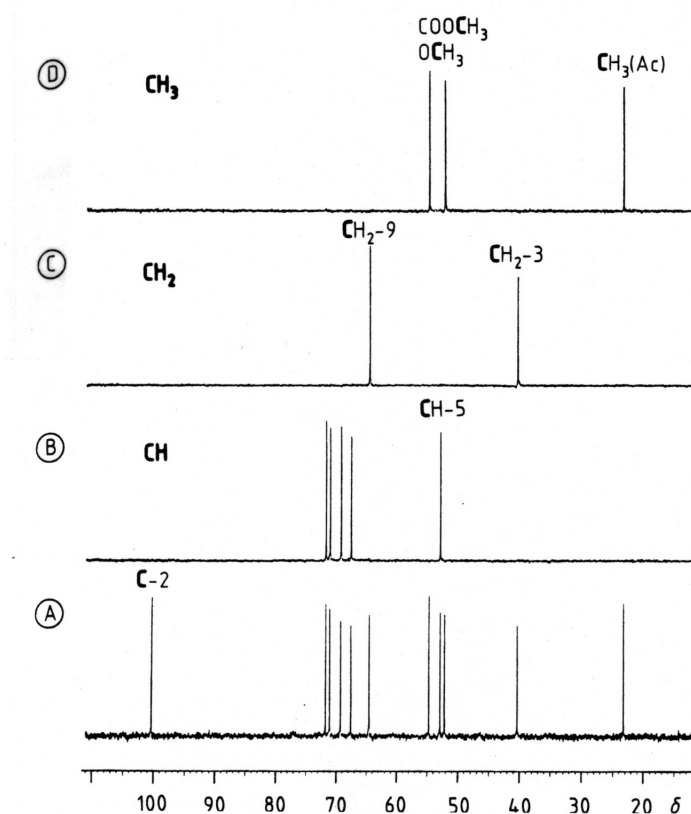


Figure 8-22.

The DEPT experiment; for pulse sequence see text.

A: 100.6 MHz ^{13}C NMR spectrum of the neuraminic acid derivative **1** with ^1H BB decoupling ($\delta = 10$ to 110 region only).

B: CH sub-spectrum: DEPT(90).

C: CH₂ sub-spectrum: DEPT(45) – DEPT(135).

D: CH₃ sub-spectrum: DEPT(45) + DEPT(135) – 0.707 DEPT(90).

(Experimental conditions:

167 mg of the compound in 2.3 ml

D₂O; 10 mm sample tube;

16 K data points; 32 FIDs for

$\theta_1 = 45^\circ$ and $\theta_3 = 135^\circ$, 64 FIDs for

$\theta_2 = 90^\circ$; $\tau = 3.57$ ms; total time

approx. 12 min.)

Pulse Sequence

^1H channel:

$90^\circ_{x'} - \tau - 180^\circ_{x'} - \tau - \Theta_{y'} - \tau - \text{BB decoupling}$

^{13}C channel:

$90^\circ_{x'} - \tau - 180^\circ - \tau - \text{FID } (t_2)$

- τ is $1/2J_{\text{CH}}$ with $J_{\text{CH}} = 140 \text{ Hz}$
- is chosen to be $\Theta = 45^\circ$, $\Theta = 90^\circ$, $\Theta = 135^\circ$
- Vector diagrams are not adequate to explain the effect of this pulse sequence and to understand this pulse sequence.
- The following curves explain the effect of Θ on the intensities of signals

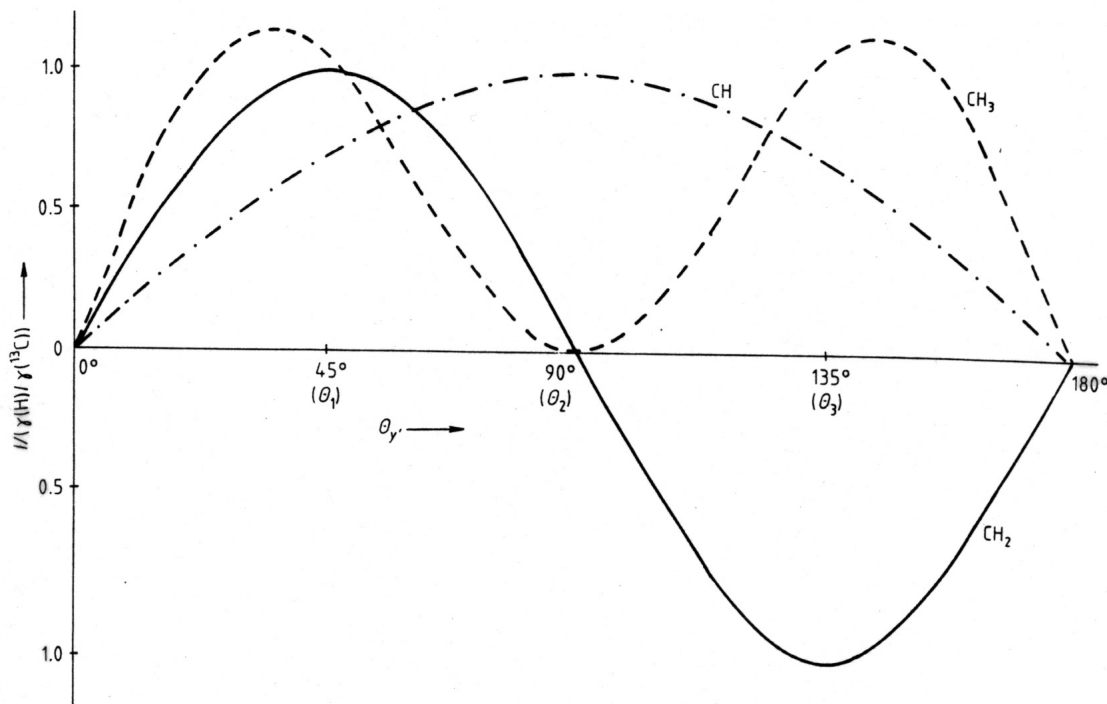


Figure 8-23.

DEPT experiment. Curves calculated from Equation (8-6) for the intensities of CH, CH₂ and CH₃ signals as functions of the pulse angle $\Theta_{y'}$; CH: ·····, CH₂: ———, CH₃: -----.

- CH sub-spectrum: $\Theta_2 = 90^\circ$ or DEPT (90)
- CH₂ sub-spectrum: DEPT(45) - DEPT(135)
- CH₃ sub-spectrum: DEPT(45) + DEPT(135) - 0.707DEPT(90)
- To compare absolute intensities the DEPT(90) must be collected with twice as many scans as for the other two DEPT experiments

Practically, it is sufficient to carry out two experiments, DEPT(90) and DEPT(135)

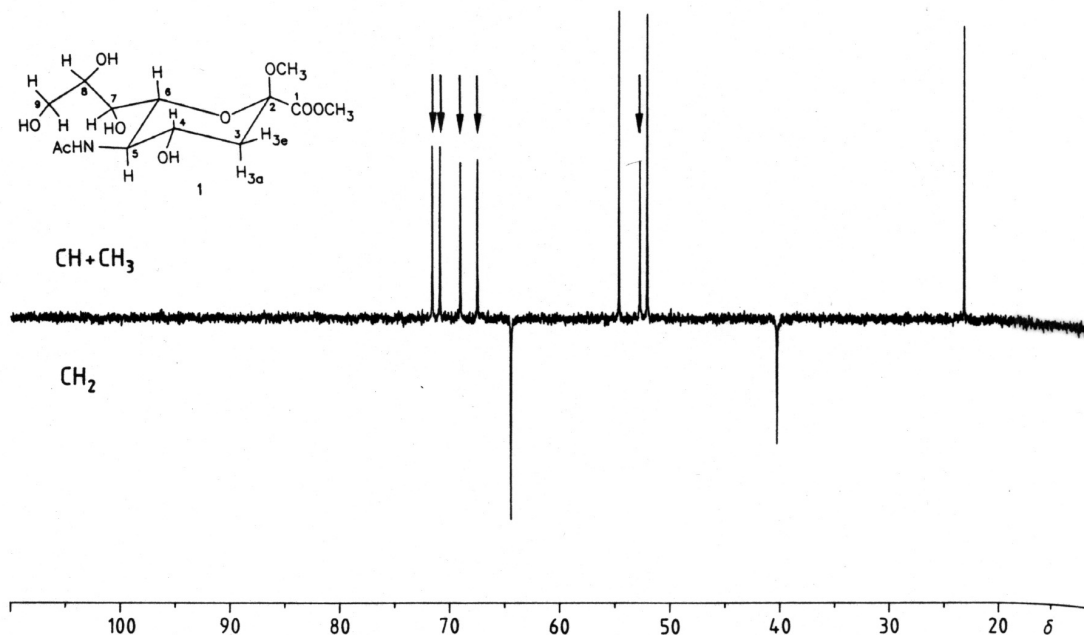


Figure 8-24.

DEPT(135) spectrum of the neuraminic acid derivative **1**, recorded using the pulse sequence given in the text, with $\theta_y = 135^\circ$. The signals of the five CH groups, identified with the help of the DEPT(90) spectrum ($\theta_y = 90^\circ$), are marked by arrows. The other three positive signals arise from CH₃ groups, and the two negative signals from CH₂ groups.

(Experimental conditions:

20 mg of the compound in 0.5 ml D₂O; 5 mm sample tube; 32 K data points; 300 FIDs; $\tau = 3.57$ ms; total time approx. 20 min.)

Table 8-2.

Partial assignment of the ¹³C NMR signals of **1** from the results of the DEPT experiment.

δ	CH ₃	CH ₂	CH	C	Assignment
23.2	×				CH ₃ (Ac)
40.31		×			C-3
52.12	×				
52.83			×		C-5
54.65	×				
64.50		×			C-9
67.51			×		
69.18			×		
70.98			×		
71.67			×		
100.32				×	C-2
171.50 ^{a)}				×	
175.93 ^{a)}				×	

^{a)} Values from the complete spectrum (Fig. 8-12 A).