DATA621-Homework3-HoddeFarrisBurmoodLin

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Problem Description

Explore, analyze and model a data set containing information on crime for various neighborhoods of a major city. Using the data set build a binary logistic regression model on the training data set to predict whether the neighborhood will be at risk for high crime levels. Provide classifications and probabilities for the evaluation data set using the developed binary logistic regression model.

Data Exploration

Data Exploration

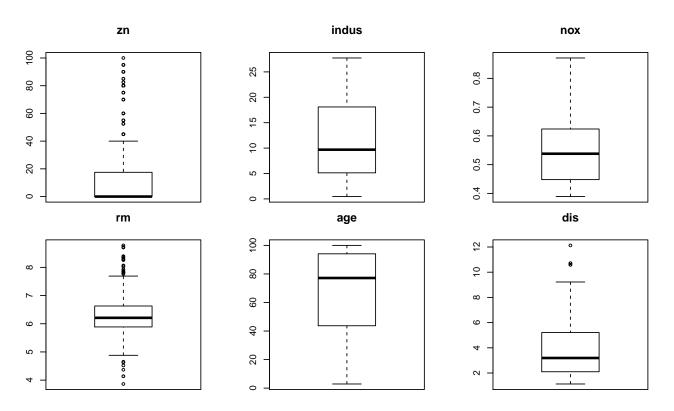
The first thirteen variables in the table below are potential predictor variables that could affect the response variable *target*.

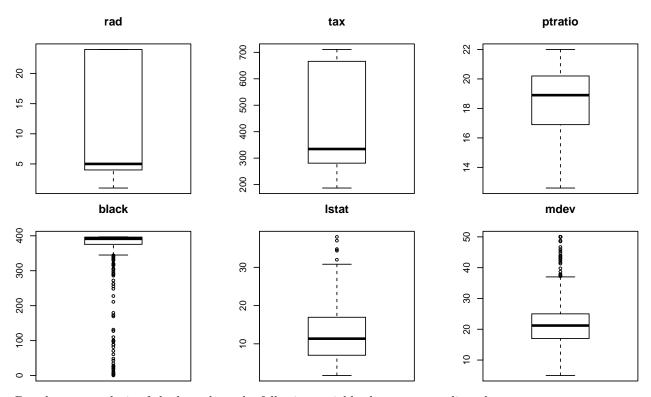
Variable	Type	Definition
zn	Double	proportion of residential land zoned for large lots
indus	Double	proportion of non-retail business acres per suburb
chas	Integer	suburb borders the Charles River $(1 = Yes, 0 = No)$
nox	Double	nitrogen oxides concentration (parts per 10 million)
$_{ m rm}$	Double	average number of rooms per dwelling
age	Double	proportion of owner-occupied units built prior to 1940
dis	Double	mean of distances to five Boston employment centers
rad	Integer	index of accessibility to radial highways
tax	Integer	full-value property-tax rate per \$10,000
ptratio	Double	pupil-teacher ratio by town
black	Double	1000(Bk - 0.63)2 where $Bk = proportion of blacks by town$
lstat	Double	lower status of the population (percent)
medv	Double	median value of owner-occupied homes in $$1000s$
target	Integer	crime rate is above the median crime rate $(1 = \text{Yes}, 0 = \text{No})$

Below is a summary of each predictor variable's basic statistics, followed by boxplots which illustrate the spread and outliers for each variable.

zn	indus	chas	nox	rm	age
Min.: 0.00	Min.: 0.460	Min. :0.00000	Min. :0.3890	Min. :3.863	Min.: 2.90
1st Qu.: 0.00	1st Qu.: 5.145	1st Qu.:0.00000	1st Qu.:0.4480	1st Qu.:5.887	1st Qu.: 43.88
Median:0.00	${\rm Median}:9.690$	Median: 0.00000	Median: 0.5380	Median: 6.210	${\rm Median}:77.15$
Mean:11.58	Mean $:11.105$	Mean $:0.07082$	Mean: 0.5543	Mean $:6.291$	$\mathrm{Mean}:68.37$
3rd Qu.: 16.25	3rd Qu.:18.100	3rd Qu.:0.00000	3rd Qu.:0.6240	3rd Qu.:6.630	3rd Qu.: 94.10
Max. $:100.00$	Max. $:27.740$	Max. $:1.00000$	Max. $:0.8710$	Max. :8.780	Max. :100.00

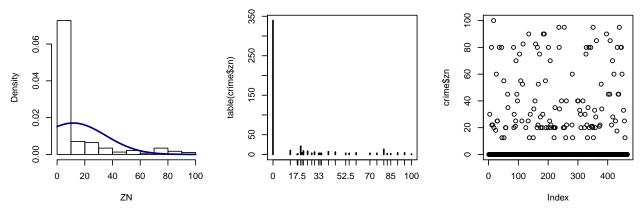
dis	rad	tax	ptratio	black	lstat
Min.: 1.130	Min.: 1.00	Min. :187.0	Min. :12.6	Min.: 0.32	Min.: 1.730
1st Qu.: 2.101	1st Qu.: 4.00	1st Qu.:281.0	1st Qu.:16.9	1st Qu.:375.61	1st Qu.: 7.043
${\rm Median}:3.191$	${\rm Median}:5.00$	${\bf Median:} 334.5$	${\bf Median:} 18.9$	Median: 391.34	${\bf Median:} 11.350$
Mean: 3.796	Mean:9.53	Mean: 409.5	Mean $:18.4$	Mean: 357.12	Mean $:12.631$
3rd Qu.: 5.215	3rd Qu.:24.00	3rd Qu.:666.0	3rd Qu.:20.2	3rd Qu.:396.24	3rd Qu.:16.930
Max. :12.127	Max. :24.00	Max. :711.0	Max. :22.0	Max. $:396.90$	Max. $:37.970$

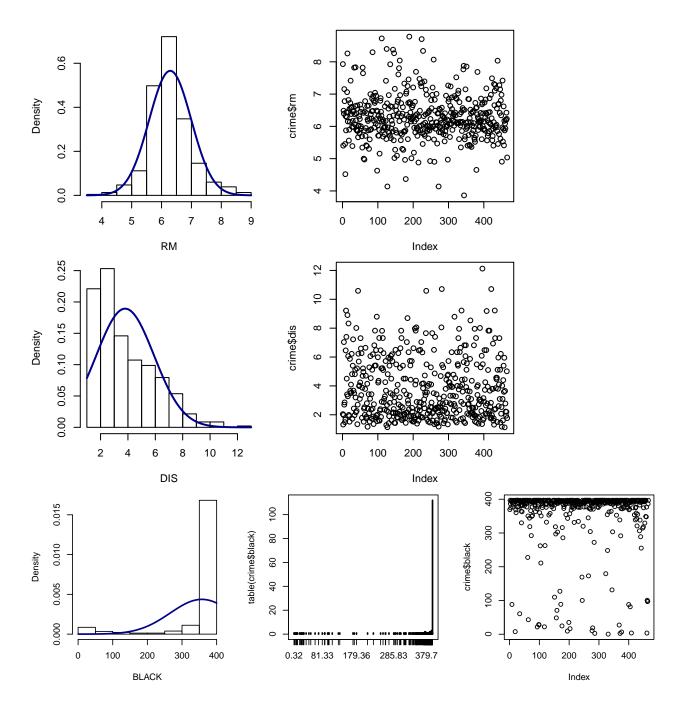


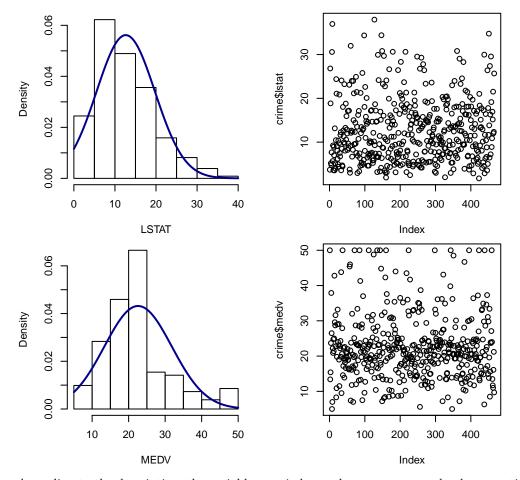


Based on an analysis of the box plots, the following variables have some outliers that may, or may not, exert influence on the regression results: - zn, rm, dis, black, lstat, medv

We'll next look at these variables more closely, starting with their histograms and frequency counts to better understand the nature of their distribution.







According to the description, the variables zn, indus, and age are area, or land, proportions. According to the statistical summary, the values for these variables are all within the range [1,100] that we would expect.

Based on our detailed review of the variables that contained outliers, the following variables could be problematic:

The predictor variable zn is highly right skewed, we can confirm this by comparing the median and mean where the median is 0.0, but the median is 11.58. The frequency count plot shows how poor the distribution is due to clustering of the data at one extreme.

The predictor variable *black* is highly left skewed. We can confirm this by comparing the median and mean where the median is 391.34 and the mean is 357.12. The frequency count plot shows how poor the distribution is due to clustering of the data at one extreme.

The predictor variable *dis* is slightly right skewed. We can confirm this by comparing the median and mean where the median is 3.191 and the mean is 3.796.

Fortunately, no missing data, or NAs, were found.

The following data corrections were identified in this section:

- (1) The predictor variable *chas* and the response variable *target* are categorical (binary), so we need to convert them to factors.
- (2) Need to determine if there are other variables highly coorelated with the zn or black variables that do not have the severe skew and outliers. This could allow us to remove the zn or black variables from the model.

Data Preparation

Data Preparation

The variable changes we identified so far include converting the predictor variable chas and the response variable target to factors. Next we will look at how each variable correlates to all the others:

	zn	indus	nox	m rm	age	dis
zn	1.0000000	-0.5382664	-0.5170452	0.3198141	-0.5725805	0.6601243
indus	-0.5382664	1.0000000	0.7596301	-0.3927118	0.6395818	-0.7036189
nox	-0.5170452	0.7596301	1.0000000	-0.2954897	0.7351278	-0.7688840
$_{ m rm}$	0.3198141	-0.3927118	-0.2954897	1.0000000	-0.2328125	0.1990158
age	-0.5725805	0.6395818	0.7351278	-0.2328125	1.0000000	-0.7508976
dis	0.6601243	-0.7036189	-0.7688840	0.1990158	-0.7508976	1.0000000
rad	-0.3154812	0.6006284	0.5958298	-0.2084457	0.4603143	-0.4949919
tax	-0.3192841	0.7322292	0.6538780	-0.2969343	0.5121245	-0.5342546
ptratio	-0.3910357	0.3946898	0.1762687	-0.3603471	0.2554479	-0.2333394
black	0.1794150	-0.3581356	-0.3801549	0.1326676	-0.2734677	0.2938441
lstat	-0.4329925	0.6071102	0.5962426	-0.6320245	0.6056200	-0.5075280
medv	0.3767171	-0.4961743	-0.4301227	0.7053368	-0.3781560	0.2566948
	rad	tax	ptratio	black	lstat	medv
zn	-0.3154812	-0.3192841	-0.3910357	0.1794150	-0.4329925	0.3767171
induc	0.6006284	0.7399909	0.3046808	0.3581356	0.6071102	0.4061743

	rad	tax	ptratio	black	lstat	medv
zn	-0.3154812	-0.3192841	-0.3910357	0.1794150	-0.4329925	0.3767171
indus	0.6006284	0.7322292	0.3946898	-0.3581356	0.6071102	-0.4961743
nox	0.5958298	0.6538780	0.1762687	-0.3801549	0.5962426	-0.4301227
m rm	-0.2084457	-0.2969343	-0.3603471	0.1326676	-0.6320245	0.7053368
age	0.4603143	0.5121245	0.2554479	-0.2734677	0.6056200	-0.3781560
dis	-0.4949919	-0.5342546	-0.2333394	0.2938441	-0.5075280	0.2566948
rad	1.0000000	0.9064632	0.4714516	-0.4463750	0.5031013	-0.3976683
tax	0.9064632	1.0000000	0.4744223	-0.4425059	0.5641886	-0.4900329
ptratio	0.4714516	0.4744223	1.0000000	-0.1816395	0.3773560	-0.5159153
black	-0.4463750	-0.4425059	-0.1816395	1.0000000	-0.3533659	0.3300286
lstat	0.5031013	0.5641886	0.3773560	-0.3533659	1.0000000	-0.7358008
medv	-0.3976683	-0.4900329	-0.5159153	0.3300286	-0.7358008	1.0000000

The correlation table above shows that the variable zn is moderately correlated to the variable dis. The plot of the dis data shows a much better distribution of values. Consequently, one possibility is to remove zn

from the model and use dis instead. Before doing this, we should look at the real-world context of the two variables to determine if they are meaningfully related.

Build Models

Build Models

One method of developing multiple regression models is to take a stepwise approach. To accomplish this, we combine our knowledge from the data exploration above with logistic regression. Univariate Logistic Regression is a useful method to understand how each predictor variable interacts individually with the target (response) variable. Looking at various statistics, we determine which variable may impact our target the most.

var	p_val	aic	auc
zn	0.0000000	413.2878	0.7076814
indus	0.0000000	345.8163	0.8091513
chas1	0.3188437	518.3011	0.5452821
nox	0.0000000	212.6269	0.8710289
$_{\rm rm}$	0.0010624	507.8644	0.5737316
age	0.0000000	317.3847	0.7937411
dis	0.0000000	307.0926	0.7970602
rad	0.0000015	330.3616	0.8440019
tax	0.0000000	353.7222	0.8319109
ptratio	0.0000011	493.3566	0.6600284
black	0.0000018	435.2948	0.7484590
lstat	0.0000000	416.8908	0.7015173

We examine the p-value (significance), the AIC statistic (goodness-of-fit) and the AUC (Area Under Curve) to measure the potential predictive value of each variable, so we can decide whether or not to include it in our multiple regression model. We are looking for p-values below .05, AIC values as low as possible, and AUC values as high as possible.

From the above table, we can see that *chas* is the least likely to produce any meaningful inference because its p-value is well above .05 (not significant), it has the highest AIC (518, where 100 is considered excellent), and the lowest AUC (.54, where random chance would yield .50). Therefore, *chas* is the most likely candidate to be removed from our model.

Model 1

As a baseline, we start with a multiple logistic regression model that includes every predictor variable:

Call:

```
glm(formula = target ~ ., family = binomial(link = "logit"),
##
       data = train)
##
##
  Deviance Residuals:
##
       Min
                 1Q
                      Median
                                    3Q
                                            Max
  -1.7132
                      0.0000
            -0.0934
                                0.0016
##
                                         3.4718
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
##
  (Intercept) -24.342449
                             9.762679
                                       -2.493 0.012652 *
## zn
                -0.038247
                             0.038733
                                       -0.987 0.323420
## indus
                -0.082035
                             0.066940
                                       -1.225 0.220391
## chas1
                 1.189371
                             0.904623
                                        1.315 0.188587
## nox
                                        5.240
                53.285171
                            10.168667
                                               1.6e-07 ***
## rm
                -1.183564
                             0.917904
                                       -1.289 0.197252
                 0.054774
                             0.016677
                                        3.284 0.001022 **
## age
                                        2.477 0.013233 *
                             0.286890
## dis
                 0.710750
                 0.703069
                             0.203161
                                        3.461 0.000539 ***
## rad
                -0.010313
                             0.004648
                                       -2.219 0.026491 *
## tax
## ptratio
                 0.560259
                             0.180922
                                        3.097 0.001957 **
## black
                -0.044213
                             0.018559
                                       -2.382 0.017206 *
                                       -0.690 0.490500
## 1stat
                -0.046652
                             0.067660
                 0.187979
                             0.084565
                                        2.223 0.026223 *
## medv
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
##
       Null deviance: 515.31
                               on 371
                                       degrees of freedom
## Residual deviance: 130.18
                              on 358
                                       degrees of freedom
  AIC: 158.18
##
## Number of Fisher Scoring iterations: 9
```

In this model we set aside 20% of the training data and use 80% to train the model, we then use the model to predict the outcome of the remaining 20% of the data. The model yields an Area Under Curve of .95, meaning it chose correctly 95% of the time.

Model 2

In this scenario we attempt to create the simplest model possible by using only one variable - the one that provides the highest overall AUC (performance) by itself. We calculate AUC for each variable separately and then select the highest result.

```
## [1] 0.8710289
```

[1] 0.9506875

The best predictor variable is nox, yielding an AUC of .87.

Next we combine nox with each of the remaining variables individually and select the highest AUC result.

```
## [1] 0.9338549
```

We find that nox plus rad is the strongest combination of two variables, yielding an AUC of .93.

Finally, we search for a third critical predictor by combining nos plus rad with the remaining variables, individually.

[1] 0.9419156

By combining three variables - nox, rad and zn - that is, the concentration of nitrogen oxides, access to radial highways and the proportion of land zoned for large lots, we can predict with 94% accuracy whether the crime rate at this property is above or below average. Since this is very close to the performance of the model using all variables (95%), we can be confident in using these three variables for our decision support process, and disregarding the others.

Model 3

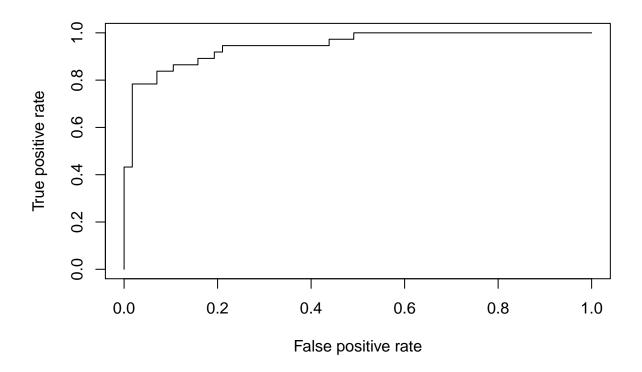
The GLM Model summary in Model 1 illustrates the outsize impact of the predictor variable *nox* compared to all the others. It carries an Estimate of 53.3 where the next closest in magnitude is only 1.2. We thought it would be interesting to remove *nox* from the model just to see how the other variables perform without it. First we will perform a simple backward variable selection optimization process including it.

MODEL 3 WITH NOX VARIABLE

```
## Start: AIC=158.18
## target ~ zn + indus + chas + nox + rm + age + dis + rad + tax +
##
       ptratio + black + lstat + medv
##
##
             Df Deviance
                             AIC
                  130.66 156.66
## - 1stat
              1
## - zn
              1
                  131.32 157.32
                  131.71 157.71
## - indus
              1
                  131.88 157.88
## - rm
              1
                  131.90 157.90
## - chas
              1
                  130.18 158.18
## <none>
## - medv
                  135.74 161.74
              1
## - tax
              1
                  135.83 161.83
## - dis
              1
                  137.13 163.13
## - black
              1
                  141.32 167.32
## - ptratio
              1
                  141.36 167.36
## - age
              1
                  142.62 168.62
## - rad
              1
                  160.19 186.19
## - nox
              1
                  179.04 205.04
##
## Step: AIC=156.66
##
  target ~ zn + indus + chas + nox + rm + age + dis + rad + tax +
##
       ptratio + black + medv
##
             Df Deviance
##
                             AIC
## - rm
                  131.88 155.88
## - zn
              1
                  131.97 155.97
              1
                  132.07 156.07
## - chas
## - indus
                  132.13 156.13
                  130.66 156.66
## <none>
                  135.85 159.85
## - medv
              1
```

```
1 137.03 161.03
## - tax
## - dis
            1 137.28 161.28
               141.42 165.42
## - ptratio 1
## - black
               141.78 165.78
            1
## - age
            1
               143.67 167.67
## - rad
           1 161.04 185.04
## - nox
            1 179.22 203.22
##
## Step: AIC=155.88
## target ~ zn + indus + chas + nox + age + dis + rad + tax + ptratio +
      black + medv
##
           Df Deviance
##
                         AIC
## - indus
          1 133.18 155.18
## - chas
           1 133.31 155.31
## - zn
            1
               133.35 155.35
## <none>
                131.88 155.88
## - dis
           1 137.63 159.63
## - medv
            1 138.52 160.52
## - tax
            1
               138.80 160.80
## - ptratio 1 141.43 163.43
## - black
            1 143.36 165.36
            1 143.79 165.79
## - age
            1 162.26 184.26
## - rad
## - nox
            1 179.24 201.24
## Step: AIC=155.18
## target ~ zn + chas + nox + age + dis + rad + tax + ptratio +
##
      black + medv
##
           Df Deviance
##
                       AIC
## - chas
           1 133.91 153.91
## - zn
            1 134.74 154.74
## <none>
                133.18 155.18
## - dis
            1
               138.30 158.30
## - medv
            1 139.50 159.50
## - ptratio 1
               141.70 161.70
## - black
            1
               144.01 164.01
## - age
            1
               144.79 164.79
## - tax
           1 147.18 167.18
## - rad
           1 169.58 189.58
            1 185.71 205.71
## - nox
## Step: AIC=153.91
## target ~ zn + nox + age + dis + rad + tax + ptratio + black +
##
     medv
##
##
           Df Deviance
                         AIC
## <none>
                133.91 153.91
               135.92 153.92
## - zn
            1
## - dis
           1 138.75 156.75
## - medv
           1 139.87 157.87
## - ptratio 1 141.76 159.76
## - black 1 144.48 162.48
```

```
## - age
            1 146.79 164.79
## - tax
               149.18 167.18
            1
## - rad
            1
               174.36 192.36
## - nox
               185.81 203.81
            1
##
## Call:
## glm(formula = target ~ zn + nox + age + dis + rad + tax + ptratio +
      black + medv, family = binomial(link = "logit"), data = train)
## Deviance Residuals:
      Min 10 Median
                               3Q
                                      Max
## -1.8622 -0.1135 0.0000 0.0018
                                   3.3120
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -21.935844 9.197361 -2.385 0.017078 *
             -0.048462
                        0.037132 -1.305 0.191848
                        7.922146 5.579 2.43e-08 ***
## nox
             44.193814
              0.043782
                        0.013013 3.364 0.000767 ***
## age
## dis
              0.551173
                        0.260500 2.116 0.034359 *
                        0.188980 4.043 5.27e-05 ***
## rad
              0.764131
## tax
              -0.013328
                        0.004197 -3.176 0.001496 **
                        0.145949 2.720 0.006534 **
              0.396941
## ptratio
## black
              ## medv
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 515.31 on 371 degrees of freedom
## Residual deviance: 133.91 on 362 degrees of freedom
## AIC: 153.91
##
## Number of Fisher Scoring iterations: 9
```



[1] 0.9468943

The model reduces to nine variables and yields a nice low residual deviance of 133.9, compared to a null deviance of 515.3. This roughly means that the model eliminates about 80% of the error compared to choosing at random. The AUC is .947 which is roughly the same as the full model using all variables.

Let's look at what happens when we remove the nox variable:

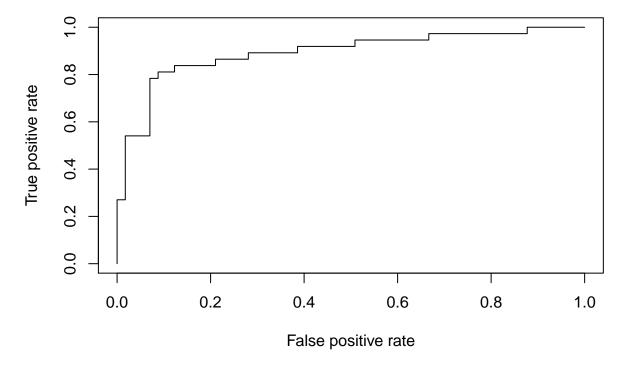
MODEL 3 WITHOUT NOX VARIABLE

```
## Start:
          AIC=205.04
  target ~ (zn + indus + chas + nox + rm + age + dis + rad + tax +
##
       ptratio + black + lstat + medv) - nox
##
##
             Df Deviance
                             AIC
                   179.04 203.04
## - rm
## - 1stat
                  179.22 203.22
              1
##
  - medv
                  179.49 203.49
## - ptratio
                   179.50 203.50
              1
## - zn
                   179.72 203.72
                   180.12 204.12
## - chas
## <none>
                   179.04 205.04
## - dis
                  184.69 208.69
              1
## - indus
              1
                   185.26 209.26
## - tax
                  189.25 213.25
              1
                   194.42 218.42
## - age
## - black
              1
                   194.48 218.48
## - rad
                  224.28 248.28
##
## Step: AIC=203.04
## target ~ zn + indus + chas + age + dis + rad + tax + ptratio +
```

```
##
     black + lstat + medv
##
           Df Deviance
##
                       AIC
              179.24 201.24
## - lstat
            1
## - ptratio 1
               179.55 201.55
## - zn
            1 179.74 201.74
## - chas
           1 180.14 202.14
## - medv
            1 180.33 202.33
## <none>
                179.04 203.04
## - dis
           1 184.75 206.75
## - indus 1 185.26 207.26
## - tax
               189.48 211.48
            1
               194.49 216.49
## - black 1
## - age
          1 199.65 221.65
## - rad
           1
                224.29 246.29
##
## Step: AIC=201.23
## target ~ zn + indus + chas + age + dis + rad + tax + ptratio +
##
     black + medv
##
##
           Df Deviance
                        AIC
## - ptratio 1 179.66 199.66
## - zn
            1 179.94 199.94
## - chas
            1
               180.24 200.24
## - medv
           1 180.39 200.39
## <none>
               179.24 201.24
## - dis
           1 184.87 204.87
## - indus
            1 185.71 205.71
## - tax
           1 189.73 209.73
## - black
          1 194.65 214.65
            1 203.76 223.76
## - age
## - rad
            1 224.87 244.87
##
## Step: AIC=199.66
## target ~ zn + indus + chas + age + dis + rad + tax + black +
##
     medv
##
##
         Df Deviance
                     AIC
## - medv
         1 180.44 198.44
## - chas 1 180.84 198.84
## - zn
         1 180.88 198.88
## <none>
             179.66 199.66
## - dis
          1 184.91 202.91
## - indus 1 186.30 204.30
## - tax
          1 189.81 207.81
## - black 1 194.65 212.65
          1 203.82 221.82
## - age
## - rad
        1 224.87 242.87
##
## Step: AIC=198.44
## target ~ zn + indus + chas + age + dis + rad + tax + black
##
##
        Df Deviance AIC
## - zn 1 181.18 197.18
```

```
1 181.53 197.53
## - chas
## <none>
              180.44 198.44
## - indus 1 186.61 202.61
## - dis
          1 190.36 206.36
## - tax
          1
             193.03 209.03
## - black 1
             195.03 211.03
## - age 1 203.82 219.82
## - rad
          1 229.86 245.86
##
## Step: AIC=197.18
## target ~ indus + chas + age + dis + rad + tax + black
##
          Df Deviance
##
                       AIC
          1 182.11 196.11
## - chas
## <none>
              181.18 197.18
## - indus 1 187.57 201.57
## - dis
          1 192.85 206.85
## - tax
          1 193.44 207.44
## - black 1 196.02 210.02
             206.37 220.37
## - age
          1
## - rad
          1
             230.37 244.37
##
## Step: AIC=196.11
## target ~ indus + age + dis + rad + tax + black
##
          Df Deviance
                      AIC
## <none>
             182.11 196.11
             187.66 199.66
## - indus 1
## - tax
          1 193.45 205.45
          1 193.52 205.52
## - dis
## - black 1 196.74 208.74
## - age
          1 206.70 218.70
## - rad
        1 231.11 243.11
##
## glm(formula = target ~ indus + age + dis + rad + tax + black,
      family = binomial(link = "logit"), data = train)
##
## Deviance Residuals:
##
      Min
               1Q Median
                                3Q
                                       Max
## -2.3129 -0.3415 0.0000
                          0.0139
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
                       5.329705 2.315 0.02060 *
## (Intercept) 12.339156
                                 2.208 0.02723 *
## indus
             0.112098
                       0.050765
## age
             0.047489
                       0.010497
                                 4.524 6.06e-06 ***
             ## dis
## rad
             0.647494
                        0.160850
                                 4.025 5.69e-05 ***
             -0.011195
## tax
                        0.003676 -3.045 0.00232 **
## black
             -0.039095
                        0.013024 -3.002 0.00268 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 515.31 on 371 degrees of freedom
## Residual deviance: 182.11 on 365 degrees of freedom
## AIC: 196.11
##
## Number of Fisher Scoring iterations: 9
```



[1] 0.8933144

We still have a good model - the Residual Deviance increased to 182, but that is still much better than predicting with no model at all. The AUC is now .89 - again, very good. But the AUC with only one variable nox was .87. And in certain trials the AUC with nox exceeded .95 (due to randomly selected evaluation samples).

Why is the *nox* variable so powerful? We can look back at the Correlation table for clues. More variables are significantly correlated to *nox* than any other. It is like a super-variable, somehow encapsulating the properties of the variables around it. Is it because *nox* is an indicator of so many problems, like pollution, industrial decay, lax building codes? The *nox* variable is a stellar example of a finding that opens up many paths for further research.

Choose Model

MODEL 3 WITH NOX VARIABLE USING FULL DATASETS

```
## Start: AIC=214.15
## target ~ zn + indus + chas + nox + rm + age + dis + rad + tax +
```

```
##
      ptratio + black + lstat + medv
##
##
           Df Deviance
                         AIC
               186.91 212.91
## - 1stat
            1
## - rm
            1
               187.03 213.03
           1 188.02 214.02
## - chas
## <none>
                186.15 214.15
## - indus
          1 188.52 214.52
## - zn
               190.49 216.49
            1
## - tax
           1 191.03 217.03
## - black
          1
               192.05 218.05
## - age
               192.96 218.96
            1
               195.29 221.29
## - medv
            1
           1 198.48 224.48
## - dis
## - ptratio 1 198.76 224.76
## - rad
            1 223.66 249.66
## - nox
            1 257.46 283.46
##
## Step: AIC=212.91
## target ~ zn + indus + chas + nox + rm + age + dis + rad + tax +
##
      ptratio + black + medv
##
##
           Df Deviance AIC
## - rm
            1 188.88 212.88
                186.91 212.91
## <none>
## - indus 1 189.14 213.14
## - chas
            1 189.17 213.17
               190.90 214.90
## - zn
            1
## - tax
           1 191.41 215.41
## - black
          1 192.77 216.77
## - medv
            1
               196.21 220.21
## - age
            1
                197.65 221.65
## - dis
           1
               199.62 223.62
## - ptratio 1
               200.26 224.26
## - rad
            1
                224.12 248.12
## - nox
            1 259.54 283.54
##
## Step: AIC=212.88
## target ~ zn + indus + chas + nox + age + dis + rad + tax + ptratio +
##
      black + medv
##
##
           Df Deviance AIC
                188.88 212.88
## <none>
## - indus
               190.94 212.94
          1
## - chas
               191.35 213.35
            1
                193.34 215.34
## - zn
            1
## - tax
            1
                193.67 215.67
## - black
                194.32 216.32
          1
## - age
            1
                197.65 219.65
                200.09 222.09
## - dis
            1
## - ptratio 1
                200.29 222.29
## - medv
            1
               201.97 223.97
## - rad
            1 225.37 247.37
## - nox
          1 259.83 281.83
```

```
##
## Call:
## glm(formula = target ~ zn + indus + chas + nox + age + dis +
      rad + tax + ptratio + black + medv, family = binomial(link = "logit"),
##
      data = crime)
##
## Deviance Residuals:
      Min
           1Q
                   Median
                               3Q
                                      Max
## -2.4411 -0.1739 -0.0026 0.0030
                                    3.4506
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -36.364060 6.862463 -5.299 1.16e-07 ***
                        0.032498 -1.818 0.069016 .
## zn
              -0.059091
## indus
              -0.067194
                        0.048295 -1.391 0.164128
## chas1
              1.217987
                         0.777917
                                   1.566 0.117418
              48.468529
                         7.790233
                                  6.222 4.92e-10 ***
## nox
## age
             0.031961
                         0.011164 2.863 0.004197 **
              0.703484
                        0.220707
                                   3.187 0.001436 **
## dis
## rad
              0.620491
                        0.156587
                                  3.963 7.41e-05 ***
## tax
              ## ptratio
              ## black
              -0.012935 0.006940 -1.864 0.062342 .
## medv
               0.119666
                       0.035873 3.336 0.000851 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 645.88 on 465 degrees of freedom
## Residual deviance: 188.88 on 454 degrees of freedom
## AIC: 212.88
## Number of Fisher Scoring iterations: 9
```

The Smooth Operators