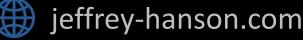
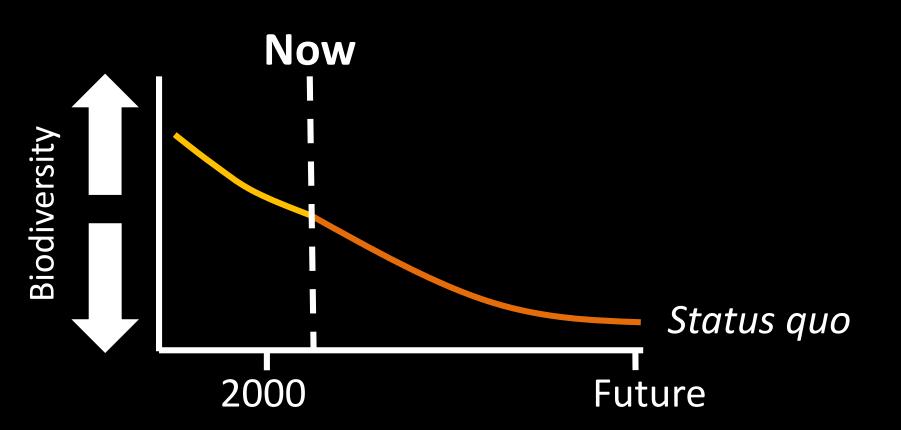
# Conservation decisions with exact algorithm solvers

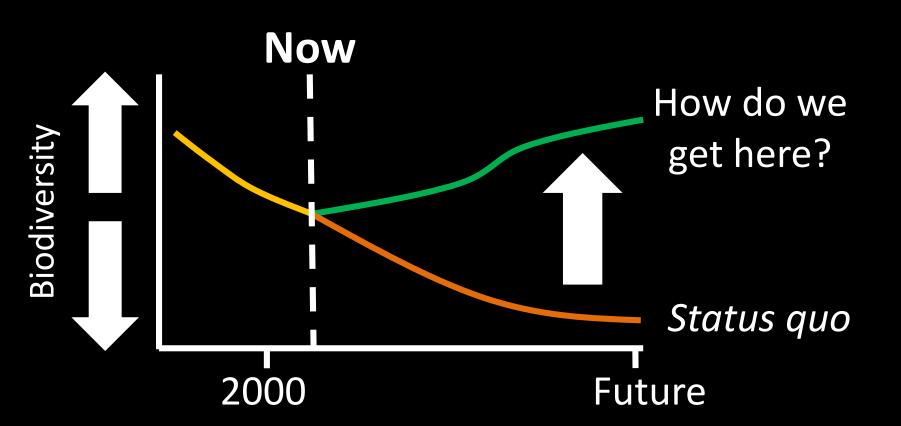


Jeffrey Hanson

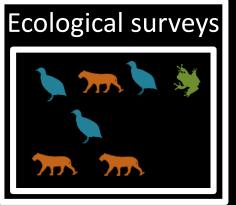


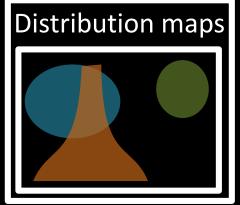


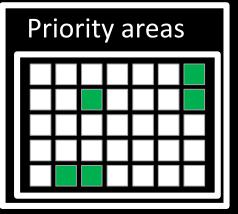


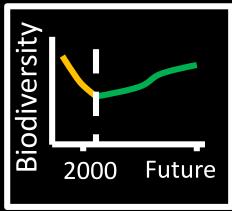


## How do we bend the curve?



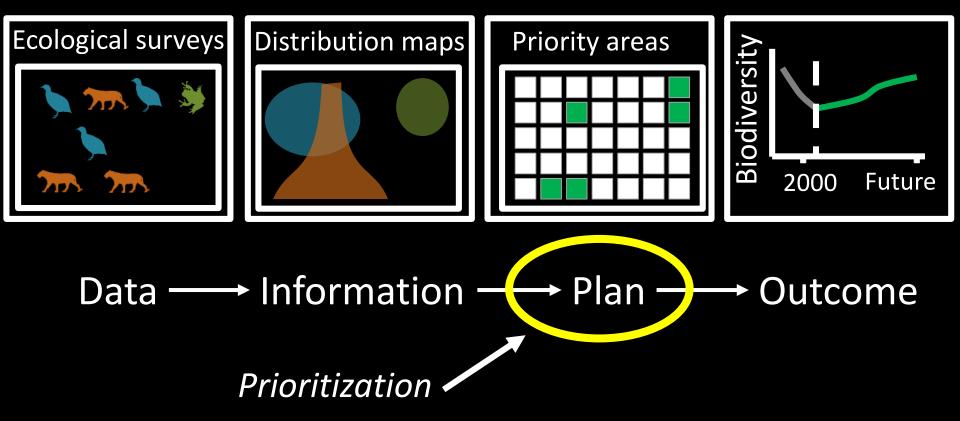






Data → Information → Plan → Outcome

## How do we bend the curve?



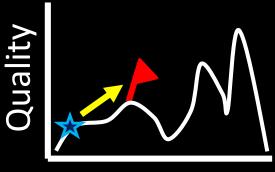
# Framing conservation as a decision science problem

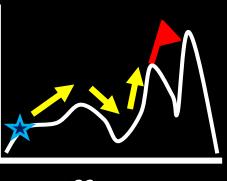
- Goal: what is our vision for the future?
- Objective: what quantity are we maximizing/minimizing to help achieve the goal?
- Constraints: what things must our solution do to help achieve the goal?
- <u>Decisions</u>: what actions could we do to maximize/minimize the objective?

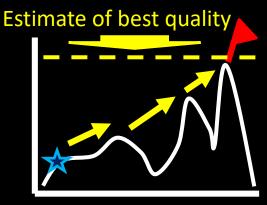
Heuristic algorithm

Meta-heuristic algorithms

Exact algorithms







Different solutions

Different solutions

Different solutions







# Exact algorithm solvers

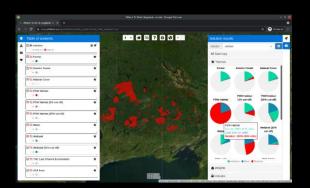
- Open source and commercial solvers available (e.g., Gurobi, IBM CPLEX, CBC, HiGHS, SYMPHONY)
- Automatically select algorithms for different problems (e.g., presolve, simplex, barrier, branch-and-bound)
- Broadly speaking have similar functionality, but have different implementations of the underlying algorithms, and have different performance for different kinds of problems

## Exact algorithm solvers

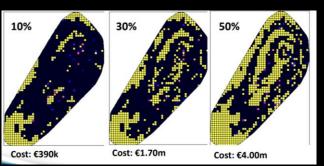
- Solve multiple problem types:
  - linear programming (LP) = continuous decision variables

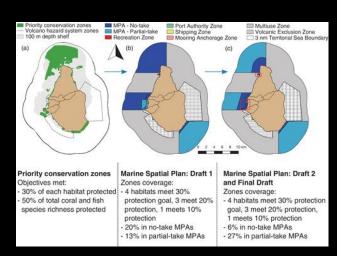
- integer programming (IP/ILP) = binary/integer decision variables
- mixed integer linear programming (MILP) = continuous + binary/integer decision variables

# Conservation examples



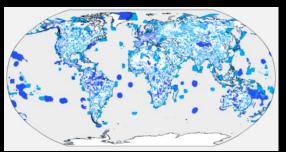
Nature Conservancy of Canada for land acquisition





Waitt Institute to help Government of Montserrat

Scottish Government for marine spatial planning in Rockall Bank



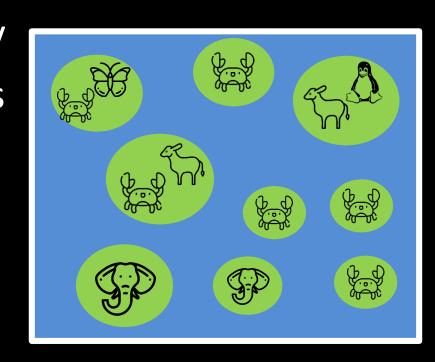
McKinsey Consulting

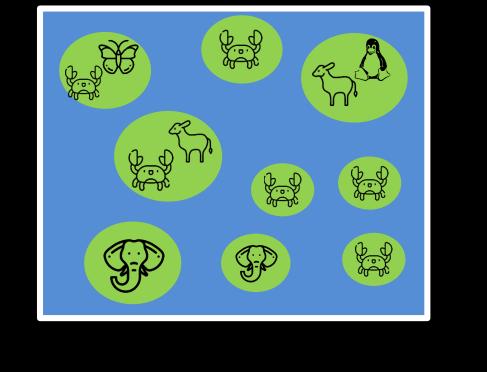


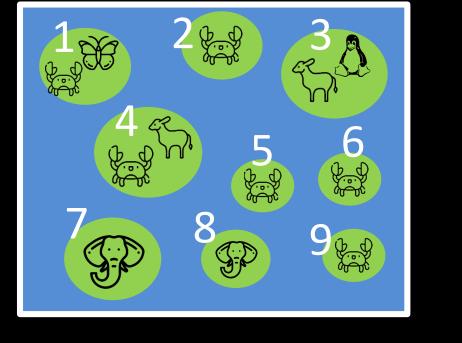
USGS to prioritize recovery areas in Hawaii

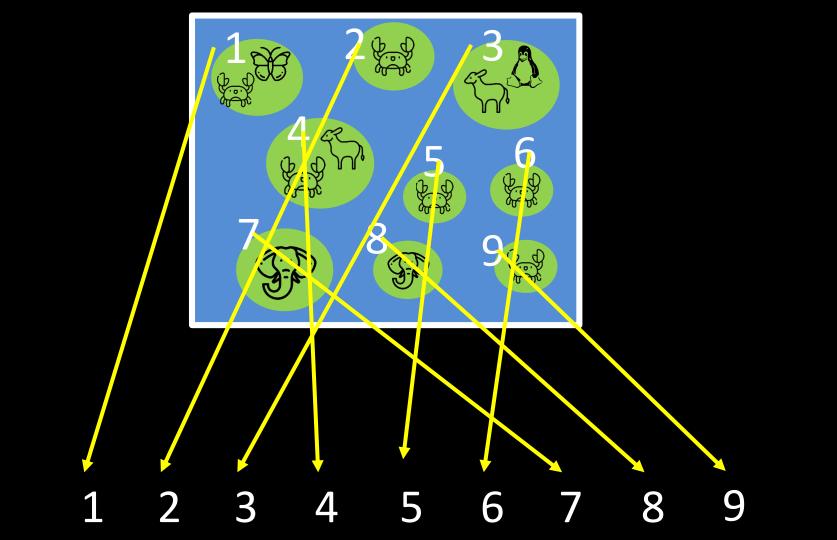
## Reserve selection as optimization

- Goal: conserve biodiversity
- Objective: min. # of islands
- Constraints: sufficient habitat for each species
- <u>Decisions</u>: create a reserve on an island or not?





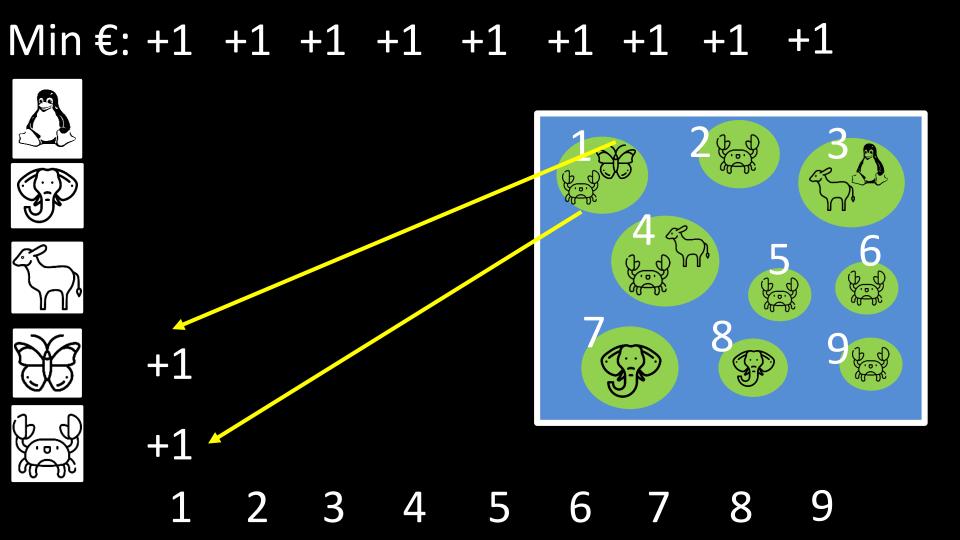


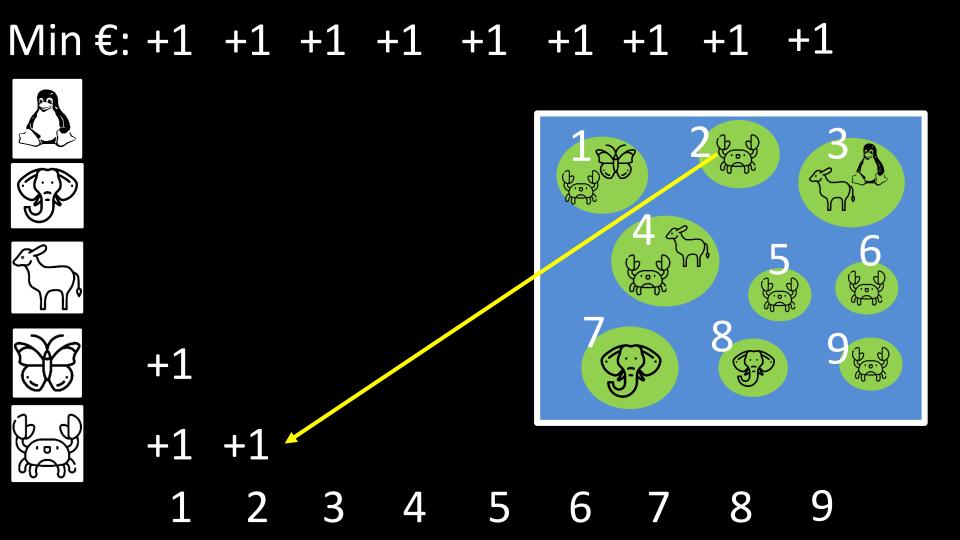


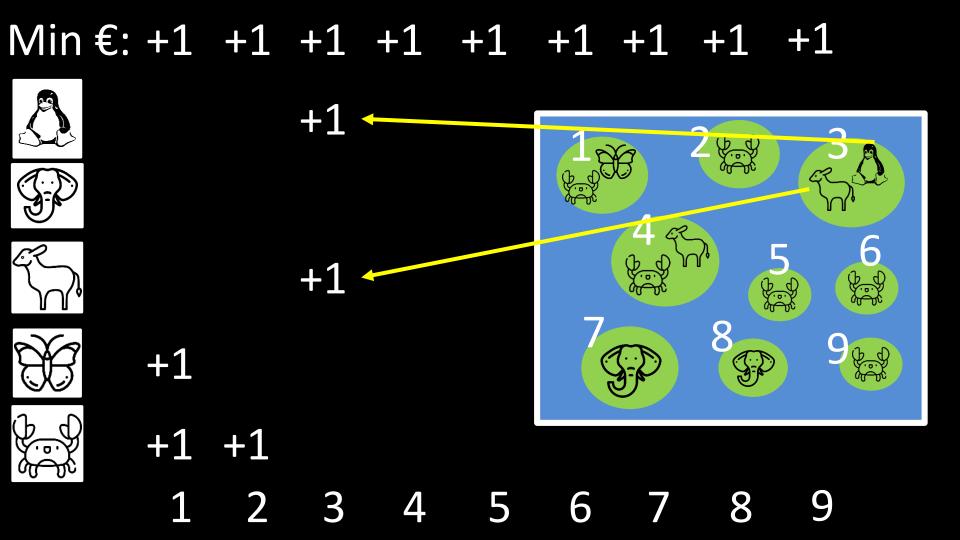
1 2 3 4 5 6 7 8 9

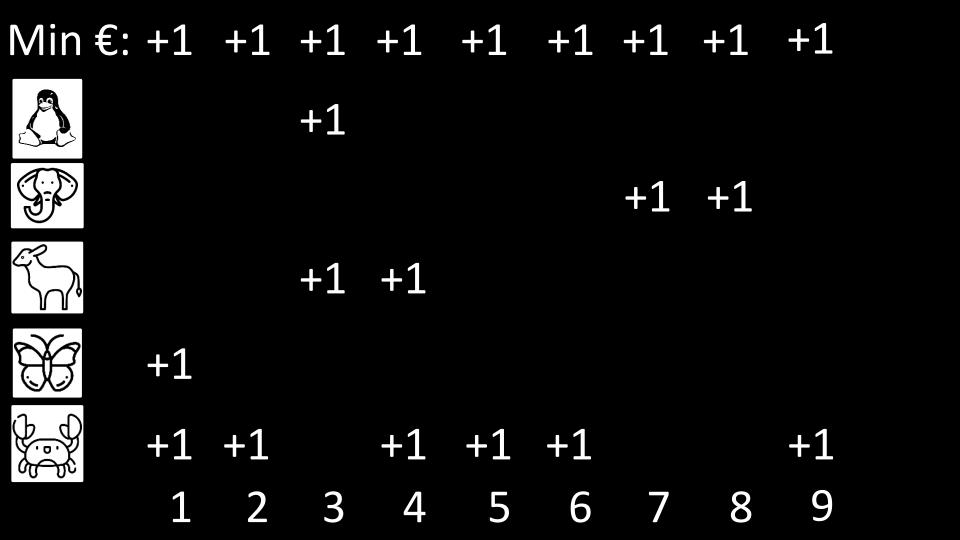






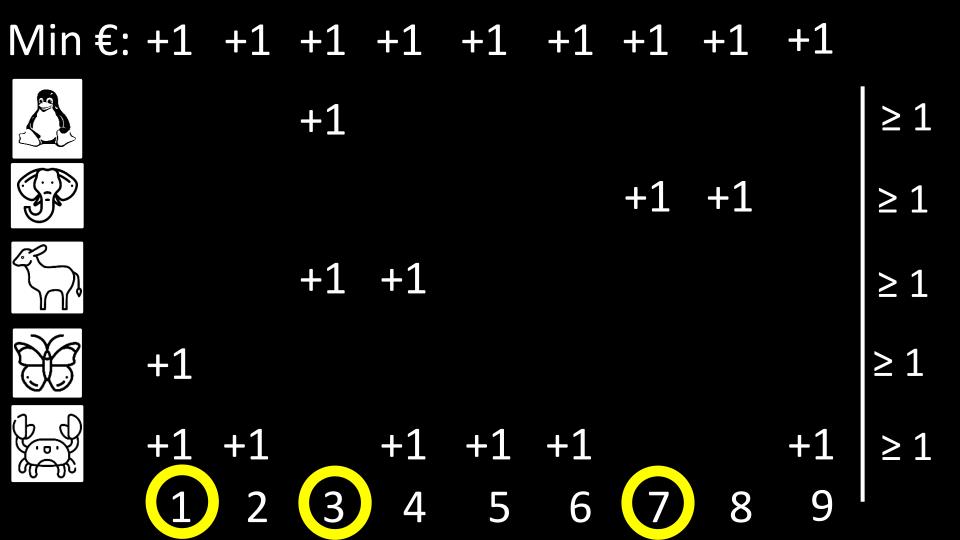


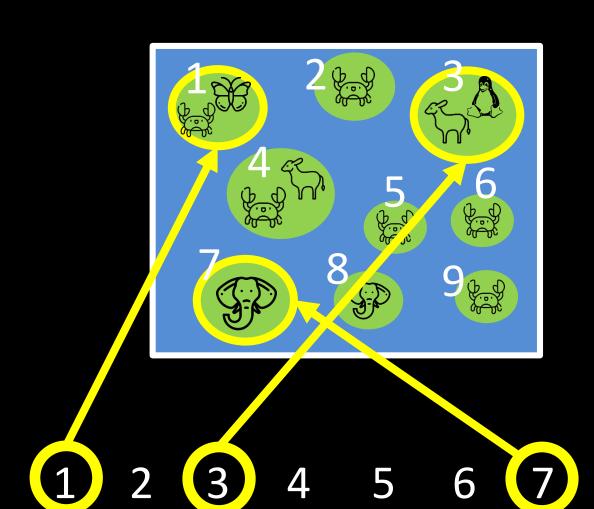




Min €:	+1	+1	+1	+1	+1	+1	+1	+1	+1	
			+1							≥ 1
(J-1)							+1	+1		≥ 1
			+1	+1						≥ 1
A.	+1									≥ 1
29. 29. 20.	+1	+1		+1	+1	+1			+1	≥ 1
	1	2	3	4	5	6	7	8	9	







# **Exact algorithm solvers**





coin-or/ SYMPHONY





## coin-or/Cbc



lp solve

COIN-OR Branch-and-Cut solver

## Cost and licensing

Open source

Commercial GUROBI OPTIMIZATION CPLEX



## General performance

Modern benchmarks (April 2023)

164

204

2.01

CBC vs Gurobi vs HiGHS

81.5

227

unscal

scaled

solved

1328

16.3

107

```
Unscaled and scaled shifted geometric means of run times

All non-successes are counted as max-time.
The third line lists the number of problems (240 total) solved.

CBC Gurobi COPT SCIP SCIPC HiGHS
```

888

137

10.9

727

152

8.92

715

158

8.77

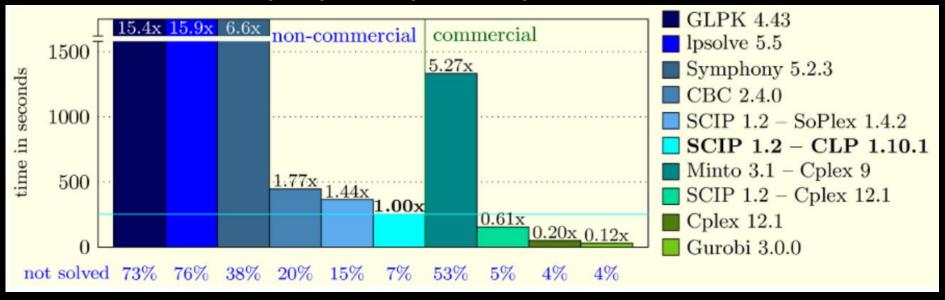
# General performance

- Historical benchmarks (Oct 2018)
- See how CPLEX and Ip\_solve compare

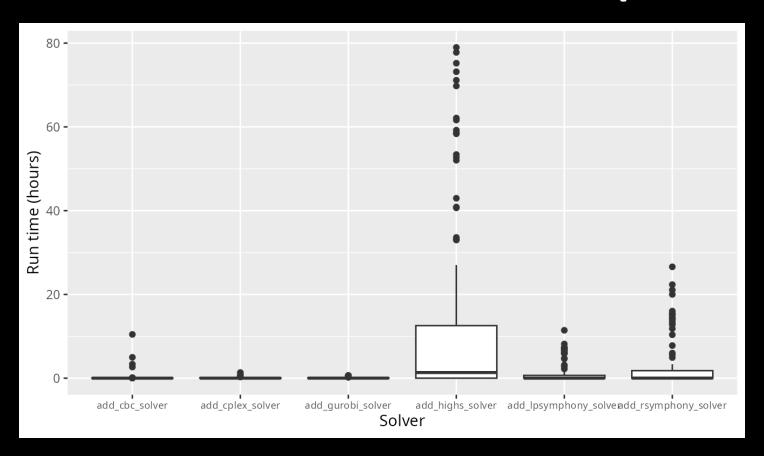
1 thr	CBC	CPLEX	GUROBI	SCIPC	SCIPS	XPRESS	MATLB	SAS	MIPCL	GLPK	LP_SOL
unscal	1639	72.2	41.6	239	330	83.1	3002	121	453	6925	5616
scaled	39	1.74	1	5.75	7.94	2.00	72.2	2.90	10.9	167	135
solved	53	87	87	83	76	86	32	84	76	2	7

## General performance

- Historical benchmarks (2010)
- See how Symphony compares



#### Performance for a conservation problem



#### Running the software programmatically

- Gurobi (gurobi R package)
- IBM CPLEX (cplexAPI and Rcplex R packages
- Symphony (Ipsymphony and Rsymphony R packages)
- CBC (rcbc R package)
- lp\_solve (lpsolveAPI R package)
- HiGHS (highs R package)

## Recommendations

- 1. Gurobi is the best solver, and a special academic license is freely available
- 2. CBC and HiGHS are the best open source solvers
- 3. All three solvers have fairly similar R package interface, so running the same analyses with different solvers is relatively straight forward





coin-or/Cbc



COIN-OR Branch-and-Cut solver



Project data





Recovery projects





#### Cost data



\$



\$\$



\$\$\$



\$0









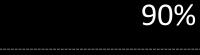










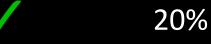




projects

Recovery



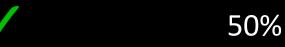
















100%

## Cost data











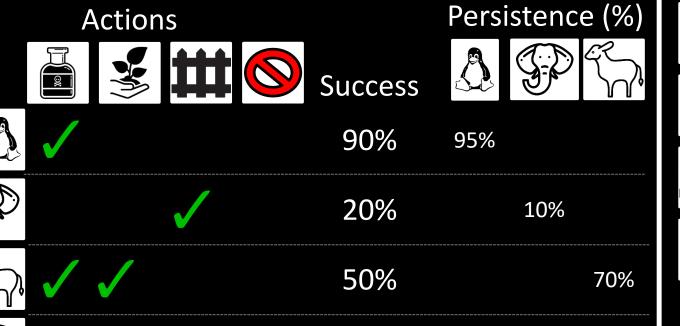




## Project data

projects

Recovery



100%

40%

9%

65%

#### Cost data



\$



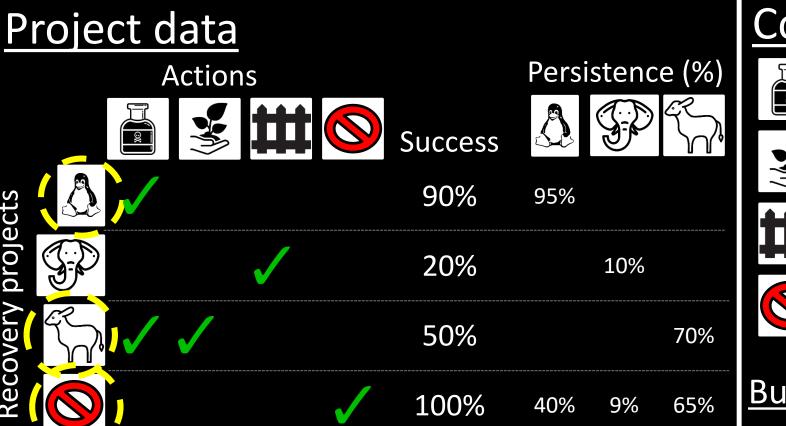
\$\$



\$\$5



\$0



## Cost data









Budget \$\$\$