## Jeff's Variable Analysis

### **Executive Summary**

```
This is an analysis of the following predictor variables:
$ Filler.Level: num 121 119 120 118 119 ...
$ Filler.Speed: int 4002 3986 4020 4012 4010 4014 0 1004 4014 4028 ...
$ Temperature: num 66 67.6 67 65.6 65.6 66.2 65.8 65.2 65.4 66.6 ...
$ Usage.cont: num 16.2 19.9 17.8 17.4 17.7 ...
$ Carb.Flow: int 2932 3144 2914 3062 3054 2948 30 684 2902 3038 ...
$ Density: num 0.88 0.92 1.58 1.54 1.54 1.52 0.84 0.84 0.9 0.9 ...
$ MFR: num 725 727 735 731 723 ...
$ Balling: num 1.4 1.5 3.14 3.04 3.04 ...
```

The following activities were performed:

- 1) Review basic statistics for each variable.
- 2) Remove rows where response variable value is zero.
- 3) Determined high number of zeros for predictor variables were actually missing data so replaced zeros with NAs.
- 4) Generated imputed values for all missing data in predictor variables.
- 5) Generated boxplots, histograms, and scatter plots for each predictor variable to analyze distributions.
- 6) Performed Box Cox transformations for variable with poor distributions.
- 7) Performed 1-on-1 regression analysis for each predictor variable against the response variable for numerous regression model focusing on RMSE optimization and compared models results.
- 8) Performed a step-wise, both forward and backward, generalize linear model analysis focused on optimizing AIC to identify the most revelant variable relationships.

#### Variable Analysis Results:

The predictor variable distributions are generally poor, and all but one variable required a Box Cox-selected transformation which, in most cases, yielded only slight improvements.

The 1-on-1 regression modeling yielding generally poor results with poor RMSE values and terrible R-squared values resulting in the conclusion that no single predictor variable from the set has a significant influence or effect on the response variable.

The step-wise regression modeling resulting in generally poor results as well, but the resulting model did eliminate the variable Filler. Speed when arriving an the final model.

#### Conclusions:

None of the predictor variables in this set have a significant influence on PH, and all have troubled data distributions. A comparision of the distribution anomallies should be made across all of the data set variables to determine if there is a systemic cause. Pending that analysis, the variables in this set, minus the Filler. Speed variable, should be combined with other candidate predictor variables for further modeling analysis.

```
suppressWarnings(suppressMessages(library(knitr)))
suppressWarnings(suppressMessages(library(mice)))
suppressWarnings(suppressMessages(library(fBasics)))
suppressWarnings(suppressMessages(library(nnet)))
suppressWarnings(suppressMessages(library(kernlab)))
suppressWarnings(suppressMessages(library(caret)))
suppressWarnings(suppressMessages(library(randomForest)))
suppressWarnings(suppressMessages(library(mlbench)))
suppressWarnings(suppressMessages(library(MASS)))
suppressWarnings(suppressMessages(library(rpart)))
```

```
suppressWarnings(suppressMessages(library(party)))
suppressWarnings(suppressMessages(library(partykit)))
suppressWarnings(suppressMessages(library(gbm)))
suppressWarnings(suppressMessages(library(ipred)))
suppressWarnings(suppressMessages(library(forecast)))
"suppressMessages(libraries("tidyverse", "nnet", "kernlab", "caret", "randomForest", "mlbench","MASS",
# read in the data locally
ph.data <- read.csv("/Users/JeffAtLaptop/Dropbox/School/DATA624-PredictiveAnalytics/Project2/StudentDat
summary(ph.data)
                                                           PC.Volume
##
     Brand.Code
                         Carb.Volume
                                         Fill.Ounces
##
    Length:2571
                        Min.
                               :0.000
                                        Min.
                                               : 0.00
                                                         Min.
                                                                :0.0000
##
    Class : character
                        1st Qu.:5.293
                                        1st Qu.:23.92
                                                         1st Qu.:0.2370
    Mode :character
                        Median :5.347
                                        Median :23.97
                                                         Median :0.2700
##
                        Mean
                               :5.349
                                        Mean
                                                :23.62
                                                         Mean
                                                                :0.2729
##
                                        3rd Qu.:24.03
                                                         3rd Qu.:0.3110
                        3rd Qu.:5.453
##
                                                :24.32
                                                                :0.4780
                               :5.700
                                        Max.
                        Max.
                                                         Max.
                                          PSC
##
    Carb.Pressure
                       Carb.Temp
                                                           PSC.Fill
##
    Min.
          : 0.00
                    Min.
                           : 0.0
                                     Min.
                                             :0.00000
                                                        Min.
                                                               :0.0000
##
    1st Qu.:65.60
                    1st Qu.:138.4
                                     1st Qu.:0.04800
                                                        1st Qu.:0.1000
##
    Median :68.00
                    Median :140.8
                                     Median :0.07600
                                                        Median :0.1800
    Mean
           :67.47
                           :139.7
                                     Mean
                                            :0.08349
                                                        Mean
                                                               :0.1936
                    Mean
##
    3rd Qu.:70.60
                    3rd Qu.:143.8
                                     3rd Qu.:0.11200
                                                        3rd Qu.:0.2600
##
    Max.
           :79.40
                            :154.0
                                             :0.27000
                                                               :0.6200
                    Max.
                                     Max.
                                                        Max.
##
       PSC.CO2
                         Mnf.Flow
                                         Carb.Pressure1 Fill.Pressure
                                                : 0.0
##
   Min.
           :0.00000
                      Min.
                              :-100.20
                                         Min.
                                                          Min.
                                                                 : 0.00
##
    1st Qu.:0.02000
                      1st Qu.:-100.00
                                         1st Qu.:118.8
                                                          1st Qu.:46.00
    Median :0.04000
                                                          Median :46.40
##
                      Median: 64.80
                                         Median :123.0
           :0.05556
                      Mean
                            : 24.55
                                         Mean
                                                :121.1
                                                          Mean
                                                                 :47.51
##
    3rd Qu.:0.08000
                       3rd Qu.: 140.80
                                         3rd Qu.:125.4
                                                          3rd Qu.:50.00
##
    Max.
           :0.24000
                              : 229.40
                                         Max.
                                                 :140.2
                                                          Max.
                                                                 :60.40
                      Max.
##
    Hyd.Pressure1
                    Hyd.Pressure2
                                     Hyd.Pressure3
                                                      Hyd.Pressure4
    Min.
           :-0.80
                            : 0.00
                    Min.
                                     Min.
                                             :-1.20
                                                      Min.
                                                             : 0.00
    1st Qu.: 0.00
                    1st Qu.: 0.00
                                     1st Qu.: 0.00
                                                      1st Qu.: 86.00
##
   Median :11.40
                    Median :28.60
                                     Median :27.40
##
                                                      Median : 96.00
##
    Mean
           :12.38
                    Mean
                            :20.84
                                     Mean
                                           :20.34
                                                             : 95.17
                                                      Mean
    3rd Qu.:20.20
                    3rd Qu.:34.60
                                     3rd Qu.:33.20
                                                      3rd Qu.:102.00
                            :59.40
##
    Max.
           :58.00
                    Max.
                                     Max.
                                            :50.00
                                                      Max.
                                                             :142.00
##
    Filler.Level
                     Filler.Speed
                                     Temperature
                                                       Usage.cont
    Min.
##
          : 0.0
                    Min.
                                0
                                    Min.
                                           : 0.00
                                                            : 0.00
##
    1st Qu.: 96.2
                    1st Qu.:3815
                                    1st Qu.:65.20
                                                     1st Qu.:18.35
    Median :118.2
##
                    Median:3980
                                    Median :65.60
                                                     Median :21.78
    Mean
          :108.4
                    Mean
                            :3605
                                                            :20.95
##
                                    Mean
                                           :65.61
                                                     Mean
    3rd Qu.:120.0
                    3rd Qu.:3996
                                    3rd Qu.:66.40
                                                     3rd Qu.:23.74
    Max.
           :161.2
                            :4030
                                                            :25.90
##
                    Max.
                                    Max.
                                           :76.20
                                                     Max.
```

: 0.0

:646.0

:868.6

MFR

1st Qu.:694.9

Median :721.4

3rd Qu.:730.4

Min.

Mean

Max.

Balling

1st Qu.: 1.496

Median: 1.648

3rd Qu.: 3.292

Min.

Mean

Max.

:-0.170

: 2.197

: 4.012

##

##

##

##

Min.

Mean

Max.

Carb.Flow

1st Qu.:1133

3rd Qu.:3186

:2466

:5104

Median:3028

Density

1st Qu.:0.900

Median :0.980

3rd Qu.:1.620

Min.

Mean

Max.

:0.000

:1.173

:1.920

```
## Pressure.Vacuum
                          PH
                                   Oxygen.Filler
                                                     Bowl.Setpoint
          :-6.600
## Min.
                           :0.000
                                   Min. :0.00000
                                                     Min. : 0.0
                    Min.
                    1st Qu.:8.440
## 1st Qu.:-5.600
                                   1st Qu.:0.02200
                                                     1st Qu.:100.0
## Median :-5.400
                    Median :8.540
                                   Median :0.03340
                                                     Median :120.0
## Mean
         :-5.216
                    Mean :8.532
                                   Mean
                                          :0.04662
                                                     Mean
                                                            :109.2
## 3rd Qu.:-5.000
                    3rd Qu.:8.680
                                   3rd Qu.:0.05960
                                                     3rd Qu.:120.0
## Max.
          :-3.600
                          :9.360
                                   Max.
                                          :0.40000
                                                     Max.
                    Max.
                                                           :140.0
## Pressure.Setpoint Air.Pressurer
                                       Alch.Rel
                                                       Carb.Rel
## Min.
         : 0.00
                     Min. :140.8
                                    Min.
                                           :0.000
                                                    Min.
                                                           :0.000
  1st Qu.:46.00
##
                     1st Qu.:142.2
                                    1st Qu.:6.540
                                                    1st Qu.:5.340
## Median :46.00
                     Median :142.6
                                  Median :6.560
                                                    Median :5.400
## Mean
         :47.39
                     Mean
                          :142.8
                                   Mean
                                           :6.873
                                                    Mean
                                                         :5.416
##
   3rd Qu.:50.00
                     3rd Qu.:143.0
                                    3rd Qu.:7.220
                                                    3rd Qu.:5.540
## Max.
                     Max. :148.2
                                                    Max. :6.060
          :52.00
                                    Max. :8.620
##
   Balling.Lvl
##
   Min.
          :0.000
  1st Qu.:1.380
##
## Median :1.480
## Mean
         :2.049
## 3rd Qu.:3.140
## Max.
          :3.660
# setup the dataset with just jeffs variables
jeffsList <- c("PH", "Filler.Level", "Filler.Speed", "Temperature", "Usage.cont", "Carb.Flow", "Density", "MF.
jeffsVars <- data.frame(ph.data[,jeffsList])</pre>
summary(jeffsVars)
##
         PH
                    Filler.Level
                                   Filler.Speed
                                                  Temperature
## Min. :0.000
                   Min. : 0.0
                                  Min. : 0
                                                 Min.
                                                        : 0.00
   1st Qu.:8.440
                   1st Qu.: 96.2
                                  1st Qu.:3815
                                                 1st Qu.:65.20
## Median :8.540
                   Median :118.2
                                  Median:3980
                                                 Median :65.60
## Mean
         :8.532
                   Mean
                        :108.4
                                  Mean
                                        :3605
                                                 Mean
                                                       :65.61
##
   3rd Qu.:8.680
                   3rd Qu.:120.0
                                  3rd Qu.:3996
                                                 3rd Qu.:66.40
##
  Max.
          :9.360
                 Max.
                         :161.2
                                  Max.
                                         :4030
                                                 Max.
                                                      :76.20
     Usage.cont
##
                     Carb.Flow
                                    Density
                                                      MFR
  Min. : 0.00
                   Min. : 0
                                 Min.
                                        :0.000
                                                 Min. : 0.0
  1st Qu.:18.35
                   1st Qu.:1133
                                 1st Qu.:0.900
                                                 1st Qu.:694.9
##
## Median :21.78
                   Median:3028
                                 Median :0.980
                                                 Median :721.4
## Mean :20.95
                   Mean :2466
                                 Mean :1.173
                                                 Mean :646.0
## 3rd Qu.:23.74
                   3rd Qu.:3186
                                                 3rd Qu.:730.4
                                 3rd Qu.:1.620
## Max.
         :25.90
                   Max. :5104
                                 Max. :1.920
                                                 Max.
                                                        :868.6
##
      Balling
## Min.
         :-0.170
## 1st Qu.: 1.496
## Median: 1.648
## Mean
         : 2.197
  3rd Qu.: 3.292
## Max.
          : 4.012
# run the basic stats on the variables
# Let's start by exploring the type of each variable
types <- sapply(1:length(jeffsVars),function(x) typeof(jeffsVars[,x]))</pre>
types.df <- data.frame(VAR=names(jeffsVars), TYPE=types)</pre>
kable(types.df)
```

VAR	TYPE
PH	double
Filler.Level	double
Filler.Speed	integer
Temperature	double
Usage.cont	double
Carb.Flow	integer
Density	double
MFR	double
Balling	double

# # Show a statistical summary of the data kable(summary(jeffsVars[,1:5]))

PH	Filler.Level	Filler.Speed	Temperature	Usage.cont
Min. :0.000	Min.: 0.0	Min. : 0	Min.: 0.00	Min.: 0.00
1st Qu.:8.440	1st Qu.: 96.2	1st Qu.:3815	1st Qu.:65.20	1st Qu.:18.35
Median $:8.540$	Median :118.2	Median $:3980$	Median $:65.60$	Median :21.78
Mean $:8.532$	Mean : $108.4$	Mean $:3605$	Mean $:65.61$	Mean $:20.95$
3rd Qu.:8.680	3rd Qu.:120.0	3rd Qu.:3996	3rd Qu.:66.40	3rd Qu.:23.74
Max. $:9.360$	Max. :161.2	Max. $:4030$	Max. $:76.20$	Max. $:25.90$

#### kable(summary(jeffsVars[,6:9]))

Carb.Flow	Density	MFR	Balling
Min.: 0	Min. :0.000	Min.: 0.0	Min. :-0.170
1st Qu.:1133	1st Qu.:0.900	1st Qu.:694.9	1st Qu.: 1.496
Median $:3028$	Median $:0.980$	Median :721.4	Median: 1.648
Mean:2466	Mean $:1.173$	Mean $:646.0$	Mean: 2.197
3rd Qu.:3186	3rd Qu.:1.620	3rd Qu.:730.4	3rd Qu.: 3.292
Max. :5104	Max. $:1.920$	Max. :868.6	Max. : 4.012

```
# based on the summary, some of the PH values are 0.0, these rows should be removed since
# we cannot calculate for a 0.0 PH
jeffsVars <- jeffsVars[jeffsVars$PH>0.0,]
# now we'll check how many variables have values of zero
# show the frequency of zeros in the data for each variable
apply(jeffsVars,2,function(x){sum(abs(x-0.0)<=1e-6)})</pre>
##
             PH Filler.Level Filler.Speed Temperature
                                                            Usage.cont
##
                           16
                                        54
                                                      12
                                        MFR
##
      Carb.Flow
                      Density
                                                 Balling
##
                                        208
# based on these counts, we'll replace zeros with NAs for the following variables
index <- which(jeffsVars$Filler.Level <= 0.0)</pre>
is.na(jeffsVars$Filler.Level) <- index</pre>
index <- which(jeffsVars$Filler.Speed <= 0.0)</pre>
is.na(jeffsVars$Filler.Speed) <- index</pre>
```

```
index <- which(jeffsVars$Temperature <= 0.0)
is.na(jeffsVars$Temperature) <- index
index <- which(jeffsVars$Usage.cont <= 0.0)
is.na(jeffsVars$Usage.cont) <- index
index <- which(jeffsVars$Carb.Flow <= 0.0)
is.na(jeffsVars$Carb.Flow) <- index
index <- which(jeffsVars$MFR<= 0.0)
is.na(jeffsVars$MFR) <- index
# now we'll impute the NA values which represent missing values
# uses Predictive Mean Matching.
jeffsVars.imp <- complete(mice(jeffsVars, m = 3, print=F))
# jeffsVars.imp <- complete(jeffsVars.tmp,1)
# check that the NAs have all been resolved with imputed data
any(is.na(jeffsVars.imp))</pre>
```

#### ## [1] FALSE

# generate the basic stats for all variables, including the imputed values
kable(basicStats(jeffsVars.imp[,1:5]))

	РН	Filler.Level	Filler.Speed	Temperature	Usage.cont
nobs	2567.000000	2567.000000	2.567000e+03	2.567000e+03	2567.000000
NAs	0.000000	0.000000	0.000000e+00	0.000000e+00	0.000000
Minimum	7.880000	55.800000	9.980000e+02	6.360000e+01	12.080000
Maximum	9.360000	161.200000	4.030000e+03	7.620000e+01	25.900000
1. Quartile	8.440000	97.700000	3.851000e+03	6.520000e+01	18.380000
3. Quartile	8.680000	120.000000	3.997000e+03	6.640000e+01	23.750000
Mean	8.545649	109.242929	3.651046e+03	6.596619e+01	20.995014
Median	8.540000	118.400000	3.980000e+03	6.560000e+01	21.780000
Sum	21936.680000	280426.600000	9.372236e+06	1.693352e + 05	53894.200000
SE Mean	0.003405	0.309647	1.614337e + 01	2.720100e-02	0.058705
LCL Mean	8.538972	108.635745	3.619391e+03	6.591285e+01	20.879899
UCL Mean	8.552325	109.850114	3.682702e+03	6.601953e+01	21.110129
Variance	0.029762	246.127868	$6.689818e{+05}$	1.899339e+00	8.846730
Stdev	0.172516	15.688463	8.179131e+02	1.378165e+00	2.974345
Skewness	-0.290644	-0.846172	-2.633553e+00	2.385686e+00	-0.535497
Kurtosis	0.064429	0.038673	5.338732e+00	$1.022225e{+01}$	-1.014588

#### kable(basicStats(jeffsVars.imp[,6:9]))

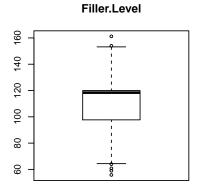
	Carb.Flow	Density	MFR	Balling
nobs	2.567000e+03	2567.000000	2.567000e+03	2567.000000
NAs	0.000000e+00	0.000000	0.000000e+00	0.000000
Minimum	2.600000e+01	0.240000	3.140000e+01	0.160000
Maximum	5.104000e+03	1.920000	8.686000e+02	4.012000
1. Quartile	1.166000e+03	0.900000	6.950000e+02	1.496000
3. Quartile	3.187000e+03	1.620000	7.304000e+02	3.292000
Mean	2.471698e + 03	1.174453	6.732807e + 02	2.199842
Median	3.028000e+03	0.980000	7.214000e+02	1.648000
Sum	6.344848e+06	3014.820000	1.728312e+06	5646.994000
SE Mean	2.112710e+01	0.007440	2.590541e+00	0.018347
LCL Mean	2.430270e + 03	1.159863	6.682010e+02	2.163866

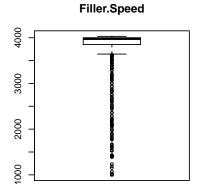
	Carb.Flow	Density	MFR	Balling
UCL Mean	2.513126e+03	1.189042	6.783605e+02	2.235818
Variance	1.145792e + 06	0.142105	1.722689e + 04	0.864058
Stdev	1.070417e + 03	0.376968	1.312513e + 02	0.929547
Skewness	-9.907760e-01	0.531113	-2.772375e+00	0.600459
Kurtosis	-5.754890e-01	-1.209505	6.841615e+00	-1.399653
Now we'll proc	eed with our ana	lysis of the p	redictor variabl	es.

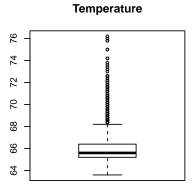
```
# set up the data combinations needed for the analysis
jeffsVars.pred <- jeffsVars.imp[,-c(1)]
head(jeffsVars.pred)</pre>
```

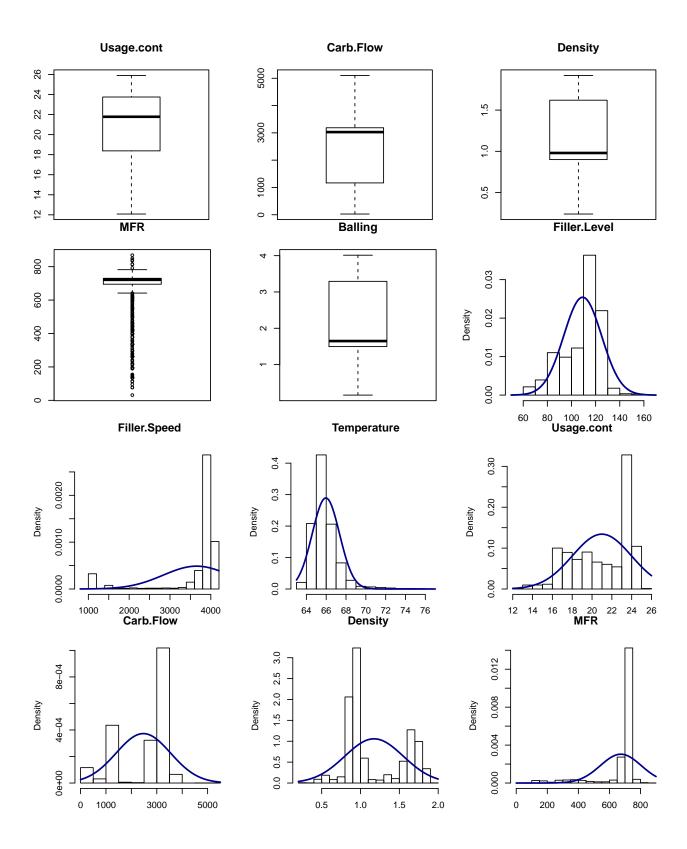
```
##
     Filler.Level Filler.Speed Temperature Usage.cont Carb.Flow Density
## 1
            121.2
                           4002
                                        66.0
                                                   16.18
                                                               2932
                                                                       0.88 725.0
## 2
                           3986
                                        67.6
            118.6
                                                   19.90
                                                               3144
                                                                       0.92 726.8
## 3
            120.0
                           4020
                                        67.0
                                                   17.76
                                                               2914
                                                                       1.58 735.0
## 4
            117.8
                           4012
                                        65.6
                                                   17.42
                                                               3062
                                                                       1.54 730.6
## 5
                           4010
                                        65.6
                                                   17.68
            118.6
                                                               3054
                                                                       1.54 722.8
## 6
            120.2
                           4014
                                        66.2
                                                   23.82
                                                               2948
                                                                       1.52 738.8
##
     Balling
## 1
       1.398
## 2
       1.498
       3.142
## 3
       3.042
## 4
## 5
       3.042
## 6
       2.992
```

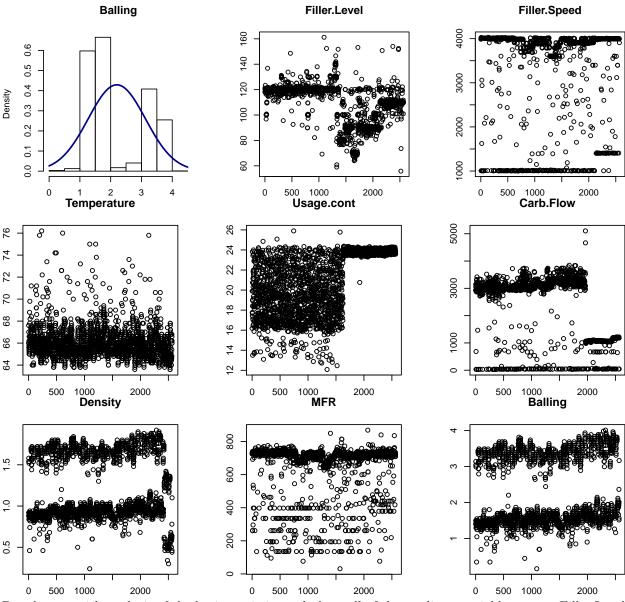
```
# required data sets include a train and test set
# form the training and test data partitions
n = nrow(jeffsVars.imp)
index <- sample(1:n, size = round(.80*n), replace = FALSE)
jeffsVars.train <- jeffsVars.imp[index,]
jeffsVars.test <- jeffsVars.imp[-index,]
jeffsVars.pred.train <- jeffsVars.pred[index,]
jeffsVars.pred.test <- jeffsVars.pred[-index,]</pre>
```











Based on a quick analysis of the basic statistics and plots, all of the predictor variables except Filler.Level will require a transformation to address issues with the variable's data distribution.

The Filler.Level variable distribution is fairly normal with few outliers so we will not perform any transformations and, instead, perform an analysis of how the variable interacts with the response variable in various regression models.

```
fit.glm <- train(PH~Filler.Level, data=jeffsVars.imp, method="glm", metric=metric,</pre>
                 preProc=c("center", "scale"), trControl=trainControl)
# GLMNET
set.seed(624)
#fit.qlmnet <- train(PH~Filler.Speed, data=jeffsVars.imp, method="qlmnet", metric=metric,
                     preProc=c("center", "scale"), trControl=trainControl)
# SVM
set.seed(624)
fit.svm <- train(PH~Filler.Level, data=jeffsVars.imp, method="svmRadial", metric=metric,</pre>
                 preProc=c("center", "scale"), trControl=trainControl)
# CART
set.seed(624)
grid \leftarrow expand.grid(.cp=c(0, 0.05, 0.1))
fit.cart <- train(PH~Filler.Level, data=jeffsVars.imp, method="rpart", metric=metric,</pre>
                  tuneGrid=grid, preProc=c("center", "scale"),
                  trControl=trainControl)
# KNN
set.seed(624)
fit.knn <- train(PH~Filler.Level, data=jeffsVars.imp, method="knn", metric=metric,
                 preProc=c("center", "scale"), trControl=trainControl)
# Compare algorithms
#feature_results <- resamples(list(LM=fit.lm, GLM=fit.glm, GLMNET=fit.glmnet,
                                    SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
feature_results <- resamples(list(LM=fit.lm, GLM=fit.glm,</pre>
                                   SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
summary(feature_results)
##
## Call:
## summary.resamples(object = feature_results)
## Models: LM, GLM, SVM, CART, KNN
## Number of resamples: 30
##
## MAE
##
                    1st Qu.
                                                   3rd Qu.
             Min.
                               Median
                                            Mean
        0.1201909 0.1284526 0.1314975 0.1311820 0.1339421 0.1392124
## GLM 0.1201909 0.1284526 0.1314975 0.1311820 0.1339421 0.1392124
                                                                         0
## SVM 0.1133574 0.1221499 0.1236970 0.1240205 0.1254063 0.1344164
                                                                         0
## CART 0.1136421 0.1239664 0.1259076 0.1263105 0.1289934 0.1330929
                                                                         0
## KNN 0.1161650 0.1252560 0.1265473 0.1273230 0.1300956 0.1367542
                                                                         0
##
## RMSE
##
             Min.
                    1st Qu.
                               Median
                                            Mean
                                                   3rd Qu.
        0.1453883\ 0.1593047\ 0.1629767\ 0.1632092\ 0.1672134\ 0.1767618
## LM
                                                                         0
## GLM 0.1453883 0.1593047 0.1629767 0.1632092 0.1672134 0.1767618
                                                                         0
## SVM 0.1427099 0.1543673 0.1575158 0.1583896 0.1612493 0.1752402
                                                                         0
## CART 0.1399061 0.1549897 0.1591494 0.1587623 0.1618148 0.1731220
## KNN 0.1445333 0.1568286 0.1601584 0.1605119 0.1634267 0.1780267
                                                                         0
##
## Rsquared
##
              Min.
                     1st Qu.
                                Median
                                             Mean
                                                    3rd Qu.
                                                                  Max. NA's
```

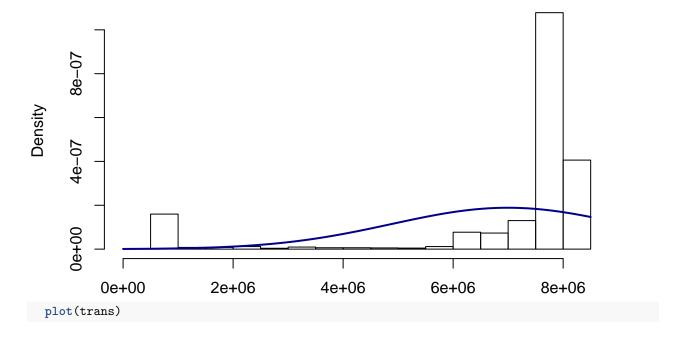
```
## LM 0.02986735 0.0854933 0.1077226 0.1079414 0.1244161 0.1848261 0 ## GLM 0.02986735 0.0854933 0.1077226 0.1079414 0.1244161 0.1848261 0 ## SVM 0.06404251 0.1543401 0.1733811 0.1688094 0.1924288 0.2262500 0 ## CART 0.06792278 0.1367975 0.1608383 0.1549523 0.1815269 0.2076281 0 ## KNN 0.06679426 0.1263891 0.1454547 0.1408140 0.1602291 0.1798211 0
```

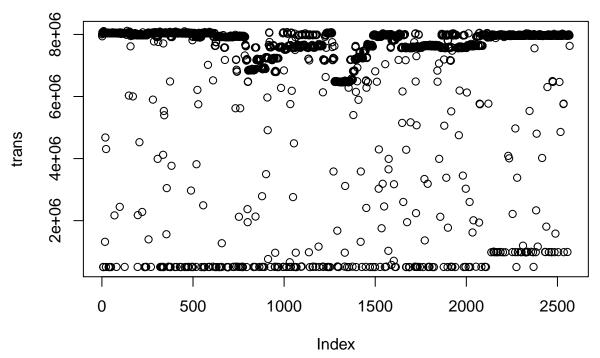
Next, we'll explore the effect of Box Cox transformations on the predictor variables with skewed or non-normal distributions.

We'll start with Filler.Speed first.

```
# perform the Box Cox transformation and then look at the distribution
lambda <- BoxCox.lambda(jeffsVars.pred$Filler.Speed)
trans <- BoxCox(jeffsVars.pred$Filler.Speed,lambda)
m <- mean(trans)
s <- sd(trans)
hist(trans,freq=FALSE,main = "Filler.Speed",xlab="")
curve(dnorm(x,mean=m,sd=s),col="darkblue",lwd=2,add=TRUE)</pre>
```

### Filler.Speed



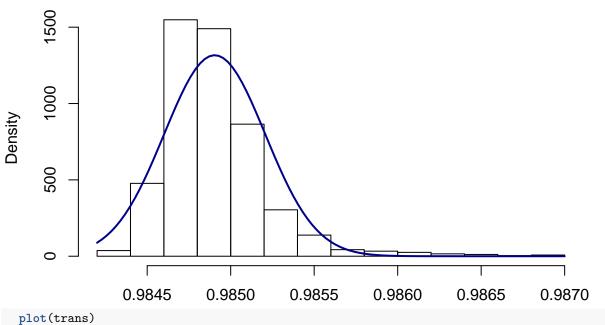


```
jeffsVars.imp <- cbind(jeffsVars.imp,Filler.Speed.Trans=trans)</pre>
# Run algorithms using 10-fold cross-validation
trainControl <- trainControl(method="repeatedcv", number=10, repeats=3)</pre>
metric <- "RMSE"</pre>
# LM
set.seed(624)
fit.lm <- train(PH~Filler.Speed.Trans, data=jeffsVars.imp, method="lm", metric=metric,</pre>
                                             preProc=c("center", "scale"), trControl=trainControl)
# GLM
set.seed(624)
fit.glm <- train(PH~Filler.Speed.Trans, data=jeffsVars.imp, method="glm", metric=metric,
                                                preProc=c("center", "scale"), trControl=trainControl)
# GLMNET
set.seed(624)
\#fit.glmnet \leftarrow train(PH\sim Filler.Speed, data=jeffsVars.imp, method="glmnet", metric=metric, metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metr
                                                            preProc=c("center", "scale"), trControl=trainControl)
# SVM
set.seed(624)
fit.svm <- train(PH~Filler.Speed.Trans, data=jeffsVars.imp, method="svmRadial", metric=metric,
                                                preProc=c("center", "scale"), trControl=trainControl)
# CART
set.seed(624)
grid <- expand.grid(.cp=c(0, 0.05, 0.1))
fit.cart <- train(PH~Filler.Speed.Trans, data=jeffsVars.imp, method="rpart", metric=metric,</pre>
                                                   tuneGrid=grid, preProc=c("center", "scale"),
                                                   trControl=trainControl)
# KNN
set.seed(624)
```

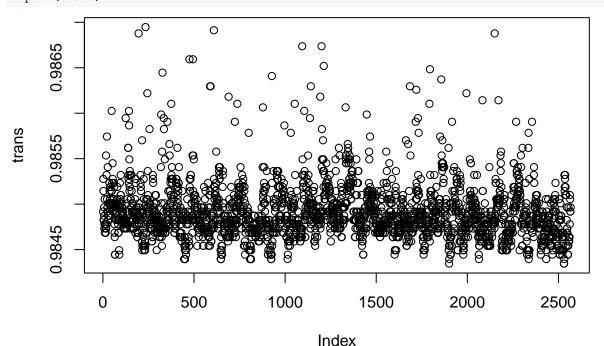
```
fit.knn <- train(PH~Filler.Speed.Trans, data=jeffsVars.imp, method="knn", metric=metric,
                 preProc=c("center", "scale"), trControl=trainControl)
# Compare algorithms
#feature_results <- resamples(list(LM=fit.lm, GLM=fit.qlm, GLMNET=fit.qlmnet,
                                    SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
feature_results <- resamples(list(LM=fit.lm, GLM=fit.glm,</pre>
                                   SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
summary(feature results)
##
## Call:
## summary.resamples(object = feature_results)
## Models: LM, GLM, SVM, CART, KNN
## Number of resamples: 30
##
## MAE
##
             Min.
                    1st Qu.
                               Median
                                            Mean
                                                   3rd Qu.
        0.1271923 0.1374589 0.1387211 0.1388418 0.1417721 0.1451230
## GLM 0.1271923 0.1374589 0.1387211 0.1388418 0.1417721 0.1451230
## SVM 0.1268878 0.1365774 0.1383034 0.1382064 0.1407241 0.1454906
                                                                         0
## CART 0.1162936 0.1272527 0.1310536 0.1296433 0.1323307 0.1384287
                                                                         0
## KNN 0.1160903 0.1270957 0.1300847 0.1290870 0.1318104 0.1374562
                                                                         0
##
## RMSE
##
                    1st Qu.
                               Median
                                            Mean
                                                   3rd Qu.
             Min.
        0.1547218 0.1695665 0.1715192 0.1724542 0.1774874 0.1842025
## GLM 0.1547218 0.1695665 0.1715192 0.1724542 0.1774874 0.1842025
## SVM 0.1547329 0.1693693 0.1711177 0.1722107 0.1770796 0.1839634
                                                                         0
## CART 0.1460320 0.1623519 0.1648594 0.1650456 0.1684791 0.1796409
                                                                         0
## KNN 0.1471417 0.1609710 0.1641329 0.1641600 0.1679500 0.1781773
                                                                         0
##
## Rsquared
##
                Min.
                           1st Qu.
                                        Median
                                                      Mean
                                                                3rd Qu.
        0.0000496871\ 0.0003409577\ 0.002479442\ 0.004181521\ 0.006748008
       0.0000496871 0.0003409577 0.002479442 0.004181521 0.006748008
## SVM 0.0001831605 0.0021416531 0.003759548 0.006611637 0.006423930
## CART 0.0469298405 0.0814837427 0.092009728 0.095301140 0.108929678
        0.0591161985 0.0781351847 0.098736862 0.102030486 0.115897337
## KNN
##
              Max. NA's
        0.02018689
## LM
## GLM 0.02018689
                      0
## SVM 0.03372577
                      0
                      0
## CART 0.16259133
## KNN 0.18211138
                      0
Next, we'll work with the Temperature variable.
We'll start with Filler.Speed first.
# look at a couple of the variables first
lambda <- BoxCox.lambda(jeffsVars.pred$Temperature)</pre>
trans <- BoxCox(jeffsVars.pred$Temperature,lambda)</pre>
  m <- mean(trans)
 s <- sd(trans)
```

```
hist(trans,freq=FALSE,main = "Temperature",xlab="")
curve(dnorm(x,mean=m,sd=s),col="darkblue",lwd=2,add=TRUE)
```

### **Temperature**







jeffsVars.imp <- cbind(jeffsVars.imp,Temperature.Trans=trans)</pre>

```
# Run algorithms using 10-fold cross-validation
trainControl <- trainControl(method="repeatedcv", number=10, repeats=3)</pre>
metric <- "RMSE"</pre>
```

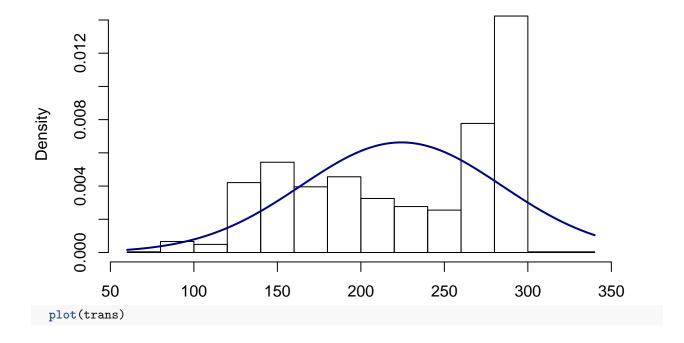
```
# LM
set.seed(624)
fit.lm <- train(PH~Temperature.Trans, data=jeffsVars.imp, method="lm", metric=metric,
                preProc=c("center", "scale"), trControl=trainControl)
# GI.M
set.seed(624)
fit.glm <- train(PH~Temperature.Trans, data=jeffsVars.imp, method="glm", metric=metric,</pre>
                 preProc=c("center", "scale"), trControl=trainControl)
# GLMNET
set.seed(624)
#fit.qlmnet <- train(PH~Filler.Speed, data=jeffsVars.imp, method="qlmnet", metric=metric,
                     preProc=c("center", "scale"), trControl=trainControl)
# SVM
set.seed(624)
fit.svm <- train(PH~Temperature.Trans, data=jeffsVars.imp, method="svmRadial", metric=metric,
                 preProc=c("center", "scale"), trControl=trainControl)
# CART
set.seed(624)
grid <- expand.grid(.cp=c(0, 0.05, 0.1))</pre>
fit.cart <- train(PH~Temperature.Trans, data=jeffsVars.imp, method="rpart", metric=metric,</pre>
                  tuneGrid=grid, preProc=c("center", "scale"),
                  trControl=trainControl)
# KNN
set.seed(624)
fit.knn <- train(PH~Temperature.Trans, data=jeffsVars.imp, method="knn", metric=metric,
                 preProc=c("center", "scale"), trControl=trainControl)
# Compare algorithms
#feature_results <- resamples(list(LM=fit.lm, GLM=fit.glm, GLMNET=fit.glmnet,
                                    SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
feature_results <- resamples(list(LM=fit.lm, GLM=fit.glm,</pre>
                                  SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
summary(feature results)
##
## Call:
## summary.resamples(object = feature results)
## Models: LM, GLM, SVM, CART, KNN
## Number of resamples: 30
##
## MAE
##
                    1st Qu.
                               Median
                                                   3rd Qu.
                                            Mean
## LM
        0.1278340\ 0.1339411\ 0.1368592\ 0.1369722\ 0.1402438\ 0.1427002
## GLM 0.1278340 0.1339411 0.1368592 0.1369722 0.1402438 0.1427002
## SVM 0.1260045 0.1314833 0.1366965 0.1352213 0.1393344 0.1413296
                                                                         0
## CART 0.1264456 0.1319398 0.1364626 0.1357145 0.1393085 0.1444363
                                                                         0
## KNN 0.1255462 0.1313143 0.1361359 0.1352214 0.1392505 0.1433164
##
## RMSE
             Min.
                    1st Qu.
                               Median
                                            Mean
                                                   3rd Qu.
                                                                Max. NA's
       0.1554725 0.1661963 0.1700972 0.1701033 0.1754110 0.1818608
```

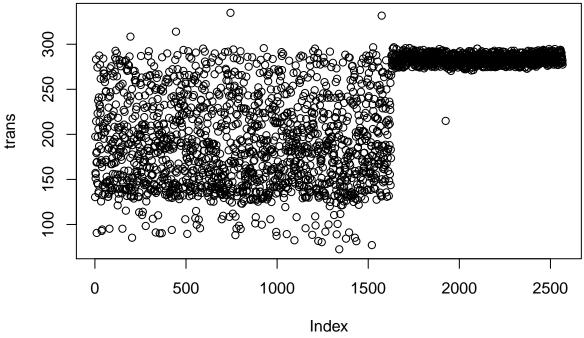
```
## GLM 0.1554725 0.1661963 0.1700972 0.1701033 0.1754110 0.1818608
                                                                         0
## SVM 0.1549669 0.1650627 0.1676289 0.1682999 0.1736941 0.1795348
                                                                         0
  CART 0.1555936 0.1649727 0.1680420 0.1689323 0.1734466 0.1818727
                                                                         0
        0.1531764 0.1649054 0.1679697 0.1684522 0.1734633 0.1806526
                                                                         0
##
## Rsquared
##
                         1st Qu.
                                     Median
                Min.
                                                  Mean
                                                           3rd Qu.
                                                                         Max.
        0.0001357553 0.01486673 0.02882928 0.03146091 0.04211416 0.08112341
## LM
  GLM
        0.0001357553 0.01486673 0.02882928 0.03146091 0.04211416 0.08112341
        0.0058105075\ 0.02962261\ 0.05327520\ 0.05333067\ 0.07889755\ 0.10772969
  CART 0.0052320741 0.02931945 0.03919873 0.04854575 0.06525373 0.13217649
        0.0055890244\ 0.03007223\ 0.04850929\ 0.05315718\ 0.06540948\ 0.13996601
  KNN
##
##
        NA's
## LM
           0
## GLM
           0
## SVM
           0
## CART
           0
## KNN
           0
```

Next, we'll work with the Usage.cont variable.

```
# look at a couple of the variables first
lambda <- BoxCox.lambda(jeffsVars.pred$Usage.cont)
trans <- BoxCox(jeffsVars.pred$Usage.cont,lambda)
m <- mean(trans)
s <- sd(trans)
hist(trans,freq=FALSE,main = "Usage.cont",xlab="")
curve(dnorm(x,mean=m,sd=s),col="darkblue",lwd=2,add=TRUE)</pre>
```

### **Usage.cont**



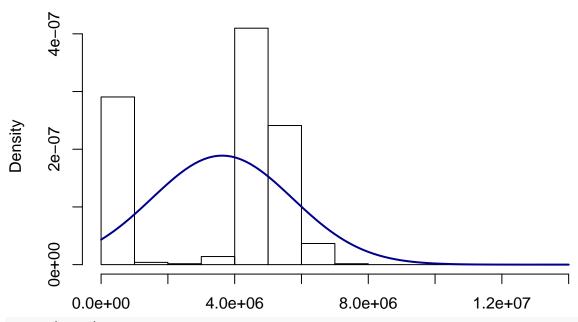


```
jeffsVars.imp <- cbind(jeffsVars.imp,Usage.cont.Trans=trans)</pre>
# Run algorithms using 10-fold cross-validation
trainControl <- trainControl(method="repeatedcv", number=10, repeats=3)</pre>
metric <- "RMSE"</pre>
# LM
set.seed(624)
fit.lm <- train(PH~Usage.cont.Trans, data=jeffsVars.imp, method="lm", metric=metric,
                preProc=c("center", "scale"), trControl=trainControl)
# GI.M
set.seed(624)
fit.glm <- train(PH~Usage.cont.Trans, data=jeffsVars.imp, method="glm", metric=metric,
                 preProc=c("center", "scale"), trControl=trainControl)
# GLMNET
set.seed(624)
#fit.glmnet <- train(PH~Filler.Speed, data=jeffsVars.imp, method="glmnet", metric=metric,
                     preProc=c("center", "scale"), trControl=trainControl)
# SVM
set.seed(624)
fit.svm <- train(PH~Usage.cont.Trans, data=jeffsVars.imp, method="svmRadial", metric=metric,
                 preProc=c("center", "scale"), trControl=trainControl)
# CART
set.seed(624)
grid <- expand.grid(.cp=c(0, 0.05, 0.1))</pre>
fit.cart <- train(PH~Usage.cont.Trans, data=jeffsVars.imp, method="rpart", metric=metric,</pre>
                  tuneGrid=grid, preProc=c("center", "scale"),
                  trControl=trainControl)
# KNN
set.seed(624)
fit.knn <- train(PH~Usage.cont.Trans, data=jeffsVars.imp, method="knn", metric=metric,
```

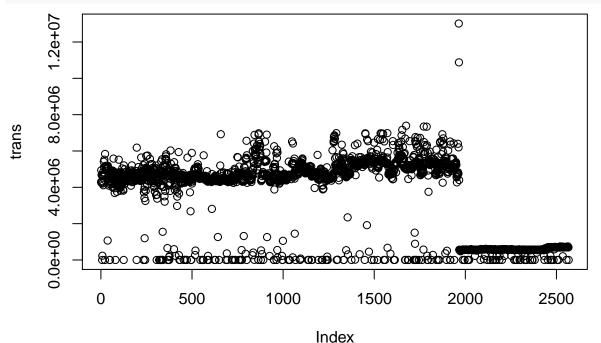
```
preProc=c("center", "scale"), trControl=trainControl)
# Compare algorithms
#feature_results <- resamples(list(LM=fit.lm, GLM=fit.qlm, GLMNET=fit.qlmnet,
                                    SVM=fit.sum, CART=fit.cart, KNN=fit.knn))
feature_results <- resamples(list(LM=fit.lm, GLM=fit.glm,</pre>
                                   SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
summary(feature results)
##
## Call:
## summary.resamples(object = feature_results)
## Models: LM, GLM, SVM, CART, KNN
## Number of resamples: 30
##
## MAE
                    1st Qu.
                               Median
             Min.
                                            Mean
                                                   3rd Qu.
                                                                 Max. NA's
        0.1212672\ 0.1263601\ 0.1298071\ 0.1296214\ 0.1326648\ 0.1367856
## LM
        0.1212672 0.1263601 0.1298071 0.1296214 0.1326648 0.1367856
                                                                         0
## SVM 0.1184250 0.1222279 0.1250092 0.1254985 0.1275440 0.1368081
                                                                         0
## CART 0.1165529 0.1217735 0.1245267 0.1251947 0.1278804 0.1356898
                                                                         0
## KNN 0.1189963 0.1249875 0.1272540 0.1287365 0.1310773 0.1441659
                                                                         0
##
## RMSE
##
                               Median
             Min.
                    1st Qu.
                                            Mean
                                                   3rd Qu.
                                                                 Max. NA's
        0.1474118 0.1583714 0.1635745 0.1628401 0.1667021 0.1773201
## GLM 0.1474118 0.1583714 0.1635745 0.1628401 0.1667021 0.1773201
                                                                         0
## SVM 0.1442978 0.1546044 0.1583267 0.1585363 0.1613678 0.1745178
                                                                         0
## CART 0.1419906 0.1532369 0.1579076 0.1574653 0.1606953 0.1736164
                                                                         0
## KNN 0.1464399 0.1595329 0.1619874 0.1622126 0.1639815 0.1805287
                                                                         0
##
## Rsquared
##
                      1st Qu.
                                  Median
                                              Mean
                                                     3rd Qu.
                                                                   Max. NA's
              Min.
        0.05316995 0.08853612 0.1124225 0.1118365 0.1312455 0.2085573
## GLM 0.05316995 0.08853612 0.1124225 0.1118365 0.1312455 0.2085573
                                                                           0
       0.06370052 0.14644607 0.1611852 0.1622991 0.1996278 0.2260597
## SVM
                                                                           0
## CART 0.09043158 0.14867365 0.1722759 0.1695019 0.2073174 0.2353797
                                                                           0
## KNN 0.05925625 0.10764813 0.1410987 0.1360204 0.1652828 0.2024995
Next, we'll work with the Carb.Flow variable.
# look at a couple of the variables first
lambda <- BoxCox.lambda(jeffsVars.pred$Carb.Flow)</pre>
trans <- BoxCox(jeffsVars.pred$Carb.Flow,lambda)</pre>
  m <- mean(trans)
  s <- sd(trans)
 hist(trans,freq=FALSE,main = "Carb.Flow",xlab="")
```

curve(dnorm(x,mean=m,sd=s),col="darkblue",lwd=2,add=TRUE)

### Carb.Flow







```
jeffsVars.imp <- cbind(jeffsVars.imp,Carb.Flow.Trans=trans)</pre>
```

```
# Run algorithms using 10-fold cross-validation
trainControl <- trainControl(method="repeatedcv", number=10, repeats=3)
metric <- "RMSE"

# LM
set.seed(624)
fit.lm <- train(PH~Carb.Flow.Trans, data=jeffsVars.imp, method="lm", metric=metric,</pre>
```

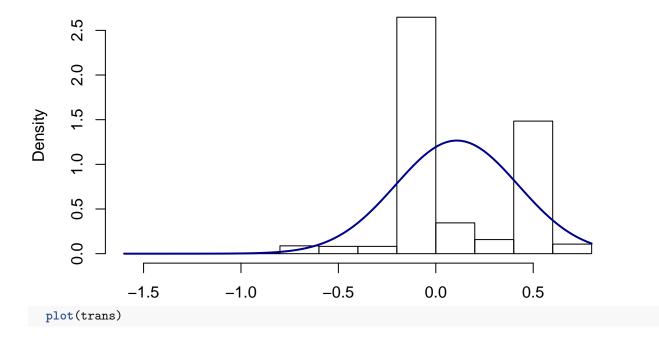
```
preProc=c("center", "scale"), trControl=trainControl)
# GLM
set.seed(624)
fit.glm <- train(PH~Carb.Flow.Trans, data=jeffsVars.imp, method="glm", metric=metric,
                 preProc=c("center", "scale"), trControl=trainControl)
# GLMNET
set.seed(624)
#fit.glmnet <- train(PH~Filler.Speed, data=jeffsVars.imp, method="glmnet", metric=metric,
                     preProc=c("center", "scale"), trControl=trainControl)
# SVM
set.seed(624)
fit.svm <- train(PH~Carb.Flow.Trans, data=jeffsVars.imp, method="svmRadial", metric=metric,
                 preProc=c("center", "scale"), trControl=trainControl)
# CART
set.seed(624)
grid <- expand.grid(.cp=c(0, 0.05, 0.1))
fit.cart <- train(PH~Carb.Flow.Trans, data=jeffsVars.imp, method="rpart", metric=metric,</pre>
                  tuneGrid=grid, preProc=c("center", "scale"),
                  trControl=trainControl)
# KNN
set.seed(624)
fit.knn <- train(PH~Carb.Flow.Trans, data=jeffsVars.imp, method="knn", metric=metric,
                 preProc=c("center", "scale"), trControl=trainControl)
# Compare algorithms
#feature_results <- resamples(list(LM=fit.lm, GLM=fit.glm, GLMNET=fit.glmnet,
                                    SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
feature_results <- resamples(list(LM=fit.lm, GLM=fit.glm,</pre>
                                  SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
summary(feature_results)
##
## Call:
## summary.resamples(object = feature_results)
## Models: LM, GLM, SVM, CART, KNN
## Number of resamples: 30
##
## MAE
##
             Min.
                    1st Qu.
                               Median
                                           Mean
                                                   3rd Qu.
## T.M
       0.1241236\ 0.1349304\ 0.1372162\ 0.1370214\ 0.1398379\ 0.1451241
## GLM 0.1241236 0.1349304 0.1372162 0.1370214 0.1398379 0.1451241
                                                                        0
## SVM 0.1182172 0.1285998 0.1315154 0.1314406 0.1352706 0.1396238
                                                                        0
## CART 0.1202369 0.1336060 0.1366733 0.1369843 0.1404501 0.1484637
                                                                        0
## KNN 0.1182755 0.1320064 0.1341726 0.1347674 0.1377288 0.1460630
                                                                        0
##
## RMSE
##
             Min.
                    1st Qu.
                               Median
                                           Mean
                                                   3rd Qu.
## LM
       0.1512740 0.1679135 0.1708299 0.1703785 0.1736246 0.1845862
## GLM 0.1512740 0.1679135 0.1708299 0.1703785 0.1736246 0.1845862
                                                                        0
## SVM 0.1458013 0.1626592 0.1656994 0.1655638 0.1690097 0.1818950
                                                                        0
## CART 0.1484250 0.1683059 0.1715341 0.1716644 0.1746056 0.1896656
```

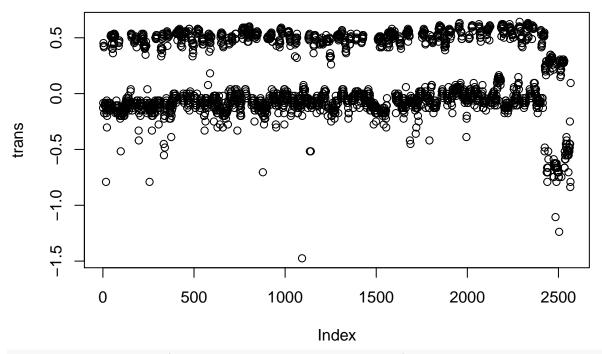
```
## KNN 0.1458705 0.1649942 0.1677449 0.1682364 0.1712889 0.1860165
##
## Rsquared
##
                        1st Qu.
                                    Median
                                                          3rd Qu.
                Min.
                                                  Mean
                                                                        Max.
## LM
        1.059423e-07 0.01450212 0.02860950 0.02885432 0.04033276 0.07312242
## GLM
       1.059423e-07 0.01450212 0.02860950 0.02885432 0.04033276 0.07312242
## SVM
       4.199900e-02 0.05874813 0.08254345 0.08480841 0.10415913 0.15600255
## CART 1.597245e-02 0.04179563 0.05758382 0.06559880 0.09364391 0.13026163
       3.103466e-02 0.05671126 0.07340516 0.07805263 0.10445217 0.13925275
##
        NA's
## LM
           0
## GLM
           0
## SVM
           0
           0
## CART
## KNN
           0
```

Next, we'll work with the Density variable.

```
# look at a couple of the variables first
lambda <- BoxCox.lambda(jeffsVars.pred$Density)
trans <- BoxCox(jeffsVars.pred$Density,lambda)
  m <- mean(trans)
  s <- sd(trans)
  hist(trans,freq=FALSE,main = "Density",xlab="")
  curve(dnorm(x,mean=m,sd=s),col="darkblue",lwd=2,add=TRUE)</pre>
```

### **Density**

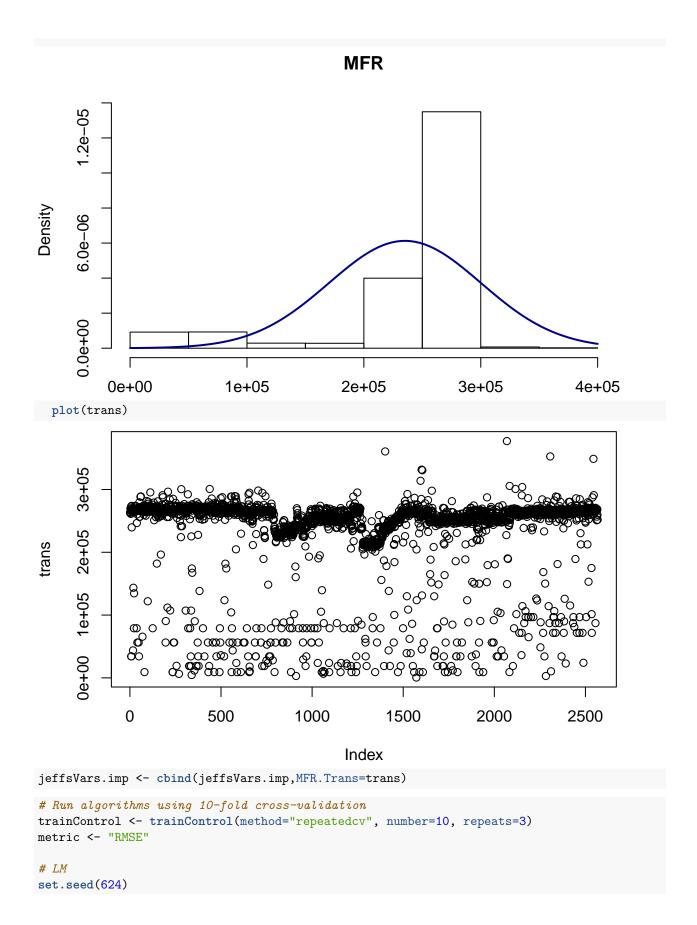




jeffsVars.imp <- cbind(jeffsVars.imp,Density.Trans=trans)</pre>

```
# Run algorithms using 10-fold cross-validation
trainControl <- trainControl(method="repeatedcv", number=10, repeats=3)</pre>
metric <- "RMSE"</pre>
# LM
set.seed(624)
fit.lm <- train(PH~Density.Trans, data=jeffsVars.imp, method="lm", metric=metric,
                preProc=c("center", "scale"), trControl=trainControl)
# GI.M
set.seed(624)
fit.glm <- train(PH~Density.Trans, data=jeffsVars.imp, method="glm", metric=metric,</pre>
                 preProc=c("center", "scale"), trControl=trainControl)
# GLMNET
set.seed(624)
#fit.glmnet <- train(PH~Filler.Speed, data=jeffsVars.imp, method="glmnet", metric=metric,
                     preProc=c("center", "scale"), trControl=trainControl)
# SVM
set.seed(624)
fit.svm <- train(PH~Density.Trans, data=jeffsVars.imp, method="svmRadial", metric=metric,
                 preProc=c("center", "scale"), trControl=trainControl)
# CART
set.seed(624)
grid <- expand.grid(.cp=c(0, 0.05, 0.1))</pre>
fit.cart <- train(PH~Density.Trans, data=jeffsVars.imp, method="rpart", metric=metric,</pre>
                  tuneGrid=grid, preProc=c("center", "scale"),
                  trControl=trainControl)
# KNN
set.seed(624)
fit.knn <- train(PH~Density.Trans, data=jeffsVars.imp, method="knn", metric=metric,
```

```
preProc=c("center", "scale"), trControl=trainControl)
# Compare algorithms
#feature_results <- resamples(list(LM=fit.lm, GLM=fit.qlm, GLMNET=fit.qlmnet,
                                    SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
feature_results <- resamples(list(LM=fit.lm, GLM=fit.glm,</pre>
                                   SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
summary(feature results)
##
## Call:
## summary.resamples(object = feature_results)
## Models: LM, GLM, SVM, CART, KNN
## Number of resamples: 30
##
## MAE
             Min.
                    1st Qu.
                               Median
                                            Mean
                                                   3rd Qu.
                                                                 Max. NA's
        0.1259148 \ 0.1366626 \ 0.1375890 \ 0.1381896 \ 0.1410775 \ 0.1441072
## LM
        0.1259148 0.1366626 0.1375890 0.1381896 0.1410775 0.1441072
                                                                         0
## SVM 0.1206728 0.1294410 0.1328013 0.1324740 0.1355260 0.1388555
                                                                         0
## CART 0.1222047 0.1296428 0.1328848 0.1323287 0.1351617 0.1376902
                                                                         0
## KNN 0.1221373 0.1296131 0.1325631 0.1321520 0.1350807 0.1382186
                                                                         0
##
## RMSE
##
                               Median
             Min.
                    1st Qu.
                                            Mean
                                                   3rd Qu.
                                                                 Max. NA's
        0.1543272 0.1691211 0.1718563 0.1720389 0.1768771 0.1830566
## GLM 0.1543272 0.1691211 0.1718563 0.1720389 0.1768771 0.1830566
                                                                         0
## SVM 0.1512251 0.1637221 0.1664892 0.1671117 0.1719010 0.1783252
                                                                         0
## CART 0.1515065 0.1622659 0.1675605 0.1669726 0.1717553 0.1759668
                                                                         0
## KNN 0.1508530 0.1625653 0.1671192 0.1666046 0.1715170 0.1757176
                                                                         0
##
## Rsquared
##
                         1st Qu.
                                       Median
                Min.
                                                     Mean
                                                              3rd Qu.
        5.830486e-06 0.001985787 0.008314255 0.008010528 0.01125320
## GLM 5.830486e-06 0.001985787 0.008314255 0.008010528 0.01125320
        2.275359e-02 0.049529010 0.059899344 0.065049448 0.07770287
## SVM
## CART 1.912344e-02 0.052927012 0.066619049 0.070330750 0.08712817
        2.675947e-02 0.058805891 0.068280337 0.072360521 0.08987026
##
              Max. NA's
## LM
        0.02306657
## GLM 0.02306657
                      0
## SVM 0.16028619
                      0
## CART 0.13153455
                      0
## KNN 0.13321256
Next, we'll work with the MFR variable.
# look at a couple of the variables first
lambda <- BoxCox.lambda(jeffsVars.pred$MFR)</pre>
trans <- BoxCox(jeffsVars.pred$MFR,lambda)</pre>
  m <- mean(trans)
  s <- sd(trans)
  hist(trans,freq=FALSE,main = "MFR",xlab="")
  curve(dnorm(x,mean=m,sd=s),col="darkblue",lwd=2,add=TRUE)
```



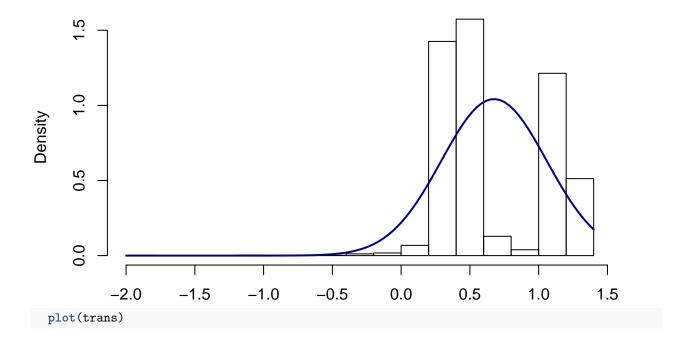
```
fit.lm <- train(PH~MFR.Trans, data=jeffsVars.imp, method="lm", metric=metric,</pre>
                                preProc=c("center", "scale"), trControl=trainControl)
# GLM
set.seed(624)
fit.glm <- train(PH~MFR.Trans, data=jeffsVars.imp, method="glm", metric=metric,</pre>
                                  preProc=c("center", "scale"), trControl=trainControl)
# GLMNET
set.seed(624)
\#fit.glmnet \leftarrow train(PH-Filler.Speed, data=jeffsVars.imp, method="glmnet", metric=metric, metric=metric, metric=metric, metrod=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=metric=
                                          preProc=c("center", "scale"), trControl=trainControl)
# SVM
set.seed(624)
fit.svm <- train(PH~MFR.Trans, data=jeffsVars.imp, method="svmRadial", metric=metric,
                                  preProc=c("center", "scale"), trControl=trainControl)
# CART
set.seed(624)
grid \leftarrow expand.grid(.cp=c(0, 0.05, 0.1))
fit.cart <- train(PH~MFR.Trans, data=jeffsVars.imp, method="rpart", metric=metric,
                                    tuneGrid=grid, preProc=c("center", "scale"),
                                    trControl=trainControl)
# KNN
set.seed(624)
fit.knn <- train(PH~MFR.Trans, data=jeffsVars.imp, method="knn", metric=metric,
                                  preProc=c("center", "scale"), trControl=trainControl)
# Compare algorithms
#feature_results <- resamples(list(LM=fit.lm, GLM=fit.glm, GLMNET=fit.glmnet,
                                                                      SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
feature_results <- resamples(list(LM=fit.lm, GLM=fit.glm,</pre>
                                                                    SVM=fit.svm, CART=fit.cart, KNN=fit.knn))
summary(feature_results)
##
## Call:
## summary.resamples(object = feature_results)
## Models: LM, GLM, SVM, CART, KNN
## Number of resamples: 30
##
## MAE
##
                          Min.
                                       1st Qu.
                                                              Median
                                                                                      Mean
                                                                                                    3rd Qu.
               0.1271927 0.1374235 0.1387372 0.1388281 0.1417470 0.1451214
## GLM 0.1271927 0.1374235 0.1387372 0.1388281 0.1417470 0.1451214
                                                                                                                                               0
## SVM 0.1267783 0.1366648 0.1381861 0.1384726 0.1414777 0.1462941
## CART 0.1272557 0.1372381 0.1387320 0.1387509 0.1417459 0.1451763
                                                                                                                                               0
## KNN 0.1257882 0.1360143 0.1409684 0.1400099 0.1436910 0.1506375
##
## RMSE
                                                                                                                               Max. NA's
##
                          Min.
                                        1st Qu.
                                                              Median
                                                                                      Mean
                                                                                                    3rd Qu.
                0.1547053 0.1695260 0.1714954 0.1724423 0.1774725 0.1842028
## LM
## GLM 0.1547053 0.1695260 0.1714954 0.1724423 0.1774725 0.1842028
                                                                                                                                               0
## SVM 0.1545132 0.1696239 0.1720508 0.1723559 0.1772828 0.1842605
```

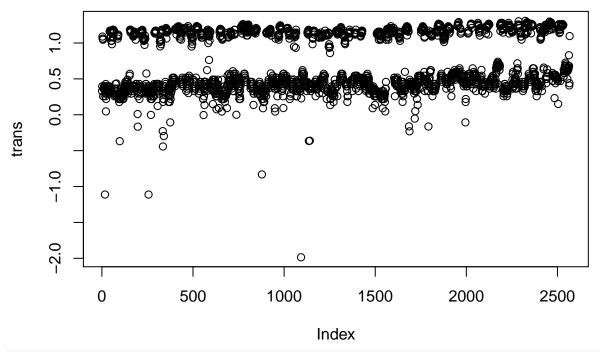
```
## CART 0.1548066 0.1694532 0.1715767 0.1723899 0.1774563 0.1842563
                                                                         0
## KNN 0.1516632 0.1709094 0.1769157 0.1752070 0.1799176 0.1948919
                                                                         0
##
## Rsquared
##
                Min.
                           1st Qu.
                                        Median
                                                      Mean
                                                                3rd Qu.
## LM
        1.985897e-07 0.0002442781 0.002253521 0.003767926 0.005522049
        1.985897e-07 0.0002442781 0.002253521 0.003767926 0.005522049
        4.045557e-05 0.0010331188 0.002637306 0.006183408 0.007490397
## SVM
  CART
                  NA
                                NA
                                            NA
                                                       NaN
## KNN
        4.183698e-05 0.0092037323 0.017492110 0.018863525 0.023865447
##
        0.01595261
## LM
        0.01595261
                      0
##
  GLM
        0.03558619
                      0
## SVM
## CART
                NA
                     30
## KNN
        0.06038659
                      0
```

Next, we'll work with the Bslling variable.

```
# look at a couple of the variables first
lambda <- BoxCox.lambda(jeffsVars.pred$Balling)
trans <- BoxCox(jeffsVars.pred$Balling,lambda)
m <- mean(trans)
s <- sd(trans)
hist(trans,freq=FALSE,main = "Balling",xlab="")
curve(dnorm(x,mean=m,sd=s),col="darkblue",lwd=2,add=TRUE)</pre>
```

### **Balling**





jeffsVars.imp <- cbind(jeffsVars.imp,Balling.Trans=trans)</pre>

```
# Run algorithms using 10-fold cross-validation
trainControl <- trainControl(method="repeatedcv", number=10, repeats=3)</pre>
metric <- "RMSE"</pre>
# LM
set.seed(624)
fit.lm <- train(PH~Balling.Trans, data=jeffsVars.imp, method="lm", metric=metric,
                preProc=c("center", "scale"), trControl=trainControl)
# GI.M
set.seed(624)
fit.glm <- train(PH~Balling.Trans, data=jeffsVars.imp, method="glm", metric=metric,</pre>
                 preProc=c("center", "scale"), trControl=trainControl)
# GLMNET
set.seed(624)
#fit.glmnet <- train(PH~Filler.Speed, data=jeffsVars.imp, method="glmnet", metric=metric,
                     preProc=c("center", "scale"), trControl=trainControl)
# SVM
set.seed(624)
fit.svm <- train(PH~Balling.Trans, data=jeffsVars.imp, method="svmRadial", metric=metric,
                 preProc=c("center", "scale"), trControl=trainControl)
# CART
set.seed(624)
grid <- expand.grid(.cp=c(0, 0.05, 0.1))</pre>
fit.cart <- train(PH~Balling.Trans, data=jeffsVars.imp, method="rpart", metric=metric,</pre>
                  tuneGrid=grid, preProc=c("center", "scale"),
                  trControl=trainControl)
# KNN
set.seed(624)
fit.knn <- train(PH~Balling.Trans, data=jeffsVars.imp, method="knn", metric=metric,
```

```
## summary.resamples(object = feature_results)
## Models: LM, GLM, SVM, CART, KNN
## Number of resamples: 30
##
## MAE
##
             Min.
                    1st Qu.
                               Median
                                            Mean
                                                   3rd Qu.
                                                                 Max. NA's
        0.1266276 0.1369666 0.1382339 0.1385185 0.1415090 0.1447364
## LM
        0.1266276 0.1369666 0.1382339 0.1385185 0.1415090 0.1447364
                                                                         0
## SVM 0.1210123 0.1306028 0.1331553 0.1323495 0.1350785 0.1387711
                                                                         0
## CART 0.1210872 0.1284054 0.1324030 0.1314425 0.1351302 0.1364562
                                                                         0
## KNN 0.1208905 0.1284944 0.1320758 0.1307691 0.1340340 0.1364024
                                                                         0
##
## RMSE
                                            Mean
                                                                 Max. NA's
##
             Min.
                    1st Qu.
                               Median
                                                   3rd Qu.
        0.1547101 0.1693703 0.1716753 0.1724054 0.1772578 0.1840733
## GLM 0.1547101 0.1693703 0.1716753 0.1724054 0.1772578 0.1840733
                                                                         0
## SVM 0.1500447 0.1632652 0.1655961 0.1659218 0.1715056 0.1769712
                                                                         0
## CART 0.1492675 0.1621286 0.1660909 0.1660337 0.1721116 0.1774060
                                                                         0
## KNN 0.1495694 0.1621816 0.1646886 0.1651819 0.1709270 0.1756947
                                                                         0
##
## Rsquared
##
                         1st Qu.
                                       Median
                                                               3rd Qu.
                Min.
                                                     Mean
        6.241192e-06 0.000790578 0.002662098 0.004693808 0.006526726
        6.241192e-06 0.000790578 0.002662098 0.004693808 0.006526726
## GLM
        3.136045e-02 0.060732038 0.069267516 0.077273276 0.090490935
## CART 3.125766e-02 0.061486740 0.083684605 0.085903689 0.102055374
        3.571639e-02 0.066262307 0.084046226 0.092334003 0.118251132
##
              Max. NA's
## LM
        0.02629823
## GLM 0.02629823
                      0
## SVM 0.15194152
                      0
## CART 0.15520604
                      0
## KNN 0.15846199
The 1-on-1 modeling results have been so poor that we're going to try a modeling experiment using all
variables in the set (in their transformed state if applicable).
# generate a generalize linear model with all variables
whole.model <- glm(PH ~ Filler.Level+Filler.Speed.Trans+Temperature.Trans+Usage.cont.Trans+Carb.Flow.Tr
stepwise <- step(whole.model, direction = "both")</pre>
## Start: AIC=-2344.26
## PH ~ Filler.Level + Filler.Speed.Trans + Temperature.Trans +
```

preProc=c("center", "scale"), trControl=trainControl)

SVM=fit.svm, CART=fit.cart, KNN=fit.knn))

SVM=fit.svm, CART=fit.cart, KNN=fit.knn))

#feature\_results <- resamples(list(LM=fit.lm, GLM=fit.qlm, GLMNET=fit.qlmnet,

feature\_results <- resamples(list(LM=fit.lm, GLM=fit.glm,</pre>

# Compare algorithms

summary(feature results)

## Call:

```
##
       Usage.cont.Trans + Carb.Flow.Trans + Density.Trans + MFR.Trans +
##
       Balling.Trans
##
##
                        Df Deviance
                                        AIC
## - Filler.Speed.Trans
                        1
                             59.845 -2345.9
## - MFR.Trans
                         1
                             59.845 -2345.9
## <none>
                             59.835 -2344.3
## - Balling.Trans
                             59.937 -2341.9
                         1
## - Density.Trans
                         1
                             60.001 -2339.1
## - Carb.Flow.Trans
                         1
                             60.316 -2325.7
## - Usage.cont.Trans
                         1
                             62.010 -2254.6
## - Temperature.Trans
                             63.351 -2199.7
                         1
## - Filler.Level
                         1
                             64.393 -2157.8
##
## Step: AIC=-2345.86
## PH ~ Filler.Level + Temperature.Trans + Usage.cont.Trans + Carb.Flow.Trans +
##
       Density.Trans + MFR.Trans + Balling.Trans
##
##
                        Df Deviance
                                        ATC
## <none>
                             59.845 -2345.9
## + Filler.Speed.Trans 1
                             59.835 -2344.3
## - Balling.Trans
                             59.947 -2343.5
                         1
## - Density.Trans
                             60.012 -2340.7
                         1
## - Carb.Flow.Trans
                         1
                             60.317 -2327.7
## - MFR.Trans
                         1
                             60.357 -2326.0
## - Usage.cont.Trans
                         1
                             62.060 -2254.6
## - Temperature.Trans
                             63.354 -2201.6
                         1
## - Filler.Level
                         1
                             64.402 -2159.4
stepwise
##
## Call: glm(formula = PH ~ Filler.Level + Temperature.Trans + Usage.cont.Trans +
##
       Carb.Flow.Trans + Density.Trans + MFR.Trans + Balling.Trans,
##
       family = gaussian(link = "identity"), data = jeffsVars.imp)
##
## Coefficients:
                           Filler.Level Temperature.Trans
##
         (Intercept)
##
           1.406e+02
                              2.961e-03
                                                 -1.342e+02
##
   Usage.cont.Trans
                        Carb.Flow.Trans
                                             Density.Trans
##
          -5.940e-04
                              7.868e-09
                                                 6.943e-02
##
           MFR.Trans
                          Balling.Trans
          -2.484e-07
                             -4.538e-02
##
##
## Degrees of Freedom: 2566 Total (i.e. Null); 2559 Residual
## Null Deviance:
                        76.37
## Residual Deviance: 59.84
                                AIC: -2346
```