rapr: Representative and Adequate Prioritisations in R

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Abstract

A central aim in conservation is to maximise the long-term persistence of biodiversity. To fulfil this aim, reserve networks are used to safeguard biodiversity patterns (eg. species, populations) and processes (eg. evolutionary processes that underpin genetic variation). Reserve selection is often formulated as an optimisation problem to identify cost-effective prioritisations. However, most existing decision support tools are based on formulations that are well suited for preserving biodiversity patterns, but not biodiversity processes. To fill this gap in the conservation planning toolbox, we developed the `rapr` R package. This R package provides functions to solve reserve selection problems using two novel formulations. Here, we explore the functionality of this R package using simulated species and a conservation planning exercise in Queensland, Australia as a case-study. We demonstrate how explicitly considering biodiversity processes can alter a prioritisation. In most cases, we found that only a few additional plannning units are required to sufficiently preserve of biodiversity processes.

Contents

Introduction

The overarching aim of conservation is to maximise the long-term persistence of biodiversity (McNeely 1994; Margules and Pressey 2000). To achieve this, conservation actions must preserve biodiversity patterns (eg. species, populations) and the processes that sustain them. One of the major tangible achievements of modern conservation has been the act of setting aside areas for preservation (Sanderson *et al.* 2015). Reserve networks buffer species from threatening processes [Margules and Pressey (2000); eg. urbanisation] and set the stage for direct management interventions (eg. captive breeding and reintroduction programs; Kleiman 1989). However, the resources available for conservation action are limited, and so reserve networks must be sited in places that satisfy conservation objectives for minimum cost (Margules and Pressey 2000). To achieve this, reserve selection is often formulated as an optimisation problem and then solved to identify cost-effective candidate reserve systems (prioritisations; Margules and Pressey 2000).

To fulfil the overarching aims of conservation, reserve networks must preserve both ecological and evolutionary processes (Margules and Pressey 2000; Crandall *et al.* 2000). Ecological processes, such as predator-prey interactions, pollination, and decomposition, are required for biodiversity to persist over short time-scales. Typically, they operate over small geographic domains–with exceptions such as migration and refugial habitats–and can be preserved using suitably large planning units (Ciarleglio *et al.* 2009) that each contain a discrete unit of habitat (Klein *et al.* 2009). On the other hand, evolutionary processes are required for biodiversity to persist over long time-scales, and they typically operate over large geographic domains. Adaptive evolutionary processes can be preserved by securing populations with different adaptations and/or along selection pressure gradients (eg. environmental gradients; Moritz 2002; Crandall *et al.* 2000; Rouget *et al.* 2003; Cowling *et al.* 2003). Neutral evolutionary processes can be preserved by securing populations with different evolutionary histories and/or with limited gene flow (Moritz 2002; Carvalho *et al.* 2011; Ponce-Reyes *et al.* 2014). Due to advances in technology in recent decades, a wealth of data on biodiversity processes has become freely available to conservation planners. Yet this data is only rarely used to guide conservation planning exercises (Hendry *et al.* 2010). Existing decision support tools focus primarily on preserving biodiversity patterns or occasionally processes–but not both.

Many tools have been developed to assist conservation planners in preserving biodiversity patterns (eg. `C-Plan`, Pressey *et al.* 2009;`ConsNet`, Ciarleglio *et al.* 2009;`Marxan`, Ball *et al.* 2009;`Zonation`, Moilanen 2007). They use targets (eg. `Marxan`) or weights (eg. `Zonation`) to identify prioritisations that contain an adequate amount of individuals or habitat for a set of species (features). To accommodate information on biodiversity processes, conservation planners can split features into sub-features as a pre-processing step (eg. Carvalho *et al.* 2011). However, this approach is limited because data on biodiversity processes is often continuous and hyper-dimensional (eg. bioclimatic data; Hijmans *et al.* 2005), and therefore they often cannot be reduced to a few categories without significant information loss (Faith and Walker 1996). Additionally, these problem formulations cannot accommodate variation within sub-features, and nor can they account for relationships between sub-features (Faith and Walker 1996).

Very few tools have been developed with a specific focus on biodiversity processes. The `DIVERSITY` decision support tool (Faith 2003) uses continuous data to site reserves in places that secure a representative sample of variation across a study area (eg. environmental variation). Originally, this tool was developed to identify prioritizations that secure a comprehensive set of habitats without using any species-level data. As a consequence, the effectiveness of this tool has been highly contested [@346; @347; @344]. Additionally, this tool tended to deliver excessively fragmented prioritisations (cf. `Marxan`). However, unlike tools that primarily focus on biodiversity patterns, this tool can only accommodate data on the distribution of a single feature.

Today, one of the key issues preventing decision makers from explicitly considering both biodiversity patterns and processes in the reserve selection process is the lack of a decision support tool that can accommodate data on both in a multi-species context. To fill this void, we present the `rapr` `R` package. This `R` package provides decision makers with the tools to identify prioritisations that preserve biodiversity patterns and processes. These prioritisations are generated by solving novel formulations of the reserve selection problem that use adequacy- and representation-based targets. We also provide a tutorial showcasing the functionality of this `R` package using simulated species and a case-study conservation planning scenario in Queensland, Australia.

Problem formulations

The `rapr` `R` package uses two novel formulations of the reserve selection problem to identify cost-effective prioritisations. These formulations share many constraints and variables. For brevity, the variables used by both formulations will be defined. Biodiversity features are defined as the entity(s) that the prioritisation is required to preserve (eg. species, populations). Spatial attributes are defined as the intra-feature variation that the prioritisation is required to sample. These attributes are related to the biodiversity processes that the prioritisation needs to represent (eg. environmental variation).

Each attribute is conceptualised as a space and planning units are thought to occupy points inside each space. This space is termed an attribute space. For example, a decision maker may require a prioritisation that preserves populations along climatic gradients. To achieve this, the decision maker might use an "climatic" attribute space with dimensions relating to mean annual temperature (°C) and precipitation (mm). Any given combination of temperature and precipitation may be conceived as a point in this environmental space. By associating planning units with climatic data, they can be mapped from geographic space to this environmental attribute space.

Demand points are points that exist in an attribute space. They are designated by the decision maker to indicate regions of the attribute space that should be preserved in the prioritisation. The amount of variation in the attribute space that a prioritisation secures is a function of the distance between each demand point and each planning unit in the attribute space. The shorter the distances between the demand points and the planning units; the better the prioritisation is at representing the variation in the spatial attribute. To convert these amounts to a proportion–a meaningful unit for a decision maker–the distances between the selected planing units and the demand points are scaled by the distances between the demand points to the centroid of the demand points. In any attribute space there may exist points that are impossible (eg. mean annual rainfall -5 mm), do not occur in the study area (eg. mean annual temperature 30°C in Antarctica), or are undesirable (eg. conditions known to be outside the physiological tolerance of a species). By placing demand points in desirable regions of an attribute space, the decision maker can ensure that prioritisations secure desirable values of a spatial attribute.

To illustrate these concepts, we will briefly describe a conservation planning scenario example involving attribute spaces and demand points. A decision maker may wish to develop a prioritisation for a single species. This species has four populations in the study area. These populations are in the process of divergent evolution, with different populations inhabiting different environmental conditions and accruing different adaptations. However, the decision maker can only afford to preserve three of the populations. The decision maker needs to select a set of populations that will secure the most of intra-specific variation. To describe this intra-specific variation–given that no genetic data was available–the decision maker obtained data on the environmental conditions (rainfall (ml) and temperature (°C)) where each population was found. The decision maker then used this environmental data to construct a two-dimensional environmental attribute space. Next, the decision maker generated demand points as equi-distant points between the range of values where the populations were found ($\pm$ 20% to avoid edge effects; Faith and Walker 1996). By comparing the distribution of the demand points to the distribution of the populations in the attribute space, the decision maker can identify a suitable prioritisation (Figure 1). We can see that if the decision maker preserves both populations A and C, they will effectively "double-up" on the same environmental characteristics, and in turn their waste resources. Instead, a more representative sample of the intra-specific variation could be preserved by securing populations A, B, and D. This example demonstrates how the inclusion of biodiversity processes can guide the reserve selection process.
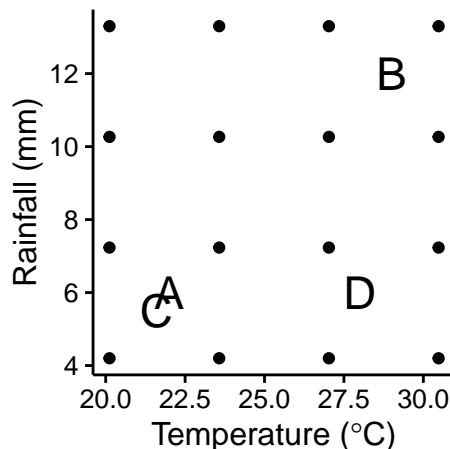

Figure 1 Example of an attribute space. This environmental attribute space has dimensions relating to annual temperature (°C)and rainfall (ml) values. Letters denote the environmental conditions associated with the geographic locations where four hypothetical populations are found. Points represent demand points. In this space, populations closer to each other are considered more similar to each other.

The problem formulations used to guide reserve selection in the `rapr R` package are based on a combination of the `Marxan` reserve selection problem and uncapacitated facility location problems (all mathematical terms defined hereafter are described in Table S1 for convenience). For convenience, the cardinality of sets will be denoted using the same symbol used to denote the variable. Define F to be the set of features (indexed by f). Let J be a set of planning units (indexed by j). Also, let A_j denote the area, and C_j denote the cost of preserving planning unit $j \in J$. To assess the extent to which each feature is secured in a given prioritisation, let q_{fj} denote the probability of feature f occupying planning unit j. The level of fragmentation associated with a prioritisation is parametrised as the net exposed boundary length. Let the shared boundary length between each planning unit $j \in J$ and $k \in J$ be b_{jk}. In any real-world problem, some planning units will have

edges that are not associated with any neighbouring planning units (eg. edges along coastlines), these cases will be denoted using b_{jj} for $j \in J$.

Let S denote a set of attribute spaces (indexed by s). Each $j \in J$ is associated with spatially explicit data that represent coordinates for each attribute space $s \in S$. Let I_{fsi} denote a set of demand points (indexed by i) for each feature $f \in F$ and each attribute space $s \in S$. Let λ_{fsi} denote the weighting for each demand point $i \in I$, $f \in F$ and $s \in S$. Let d_{fsij} denote the distance between each demand point $i \in I$ and each planning unit $j \in J$ for each feature $f \in F$ and attribute space $s \in S$. Demand points with greater weight λ_{fsi} are more important, and the optimal solution will be likely to select planning units close to highly weighted demand points. As a consequence, the decision maker will need to choose an appropriate weighting for each demand point. The decision maker will also need to choose an appropriate distance metric for each attribute space. For example, Euclidean, Mahalanobis (Mahalanobis 1936), Bray-Curtis, or other distance metrics may be appropriate given the nature of the attribute space (Faith *et al.* 1987).

Targets are used to ensure that prioritisations adequately preserve each species. Amount-based targets are used to ensure that the total amount of habitat preserved is sufficient. Let $\hat{T}_f$ denote the expected amount of area that needs to be preserved for each feature $f \in F$. Space-based targets are ensure that a sufficient proportion of the intra-specific variation is secured. Let $\bar{T}_{fs}$ denote the space-based targets for feature $f \in F$ and attribute space $a \in A$. For convenience, these both types of targets are expressed as proportions in the R package.

The R package provides two formulations for reserve selection. They are based on the unreliable (Fernández and Landete 2015) and reliable uncapacitated facility location (Cui *et al.* 2010) problems. The key difference between them is that the reliable formulation explicitly considers the probability that the planning units are occupied when calculating the proportion of variation that a given solution secures, whereas the unreliable formulation does not.

Unreliable formulation

In the unreliable formulation, the control variables are the BLM, $\hat{t}_s$, and $\bar{t}_{sa}$ variables, and the decision variables are the X and Y_{fsi} variables.

$$X_j = \begin{cases} 1, & \text{if planning unit } j \text{ is selected for conservation action} \\ 0, & \text{otherwise} \end{cases} \tag{1a}$$

$$\hat{T}_s = \text{amount target for feature } f \tag{1b}$$

$$\bar{T}_{sa} = \text{representation target for feature } f \text{ in attribute space } a \tag{1c}$$

$$BLM = \text{boundary length modifier: penalises overly fragmented solutions} \tag{1d}$$

$$Y_{fsi} = \begin{cases} 1, & \text{if planning unit } i \text{ is assigned to planning unit } j \text{ for feature } f \text{ in space } s \\ 0, & \text{otherwise} \end{cases} \tag{1e}$$

The unreliable formulation (URAP) is a defined as a multi-objective optimisation problem.

$$\text{(URAP)} \quad \text{Min} \sum_{j=0}^{J-1} C_j + BLM \times \sum_{j=0}^{J-1} \sum_{k=j}^{J-1} X_j \left(1 - X_k\right) b_{jk} + BLM \times \sum_{j=0}^{J-1} x_j b_{jj} \tag{2a}$$

$$\text{s.t.} \sum_{j=0}^{J-1} A_j q_{jf} \geq \bar{T}_f \qquad\qquad \forall 0 \leq f \leq F - 1 \tag{2b}$$

$$1 - \frac{\sum_{i=0}^{I-1} \sum_{j=0}^{J-1} \left(\lambda_{fsi} d_{fsij} Y_{fsij}\right)^2}{\sum_{i=0}^{I-1} \sum_{l=0}^{I-1} \left(\lambda_{fsi} D_{fsil}\right)^2} \geq \hat{T}_{fs} \qquad\qquad \forall 0 \leq f \leq F - 1, \tag{2c}$$
$$0 \leq s \leq S - 1$$

$$\sum_{j=0}^{J-1} Y_{fsij} = 1 \qquad\qquad \forall 0 \leq f \leq F - 1, \tag{2d}$$
$$0 \leq s \leq S - 1,$$
$$0 \leq i \leq I - 1$$

$$Y_{fsij} \leq X_j \qquad\qquad \forall 0 \leq f \leq F - 1, \tag{2e}$$
$$0 \leq s \leq S - 1,$$
$$0 \leq i \leq I - 1,$$
$$0 \leq j \leq J - 1$$

$$X_j, Y_{fsij} \in 0, 1 \qquad\qquad \forall 0 \leq f \leq F - 1, \tag{2f}$$
$$0 \leq s \leq S - 1,$$
$$0 \leq i \leq I - 1$$

The objective function (2a) determines the utility of a given prioritisation: a combination of the total cost of a prioritisation and how fragmented it is. Constraints (2b–2c) ensure that all the amount-based and space-based targets are met. Constraints (2d) ensure that only one planning unit is assigned to each demand point. Constraints (2e) ensure that demand points are only assigned to selected planning units. Constraints (2f) ensure that the X and Y variables are binary.

Reliable formulation

The reliable formulation explicitly considers the probability that the planning units are inhabited. As a consequence, it may deliver prioritisations that will sufficiently represent an attribute space even if the features do not inhabit several of the planning units when the prioritisation is implemented. This behaviour is achieved by siting back-up planning units near selected planning units with low occupancy probabilities in the attribute space(s). To ensure that prioritisations are robust against multiple planning units being uninhabited, the problem assigns planning units at multiple backup levels.

Backup levels levels are defined as r-levels (similar to failure levels in Snyder and Daskin 2005). The first backup r-level is used to calculate the level of representation when all of the selected planning units are occupied by all $f \in F$. For this scenario, the closest selected planning unit to each demand point i for attribute space s is assigned at r-level= 0. This scenario essentially represents Y_{fsij} in the unreliable formulation. The second backup r-level is used to assess the level of representation when the closest planning unit to each demand point i is unoccupied. For this scenario, the second closest planning units are assigned at r-level= 1. The third backup r-level is used to assess representation when the first two closest planning units are unoccupied. The third closest planning units are assigned at r-level= 2. Continuing on, in this manner, the selected planning units in a prioritisation are assigned to each demand point $i \in I$, attribute space $s \in S$, and each feature $f \in F$ at an r-level.

A final backup r-level when $r = R$ is used to assess the level of representation when the features $f \in F$ do not occupy any selected planning units in a prioritisation. Each demand point $i \in I$ for each $s \in S$ and $f \in F$ is assigned to an "imaginary" planning unit $j = J$ at $r = R$. The distance variables associated with this imaginary planning unit d_{fsiJ} denote the loss of biological value associated with failing to secure a representative sample of feature f in attribute space s. However, the d variables are in distance units which are meaningless units in this context. Thus these variables are calculated using a failure multiplier (M) and the maximum distance between the planning units and the demand points for $f \in F$, $s \in S$ (3).

$$d_{fsiJ} = M \times \max_{0 \leq i \leq I-1, 0 \leq j \leq J-1} d_{fsij} \qquad \forall 0 \leq f \leq F - 1, \qquad (3)$$
$$0 \leq s \leq S - 1$$

Moderately-sized conservation planning problems often include several thousand planning units. It is currently not be feasible to solve this problem when considering all possible failure scenarios. As a consequence, the R variable can be any $1 \leq R \leq J - 1$. For instance, when $R = 3$ only 2 backup levels are considered in addition to the final backup level. Cui et al. (2010) found that $R = 5$ yields similar solutions to $R = J$ when $J >> 5$. However, depending on the number of features, demand points, attribute spaces, and planning units, decision makers will likely be limited to $R = 1$ to obtain prioritisations in a feasible amount of time.

In the reliable formulation, the control variables are the X, BLM, $\hat{t}_s$, $\bar{t}_{sa}$, R, and M variables and the decision variables are the P_{fsijr} variables.

$$ (1a–1d) $$
$$ R = \text{number of failure levels} \qquad (4a) $$
$$ M = \text{failure multiplier} \qquad (4b) $$
$$ P_{fsijr} = \text{probability that demand point } i \text{ is assigned to planning unit } j \text{ at back-up level } r \text{ for feature } f \text{ and space} \qquad (4c) $$

The reliable formulation (RRAP) is a multi-objective optimisation problem.

$$(\text{RRAP}) \qquad \text{Min (2a)}$$

$$\text{s.t. (2b)}$$

$$\sum_{i=0}^{I-1} \sum_{j=0}^{J} \sum_{r=0}^{R} \lambda_{fsijr} P_{fsijr} Y_{fsijr} \leq \hat{T}_{fs} \qquad \forall 0 \leq f \leq F-1, \qquad (5a)$$

$$0 \leq s \leq S-1$$

$$\sum_{j=0}^{J-1} Y_{fsijr} = 1 \qquad \forall 0 \leq f \leq F-1, \qquad (5b)$$

$$0 \leq s \leq S-1,$$
$$0 \leq i \leq I-1,$$
$$0 \leq r \leq R$$

$$\sum_{r=0}^{R} Y_{fsijr} = 1 \qquad \forall 0 \leq f \leq F-1, \qquad (5c)$$

$$0 \leq s \leq S-1,$$
$$0 \leq i \leq I-1,$$
$$0 \leq j \leq J$$

$$\sum_{r=0}^{R-1} Y_{fsijr} \leq X_j \qquad \forall 0 \leq f \leq F-1, \qquad (5d)$$

$$0 \leq s \leq S-1,$$
$$0 \leq i \leq I-1,$$
$$0 \leq j \leq J-1$$

$$Y_{fsiJR} = 1 \qquad \forall 0 \leq f \leq F-1, \qquad (5e)$$
$$0 \leq s \leq S-1,$$
$$0 \leq i \leq I-1$$

$$P_{fsij0} = q_{fj} \qquad \forall 0 \leq f \leq F-1, \qquad (5f)$$
$$0 \leq s \leq S-1,$$
$$0 \leq i \leq I-1,$$
$$0 \leq j \leq J$$

$$P_{fsijr} = (1-) \sum_{k=0}^{J-1} \frac{1-q_k}{q_k} P_{f,s,i,k,r-1} Y_{f,s,i,k,r-1} \qquad \forall 0 \leq f \leq F-1, \qquad (5g)$$

$$0 \leq s \leq S-1,$$
$$0 \leq i \leq I-1,$$
$$0 \leq j \leq J,$$
$$1 \leq r \leq R$$

$$X_j, Y_{fsijr} \in 0,1 \qquad \forall 0 \leq f \leq F-1, \qquad (5h)$$
$$0 \leq s \leq S-1,$$
$$0 \leq i \leq I-1,$$
$$0 \leq j \leq J,$$
$$0 \leq r \leq R$$

The objective function for the reliable formulation is the same as for the unreliable formation (2a). Similar to the unreliable formulation, constraints (2b) and (5a) ensure that the amount-based and space-based targets are met. Constraint (5b–5c) ensure that each planning unit is only assigned to one backup r-level for $i \in I$. Constraints (5d) ensure that only selected planning units are assigned to demand points $i \in I$. Constraints (5e) ensure that the imaginary planning unit is always assigned to the highest backup r-level. Constraints (5f–5g) determine the probability that planning unit j will be used to sample demand point $i \in I$ for $s \in S$ and $f \in F$ (Cui *et al.* 2010). Constraints (5h) ensure that the X and Y variables are binary.

Optimisation

The unreliable and reliable formulations are non-linear. However, the non-linear components can be linearised using existing techniques. First, the expression $X_j X_k$ in (2a) can be linearised using methods described by Beyer et al. (2015). Second, the expression $P_{fsijr} Y_{jsijr}$ in (5a) can be linearised using techniques described by Sherali and Alameddine (1992) as implemented in Cui et al. (2010). Linearised versions of the problems can be solved using commercial exact algorithm solvers.

The `rapr` R package provides functions to express conservation planning data as an optimisation problems using linearised versions of the unreliable and reliable formulations. These optimisation problems can then be solved to generate prioritisations using the commercial `Gurobi` software suite (http://www.gurobi.com). Note that academics can obtain a license at no cost from the Gurobi website. After installing the `Gurobi` software suite, users will need to install the `Gurobi R` package. This `R` package can be installed on Windows, Mac OSX, and Linux operating systems.

Package overview

To load the `rapr` R package and learn more about the package, type the following code into R.

```
# load rapr R package
library(rapr)

# show package overview
?rapr
```

The `rapr` R package uses a range of S4 classes to store conservation planning data, parameters, and prioritisations (Table 1).

Table 1: Main classes in the `rapr` R package

Class Name	Description	Slots
ManualOpts	place-holder class for manually specified solutions	NumberSolutions
GurobiOpts	parameters for solving optimisation problems using Gurobi	Threads, MIPGap, Presolve, TimeLimit, NumberSolutions
RapUnreliableOpts	parameters for the unreliable problem formulation	BLM

Class Name	Description	Slots
RapReliableOpts	parameters for the reliable problem formulation	failure.multiplier, max.r.level
SimplePoints	stores coordinates in an n-dimensional space	coords
DemandPoints	demand points coordinates and weights for a speciesin an attribute space	points, weights
AttributeSpace	planning unit coordinates and demand points data for an attribute space	pu, demand.points, distance.metric
RapData	planning unit, species, and attribute space data	pu, species, targets, pu.species.probabilities, attribute.spaces, boundary, polygons, .cache
RapUnsolved	data and parameters needed to generate prioritisationsusing RAP	opts, data
RapResults	prioritisations and summary statistics	summary, selections, amount.held, space.held, logging.file, .cache
RapSolved	data, parameters, and prioritisations using them	opts, data, results

Package tutorial

This tutorial is designed to provide users with an understanding of how to use the `rapr R` package to generate and compare solutions. This tutorial uses several additional packages, so first we will run the following code to load them.

```r
# load packages for tutorial
library(plyr)
library(dplyr)
library(ggplot2)
library(RandomFields)

# set seed for reproducibility
set.seed(500)
```

Simple simulated species

Data

To investigate the behaviour of the problem, we will generate prioritisations for three simulated species. We will use the unreliable formulation of the problem to understand the basics, and later move onto the reliable formulation. The first species (termed 'uniform') will represent a

hyper-generalist. This species will inhabit all areas with equal probability. The second species (termed 'normal') will represent a species with a single range core. The third species (termed 'bimodal') will represent a species with two distinct ecotypes, each with their own range core. To reduce computational time for this example, we will use a 10×10 grid of square planning units.

```r
# make planning units
sim_pus <- sim.pus(100L)

# simulate species distributions
sim_spp <- lapply(
    c('uniform', 'normal', 'bimodal'),
    sim.species,
  n=1,
  x=sim_pus,
  res=1
)
```

Let's see what these species' distributions look like.

```r
# plot species
plot(
    stack(sim_spp),
    main=c('Uniform species','Normal species','Bimodal species'),
    addfun=function(){lines(sim_pus)},
    nc=3
)
```
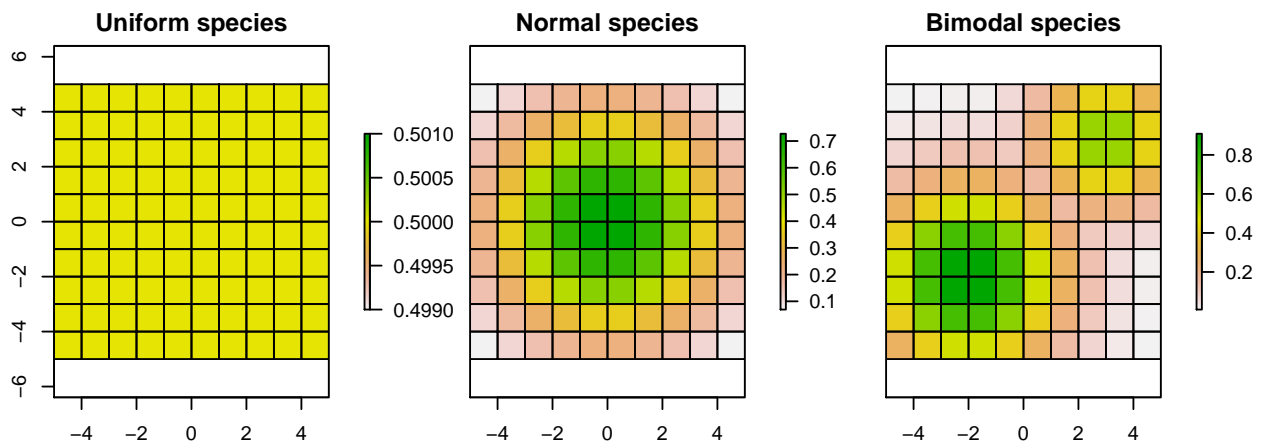

Figure 2 Distribution of three simulated species. Each square represents a planning unit. The colour of each square denotes the probability that individuals from each species occupy it.

Next, we will generate a set of demand points. To understand the effects of probabilities and weights on the demand points, we will generate the demand points in geographic space. These demand points will be the centroids of the planning units. Additionally, we will use the same set of demand points for each species and only vary the weights of the demand points between species. **Note**

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that we are only using the same distribution of demand points for different species for teaching purposes. It is strongly recommended to use different demand points for different species in real-world conservation planning exercises. See the case-study section of this tutorial for examples on how to generate suitable demand points.

```r
# generate coordinates for pus/demand points
pu_coords <- rgeos::gCentroid(sim_pus, byid=TRUE)

# calculate weights
sim_dps <- lapply(
    sim_spp,
    function(x) {
        return(extract(x, pu_coords))
    }
)

# create demand point objects
sim_dps <- lapply(
    sim_dps,
    function(x) {
        return(
            DemandPoints(
                SimplePoints(pu_coords@coords),
                c(x)
            )
        )
    }
)
```

Now, we will construct a `RapUnsolved` object to store our input data and parameters. This contains all the information to generate prioritisations.

```r
## create RapUnreliableOpts object
# this stores parameters for the unreliable formulation problem (eg. BLM)
sim_ro <- RapUnreliableOpts()

## create RapData object
# create data.frame with species info
species <- data.frame(
  name=c('uniform', 'normal', 'bimodal')
)

## create data.frame with species and space targets
# amount targets at 20% (denoted with target=0)
# space targets at 20% (denoted with target=1)
targets <- expand.grid(
  species=1:3,
  target=0:1,
```

```r
  proportion=0.2
)

# calculate probability of each species in each pu
pu_probabilities <- calcSpeciesAverageInPus(sim_pus, stack(sim_spp))

## create AttributeSpace object
# this stores the coordinates of the planning units in an attribute space
# and the coordinates and weights of demand points in the space
attr_space <- AttributeSpace(
  SimplePoints(pu_coords@coords),
  sim_dps
)

# generate boundary data information
boundary <- calcBoundaryData(sim_pus)

## create RapData object
# this stores all the input data for the prioritisation
sim_rd <- RapData(
  sim_pus@data,
  species,
  targets,
  pu_probabilities,
  list(attr_space),
  boundary,
  SpatialPolygons2PolySet(sim_pus)
)

## create RapUnsolved object
# this stores all the input data and parameters needed to generate prioritisations
sim_ru <- RapUnsolved(sim_ro, sim_rd)
```

Single-species prioritisations

Amount-based targets

To investigate the effects of space-based targets, we will generate a prioritisation for each species using only amount-based targets and compare them to prioritisations generated using amount- and space-based targets. To start off, we will generate a prioritisation for the uniform species using amount-based targets. To do this we will generate a new `sim_ru` object by subsetting out the data for the uniform species from the `sim_ru` object containing data for all the species. Then, we will update the targets in the new object. Finally, we will solve the object to generate a prioritisation that fulfills the targets for minimal cost.

```r
# create new object with just the uniform species
sim_ru_s1 <- spp.subset(sim_ru, 'uniform')
```

```
# update amount targets to 20% and space targets to 0%
sim_ru_s1 <- update(sim_ru_s1, amount.target=0.2, space.target=NA, solve=FALSE)
```

```
# solve problem to identify prioritisation
sim_rs_s1_amount <- solve(sim_ru_s1)
```

```
## Optimize a model with 1 rows, 100 columns and 100 nonzeros
## Coefficient statistics:
##   Matrix range     [5e-01, 5e-01]
##   Objective range  [1e+00, 1e+00]
##   Bounds range     [1e+00, 1e+00]
##   RHS range        [1e+01, 1e+01]
## Found heuristic solution: objective 20
## Presolve removed 1 rows and 100 columns
## Presolve time: 0.00s
## Presolve: All rows and columns removed
##
## Explored 0 nodes (0 simplex iterations) in 0.00 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.000000000000e+01, gap 0.0%
## species = 0; space = 0; tss = 412.5; spaceheld = 510; prop = -0.236364
```

```
## Warning in validityMethod(object): object@space.held contains values less
## than 0, some species are really poorly represented
```

```
## show summary
# note the format for this is similar to that used by Marxan
# see ?rapr::summary for details on this table
summary(sim_rs_s1_amount)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL    20   20             20                220
##   Connectivity_In Connectivity_Edge Connectivity_Out
## 1              42               168               10
##   Connectivity_In_Fraction
## 1                0.1909091
```

```
# show amount held
amount.held(sim_rs_s1_amount)
```

```
##   uniform
## 1     0.2
```

```
# show space held
space.held(sim_rs_s1_amount)
```

```
##   uniform (Space 1)
## 1       -0.2363636
```

Now that we have generated a prioritisation, we will see what it looks like. We can use the `spp.plot` method to see how the prioritisation overlaps with the uniform species' distribution. Note that since all planning units have equal probabilities for this species, all planning units have the same fill.

```
# plot the prioritisation and the uniform species' distribution
spp.plot(sim_rs_s1_amount, 1, main='Uniform species')
```
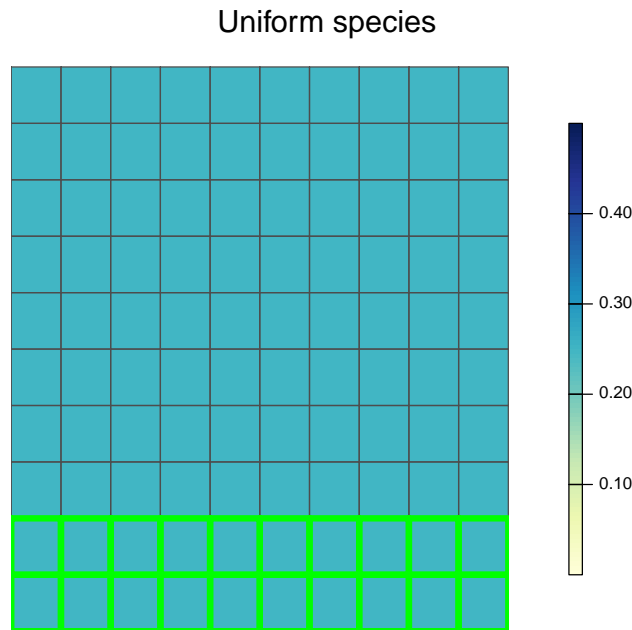

Figure 3 A prioritisation for the uniformly distributed species generated using amount-based targets (20%). Sqaures represent planning units. Planning units with a green border are selected for prioritisation, and their colour denotes the probability they are inhabited by the species.

The prioritisation for the uniform species appears to be just a random selection of planning units. This behavior is due to the fact that any prioritisation with 20 planning units is optimal. By relying on just amount targets, this solution may preserve a section of the species' range core, or just focus on the range margin, or some random part of its range—no emphasis is directed towards preserving different parts of the species' range. This behavior highlights a fundamental limitation of just using amount-based targets. In the absence of additional criteria, conventional reserve selection problems do not contain any additional information to identify the most effective prioritisation.

Now, we will generate a prioritisation for the normally distributed species using amount-targets. We will use a similar process to what we used for the uniformly distributed species, but for brevity, we will use code to generate solutions immediately after updating the object.

```r
# create new object with just the normal species
sim_ru_s2 <- spp.subset(sim_ru, 'normal')


# update amount targets to 20% and space targets to 0% and solve it
sim_rs_s2_amount <- update(sim_ru_s2, amount.target=0.2, space.target=NA, solve=TRUE)
```

```
## Optimize a model with 1 rows, 100 columns and 100 nonzeros
## Coefficient statistics:
##   Matrix range    [7e-02, 7e-01]
##   Objective range [1e+00, 1e+00]
##   Bounds range    [1e+00, 1e+00]
##   RHS range       [7e+00, 7e+00]
## Found heuristic solution: objective 27
## Presolve removed 0 rows and 86 columns
## Presolve time: 0.00s
## Presolved: 1 rows, 14 columns, 14 nonzeros
## Variable types: 0 continuous, 14 integer (0 binary)
## Presolved: 1 rows, 14 columns, 14 nonzeros
##
##
## Root relaxation: objective 9.864476e+00, 6 iterations, 0.00 seconds
##
##      Nodes    |    Current Node    |     Objective Bounds     |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0    9.86448    0     1   27.00000    9.86448  63.5%     -    0s
## H    0     0                         10.0000000   9.86448   1.36%     -    0s
##
## Explored 0 nodes (6 simplex iterations) in 0.02 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 1.000000000000e+01, best bound 1.000000000000e+01, gap 0.0%
## species = 0; space = 0; tss = 111.252; spaceheld = 38.7164; prop = 0.651993
```

```r
# show summary
summary(sim_rs_s2_amount)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL    10   10             10                220
##   Connectivity_In Connectivity_Edge Connectivity_Out
## 1              12               192               16
##   Connectivity_In_Fraction
## 1               0.05454545
```

```r
# show amount held
amount.held(sim_rs_s2_amount)
```

```
##      normal
## 1 0.2026153
```

```r
# show space held
space.held(sim_rs_s2_amount)
```

```
##   normal (Space 1)
## 1        0.6519926
```

Now let's visualise the prioritisation we made for the normal species.

```r
# plot the prioritisation and the normal species' distribution
spp.plot(sim_rs_s2_amount, 1, main='Normal species')
```
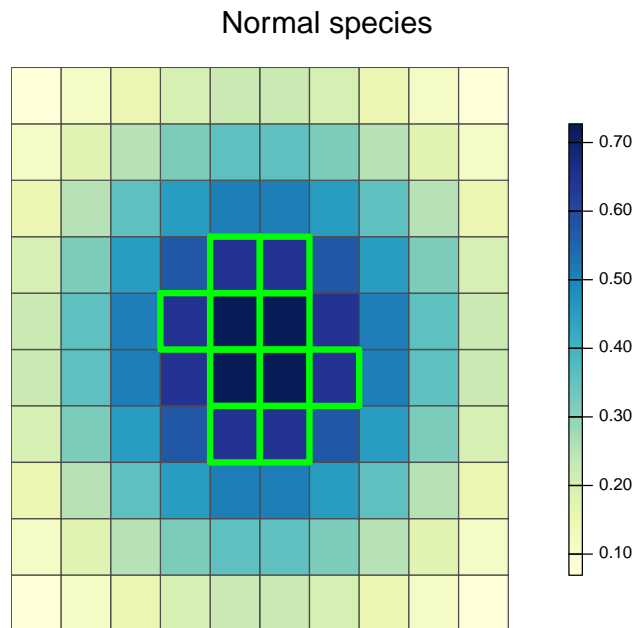

Figure 4 A prioritisation for the normally distributed species generated using amount-based targets (20%). See Figure 3 caption for conventions.

The amount-based prioritisation for the normal species focuses only on the species' range core. This prioritisation fails to secure any peripheral parts of the species' distribution. As a consequence, it may miss out on populations with novel adaptations to environmental conditions along the species' range margin.

Now, let's generate an amount-based target for the bimodally distributed species view it.

```r
# create new object with just the bimodal species
sim_ru_s3 <- spp.subset(sim_ru, 'bimodal')
```

```r
# update amount targets to 20% and space targets to 0% and solve it
sim_rs_s3_amount <- update(sim_ru_s3, amount.target=0.2, space.target=NA)
```

```
## Optimize a model with 1 rows, 100 columns and 100 nonzeros
## Coefficient statistics:
##   Matrix range     [7e-03, 9e-01]
##   Objective range  [1e+00, 1e+00]
##   Bounds range     [1e+00, 1e+00]
##   RHS range        [7e+00, 7e+00]
## Found heuristic solution: objective 21
## Presolve removed 0 rows and 75 columns
## Presolve time: 0.00s
## Presolved: 1 rows, 25 columns, 25 nonzeros
## Variable types: 0 continuous, 25 integer (0 binary)
## Presolved: 1 rows, 25 columns, 25 nonzeros
##
##
## Root relaxation: objective 7.919039e+00, 18 iterations, 0.00 seconds
##
##     Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0    7.91904    0     1   21.00000    7.91904 62.3%     -    0s
## H    0     0                         8.0000000    7.91904  1.01%     -    0s
##
## Explored 0 nodes (18 simplex iterations) in 0.00 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 8.000000000000e+00, best bound 8.000000000000e+00, gap 0.0%
## species = 0; space = 0; tss = 221.892; spaceheld = 159.117; prop = 0.282911
```

```r
# plot the prioritisation and the bimodal species' distribution
spp.plot(sim_rs_s3_amount, 1, main='Bimodal species')
```
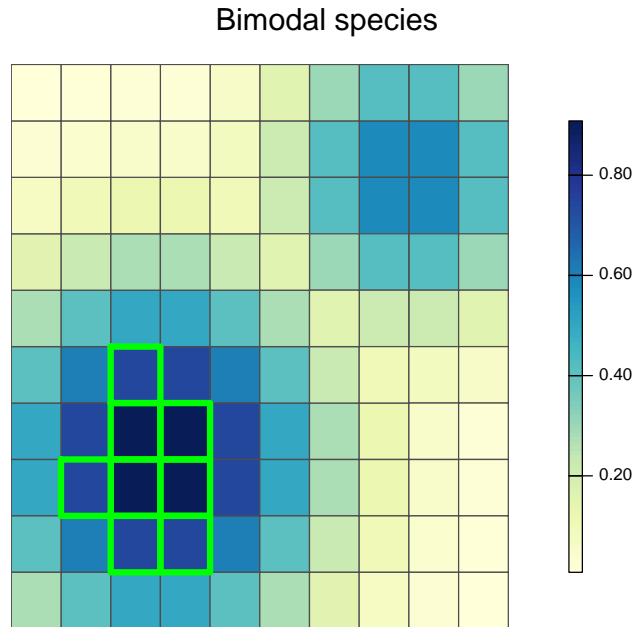
Figure 5 A prioritisation for the bimodally distributed species generated using amount-based targets (20%). See Figure 3 caption for conventions.

```
# show summary
summary(sim_rs_s3_amount)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL     8    8              8                220
##   Connectivity_In Connectivity_Edge Connectivity_Out
## 1               9               197               14
##   Connectivity_In_Fraction
## 1               0.04090909
```

```
# show amount held
amount.held(sim_rs_s3_amount)
```

```
##     bimodal
## 1 0.2018391
```

```
# show space held
space.held(sim_rs_s3_amount)
```

```
##   bimodal (Space 1)
## 1         0.2829105
```

The amount-based prioritisation for the bimodally distributed species only selects planning units in the bottom left corner of the study area. This prioritisation only preserves individuals belonging to

one of the two ecotypes. As a consequence, this prioritisation may fail to preserve a representative sample of the genetic variation found inside this species.

Amount-based and space-based targets

Now that we have generated a prioritisation for each species using only amount-based targets, we will generate a prioritisations using both amount-based and space-targets. To do this we will update the space targets in our amount-based prioritisations to 50%, and store the new prioritisations in new objects.

First, let's do this for the uniform species.

```
# make new prioritisation
sim_rs_s1_space <- update(sim_rs_s1_amount, amount.target=0.2, space.target=0.5)
```

```
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 10102 rows, 10100 columns and 40000 nonzeros
## Coefficient statistics:
##    Matrix range     [2e-01, 4e+01]
##    Objective range  [1e+00, 1e+00]
##    Bounds range     [1e+00, 1e+00]
##    RHS range        [1e+00, 2e+02]
## Found heuristic solution: objective 81
## Presolve time: 0.90s
## Presolved: 10102 rows, 10100 columns, 40000 nonzeros
## Variable types: 0 continuous, 10100 integer (10100 binary)
## Presolved: 10102 rows, 10100 columns, 40000 nonzeros
##
## Presolve removed 10102 rows and 10100 columns
##
## Root relaxation: objective 2.000000e+01, 551 iterations, 0.27 seconds
##
##     Nodes    |    Current Node    |     Objective Bounds     |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
## *    0     0                  0    20.0000000   20.00000  0.00%     -    1s
##
## Explored 0 nodes (552 simplex iterations) in 1.25 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.000000000000e+01, gap 0.0%
## species = 0; space = 0; tss = 412.5; spaceheld = 49.75; prop = 0.879394
```

```
# show summary
summary(sim_rs_s1_space)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
```

```
## 1              1 OPTIMAL      20    20                   20                       220
##    Connectivity_In Connectivity_Edge Connectivity_Out
## 1              18              147               55
##    Connectivity_In_Fraction
## 1               0.08181818
```

```r
# show amount held
amount.held(sim_rs_s1_space)
```

```
##    uniform
## 1      0.2
```

```r
# show space held
space.held(sim_rs_s1_space)
```

```
##    uniform (Space 1)
## 1          0.8793939
```

Let's take a look at the prioritisation for the uniform species with amount-based and space-based targets. Then, let's compare the solutions for the amount-based prioritisation with the new prioritisation using both amount and space targets.

```r
# plot the prioritisation and the uniform species' distribution
spp.plot(sim_rs_s1_space, 'uniform', main='Uniform species')
```
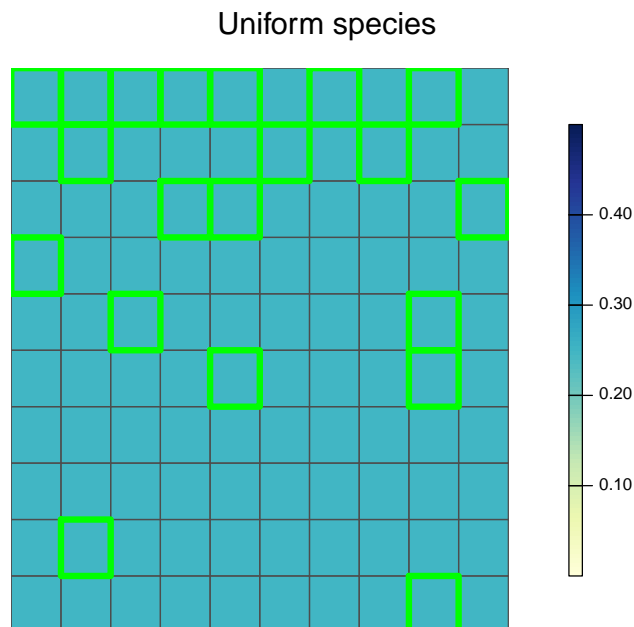

Figure 6 A prioritisation for the uniformly distributed species generated using amount-based targets (20%) and space-based targets (85%). See Figure 3 caption for conventions.

```
# plot the difference between old and new prioritisations
plot(sim_rs_s1_amount, sim_rs_s1_space, 1, 1, main='Difference between solutions')
```
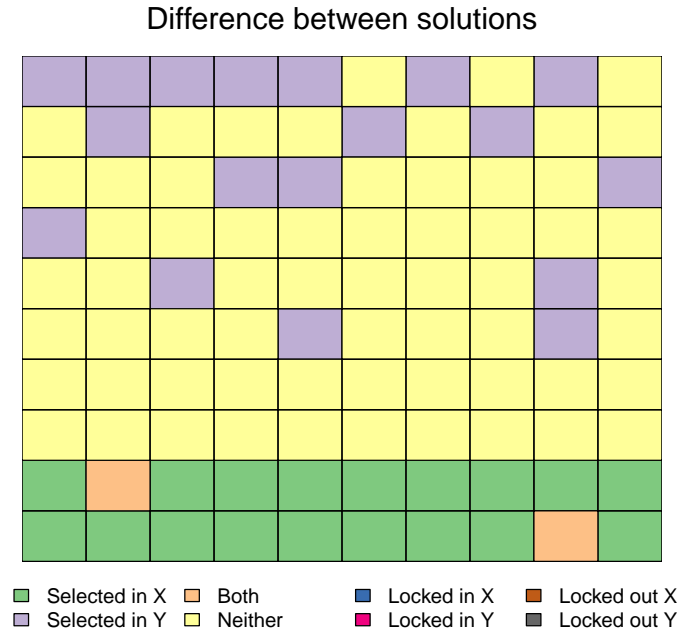
Difference between solutions

Figure 7 Difference between two prioritisations for the uniformly distributed species. Prioritisation X was generated using just amount-based targets (20%), and prioritisation Y was generated using an additional space-based target (85%).

Here we can see that by including a space-target, the prioritisation is spread out evenly across the species' distribution. Unlike the amount-based prioritisation, this prioritisation samples all the different parts of the species' distribution.

Now, let's generate a prioritisation for the normally distributed species that considers amount-based and space-based targets. Then, let's visualise the new prioritisation and compare it to the old amount-based prioritisation.

```
# make new prioritisation
sim_rs_s2_space <- update(sim_rs_s2_amount, amount.target=0.2, space.target=0.85)
```

```
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 10102 rows, 10100 columns and 40000 nonzeros
## Coefficient statistics:
##   Matrix range     [5e-03, 3e+01]
##   Objective range [1e+00, 1e+00]
##   Bounds range    [1e+00, 1e+00]
##   RHS range       [1e+00, 2e+01]
## Found heuristic solution: objective 87
## Presolve removed 1176 rows and 192 columns (presolve time = 5s) ...
```

```
## Presolve removed 1178 rows and 192 columns
## Presolve time: 9.96s
## Presolved: 8924 rows, 9908 columns, 55525 nonzeros
## Variable types: 0 continuous, 9908 integer (9908 binary)
## Presolve removed 1 rows and 0 columns
## Presolved: 8923 rows, 9908 columns, 55510 nonzeros
##
## Presolve removed 8923 rows and 9908 columns
##
## Root simplex log...
##
## Iteration    Objective       Primal Inf.     Dual Inf.      Time
##         0   1.0000000e+02   0.000000e+00   1.000000e+02     10s
##      3156   1.2049877e+01   0.000000e+00   0.000000e+00     11s
##      3156   1.2049877e+01   0.000000e+00   0.000000e+00     11s
##
## Root relaxation: objective 1.204988e+01, 3156 iterations, 0.88 seconds
##
##       Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0   12.04988    0   409   87.00000   12.04988  86.1%     -    11s
## H    0     0                        13.0000000   12.04988  7.31%     -    12s
##
## Explored 0 nodes (3431 simplex iterations) in 12.05 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 1.300000000000e+01, best bound 1.300000000000e+01, gap 0.0%
## species = 0; space = 0; tss = 111.252; spaceheld = 16.4283; prop = 0.852332
```

```
# show summary
summary(sim_rs_s2_space)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL    13   13             13                220
##   Connectivity_In Connectivity_Edge Connectivity_Out
## 1               7               175               38
##   Connectivity_In_Fraction
## 1                0.03181818
```

```
# show amount held
amount.held(sim_rs_s2_space)
```

```
##      normal
## 1 0.2122983
```

```
# show space held
space.held(sim_rs_s2_space)
```

```
##   normal (Space 1)
## 1      0.8523318
```

```
# plot the prioritisation and the normal species' distribution
spp.plot(sim_rs_s2_space, 'normal', main='Normal species')
```
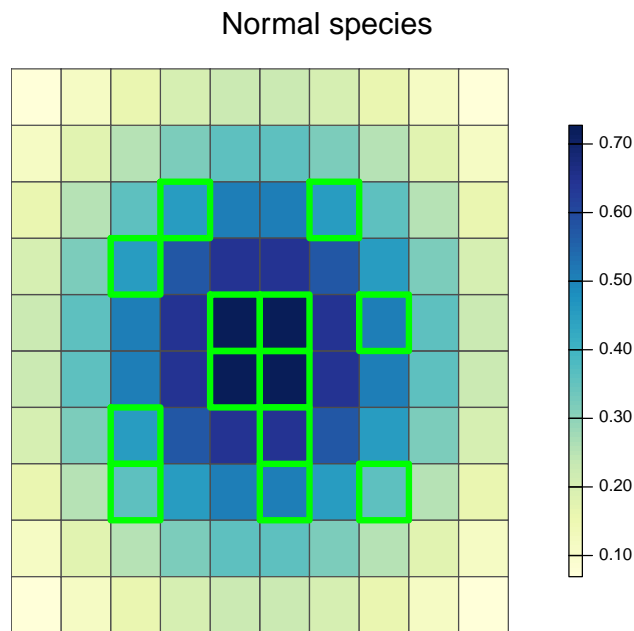

Figure 8 A prioritisation for the normally distributed species generated using amount-based targets (20%) and space-based targets (85%). See Figure 3 caption for conventions.

```
# plot the difference between old and new prioritisations
plot(sim_rs_s2_amount, sim_rs_s2_space, 1, 1, main='Difference between solutions')
```
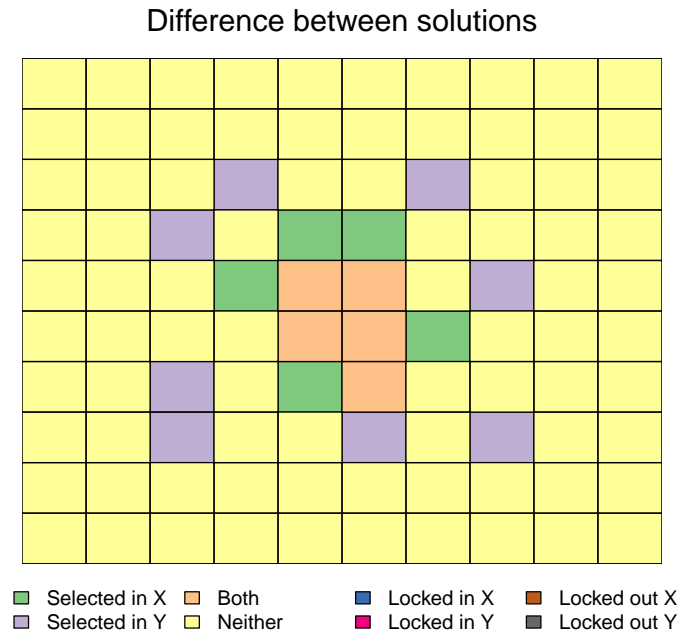
Difference between solutions

Legend:
- Selected in X
- Selected in Y
- Both
- Neither
- Locked in X
- Locked in Y
- Locked out X
- Locked out Y

Figure 9 Difference between two prioritisations for the normally distributed species. See Figure 7 caption for conventions.

We can see by using both amount-based and space-based targets we can obtain a prioritisation that secures both the species' range core and parts of its range margin. As a consequence, it may capture any novel adaptations found along the species' range margin–unlike the amount-based prioritisation.

Finally, let's generate a prioritisation for the bimodal species using amount-based and space-based targets.

```
# make new prioritisation
sim_rs_s3_space <- update(sim_rs_s3_amount, amount.target=0.2, space.target=0.85)
```

```
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 10102 rows, 10100 columns and 40000 nonzeros
## Coefficient statistics:
##   Matrix range     [6e-05, 8e+01]
##   Objective range  [1e+00, 1e+00]
##   Bounds range      [1e+00, 1e+00]
##   RHS range         [1e+00, 3e+01]
## Found heuristic solution: objective 83
## Presolve removed 817 rows and 184 columns (presolve time = 5s) ...
## Presolve removed 817 rows and 184 columns
## Presolve time: 7.36s
## Presolved: 9285 rows, 9916 columns, 50895 nonzeros
## Variable types: 0 continuous, 9916 integer (9916 binary)
## Presolve removed 2 rows and 0 columns
## Presolved: 9283 rows, 9916 columns, 50869 nonzeros
```

```
## 
## Presolve removed 9283 rows and 9916 columns
## 
## Root simplex log...
## 
## Iteration    Objective       Primal Inf.    Dual Inf.      Time
##         0    1.0000000e+02   0.000000e+00   1.000000e+02     8s
##      9465    8.1205830e+00   0.000000e+00   0.000000e+00     9s
##      9465    8.1205830e+00   0.000000e+00   0.000000e+00     9s
## 
## Root relaxation: objective 8.120583e+00, 9465 iterations, 2.03 seconds
## 
##      Nodes    |    Current Node    |     Objective Bounds     |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
## 
##      0     0    8.12058    0   207   83.00000    8.12058  90.2%     -    9s
## H    0     0                        9.0000000    8.12058  9.77%     -    9s
## 
## Explored 0 nodes (9665 simplex iterations) in 9.81 seconds
## Thread count was 1 (of 2 available processors)
## 
## Optimal solution found (tolerance 5.00e-02)
## Best objective 9.000000000000e+00, best bound 9.000000000000e+00, gap 0.0%
## species = 0; space = 0; tss = 221.892; spaceheld = 26.3218; prop = 0.881376
```

```r
# show summary
summary(sim_rs_s3_space)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL     9    9              9                220
##   Connectivity_In Connectivity_Edge Connectivity_Out
## 1               9               193               18
##   Connectivity_In_Fraction
## 1               0.04090909
```

```r
# show amount held
amount.held(sim_rs_s3_space)
```

```
##     bimodal
## 1 0.219729
```

```r
# show space held
space.held(sim_rs_s3_space)
```

```
##   bimodal (Space 1)
## 1         0.8813757
```

```
# plot the prioritisation and the bimodal species' distribution
spp.plot(sim_rs_s3_space, 'bimodal', main='Bimodal species')
```
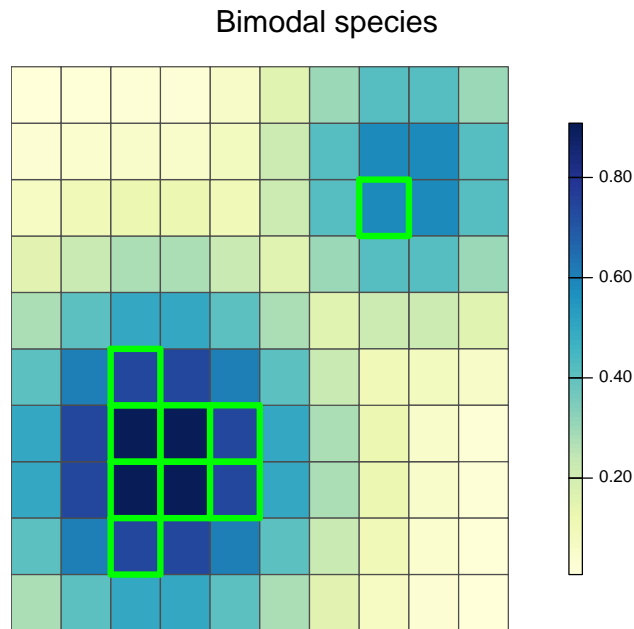

Figure 10 A prioritisation for the normally distributed species generated using amount-based targets (20%) and space-based targets (85%). See Figure 3 caption for conventions.

```
# plot the difference between old and new prioritisations
plot(sim_rs_s3_amount, sim_rs_s3_space, 1, 1, main='Difference between solutions')
```
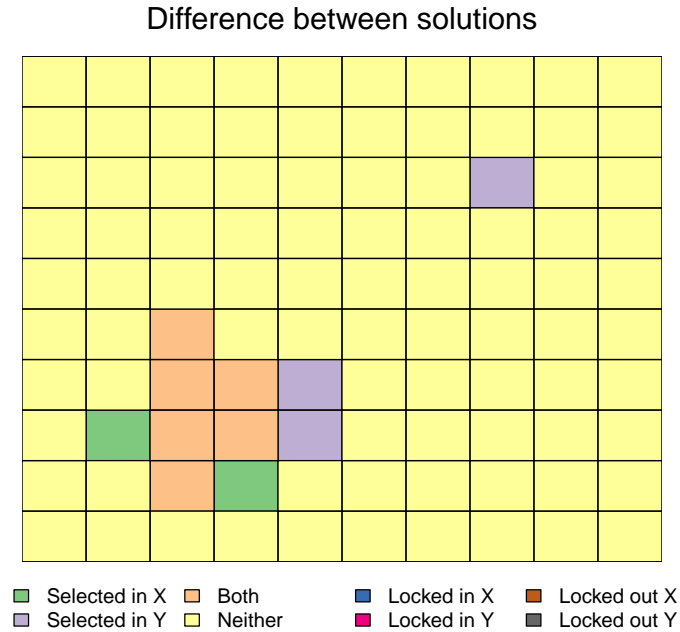
Figure 11 Difference between two prioritisations for the bimodally distributed species. See Figure 7 caption for conventions.

Earlier we found that the amount-based prioritisation only preserved individuals from a single ecotype, and would have failed to adequately preserve the intra-specific variation for this species. However, here we can see that by including space-based targets, we can develop prioritisations that secure individuals belonging to both ecotypes. This new prioritisation is much more effective at sampling the intra-specific variation for this species.

Overall, these results demonstrate that under the simplest of conditions, the use of space-based targets can improve prioritisations. However, these prioritisations were each generated for a single species. It is possible that prioritisations generated using multiple species may do a better job at preserving the intra-specific variation for individuals species by preserving them in different parts of their range. We will investigate this in the next section.

Multi-species prioritisations

Effects of including space-based targets

So far we have generated prioritisations using only a single species at a time. However, real world prioritisations are often generated using multiple species to ensure that they preserve a comprehensive set of biodiversity. Here, we will generate multi-species prioritisations that preserve all three of the simulated species. First, we will generate a prioritisation using amount-based targets that only aims to preserve 20% of the area they occupy. Then, we will generate a prioritisation that also incoperate space-based targets to also preserve 85% of their geographic distribution. We will then compare the two prioritisations.

```
# make prioritisations
sim_mrs_amount <- update(
    sim_ru,
```

```
    amount.target=c(0.2,0.2,0.2),
    space.target=c(0,0,0)
)
```

```
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 30306 rows, 30100 columns and 120000 nonzeros
## Coefficient statistics:
##   Matrix range     [6e-05, 8e+01]
##   Objective range [1e+00, 1e+00]
##   Bounds range     [1e+00, 1e+00]
##   RHS range        [1e+00, 4e+02]
## Found heuristic solution: objective 99
## Presolve removed 0 rows and 0 columns (presolve time = 5s) ...
## Presolve time: 5.19s
## Presolved: 30306 rows, 30100 columns, 120000 nonzeros
## Variable types: 0 continuous, 30100 integer (30100 binary)
## Presolved: 30306 rows, 30100 columns, 120000 nonzeros
##
## Presolve removed 30306 rows and 30100 columns
##
## Root simplex log...
##
## Iteration    Objective       Primal Inf.    Dual Inf.      Time
##        0    1.0000000e+02   0.000000e+00   1.000000e+02      7s
##     2384    2.0000000e+01   5.622070e+01   0.000000e+00     10s
##     3319    2.0000000e+01   0.000000e+00   0.000000e+00     12s
##     3319    2.0000000e+01   0.000000e+00   0.000000e+00     12s
##
## Root relaxation: objective 2.000000e+01, 3319 iterations, 6.61 seconds
##
##     Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
## *    0     0                  0      20.0000000   20.00000  0.00%     -    12s
##
## Explored 0 nodes (4618 simplex iterations) in 12.09 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.000000000000e+01, gap 0.0%
## species = 0; space = 0; tss = 412.5; spaceheld = 58; prop = 0.859394
## species = 1; space = 0; tss = 111.252; spaceheld = 19.9678; prop = 0.820516
## species = 2; space = 0; tss = 221.892; spaceheld = 25.1494; prop = 0.886659
```

```
sim_mrs_space <- update(
    sim_ru,
    amount.target=c(0.2,0.2,0.2),
```

```
    space.target=c(0.85, 0.85, 0.85)
)
```

```
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 30306 rows, 30100 columns and 120000 nonzeros
## Coefficient statistics:
##   Matrix range    [6e-05, 8e+01]
##   Objective range [1e+00, 1e+00]
##   Bounds range    [1e+00, 1e+00]
##   RHS range       [1e+00, 6e+01]
## Found heuristic solution: objective 99
## Presolve removed 1362 rows and 376 columns (presolve time = 5s) ...
## Presolve removed 1391 rows and 376 columns (presolve time = 10s) ...
## Presolve removed 1595 rows and 376 columns (presolve time = 15s) ...
## Presolve removed 1636 rows and 376 columns (presolve time = 21s) ...
## Presolve removed 1636 rows and 376 columns (presolve time = 25s) ...
## Presolve removed 1636 rows and 376 columns
## Presolve time: 26.71s
## Presolved: 28670 rows, 29724 columns, 137500 nonzeros
## Variable types: 0 continuous, 29724 integer (29724 binary)
## Presolved: 28670 rows, 29724 columns, 137500 nonzeros
##
## Presolve removed 28670 rows and 29724 columns
##
## Root simplex log...
##
## Iteration    Objective       Primal Inf.    Dual Inf.      Time
##        0    1.0000000e+02   0.000000e+00   1.000000e+02     28s
##     3720    2.2009864e+01   0.000000e+00   1.187453e+04     30s
##     4125    2.0000000e+01   0.000000e+00   0.000000e+00     30s
##     4125    2.0000000e+01   0.000000e+00   0.000000e+00     30s
##
## Root relaxation: objective 2.000000e+01, 4125 iterations, 3.70 seconds
##
##     Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0   20.00000    0    2   99.00000   20.00000  79.8%     -   31s
## H    0     0                      20.0000000   20.00000  0.00%     -   31s
##
## Explored 0 nodes (5947 simplex iterations) in 31.18 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.000000000000e+01, gap 0.0%
## species = 0; space = 0; tss = 412.5; spaceheld = 28; prop = 0.932121
## species = 1; space = 0; tss = 111.252; spaceheld = 13.2929; prop = 0.880515
```

```
## species = 2; space = 0; tss = 221.892; spaceheld = 16.3965; prop = 0.926106
```

```r
# show summaries
summary(sim_mrs_amount)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL    20   20             20                220
##   Connectivity_In Connectivity_Edge Connectivity_Out
## 1              17               147               56
##   Connectivity_In_Fraction
## 1               0.07727273
```

```r
summary(sim_mrs_space)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL    20   20             20                220
##   Connectivity_In Connectivity_Edge Connectivity_Out
## 1               7               142               71
##   Connectivity_In_Fraction
## 1               0.03181818
```

```r
# show amount held for each prioritisation
amount.held(sim_mrs_amount)
```

```
##   uniform   normal   bimodal
## 1     0.2 0.201559 0.2012952
```

```r
amount.held(sim_mrs_space)
```

```
##   uniform    normal   bimodal
## 1     0.2 0.2185579 0.2232897
```

```r
# show space held for each prioritisation
space.held(sim_mrs_amount)
```

```
##   uniform (Space 1) normal (Space 1) bimodal (Space 1)
## 1         0.8593939        0.8205165         0.8866593
```

```r
space.held(sim_mrs_space)
```

```
##   uniform (Space 1) normal (Space 1) bimodal (Space 1)
## 1         0.9321212        0.8805152         0.9261063
```

```
# plot multi-species prioritisation with amount-based targets
plot(sim_mrs_amount, 1, main='Amount-based targets')
```


Figure 12 A multi-species prioritisation for the uniformly, normally, and bimodally distributed species generated using just amount-based targets (20%). Squares represent planning units. Dark green planning units are selected for preservation.

```
# plot multi-species prioritisation with amount- and space-based targets
plot(sim_mrs_space, 1, main='Amount and space-based targets')
```

Amount and space–based targets
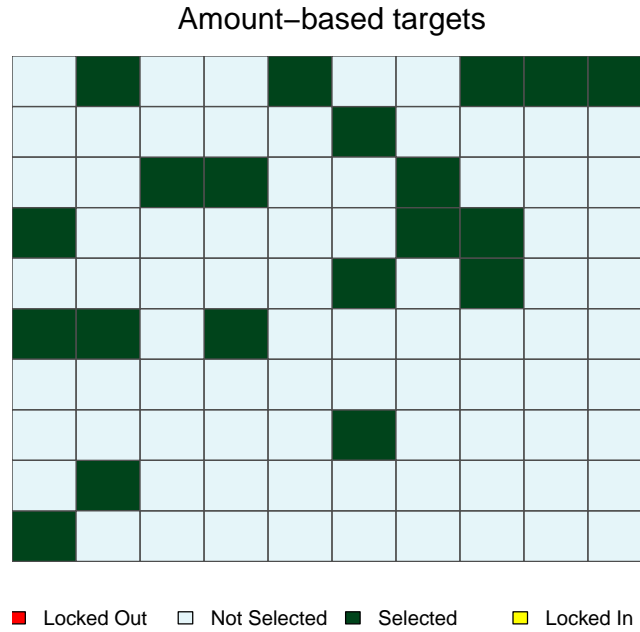

Locked Out □ Not Selected ■ Selected □ Locked In
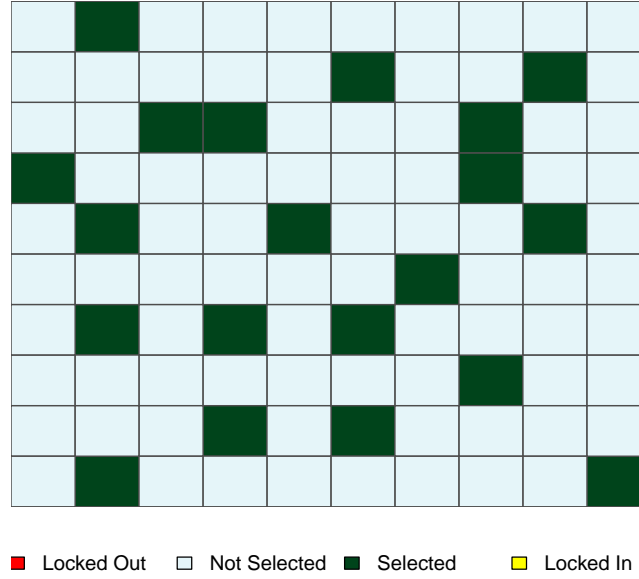
Figure 13 A multi-species prioritisation for the uniformly, normally, and bimodally distributed species generated using amount-based targets (20%) and space-based targets (85%). See Figure 12 caption for conventions.

```
# difference between the two prioritisations
plot(sim_mrs_amount, sim_mrs_space, 1, 1, main='Difference between solutions')
```

Difference between solutions

Selected in X □ Both ■ Locked in X ■ Locked out X
Selected in Y □ Neither ■ Locked in Y ■ Locked out Y

Figure 14 Difference between two multi-species prioritisations. See Figure 7 caption for conventions.

Here we can see that the inclusion of space-based targets changes which planning units are selected for prioritisation, but also the number of planning units that are selected. The amount-based prioritisation is comprised of 20 units, and the space-based prioritisation is comprised of 20 units. This result suggests that an adequate and representative prioritisation can be achieved for only a minor increase in cost.
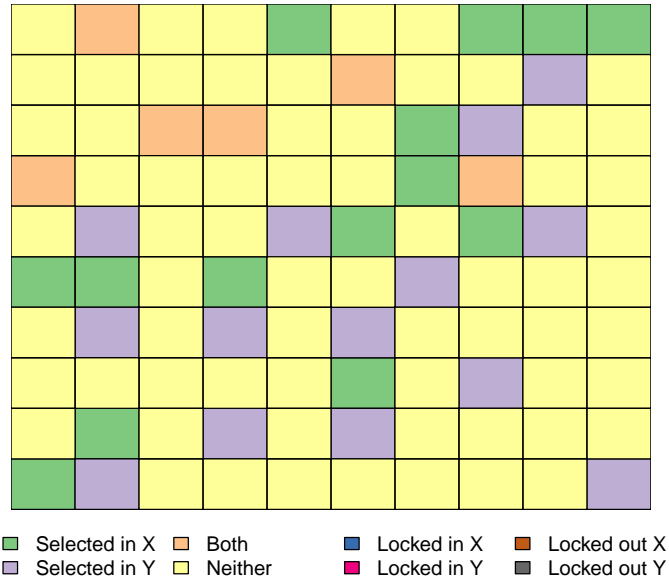
Uncertainty in species' distributions

The unreliable formulation does not consider the probability that the planning units are occupied by features when calculating how well a given solution secures a representative sample of an attribute space. Thus solutions identified using the unreliable formulation may select regions of an attribute space for a species using planning units that only have a small chance of being inhabited. As a consequence, if the prioritisation is implemented, it may fail to secure regions of an attribute space if individuals do not inhabit these planning units, and ultimately fail to fulfil the space-based targets.

A simple solution to this issue would be to ensure that planning units cannot be assigned to demand points if they have a low probability of occupancy. This can be achieved by setting a probability threshold for planning units, such that planning units with a probability of occupancy below the threshold are effectively set to zero.

```
# make new prioritisation with probability threshold of 0.5 for each species
sim_mrs_space2 <- solve(
    prob.subset(
        sim_mrs_space,
        species=1:3,
        threshold=c(0.1,0.1,0.1)
    )
)
```

```
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 27706 rows, 27500 columns and 109600 nonzeros
## Coefficient statistics:
##    Matrix range     [3e-04, 8e+01]
##    Objective range  [1e+00, 1e+00]
##    Bounds range     [1e+00, 1e+00]
##    RHS range        [1e+00, 6e+01]
## Found heuristic solution: objective 99
## Presolve removed 1198 rows and 270 columns (presolve time = 5s) ...
## Presolve removed 1234 rows and 270 columns (presolve time = 10s) ...
## Presolve removed 1365 rows and 270 columns (presolve time = 15s) ...
## Presolve removed 1366 rows and 270 columns (presolve time = 20s) ...
## Presolve removed 1366 rows and 270 columns
## Presolve time: 22.97s
## Presolved: 26340 rows, 27230 columns, 125602 nonzeros
## Variable types: 0 continuous, 27230 integer (27230 binary)
## Presolve removed 30 rows and 0 columns
## Presolved: 26310 rows, 27230 columns, 125523 nonzeros
##
## Presolve removed 26310 rows and 27230 columns
```

```
## 
## Root simplex log...
## 
## Iteration      Objective        Primal Inf.     Dual Inf.      Time
##         0    1.0000000e+02    0.000000e+00    1.000000e+02     25s
##       635    6.9733251e+01    0.000000e+00    1.123230e+04     25s
##      4330    2.0000000e+01    0.000000e+00    0.000000e+00     28s
##      4330    2.0000000e+01    0.000000e+00    0.000000e+00     28s
## 
## Root relaxation: objective 2.000000e+01, 4330 iterations, 5.03 seconds
## 
##       Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
## 
##       0     0    20.00000     0  364    99.00000    20.00000  79.8%      -    30s
## H    0     0                             22.0000000   20.00000  9.09%      -    30s
## H    0     0                             20.0000000   20.00000  0.00%      -    30s
## 
## Explored 0 nodes (7172 simplex iterations) in 30.97 seconds
## Thread count was 1 (of 2 available processors)
## 
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.000000000000e+01, gap 0.0%
## species = 0; space = 0; tss = 412.5; spaceheld = 27.25; prop = 0.933939
## species = 1; space = 0; tss = 111.252; spaceheld = 12.9016; prop = 0.884032
## species = 2; space = 0; tss = 221.892; spaceheld = 14.5032; prop = 0.934639
```

```
# show summary
summary(sim_mrs_space2)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL    20   20             20                220
##   Connectivity_In Connectivity_Edge Connectivity_Out
## 1               7               143               70
##   Connectivity_In_Fraction
## 1               0.03181818
```

```
# plot prioritisation
plot(sim_mrs_space2, 1)
```

Best solution (1)

Locked Out   Not Selected   Selected   Locked In
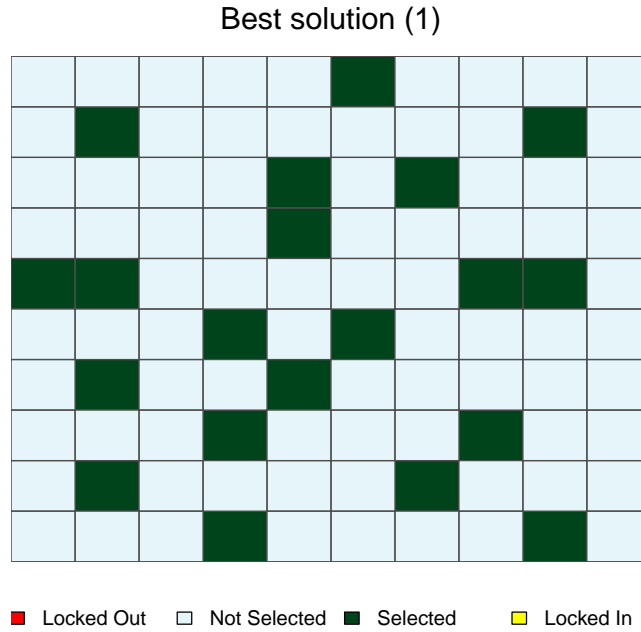
Figure 15 A multi-species prioritisation for the uniformly, normally, and bimodally distributed species generated using amount-based targets (20%) and space-based targets (85%). This prioritisation was generated to be robust against low occupancy probabilities, by preventing planning units with low probabilities from being used to represent demand points. See Figure 12 caption for conventions.

```
# difference between prioritisations that use and do not use thresholds
plot(sim_mrs_space2, sim_mrs_space, 1, 1, main='Difference between solutions')
```

Difference between solutions

Selected in X   Both   Locked in X   Locked out X
Selected in Y   Neither   Locked in Y   Locked out Y

Figure 16 Difference between two multi-species prioritisations. See Figure 7 caption for conventions.

But this method requires setting somewhat arbitrary thresholds. A more robust solution to this issue is to actually use the probabilit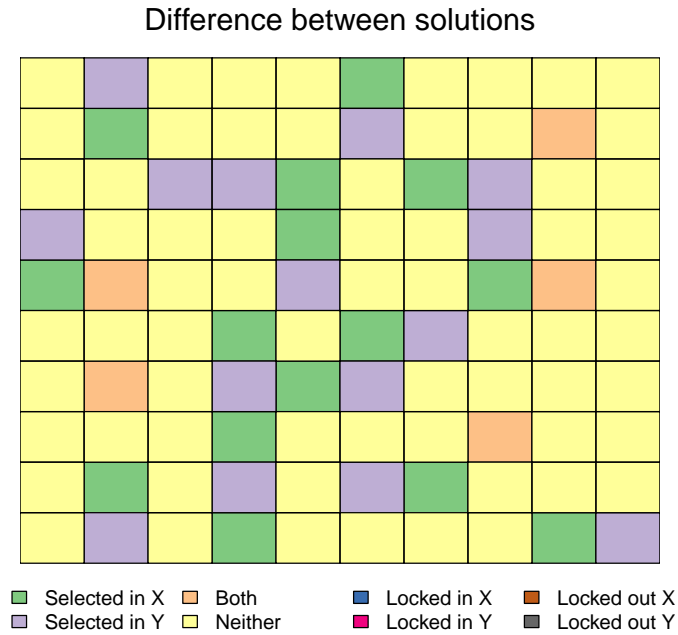y that species occupy planning units to generate the prioritisations. This is what the reliable formulation does. First we will try and generate a solution using existing targets and the reliable formulation. To reduce computational time, we will set the maximum backup R-level to 1.

```
# make new prioritisation using reliable formulation
sim_mrs_space3 <- try(update(sim_mrs_space, formulation='reliable', max.r.level=1L))
```

```
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 364206 rows, 181900 columns and 3847200 nonzeros
## Coefficient statistics:
##    Matrix range     [6e-05, 1e+02]
##    Objective range [1e+00, 1e+00]
##    Bounds range     [1e+00, 1e+00]
##    RHS range        [7e-03, 6e+01]
## Presolve removed 349813 rows and 90706 columns
## Presolve time: 4.70s
##
## Explored 0 nodes (0 simplex iterations) in 7.93 seconds
## Thread count was 1 (of 2 available processors)
##
## Model is infeasible
## Best objective -, best bound -, gap -
## Try setting lower space-based targets.
##  Below are the maximum targets for each species and space.
##    Proportion          Target
## 1   -1.97000 uniform (Space 1)
## 2  -12.67570  normal (Space 1)
## 3  -21.69092 bimodal (Space 1)
```

However, this fails. The reason why we cannot generate a prioritisation is because we require more planning units to generate a solution that fulfills the targets when we consider probabilities. This is confirmed by the negative maximum targets shown in the error message. Now, we will set lower targets and generate solution.

```
# make new prioritisation using reliable formulation and reduced targets
sim_mrs_space3 <- update(
    sim_mrs_space,
    formulation='reliable',
    max.r.level=1L,
    space.target=-25
)
```

```
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 364206 rows, 181900 columns and 3847200 nonzeros
## Coefficient statistics:
```

```
##     Matrix range     [6e-05, 1e+02]
##     Objective range  [1e+00, 1e+00]
##     Bounds range     [1e+00, 1e+00]
##     RHS range        [7e-03, 1e+04]
## Presolve removed 333501 rows and 90800 columns (presolve time = 5s) ...
## Presolve removed 333701 rows and 151600 columns (presolve time = 10s) ...
## Presolve removed 333701 rows and 151600 columns (presolve time = 108s) ...
## Presolve removed 333701 rows and 151600 columns (presolve time = 110s) ...
## Presolve removed 333701 rows and 151600 columns
## Presolve time: 111.44s
## Presolved: 30505 rows, 30300 columns, 129690 nonzeros
## Variable types: 200 continuous, 30100 integer (30100 binary)
## Found heuristic solution: objective 64.0000000
## Presolved: 30505 rows, 30300 columns, 129690 nonzeros
##
## Presolve removed 30103 rows and 11814 columns
##
## Root simplex log...
##
## Iteration    Objective       Primal Inf.    Dual Inf.      Time
##         0    0.0000000e+00   2.865759e+01   5.535568e+08    116s
##       177    2.0000000e+01   0.000000e+00   0.000000e+00    116s
##       177    2.0000000e+01   0.000000e+00   0.000000e+00    116s
##
## Root relaxation: objective 2.000000e+01, 177 iterations, 1.31 seconds
##
##     Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
## *    0     0               0      20.0000000   20.00000  0.00%     -  115s
##
## Explored 0 nodes (179 simplex iterations) in 116.10 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.000000000000e+01, gap 0.0%


## Warning in validityMethod(object): object@space.held contains values less
## than 0, some species are really poorly represented
```

```
# show summary
summary(sim_mrs_space3)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL    20   20             20                220
##   Connectivity_In Connectivity_Edge Connectivity_Out
## 1              28               161               31
```

```
##    Connectivity_In_Fraction
## 1               0.1272727
```

```
# plot prioritisation
plot(sim_mrs_space3, 1)
```

Best solution (1)
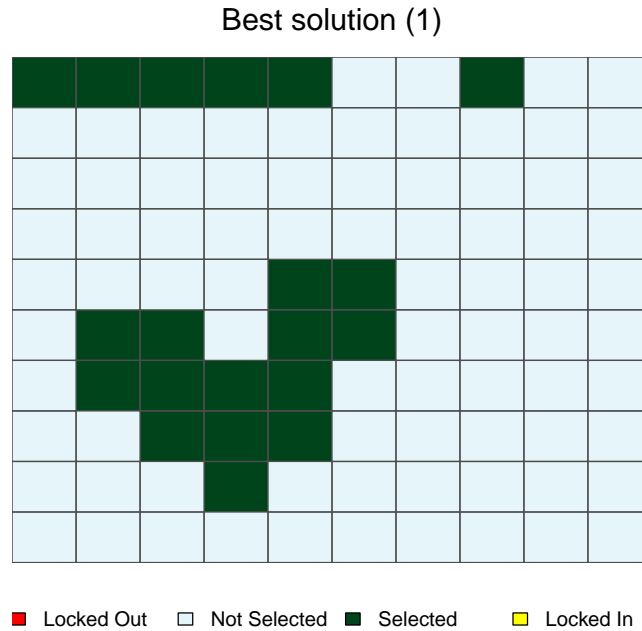
Figure 17 A multi-species prioritisation for the uniformly, normally, and bimodally distributed species generated using amount-based targets (20%) and space-based targets (85%). This prioritisation was generated to be robust against low occupancy probabilities, by explicitly using the probability of occupancy data when deriving a solution. See Figure 12 caption for conventions.

```
# difference between prioritisations based on unreliable and reliable formulation
plot(sim_mrs_space3, sim_mrs_space, 1, 1, main='Difference between solutions')
```

Difference between solutions

Figure 18 Difference between two multi-species prioritisations. See Figure 7 caption for conventions.
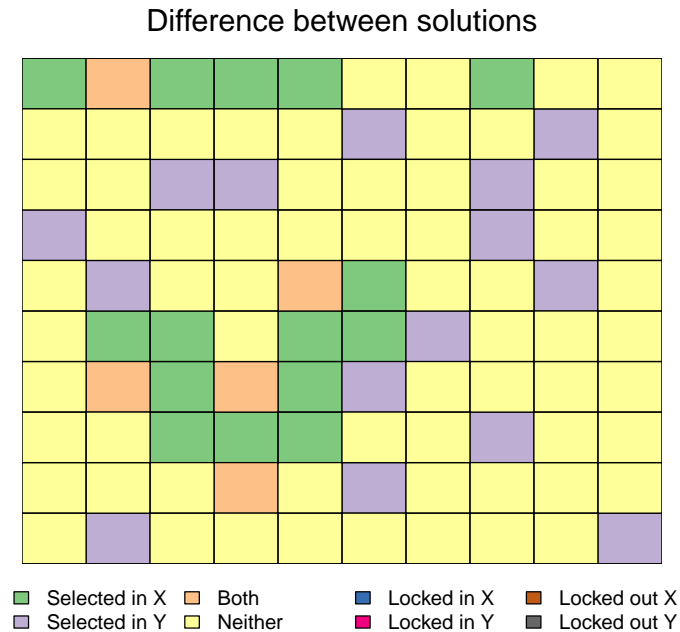
An additional planning unit was selected using the reliable formulation. The prioritisation based on the unreliable formulation had 20 planning units, but the prioritisation based on the reliable formlation has 20 planning units. This differnce occurs because the reliable formulation needs to ensure that all selected planning units with a low chance of being occupied have a suitable backup planning unit. While the reliable formulation can deliver more robust prioritisations, it takes much longer to solve conservation planning problems expressed using this formulation than the unreliable formulation. As a consequence, the reliable formulation is only feasible for particularly small problems, such as those involving few features and less than several hundred planning units.

Fragmentation

Fragmentation is an important consideration in real-world planning situations. Up until now, we haven't considered the effects of fragmentation on the viability of the prioritisation. As a consequence, our prioritisations have tended to contain planning units without any neighbours. We can use the `BLM` parameter to penalise fragmented solutions.

Let's generate a new prioritisation that heavily penalises fragmentation. Here, we will update the `sim_mrs_amount` object with `BLM` of 100.

```
# update prioritisation
sim_mrs_amount_blm <- update(sim_mrs_amount, BLM=100)
```

```
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 30666 rows, 30280 columns and 120720 nonzeros
## Coefficient statistics:
##   Matrix range    [6e-05, 8e+01]
##   Objective range [1e+02, 4e+02]
```

```
##    Bounds range     [1e+00, 1e+00]
##    RHS range        [1e+00, 4e+02]
## Found heuristic solution: objective 4299
## Presolve removed 0 rows and 0 columns (presolve time = 5s) ...
## Presolve time: 5.99s
## Presolved: 30666 rows, 30280 columns, 120720 nonzeros
## Variable types: 0 continuous, 30280 integer (30280 binary)
## Presolved: 30666 rows, 30280 columns, 120720 nonzeros
##
## Presolve removed 30666 rows and 30280 columns
##
## Root simplex log...
##
## Iteration    Objective       Primal Inf.    Dual Inf.      Time
##        0    2.2100000e+04   0.000000e+00   4.010000e+04      7s
##     2093    1.1941697e+03   0.000000e+00   3.921985e+05     10s
##     5768    6.4673127e+02   0.000000e+00   2.068700e+05     15s
##     7117    4.6444444e+02   0.000000e+00   0.000000e+00     18s
##     7117    4.6444444e+02   0.000000e+00   0.000000e+00     18s
##
## Root relaxation: objective 4.644444e+02, 7117 iterations, 12.27 seconds
##
##     Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0  464.44444    0 1725 4299.00000  464.44444  89.2%     -   18s
## H    0     0                      1953.0000000  464.44444  76.2%     -   45s
##      0     0  523.81679    0 1561 1953.00000  523.81679  73.2%     -   48s
##      0     0  523.81679    0 1560 1953.00000  523.81679  73.2%     -   49s
##      0     0  571.01549    0 1811 1953.00000  571.01549  70.8%     -   51s
##      0     0  571.01549    0 1827 1953.00000  571.01549  70.8%     -   52s
##      0     0  571.01549    0 1832 1953.00000  571.01549  70.8%     -   54s
##      0     0  571.01549    0 1831 1953.00000  571.01549  70.8%     -   54s
##      0     0  571.01549    0 1676 1953.00000  571.01549  70.8%     -   59s
##      0     0  571.01549    0 1684 1953.00000  571.01549  70.8%     -   60s
##      0     0  571.01549    0 1636 1953.00000  571.01549  70.8%     -   63s
##      0     0  571.01549    0 1651 1953.00000  571.01549  70.8%     -   63s
##      0     0  571.01549    0 1625 1953.00000  571.01549  70.8%     -   67s
##      0     0  571.01549    0 1631 1953.00000  571.01549  70.8%     -   68s
##      0     0  571.01549    0 1606 1953.00000  571.01549  70.8%     -   71s
##      0     0  571.01549    0 1611 1953.00000  571.01549  70.8%     -   72s
##      0     0  571.01549    0 1556 1953.00000  571.01549  70.8%     -   76s
##      0     0  571.01549    0 1559 1953.00000  571.01549  70.8%     -   76s
##      0     0  571.01549    0 1561 1953.00000  571.01549  70.8%     -   79s
##      0     0  571.01549    0 1562 1953.00000  571.01549  70.8%     -   79s
##      0     0  571.01549    0 1584 1953.00000  571.01549  70.8%     -   82s
##      0     0  571.01549    0 1539 1953.00000  571.01549  70.8%     -   84s
## H    0     0                      1435.0000000  571.01549  60.2%     -   97s
```

##	H	0	0				1332.0000000	571.01549	57.1%	-	108s
##		0	2	572.12289	0	1506	1332.00000	572.12289	57.0%	-	108s
##		4	6	601.87668	4	1064	1332.00000	575.86532	56.8%	1811	110s
##		10	12	702.77417	10	1108	1332.00000	575.86532	56.8%	1568	116s
##		18	20	853.33333	18	930	1332.00000	575.86532	56.8%	1274	120s
##	H	22	22				1227.0000000	575.86532	53.1%	1170	122s
##	H	28	28				1121.0000000	575.86532	48.6%	984	126s
##	*	41	33		38		1120.0000000	575.86532	48.6%	702	126s
##		49	39	713.75000	7	1290	1120.00000	585.46465	47.7%	741	131s
##		59	49	920.00000	17	954	1120.00000	585.46465	47.7%	688	135s
##		71	56	980.00000	24	587	1120.00000	585.46465	47.7%	663	140s
##		94	71	864.64286	14	1011	1120.00000	594.82736	46.9%	603	145s
##		115	84	691.48733	3	1357	1120.00000	604.26637	46.0%	581	150s
##		123	92	856.90745	11	983	1120.00000	604.26637	46.0%	608	155s
##		129	98	1002.35294	17	621	1120.00000	604.26637	46.0%	637	160s
##		140	101	695.00000	6	1519	1120.00000	613.10042	45.3%	650	165s
##		141	102	702.99776	7	1479	1120.00000	613.10042	45.3%	706	170s
##		155	116	906.11111	21	643	1120.00000	613.10042	45.3%	694	175s
##		169	123	712.59259	7	998	1120.00000	621.72786	44.5%	694	180s
##		185	139	946.47059	20	636	1120.00000	621.72786	44.5%	677	185s
##		203	152	854.16557	10	1045	1120.00000	625.00000	44.2%	671	190s
##		215	158	1020.00000	17	621	1120.00000	625.00000	44.2%	661	195s
##		238	162	750.04786	11	1008	1120.00000	641.89958	42.7%	632	201s
##		243	167	885.00000	16	986	1120.00000	641.89958	42.7%	653	205s
##		254	171	744.59580	3	1572	1120.00000	650.00000	42.0%	671	213s
##		257	174	855.18726	6	1416	1120.00000	650.00000	42.0%	671	215s
##		260	175	cutoff	9		1120.00000	650.00000	42.0%	689	222s
##		266	175	cutoff	12		1120.00000	650.00000	42.0%	690	225s
##		279	180	877.69231	13	987	1120.00000	654.29758	41.6%	687	230s
##	H	289	149				1021.0000000	654.29758	35.9%	676	234s
##		297	156	1020.00000	31	2	1021.00000	654.29758	35.9%	664	235s
##	H	353	149				1020.0000000	654.29758	35.9%	561	236s
##		362	153	882.50000	11	968	1020.00000	655.58472	35.7%	566	240s
##		385	169	748.90273	12	1285	1020.00000	658.46154	35.4%	556	245s
##		396	180	927.45527	23	914	1020.00000	658.46154	35.4%	562	250s
##		413	184	860.00000	11	919	1020.00000	660.85511	35.2%	563	255s
##		420	191	981.29032	15	587	1020.00000	660.85511	35.2%	579	261s
##		441	203	949.41176	15	835	1020.00000	663.02381	35.0%	566	265s
##		458	212	860.47619	12	938	1020.00000	663.90244	34.9%	565	270s
##		475	220	770.00000	11	677	1020.00000	671.06383	34.2%	557	275s
##		499	234	860.00000	6	1571	1020.00000	678.06452	33.5%	549	281s
##		511	245	834.28571	16	1539	1020.00000	678.06452	33.5%	547	305s
##		513	246	691.48733	4	1725	1020.00000	678.06452	33.5%	545	346s
##		514	247	920.00000	15	1642	1020.00000	678.06452	33.5%	544	351s
##		516	248	842.44898	15	1500	1020.00000	678.06452	33.5%	542	376s
##		518	250	1001.81818	17	1555	1020.00000	678.06452	33.5%	540	383s
##		519	250	898.94737	16	1594	1020.00000	678.06452	33.5%	539	385s
##		520	251	882.50000	12	1486	1020.00000	678.06452	33.5%	538	396s

```
##    522   252   737.39130   10  1562  1020.00000   678.06452   33.5%   536   403s
##    523   253   853.33333   14  1576  1020.00000   678.06452   33.5%   535   407s
##    524   254   943.40426   15  1571  1020.00000   678.06452   33.5%   534   411s
##    525   254   898.12500   17  1532  1020.00000   678.06452   33.5%   533   415s
##    526   255   717.89474   10  1483  1020.00000   678.06452   33.5%   532   426s
##    528   256   705.00031    4  1439  1020.00000   678.06452   33.5%   530   438s
##    529   257   834.28571   16  1445  1020.00000   678.06452   33.5%   529   441s
##    530   258   743.34999    8  1472  1020.00000   678.06452   33.5%   528   449s
##    531   258   834.28571   16  1483  1020.00000   678.06452   33.5%   527   451s
##    533   260   691.48733    4  1444  1020.00000   678.06452   33.5%   525   456s
##    534   260   920.00000   15  1444  1020.00000   678.06452   33.5%   524   463s
##    535   263   678.06452   15  1329  1020.00000   678.06452   33.5%   692   471s
##    538   265   804.93743   16  1480  1020.00000   678.06452   33.5%   701   475s
##    542   268   893.07553   18  1497  1020.00000   678.06452   33.5%   717   480s
##    548   269   966.15385   21   494  1020.00000   678.06452   33.5%   729   485s
##    561   266   715.71544   18  1442  1020.00000   678.06452   33.5%   729   490s
##    563   268   758.61850   19  1629  1020.00000   678.06452   33.5%   747   499s
##    564   268   801.05630   19  1346  1020.00000   678.06452   33.5%   748   500s
##    570   272   910.90909   22   648  1020.00000   678.06452   33.5%   761   507s
## *  571   254               23        920.0000000   678.06452   26.3%   761   508s
##    574   252      cutoff   23         920.00000   678.06452   26.3%   767   511s
##    580   250   784.96446   17  1564   920.00000   689.31692   25.1%   768   515s
##    582   251   827.74784   18  1391   920.00000   689.31692   25.1%   780   520s
##    586   253   882.80157   20  1600   920.00000   689.31692   25.1%   788   525s
##    595   249   872.26193   19  1052   920.00000   691.34181   24.9%   794   530s
##    607   249   826.25000   20   597   920.00000   710.96046   22.7%   802   539s
##    608   250   857.37717   21  1229   920.00000   710.96046   22.7%   812   543s
##    609   249   897.77778   21   577   920.00000   710.96046   22.7%   812   545s
##    612   248   892.72727   22   569   920.00000   710.96046   22.7%   817   551s
##    615   247      cutoff   24         920.00000   710.96046   22.7%   824   555s
##    622   248   790.00000   20   941   920.00000   715.05609   22.3%   830   561s
##    626   250   853.33333   22   640   920.00000   715.05609   22.3%   830   567s
##    627   249   916.55172   23   612   920.00000   715.05609   22.3%   832   570s
##    633   247   788.41438   18  1248   920.00000   731.83346   20.5%   834   575s
##    642   245   903.78378   20   810   920.00000   731.83346   20.5%   834   580s
##    658   240   827.58226   19  1348   920.00000   732.65856   20.4%   825   585s
##    666   239   887.87539   22   835   920.00000   732.65856   20.4%   826   590s
##    678   235   893.33333   21   743   920.00000   782.77632   14.9%   828   596s
##    719   223   916.31963   62   264   920.00000   782.77632   14.9%   788   600s
##    730   219   892.72727   23   609   920.00000   801.98120   12.8%   790   605s
##    732   218   840.82613   20  1367   920.00000   805.11605   12.5%   794   610s
##    785   200   905.24590   72  1322   920.00000   805.11605   12.5%   749   615s
##    873   170   846.90005   17  1307   920.00000   805.53064   12.4%   681   620s
##    880   167   828.68077   17  1337   920.00000   808.16731   12.2%   681   635s
##    888   163      cutoff   22         920.00000   808.16731   12.2%   688   640s
##    909   157   918.12293   38  2347   920.00000   812.30628   11.7%   686   651s
##    913   154   902.92683   21   946   920.00000   818.45124   11.0%   688   656s
##    938   146   855.51165   18  1421   920.00000   819.16697   11.0%   674   660s
```

```
##      944   142  912.93231   19 1426  920.00000  824.46334  10.4%   677  665s
##      955   137  853.33333   19  882  920.00000  828.87080  9.91%   680  670s
##      961   133  853.33333   21  581  920.00000  832.50000  9.51%   684  678s
##      962   133  904.61538   22  581  920.00000  832.50000  9.51%   686  683s
##      981   126  838.60465   20  901  920.00000  838.18182  8.89%   676  686s
##      991   123  870.00000   20  887  920.00000  843.52941  8.31%   675  690s
##     1000   117  867.82609   21  644  920.00000  850.43478  7.56%   682  697s
##     1001   117  906.36364   22  612  920.00000  850.43478  7.56%   684  702s
##     1008   113  912.00000   22  479  920.00000  853.33333  7.25%   682  705s
##     1031   103  875.17241   22 1298  920.00000  853.33333  7.25%   672  710s
##     1049    95  876.40770   19 1731  920.00000  862.02517  6.30%   667  715s
##     1053    93  909.22095   22  777  920.00000  862.02517  6.30%   671  720s
##     1102    77  909.22095   71  674  920.00000  862.02517  6.30%   646  725s
##     1129    68  899.15360   23  794  920.00000  870.00000  5.43%   637  730s
##
## Cutting planes:
##   Gomory: 11
##   Zero half: 69
##
## Explored 1157 nodes (809290 simplex iterations) in 733.75 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 9.200000000000e+02, best bound 8.780000000000e+02, gap 4.5652%
## species = 0; space = 0; tss = 412.5; spaceheld = 225; prop = 0.454545
## species = 1; space = 0; tss = 111.252; spaceheld = 60.9957; prop = 0.451733
## species = 2; space = 0; tss = 221.892; spaceheld = 76.7822; prop = 0.653967
```

```
# show summary of prioritisation
summary(sim_mrs_amount_blm)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL   920   20             20                220
##   Connectivity_In Connectivity_Edge Connectivity_Out
## 1              35               171               14
##   Connectivity_In_Fraction
## 1                0.1590909
```

```
# show amount held for each prioritisation
amount.held(sim_mrs_amount_blm)
```

```
##   uniform    normal   bimodal
## 1     0.2 0.2645832 0.3911267
```

```
# show space held for each prioritisation
space.held(sim_mrs_amount_blm)
```

```
##   uniform (Space 1) normal (Space 1) bimodal (Space 1)
## 1        0.4545455         0.4517326         0.6539667
```

```
# plot prioritisation
plot(sim_mrs_amount_blm, 1)
```
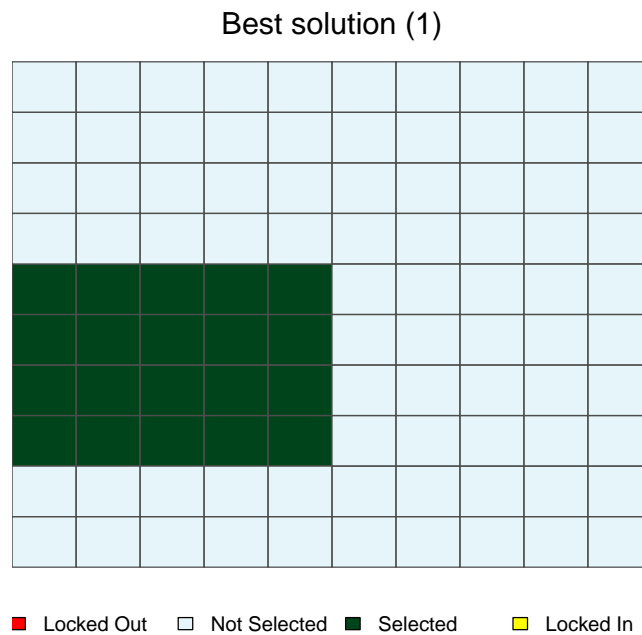
Best solution (1)

■ Locked Out   ☐ Not Selected   ■ Selected   ☐ Locked In

Figure 19 A multi-species prioritisation for the uniformly, normally, and bimodally distributed species generated using only amount-based targets (20%). Additionally, this priorititisation was specified to have high connectivity, by using a high BLM parameter. See Figure 12 caption for conventions.

```
# difference between the two prioritisations
plot(sim_mrs_amount_blm, sim_mrs_amount, 1, 1, main='Difference between solutions')
```

Difference between solutions
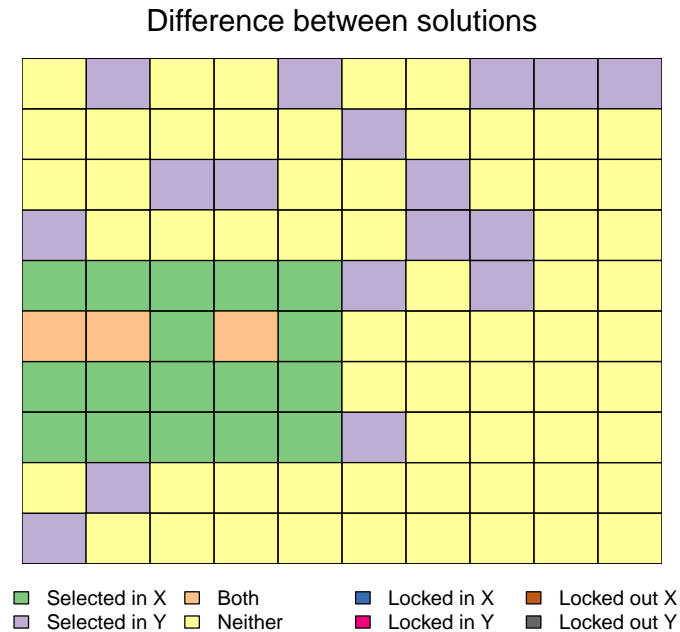
Figure 20 Difference between two multi-species prioritisations. See Figure 7 caption for conventions.

Here we can see that the prioritisation generated using a `BLM` parameter of 100 is much more clustered than the prioritisation generated using a `BLM` of 0. In practice, conservation planners will need to try a variety of `BLM` parameters to find a suitable prioritisation.

Complex simulated species

Data

In the previous examples, we have only used Euclidean distances to determine how much of an attribute space is sampled by a prioritisation. However, Euclidean distances can be poor measures of distance for multivariate, binary, or correlated variables (Faith *et al.* 1987). As a consequence this may lead to over- or under-estimates of the quality of a given solution.

The `rapr` R package provides a suite of distance metrics that can be used to calculate spatial representation (see `?AttributeSpace` for available metrics and their equations). To illustrate how using different distance metrics can affect the optimal solution, we will generate a new suite of prioritisations using different distance metrics.

First, we will simulate a new species and a three-dimensional attribute space. Note that unlike the previous examples, the attribute space will not be geographic space. Rather, each dimension in the attribute space will have values that map onto geographic space (eg. like climatic variables across the landscape). To add further complexity, we simulate their distributions using Gaussian processes.

```r
# set seed for simulations
set.seed(500)

## simulate planning units
```

```r
sim_pus <- sim.pus(25L)

# simulate species
sim_gspp <- sim.species(sim_pus, model=RPgauss(), n=1, res=0.1)

# simulate space
sim_gspace <- sim.space(sim_pus, model=RMgauss(scale=3), d=3, res=0.1)
```

```
## ...
```

```r
# increment simulated space values by 100 so there are no negative values
# so we can investigate all distance metrics
sim_gspace <- sim_gspace + 100


# generate RapUnsolved object containing data to generate prioritisations
sim_ru_gp <- rap(
    sim_pus, sim_gspp, sim_gspace,
    amount.target=0.2, space.target=0.85,
    n.demand.points=50L, kernel.method='hypervolume',
    include.geographic.space=FALSE, scale=FALSE, solve=FALSE
)
```

```
## Choosing repsperpoint=1500 (use a larger value for more accuracy.)
## Evaluating probability density...
## Building tree... done.
## Querying tree... 2.33918e-06  0.0233942  0.046786  0.0701778  0.0935696  0.116961  0.140353
## Finished evaluating probability density.
## Beginning volume calculation... done.
## Quantile requested: 0.20    obtained: 0.20
```

Let's visualise the species' distribution and the distribution of the attribute space across geographic space.

```r
# plot species distribution
plot(
    sim_gspp,
    main='Simulated species',
    col=colorRampPalette(c("#FFFFD9", "#EDF8B1", "#C7E9B4", "#7FCDBB",
        "#41B6C4", "#1D91C0", "#225EA8", "#253494", "#081D58"
    ))(100)
)
lines(sim_pus)
```
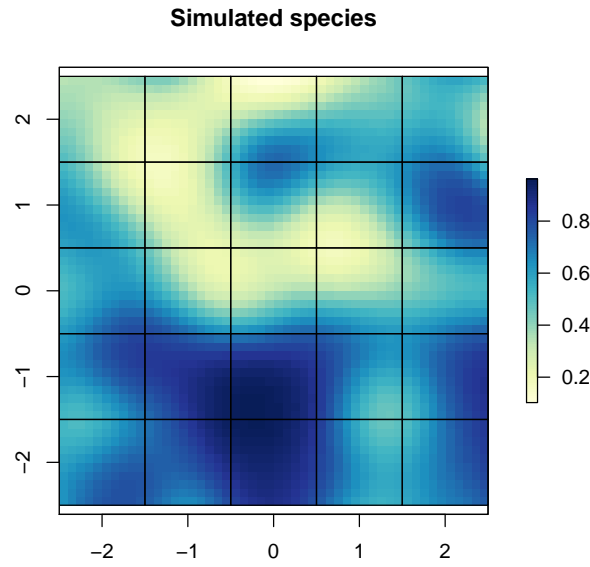
Figure 21 Distribution map of a species simulated using Gaussian prorceses. See Figure 2 caption for conventions.

```
# plot distribution of each dimension in the attribute space across geographic space
plot(
    sim_gspace,
    main=c('Attribute space (d=1)', 'Attribute space (d=2)', 'Attribute space (d=3)'),
    addfun=function(){lines(sim_pus)},
    nc=3
)
```
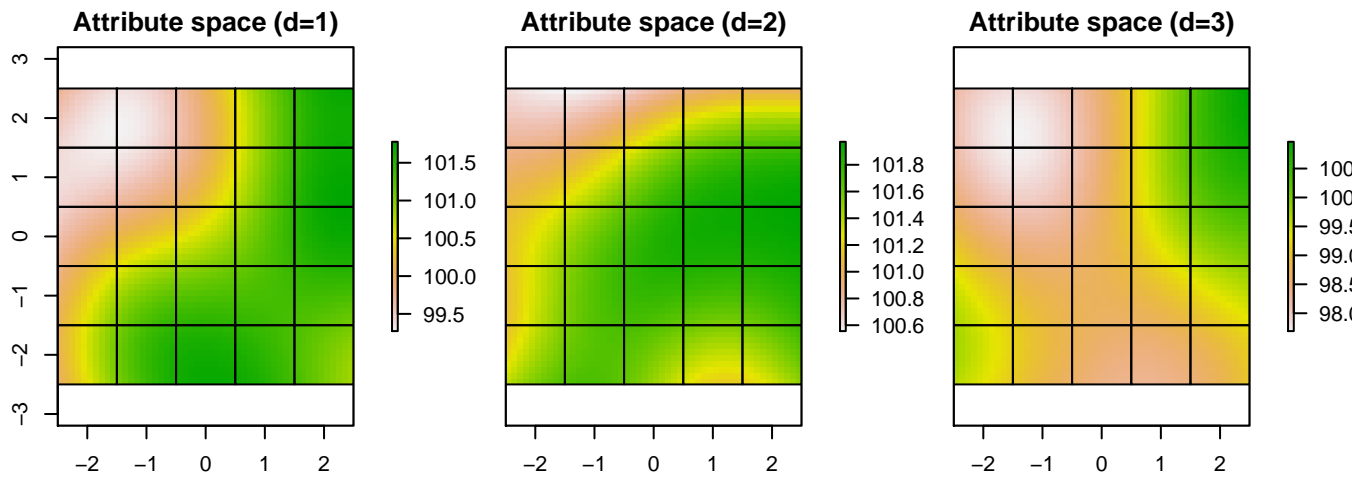

Figure 22 Distribution of spatial variables across the species' geographic range. These variables each represent a dimension of a three-dimensional attribute space.

Distance metrics

For each different distance metric, we will update the `sim_gru` object with the new distance metric, solve it, and store the solution in a list.

```r
# create vector with distance metrics
dist.metrics <- c(
    'euclidean', 'bray', 'manhattan','gower',
    'canberra', 'mahalanobis',
    'jaccard', 'kulczynski'
)

# generate solutions
solutions <- list()
for (i in dist.metrics) {
    solutions[[i]] <- update(sim_ru_gp, distance.metric=i)
}
```

```
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
##    Matrix range     [3e-01, 3e+04]
##    Objective range  [1e+00, 1e+00]
##    Bounds range     [1e+00, 1e+00]
##    RHS range        [1e+00, 5e+03]
## Presolve removed 248 rows and 143 columns
## Presolve time: 0.13s
## Presolved: 1054 rows, 1132 columns, 5329 nonzeros
## Variable types: 0 continuous, 1132 integer (1132 binary)
## Found heuristic solution: objective 19.0000000
## Presolved: 1054 rows, 1132 columns, 5329 nonzeros
##
## Presolve removed 1054 rows and 1132 columns
##
## Root relaxation: objective 4.583726e+00, 701 iterations, 0.04 seconds
##
##      Nodes    |    Current Node    |     Objective Bounds     |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0    4.58373    0   69   19.00000    4.58373  75.9%     -    0s
## H    0     0                        5.0000000    4.58373  8.33%     -    0s
##
## Explored 0 nodes (701 simplex iterations) in 0.21 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.000000000000e+00, gap 0.0%
## species = 0; space = 0; tss = 35677.7; spaceheld = 4843.09; prop = 0.864254
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
```

```
## Coefficient statistics:
##   Matrix range     [8e-06, 1e+00]
##   Objective range [1e+00, 1e+00]
##   Bounds range     [1e+00, 1e+00]
##   RHS range        [4e-02, 3e+00]
## Presolve removed 185 rows and 134 columns
## Presolve time: 0.21s
## Presolved: 1117 rows, 1141 columns, 5590 nonzeros
## Variable types: 0 continuous, 1141 integer (1141 binary)
## Found heuristic solution: objective 19.0000000
## Presolve removed 22 rows and 0 columns
## Presolved: 1095 rows, 1141 columns, 5479 nonzeros
##
## Presolve removed 493 rows and 91 columns
##
## Root relaxation: objective 4.419702e+00, 718 iterations, 0.05 seconds
##
##     Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##     0     0    4.41970    0    43   19.00000    4.41970  76.7%     -    0s
## H   0     0                         5.0000000   4.41970  11.6%     -    0s
##
## Explored 0 nodes (718 simplex iterations) in 0.30 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.000000000000e+00, gap 0.0%
## species = 0; space = 0; tss = 0.234702; spaceheld = 0.0285727; prop = 0.87826
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
##   Matrix range     [3e-01, 9e+04]
##   Objective range [1e+00, 1e+00]
##   Bounds range     [1e+00, 1e+00]
##   RHS range        [1e+00, 1e+04]
## Presolve removed 236 rows and 134 columns
## Presolve time: 0.14s
## Presolved: 1066 rows, 1141 columns, 5541 nonzeros
## Variable types: 0 continuous, 1141 integer (1141 binary)
## Found heuristic solution: objective 19.0000000
## Found heuristic solution: objective 18.0000000
## Presolved: 1066 rows, 1141 columns, 5541 nonzeros
##
## Presolve removed 1066 rows and 1141 columns
##
## Root relaxation: objective 4.422638e+00, 738 iterations, 0.04 seconds
##
##     Nodes    |    Current Node    |     Objective Bounds      |     Work
```

```
##   Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0    4.42264    0    43   18.00000    4.42264  75.4%     -    0s
## H    0     0                         5.0000000    4.42264  11.5%     -    0s
##
## Explored 0 nodes (738 simplex iterations) in 0.21 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.000000000000e+00, gap 0.0%
## species = 0; space = 0; tss = 84916.6; spaceheld = 11791.3; prop = 0.861143
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
##   Matrix range    [5e-02, 1e+03]
##   Objective range [1e+00, 1e+00]
##   Bounds range    [1e+00, 1e+00]
##   RHS range       [1e+00, 2e+02]
## Presolve removed 223 rows and 123 columns
## Presolve time: 0.15s
## Presolved: 1079 rows, 1152 columns, 5990 nonzeros
## Variable types: 0 continuous, 1152 integer (1152 binary)
## Found heuristic solution: objective 18.0000000
## Presolved: 1079 rows, 1152 columns, 5990 nonzeros
##
## Presolve removed 1079 rows and 1152 columns
##
## Root relaxation: objective 4.300502e+00, 706 iterations, 0.04 seconds
##
##      Nodes    |    Current Node    |     Objective Bounds      |     Work
##   Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0    4.30050    0    70   18.00000    4.30050  76.1%     -    0s
## H    0     0                         5.0000000    4.30050  14.0%     -    0s
##
## Explored 0 nodes (706 simplex iterations) in 0.23 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.000000000000e+00, gap 0.0%
## species = 0; space = 0; tss = 1279.62; spaceheld = 159.335; prop = 0.875483
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
##   Matrix range    [7e-05, 2e+00]
##   Objective range [1e+00, 1e+00]
##   Bounds range    [1e+00, 1e+00]
##   RHS range       [3e-01, 3e+00]
## Presolve removed 230 rows and 134 columns
## Presolve time: 0.14s
```

```
## Presolved: 1072 rows, 1141 columns, 5485 nonzeros
## Variable types: 0 continuous, 1141 integer (1141 binary)
## Found heuristic solution: objective 19.0000000
## Presolve removed 3 rows and 0 columns
## Presolved: 1069 rows, 1141 columns, 5465 nonzeros
##
## Presolve removed 1042 rows and 626 columns
##
## Root relaxation: objective 4.428373e+00, 571 iterations, 0.04 seconds
##
##      Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0    4.42837    0   43   19.00000    4.42837  76.7%     -    0s
## H    0     0                         5.0000000    4.42837  11.4%     -    0s
##
## Explored 0 nodes (571 simplex iterations) in 0.22 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.000000000000e+00, gap 0.0%
## species = 0; space = 0; tss = 2.11471; spaceheld = 0.294522; prop = 0.860727
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
##   Matrix range     [3e-01, 5e+04]
##   Objective range  [1e+00, 1e+00]
##   Bounds range     [1e+00, 1e+00]
##   RHS range        [1e+00, 9e+03]
## Presolve removed 415 rows and 381 columns
## Presolve time: 0.12s
## Presolved: 887 rows, 894 columns, 6274 nonzeros
## Variable types: 0 continuous, 894 integer (894 binary)
## Found heuristic solution: objective 21.0000000
## Presolve removed 13 rows and 0 columns
## Presolved: 874 rows, 894 columns, 6203 nonzeros
##
## Presolve removed 874 rows and 894 columns
##
## Root relaxation: objective 9.752283e+00, 244 iterations, 0.03 seconds
##
##      Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0    9.75228    0   23   21.00000    9.75228  53.6%     -    0s
## H    0     0                        10.0000000    9.75228  2.48%     -    0s
##
## Explored 0 nodes (244 simplex iterations) in 0.18 seconds
## Thread count was 1 (of 2 available processors)
```

```
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 1.000000000000e+01, best bound 1.000000000000e+01, gap 0.0%
## species = 0; space = 0; tss = 60475.3; spaceheld = 8960.37; prop = 0.851834
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
##    Matrix range     [3e-05, 1e+00]
##    Objective range [1e+00, 1e+00]
##    Bounds range     [1e+00, 1e+00]
##    RHS range        [1e-01, 3e+00]
## Presolve removed 207 rows and 134 columns
## Presolve time: 0.18s
## Presolved: 1095 rows, 1141 columns, 5597 nonzeros
## Variable types: 0 continuous, 1141 integer (1141 binary)
## Found heuristic solution: objective 19.0000000
## Presolve removed 13 rows and 0 columns
## Presolved: 1082 rows, 1141 columns, 5516 nonzeros
##
## Presolve removed 833 rows and 282 columns
##
## Root relaxation: objective 4.429824e+00, 591 iterations, 0.04 seconds
##
##     Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl | Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##     0     0    4.42982    0    43   19.00000    4.42982  76.7%     -    0s
## H   0     0                       17.0000000    4.42982  73.9%     -    0s
## H   0     0                        5.0000000    4.42982  11.4%     -    0s
##
## Explored 0 nodes (591 simplex iterations) in 0.27 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.000000000000e+00, gap 0.0%
## species = 0; space = 0; tss = 0.931362; spaceheld = 0.129782; prop = 0.860654
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
##    Matrix range     [8e-06, 1e+00]
##    Objective range [1e+00, 1e+00]
##    Bounds range     [1e+00, 1e+00]
##    RHS range        [3e-02, 3e+00]
## Presolve removed 184 rows and 134 columns
## Presolve time: 0.21s
## Presolved: 1118 rows, 1141 columns, 5819 nonzeros
## Variable types: 0 continuous, 1141 integer (1141 binary)
## Found heuristic solution: objective 19.0000000
## Presolve removed 16 rows and 0 columns
## Presolved: 1102 rows, 1141 columns, 5735 nonzeros
```

```
##
## Presolve removed 443 rows and 91 columns
##
## Root relaxation: objective 4.432050e+00, 692 iterations, 0.05 seconds
##
##      Nodes     |    Current Node    |     Objective Bounds      |     Work
##   Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0    4.43205    0    43   19.00000    4.43205  76.7%     -    0s
## H    0     0                         5.0000000    4.43205  11.4%     -    0s
##
## Explored 0 nodes (692 simplex iterations) in 0.30 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.000000000000e+00, gap 0.0%
## species = 0; space = 0; tss = 0.232971; spaceheld = 0.0285369; prop = 0.877509
```

Now, let's plot the solutions to see how they differ.

```
# set plotting window
par(mfrow=c(3,3), mar=c(0, 0, 4.1, 0))

## create plots showing the selected planning units (dark green)
for (i in seq_along(solutions)) {
    # plot i'th solution
    plot(
        sim_pus,
        main=dist.metrics[i],
        col=replace(
            rep('#ccece6',nrow(sim_pus@data)),
            which(selections(solutions[[i]])==1),
            '#00441b'
        ),
        axes=FALSE
    )
}

# reset plotting window
par(mfrow=c(1,1), mar=c(5.1, 4.1, 4.1, 2.1))
```
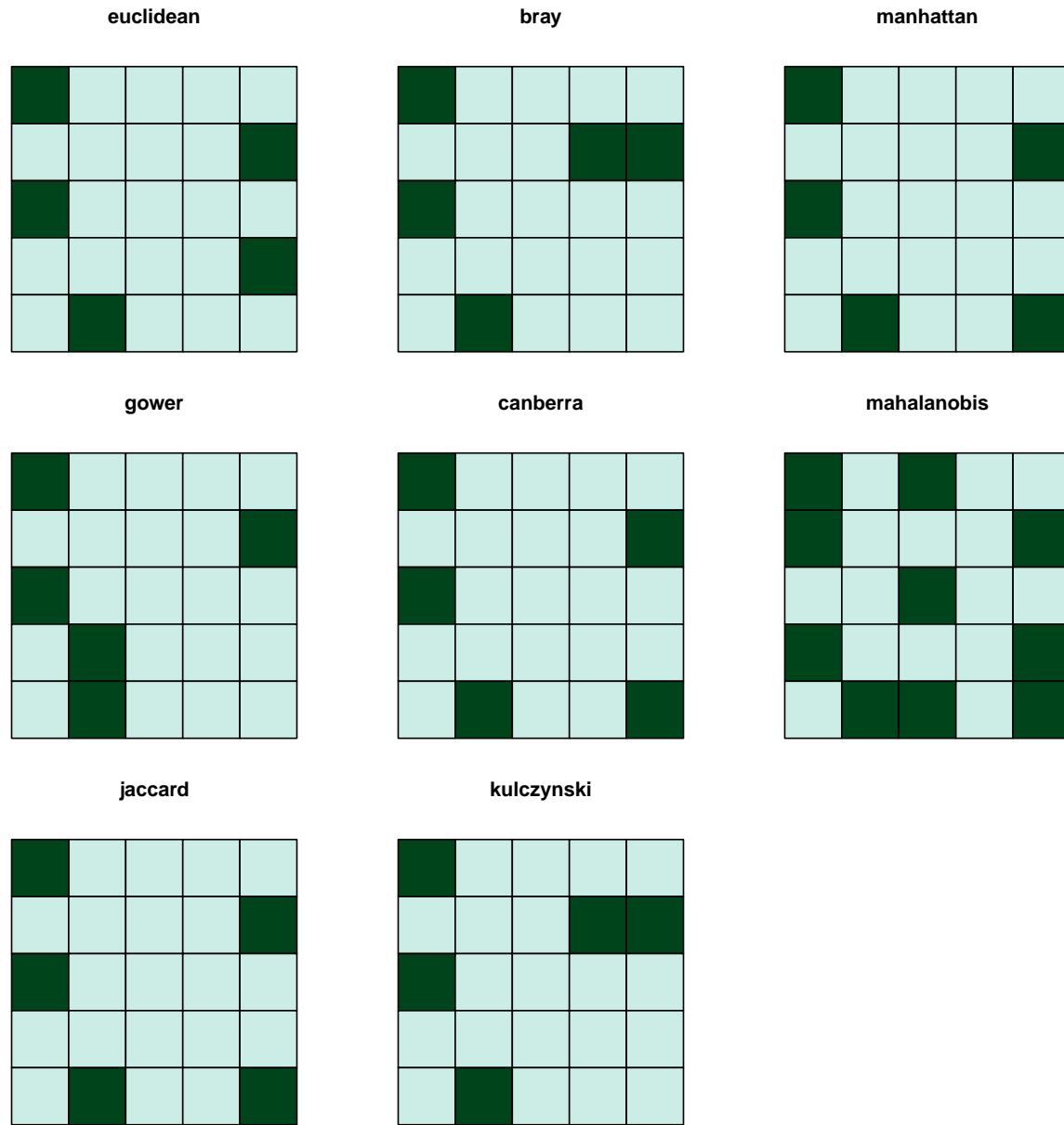
Figure 23 Prioritisations generated using different distance metrics. See Figure 12 for conventions.

It appears that main difference between the solutions is which planning units get selected in the bottom section of the study area. Some solutions tend to select a lot of planning units in this region (eg. Euclidean, Gower, and Manhattan), whereas others select fewer planning units (eg. Bray-Curtis, Jaccard, and Kulczynski). Conservation planners should think carefully which distance metric is most appropriate for their attribute spaces. See the discussion section below for guidelines on selecting an appropriate distance metric.

Case-study examples

Overview

Here we will investigate how space-based targets can affect prioritisations using a more realistic dataset. We will generate prioritisations for the four bird species– blue-winged kookaburra, brown-backed honeyeater, brown falcon, pale-headed rosella–in Queensland, Australia. This region contains a broad range of different habitats–such as rainforests, woodlands, and deserts–making it ideal for this tutorial. First, we will generate a typical amount-based prioritisation that aims to capture 20% of the species' distributions. Then we will generate a prioritisation that also aims to secure populations in representative parts of the species' distributions in terms of their geographic location and their environmental heterogeneity. To do this we will generate a prioritisation using 20% amount-based targets and 85% space-based targets. Finally, we will compare these prioritisations to Australia's existing protected network.

Data

Survey data for the species were obtained from BirdLife Australia. The survey data was rarefied using a 100km^2 grid, wherein the survey with the greatest number of repeat visits in each grid cell was chosen. To model the distribution of each species, environmental data were obtained at survey location (site). Specifically, climatic data (bio1, bio4, bio15, bio16, bio17) and classifications of the vegetation at the site were used. Occupancy-detection models (MacKenzie *et al.* 2002) were fit using Stan (Stan Development Team 2015) using manually tuned parameters (adapt deta=0.9, maximum treedepth=20, chains=4 , warmup iterations=1000, total iterations=1500) with five-fold cross-validation. In each replicate, data were partitioned into training and test sites. A full model was fit using quadratic terms for environmental variables in the site-component, and an intercept in the detection-component of the model. The full model was then subject to a step-wise backwards term deletion routine. Terms were retained when their inclusion resulted in a model with a greater area under the curve (AUC) value as calculated using the test data. Maps were generated for each species as an average of the predictions from the best model in each best replicate. To further improve the accuracy of these maps, areas well outside of the species' known distributions were set to 0. For each species, this was achieved by masking out biogeographic regions where the species was not observed, and regions that did not have a neighbouring planning unit where the species was observed. The maps were then resampled (10km^2 resolution) and cropped to the study area. The resulting maps are stored in the `cs_spp` object.

```
# load data
data(cs_spp)

# plot species' distributions
plot(cs_spp, main=c(
    "Blue-winged kookaburra", "Brown-backed honeyeater",
    "Brown falcon", "Pale-headed rosella"
))
```
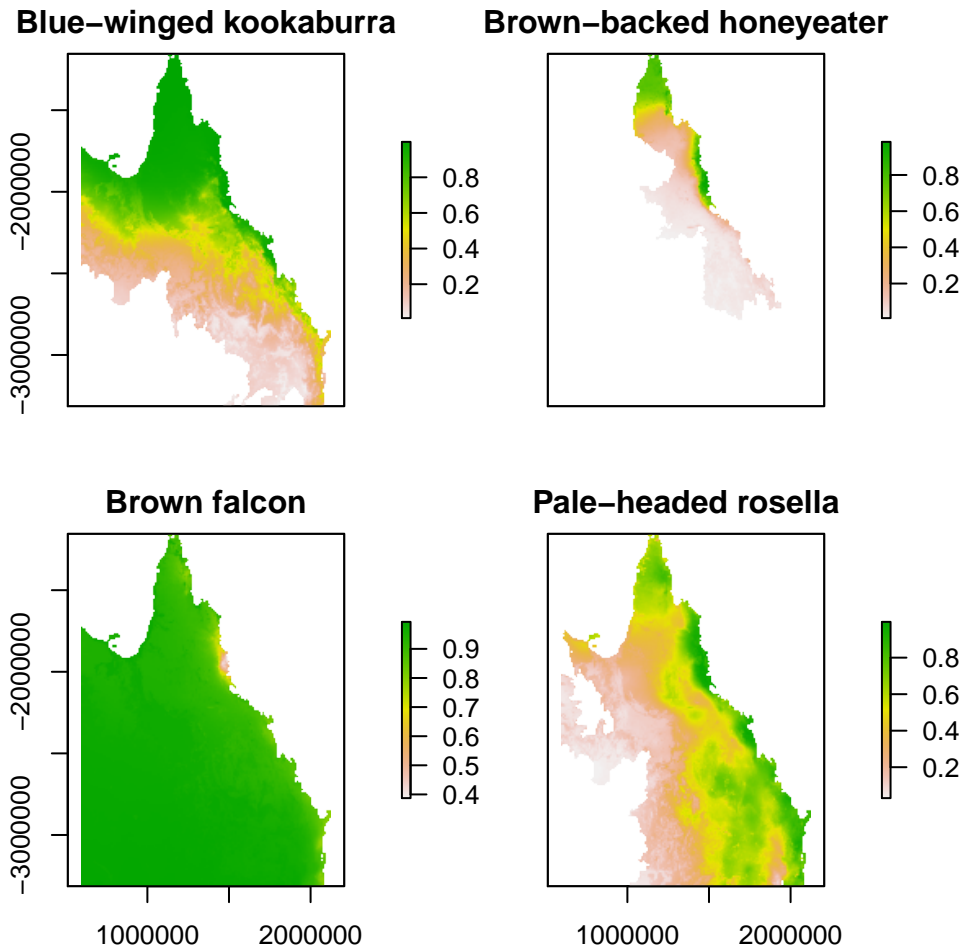
Figure 24 Distribution map for four Australian bird species. Pixel colours denote probability of occupancy.

Planning units (50km^2 resolution) were generated across Australia, and then clipped to the Queensland state borders and coastline. **Note that we are using excessively coarse planning units so that our examples will complete relatively quickly. In a real-world planning exercise, we would use much finer planning units.** To compare our prioritisations to Queensland's existing protected area network, this network was intersected with the planning units. Planning units with more than 50% of their area inside a protected area had their status set to 2 (following conventions in Marxan). Since we do not have cost data, the prioritisations will aim to select the minimum number of planning units required to meet the targets. The planning units are stored in the `cs_pu` object.

```
# load data
data(cs_pus)

## plot planning units
# convert SpatialPolygons to PolySet for quick plotting
cs_pus2 <- SpatialPolygons2PolySet(cs_pus)

# create vector of colours for planning units
```

```r
# + light green: units not already inside reserve
# + yellow: units already inside reserve
cs_pus_cols <- rep('#c7e9c0', nrow(cs_pus@data))
cs_pus_cols[which(cs_pus$status==2)] <- 'yellow'

# set plotting window
par(mar=c(0.1, 0.1, 4.1, 0.1))

# plot polygons
PBSmapping::plotPolys(
    cs_pus2, col=cs_pus_cols, border='gray30',
    xlab='', ylab='', axes=FALSE,
    main='Case-study planning units'
)
```
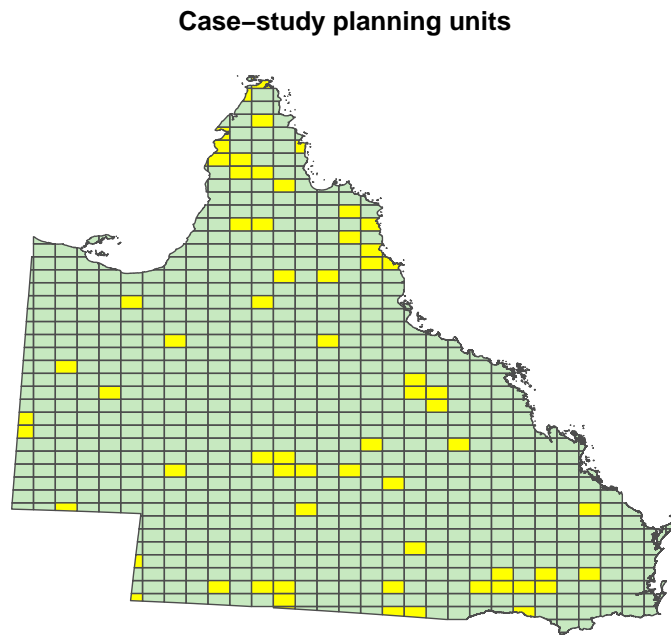
Case–study planning units

Figure 25 Planning units for the case-study examples. Yellow polygons represent planning units with more then 50% of their area already in existing reserves.

```r
# reset plotting window
par(mar=c(5.1, 4.1, 4.1, 2.1))
```

To map the distribution of environmental conditions across the species' range, 21 bioclimatic layers were obtained. These layers were cropped to Australia and subject to detrended correspondence analysis to produce two new variables. These layers are stored in the cs_space object.

```r
# load data
data(cs_space)

# plot variables
plot(cs_space, main=c('DC1', 'DC2'))
```
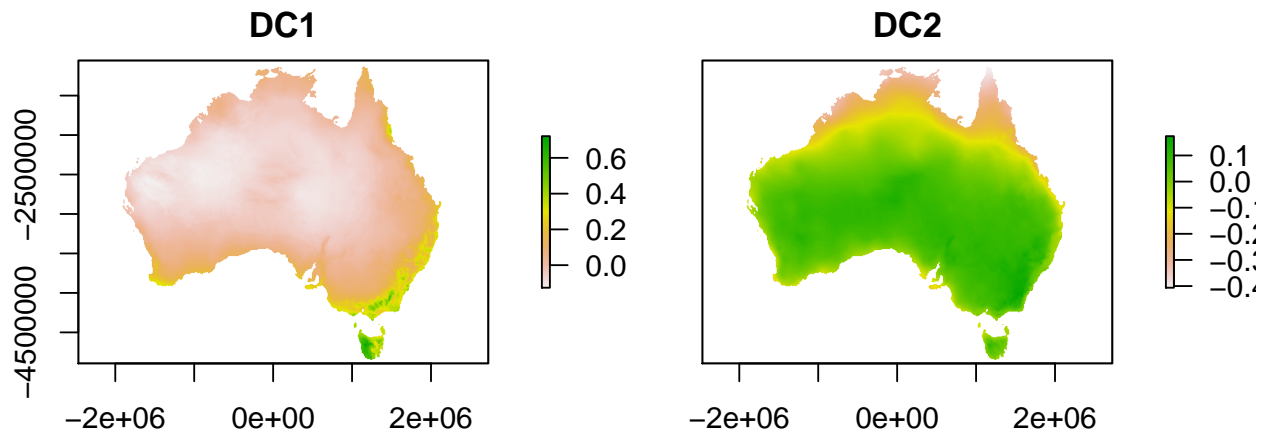

Figure 26 Broad-scale environmental variation across Australia. The variable DC1 describes the transition from wet and cool to dry and hot conditions. The variable DC2 describes the transition from wet and hot to dry and cool conditions.

Effectiveness of Australia's reserve network compared to optimal prioritisations

To simplify the process of formatting data and generating prioritisations, we can use the `rap` function. First, we will generate an amount-based prioritisation that aims to capture 20% of the rosella's range. We will use 50 demand points to map the geographic and environmental spaces. **Be warned, the examples hereafter can take 5-10 minutes to run.**

```r
# make amount-based prioritisation,
# and ignore existing protected areas by discarding values in the
# status (third) column of the attribute table
cs_rs_amount <- rap(
    cs_pus[,-2], cs_spp, cs_space,
  amount.target=0.2, space.target=NA, n.demand.points=50L,
  include.geographic.space=TRUE, formulation='unreliable',
  solve=FALSE
)
```

```
## Warning in (function (pus, species, spaces = NULL, amount.target = 0.2, :
## argument to pus does not have a 'status' column, creating default with all
## status=0L
```

```r
# threshold probabilities to 0.1 for space calculations
cs_rs_amount <- prob.subset(cs_rs_amount, species=1:4, threshold=rep(0.1,4))
```

```r
# generate prioritisation
cs_rs_amount <- solve(cs_rs_amount)
```

```
## Optimize a model with 4 rows, 762 columns and 2001 nonzeros
## Coefficient statistics:
##   Matrix range    [3e+02, 2e+04]
##   Objective range [1e+00, 1e+00]
##   Bounds range    [1e+00, 1e+00]
##   RHS range       [2e+05, 3e+06]
## Found heuristic solution: objective 176
## Presolve time: 0.01s
## Presolved: 4 rows, 762 columns, 2001 nonzeros
## Variable types: 0 continuous, 762 integer (762 binary)
## Presolved: 4 rows, 762 columns, 2001 nonzeros
##
##
## Root relaxation: objective 1.359167e+02, 832 iterations, 0.01 seconds
##
##      Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0  135.91668    0     4  176.00000  135.91668  22.8%     -    0s
## H    0     0                       136.0000000  135.91668  0.06%     -    0s
##
## Explored 0 nodes (832 simplex iterations) in 0.03 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 1.360000000000e+02, best bound 1.360000000000e+02, gap 0.0%
## species = 0; space = 0; tss = 0.00515932; spaceheld = 0.00153775; prop = 0.701946
## species = 0; space = 1; tss = 0.706739; spaceheld = 0.316627; prop = 0.551988
## species = 1; space = 0; tss = 0.0183623; spaceheld = 0.0152704; prop = 0.16838
## species = 1; space = 1; tss = 0.767747; spaceheld = 1.57318; prop = -1.04909
## species = 2; space = 0; tss = 0.0719167; spaceheld = 0.000755429; prop = 0.989496
## species = 2; space = 1; tss = 0.664411; spaceheld = 0.0931804; prop = 0.859755
## species = 3; space = 0; tss = 0.0226796; spaceheld = 0.000790625; prop = 0.965139
## species = 3; space = 1; tss = 0.596714; spaceheld = 0.0853009; prop = 0.857049
```

```
## Warning in validityMethod(object): object@space.held contains values less
## than 0, some species are really poorly represented
```

```r
# show summary
summary(cs_rs_amount)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL   136  136            136           98882414
```

```
##    Connectivity_In Connectivity_Edge Connectivity_Out
## 1         9636021         81120163         8126230
##    Connectivity_In_Fraction
## 1               0.09744929
```

```
# plot prioritisation
plot(cs_rs_amount, 1)
```
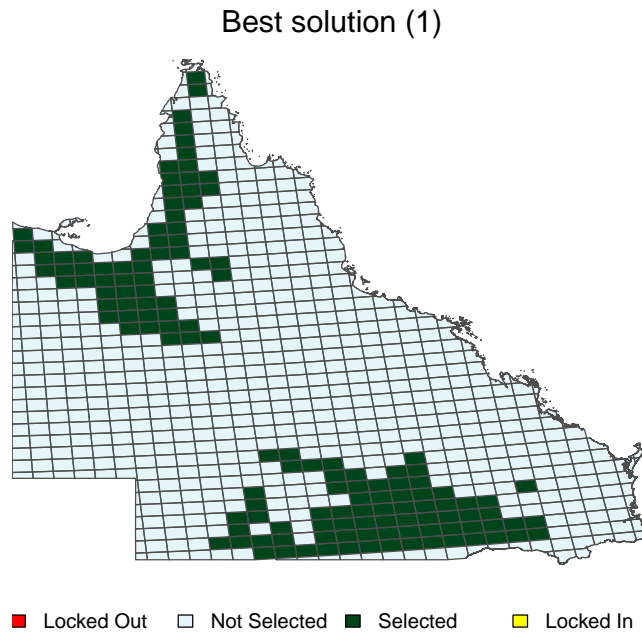
Best solution (1)

Figure 27 Multi-species prioritisation generated for four bird species using amount-based targets (20%). See Figure 12 captions for conventions.

We can also see how well the prioritisation secures the species' distributions in the geographic and environmental attribute spaces.

```
# plot prioritisation in geographic attribute space
p1 <- space.plot(cs_rs_amount, 1, 2, main='Blue-winged kookaburra')
p2 <- space.plot(cs_rs_amount, 2, 2, main='Brown-backed honeyeater')
p3 <- space.plot(cs_rs_amount, 3, 2, main='Brown falcon')
p4 <- space.plot(cs_rs_amount, 4, 2, main='Pale-headed rosella')
gridExtra::grid.arrange(p1, p2, p3, p4, ncol=2)
```
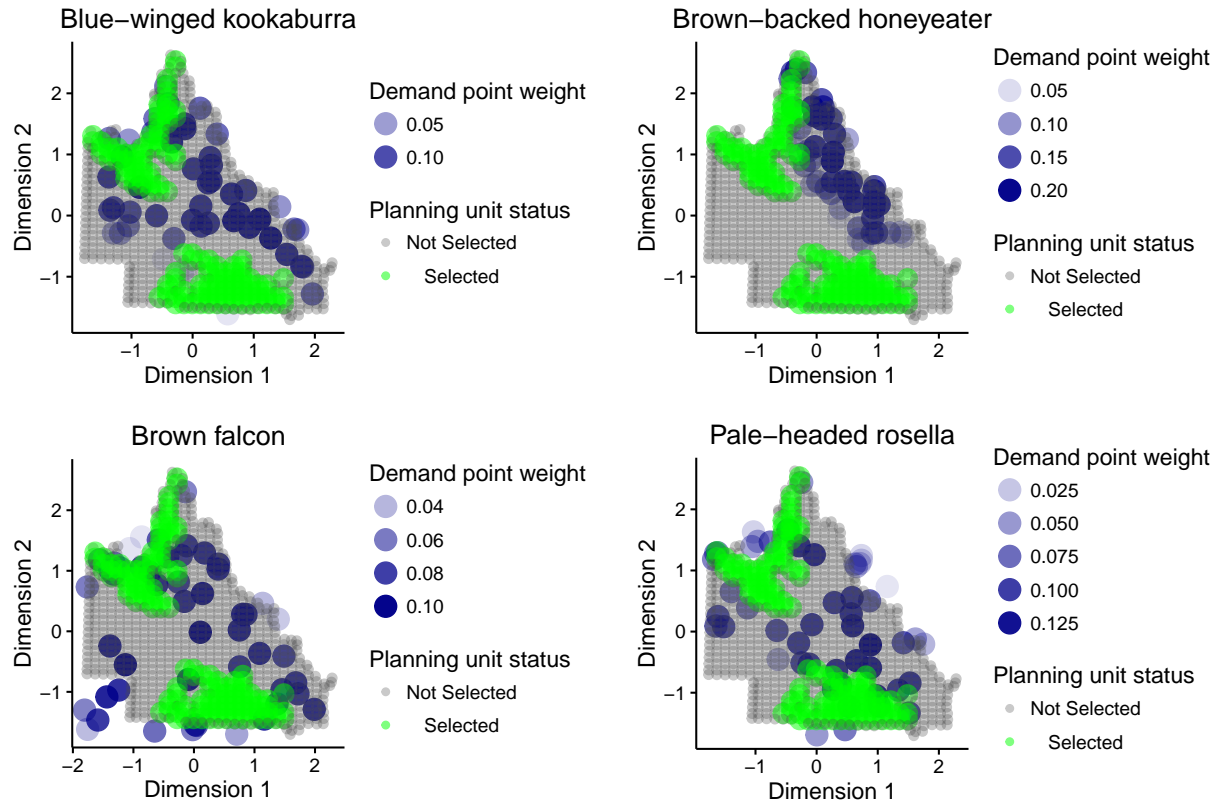
Figure 28 Distribution of amount-based prioritisation in the geographic attribute space. Points denote combinations of environmental conditions. Green and grey points represent planning unit selected for and not selected for prioritisation (respectively). Blue points denote demand points, and their size indicates their weighting.

```r
# plot prioritisation in environmental attribute space
p1 <- space.plot(cs_rs_amount, 1, 1, main='Blue-winged kookaburra')
p2 <- space.plot(cs_rs_amount, 2, 1, main='Brown-backed honeyeater')
p3 <- space.plot(cs_rs_amount, 3, 1, main='Brown falcon')
p4 <- space.plot(cs_rs_amount, 4, 1, main='Pale-headed rosella')
gridExtra::grid.arrange(p1, p2, p3, p4, ncol=2)
```
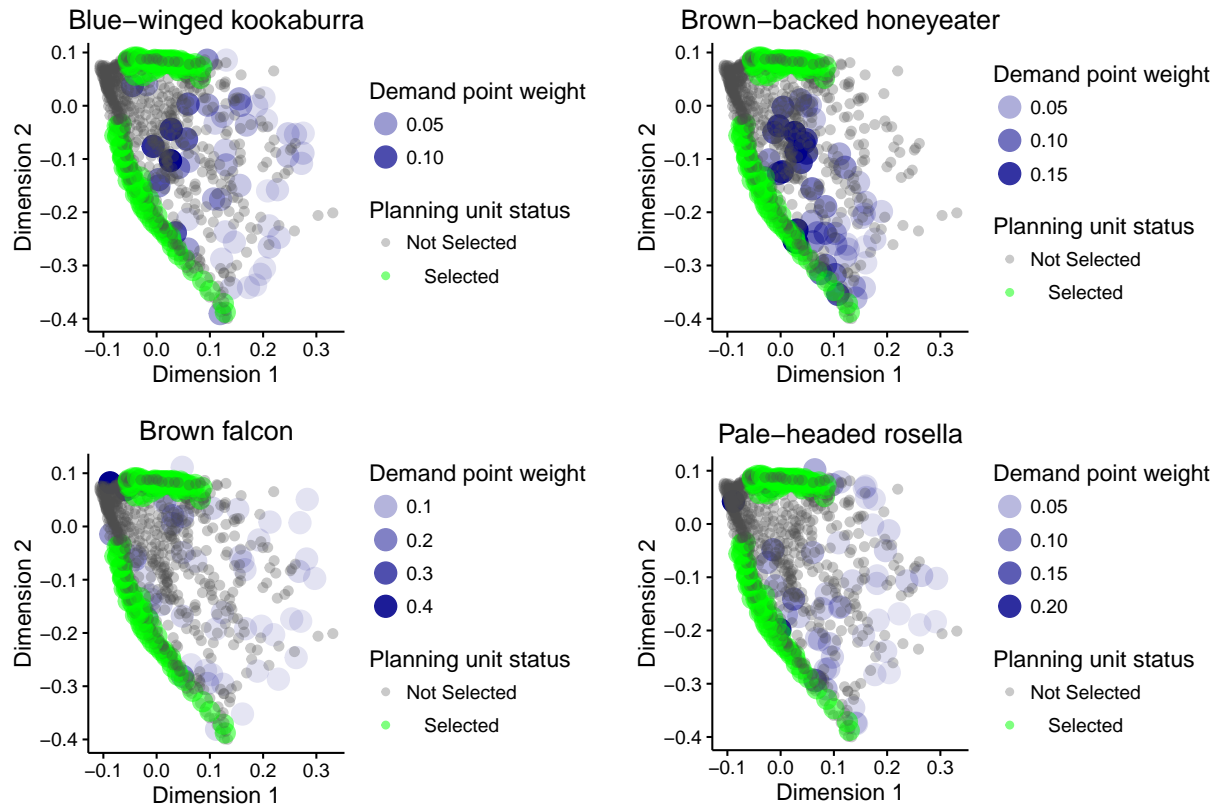
Figure 29 Distribution of amount-based prioritisation in the environmental attribute space. See Figure 28 caption for conventions.

Next, let's generate a prioritisation using amount- and space-based targets. This prioritisation will secure 50% of the species distribution in geographic and environmental space.

```
# make amount- and space-based prioritisation
cs_rs_space <- update(cs_rs_amount, space.target=0.5)
```

```
## Optimize a model with 200512 rows, 200862 columns and 802401 nonzeros
## Coefficient statistics:
##   Matrix range     [2e-11, 2e+04]
##   Objective range  [1e+00, 1e+00]
##   Bounds range     [1e+00, 1e+00]
##   RHS range        [3e-03, 3e+06]
## Warning: Model contains large matrix coefficient range
##          Consider reformulating model or setting NumericFocus parameter
##          to avoid numerical issues.
## Presolve removed 525 rows and 493 columns (presolve time = 5s) ...
## Presolve removed 566 rows and 493 columns (presolve time = 10s) ...
## Presolve removed 629 rows and 493 columns (presolve time = 15s) ...
## Presolve removed 657 rows and 493 columns (presolve time = 20s) ...
## Presolve removed 736 rows and 493 columns (presolve time = 25s) ...
```

```
## Presolve removed 786 rows and 493 columns (presolve time = 30s) ...
## Presolve removed 819 rows and 529 columns (presolve time = 35s) ...
## Presolve removed 819 rows and 529 columns (presolve time = 40s) ...
## Presolve removed 893 rows and 529 columns (presolve time = 45s) ...
## Presolve removed 893 rows and 529 columns (presolve time = 50s) ...
## Presolve removed 893 rows and 529 columns (presolve time = 55s) ...
## Presolve removed 893 rows and 529 columns (presolve time = 60s) ...
## Presolve removed 893 rows and 529 columns (presolve time = 65s) ...
## Presolve removed 916 rows and 529 columns (presolve time = 70s) ...
## Presolve removed 937 rows and 529 columns (presolve time = 75s) ...
## Presolve removed 937 rows and 529 columns (presolve time = 80s) ...
## Presolve removed 937 rows and 529 columns (presolve time = 85s) ...
## Presolve removed 1048 rows and 529 columns (presolve time = 90s) ...
## Presolve removed 1083 rows and 529 columns (presolve time = 95s) ...
## Presolve removed 1114 rows and 529 columns (presolve time = 100s) ...
## Presolve removed 1147 rows and 529 columns (presolve time = 105s) ...
## Presolve removed 1147 rows and 529 columns (presolve time = 110s) ...
## Presolve removed 1153 rows and 529 columns (presolve time = 115s) ...
## Presolve removed 1153 rows and 529 columns (presolve time = 120s) ...
## Presolve removed 1179 rows and 529 columns (presolve time = 125s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 130s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 135s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 141s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 145s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 150s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 155s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 160s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 165s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 170s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 175s) ...
## Presolve removed 1191 rows and 967 columns (presolve time = 180s) ...
## Presolve removed 1191 rows and 967 columns (presolve time = 185s) ...
## Presolve removed 1191 rows and 967 columns (presolve time = 190s) ...
## Presolve removed 1191 rows and 967 columns (presolve time = 195s) ...
## Presolve removed 1591 rows and 967 columns (presolve time = 200s) ...
## Presolve removed 1672 rows and 967 columns (presolve time = 205s) ...
## Presolve removed 1729 rows and 967 columns (presolve time = 210s) ...
## Presolve removed 1765 rows and 967 columns (presolve time = 215s) ...
## Presolve removed 1789 rows and 967 columns (presolve time = 220s) ...
## Presolve removed 1806 rows and 967 columns (presolve time = 225s) ...
## Presolve removed 1806 rows and 967 columns (presolve time = 230s) ...
## Presolve removed 1806 rows and 967 columns (presolve time = 235s) ...
## Presolve removed 1806 rows and 967 columns (presolve time = 240s) ...
## Presolve removed 1806 rows and 967 columns (presolve time = 245s) ...
## Presolve removed 1806 rows and 967 columns
## Presolve time: 247.59s
## Presolved: 198706 rows, 199895 columns, 802062 nonzeros
## Variable types: 0 continuous, 199895 integer (199895 binary)
```
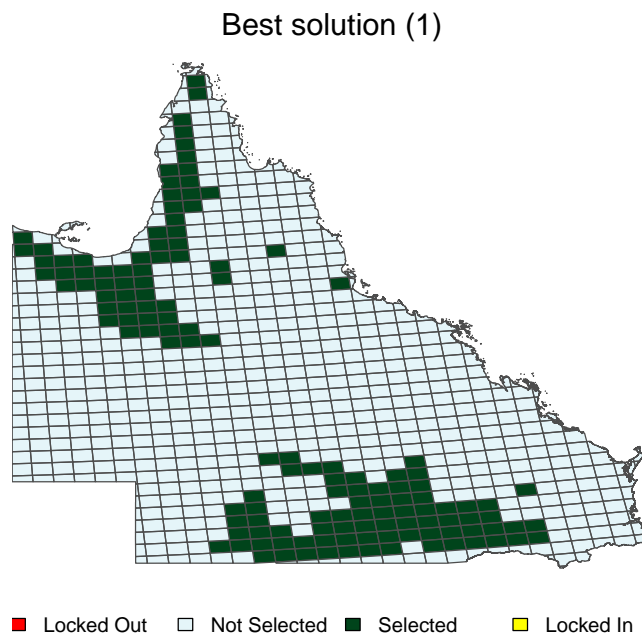
```
## Found heuristic solution: objective 236.0000000
## Presolve removed 246 rows and 0 columns (presolve time = 5s) ...
## Presolve removed 246 rows and 0 columns (presolve time = 10s) ...
## Presolve removed 248 rows and 0 columns (presolve time = 15s) ...
## Presolve removed 248 rows and 0 columns (presolve time = 20s) ...
## Presolve removed 248 rows and 0 columns
## Presolved: 198458 rows, 199895 columns, 801255 nonzeros
##
## Presolve removed 195493 rows and 9695 columns
##
## Root simplex log...
##
## Iteration    Objective      Primal Inf.    Dual Inf.      Time
##         0   0.0000000e+00   4.676020e+01   1.178365e+10    273s
##      5605   1.4004883e+02   0.000000e+00   1.101189e+03    275s
##      9980   1.3816674e+02   0.000000e+00   1.514380e+03    280s
##     14356   1.3756833e+02   0.000000e+00   5.895636e+03    285s
##     18487   1.3712582e+02   0.000000e+00   1.094329e+03    290s
##     23833   1.3703648e+02   0.000000e+00   5.514256e+03    295s
##     26750   1.3639401e+02   0.000000e+00   2.275635e+03    300s
##     31610   1.3608397e+02   0.000000e+00   1.250252e+02    305s
##     36470   1.3602867e+02   0.000000e+00   7.913232e+01    310s
##     40115   1.3599519e+02   0.000000e+00   1.925269e+00    315s
##     41032   1.3599204e+02   0.000000e+00   0.000000e+00    317s
##     41032   1.3599204e+02   0.000000e+00   0.000000e+00    318s
##
## Root relaxation: objective 1.359920e+02, 41032 iterations, 66.64 seconds
## Total elapsed time = 321.34s
##
##     Nodes    |    Current Node    |     Objective Bounds      |     Work
##  Expl Unexpl |  Obj  Depth IntInf | Incumbent    BestBd   Gap | It/Node Time
##
##      0     0  135.99204    0  189  236.00000  135.99204  42.4%     -  321s
## H    0     0                      137.0000000  135.99204  0.74%     -  323s
##
## Explored 0 nodes (53801 simplex iterations) in 323.66 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 1.370000000000e+02, best bound 1.360000000000e+02, gap 0.7299%
## species = 0; space = 0; tss = 0.00515932; spaceheld = 0.00128162; prop = 0.751592
## species = 0; space = 1; tss = 0.706739; spaceheld = 0.257508; prop = 0.635639
## species = 1; space = 0; tss = 0.0183623; spaceheld = 0.00852419; prop = 0.535778
## species = 1; space = 1; tss = 0.767747; spaceheld = 0.299352; prop = 0.610091
## species = 2; space = 0; tss = 0.0719167; spaceheld = 0.00060543; prop = 0.991582
## species = 2; space = 1; tss = 0.664411; spaceheld = 0.0707986; prop = 0.893441
## species = 3; space = 0; tss = 0.0226796; spaceheld = 0.000605414; prop = 0.973306
## species = 3; space = 1; tss = 0.596714; spaceheld = 0.0485819; prop = 0.918584
```

```r
# show summary
summary(cs_rs_space)
```

```
##   Run_Number  Status Score Cost Planning_Units Connectivity_Total
## 1          1 OPTIMAL   137  137            137           98882414
##   Connectivity_In Connectivity_Edge Connectivity_Out
## 1         9738090          80918598          8225726
##   Connectivity_In_Fraction
## 1                0.09848151
```

```r
# plot prioritisation
plot(cs_rs_space,1)
```

Best solution (1)

| ■ Locked Out | ☐ Not Selected | ■ Selected | ☐ Locked In |

```r
# plot prioritisation in geographic attribute space
p1 <- space.plot(cs_rs_space, 1, 2, main='Blue-winged kookaburra')
p2 <- space.plot(cs_rs_space, 2, 2, main='Brown-backed honeyeater')
p3 <- space.plot(cs_rs_space, 3, 2, main='Brown falcon')
p4 <- space.plot(cs_rs_space, 4, 2, main='Pale-headed rosella')
gridExtra::grid.arrange(p1, p2, p3, p4, ncol=2)
```
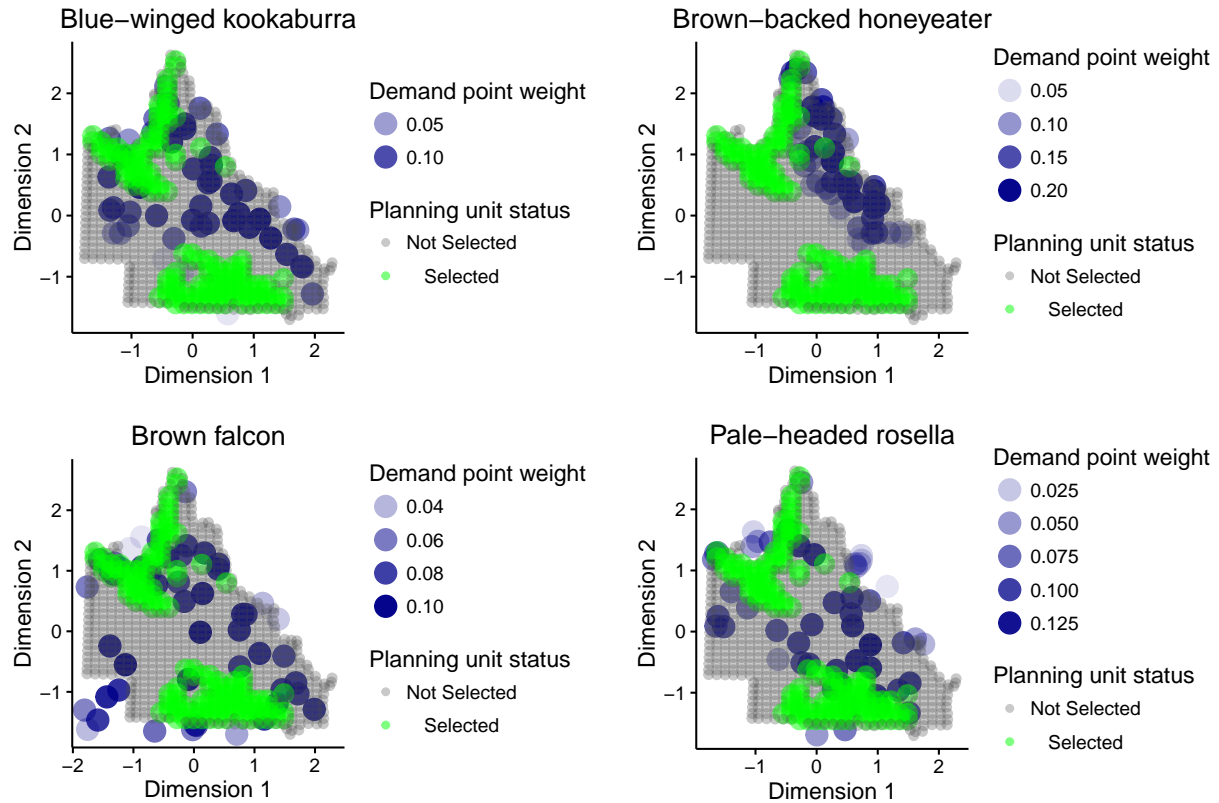
Figure 30 Distribution of the amount- and space-based prioritisation in the geographic attribute space. See Figure 28 caption for conventions.

```r
# plot prioritisation in environmental attribute space
p1 <- space.plot(cs_rs_space, 1, 1, main='Blue-winged kookaburra')
p2 <- space.plot(cs_rs_space, 2, 1, main='Brown-backed honeyeater')
p3 <- space.plot(cs_rs_space, 3, 1, main='Brown falcon')
p4 <- space.plot(cs_rs_space, 4, 1, main='Pale-headed rosella')
gridExtra::grid.arrange(p1, p2, p3, p4, ncol=2)
```
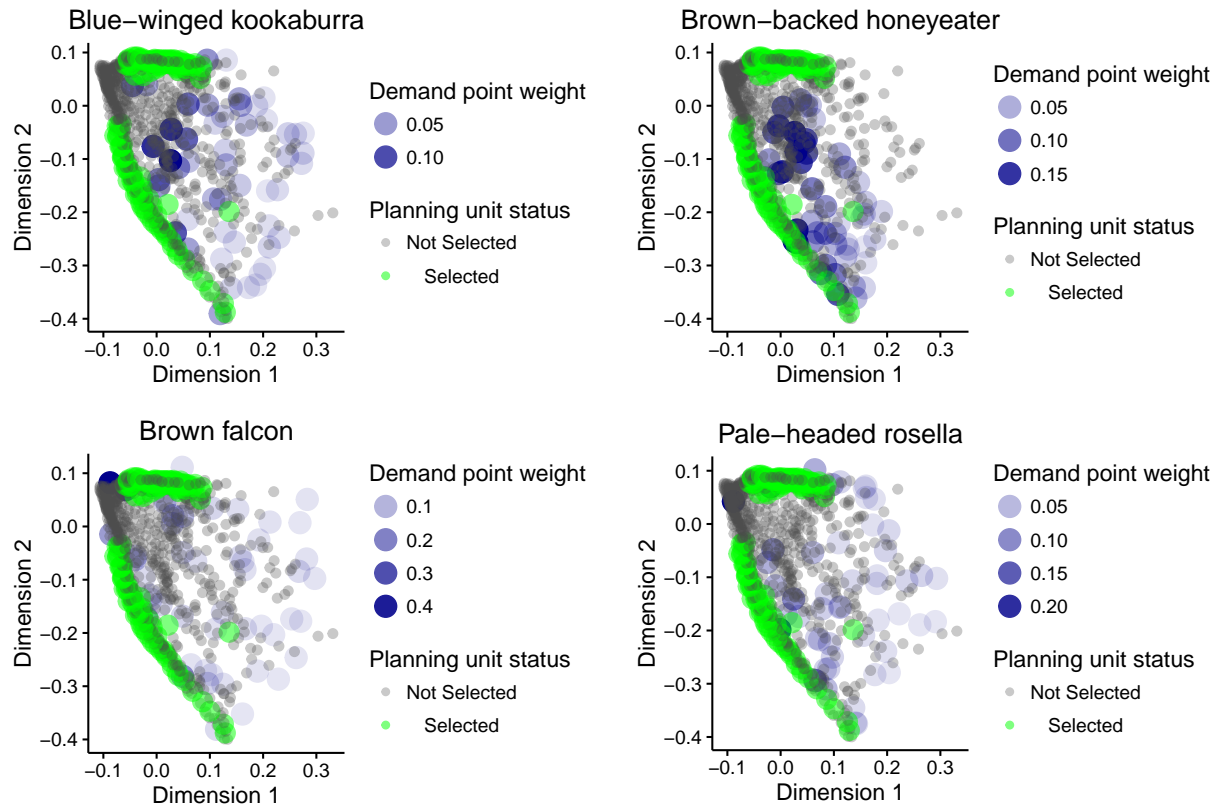
Figure 31 Distribution of the amount- and space-based prioritisation in the environmental attribute space. See Figure 28 caption for conventions.

Let's compare these prioritisations with Queensland's existing protected areas system. To do this, we can create update the `cs_rs_space` with manually specified solutions to create a `RapSolved` object to represent the Queensland's reserve network.

```r
# generate vector with Australia's selections
aus_selections <- which(cs_pus$status>0)

# create new object with Australia's network
cs_rs_aus <- update(cs_rs_amount, b=aus_selections)
```

```
## species = 0; space = 0; tss = 0.00515932; spaceheld = 0.000251321; prop = 0.951288
## species = 0; space = 1; tss = 0.706739; spaceheld = 0.0326189; prop = 0.953846
## species = 1; space = 0; tss = 0.0183623; spaceheld = 0.00865658; prop = 0.528567
## species = 1; space = 1; tss = 0.767747; spaceheld = 0.551532; prop = 0.281622
## species = 2; space = 0; tss = 0.0719167; spaceheld = 0.000362644; prop = 0.994957
## species = 2; space = 1; tss = 0.664411; spaceheld = 0.0235315; prop = 0.964583
## species = 3; space = 0; tss = 0.0226796; spaceheld = 0.000291323; prop = 0.987155
## species = 3; space = 1; tss = 0.596714; spaceheld = 0.0304933; prop = 0.948898
```

Now, let's plot the performance metrics for these prioritisations.

```r
# define standard error function
se=function(x){sd(x,na.rm=TRUE)/sqrt(sum(!is.na(x)))}

# create a table to store the values for the 3 prioritisations
cs_results <- data.frame(
    name=rep(rep(c('Amount-based prioritisation',
        'Amount+space-based prioritsation', 'Queensland reserve network'),
        each=4),3),
    variable=rep(c('Amount', 'Geographic space', 'Environmental space'), each=12),
    species=colnames(amount.held(cs_rs_amount)),
    value=c(
        amount.held(cs_rs_amount)[1,], amount.held(cs_rs_space)[1,],
            amount.held(cs_rs_aus)[1,],
        space.held(cs_rs_amount, space=2)[1,], space.held(cs_rs_space, space=2)[1,],
            space.held(cs_rs_aus, space=2)[1,],
        space.held(cs_rs_amount, space=1)[1,], space.held(cs_rs_space, space=1)[1,],
            space.held(cs_rs_aus, space=1)[1,]
    )
) %>% group_by(
    name,
    variable
) %>% summarise(
    mean=mean(value),
    se=se(value)
)


# plot the performance metrics
ggplot(aes(x=variable, y=mean, fill=name), data=cs_results) +
    geom_bar(position=position_dodge(0.9), stat='identity') +
    geom_errorbar(
        aes(ymin=mean-se, ymax=mean+se), position=position_dodge(0.9),
        width=0.2
    ) +
    xlab('Property of species') +
    ylab('Proportion held in\nselected planning units (%)') +
    scale_fill_discrete(
        name=''
    ) +
    theme_classic() +
    theme(legend.position='bottom',legend.direction='horizontal')
```
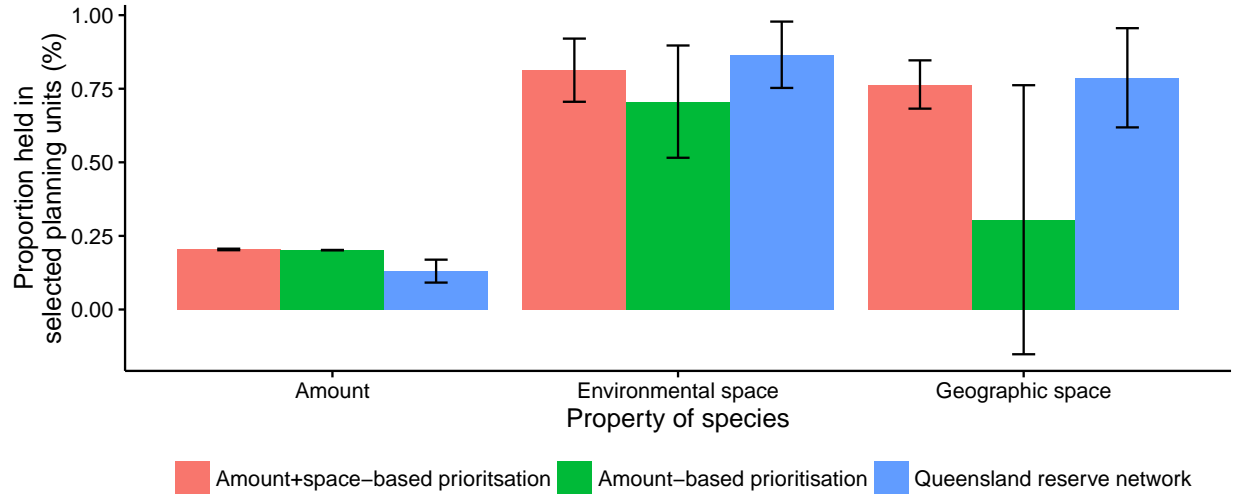
We can see that a greater number of planning units is needed to satisfy the space-based targets. The prioritisation generated using just amount-based targets has 136 planning units, and the prioritisations using amount-based and space-based targets has 137 targets. These results suggest that prioritisations based only on amount-based targets can obtain a moderately representative sample of the species' geographic distribution and climatic niche.

Implications and future directions

The `rapr` R package provides a unified approach to reserve selection. This R package provides a decision maker with the tools to generate prioritisations that secure an adequate amount of a representative sample of biodiversity patterns and processes. Additionally, the decision maker can accommodate uncertainty in the distribution of features, and also identify suitably connected reserves. Both the simulated and case-study species suggest that conservation planning exercises need to explicitly consider biodiversity processes during the reserve selection process.

One of the key advantages of the `rapr` R package is that it is general enough that any spatial variation could be considered an attribute space, regardless of whether this variation is intrinsic or extrinsic to the feature(s). As a consequence, in addition to biodiversity processes, this R package could be used to secure intra-specific (within feature) biodiversity patterns. For example, advances in genomic fields produced high resolution data on genetic information (eg. amplified fragment length polymorphisms (AFLPs), single nucleotide polymorphisms (SNPs)). By using geostatistical analysis (eg. generalised dissimilarity modelling GDMs (Ferrier et al. (2007)); gradients forests (GFs)), this data has been used to generate maps describing the spatial distribution of genomic variation within a species (Thomassen *et al.* 2010; Fitzpatrick and Keller 2015). These maps in turn could be used to construct a genomic attribute space, and in turn, could be used to generate prioritisations that secure a representative sample of genomic variation within a species. However, because the problem formulations used in this package are so general, the tools in this package could be misused, and generate poor quality prioritisations.

The degree to which a prioritisation truly secures a representative sample of a feature depends on the attribute spaces and distribution of demand points chosen by the decision maker. The space-based targets are set as a proportion based on the level of representation if all the planning units are selected, and the worst prioritisation containing only one planning unit. As a consequence,

if the decision maker uses an inappropriate set of spatial variables to construct an attribute space, or an inappropriate set of demand points, then the optimal solution based on this data will not be a cost-effective prioritisation. We therefore stress that decision makers must carefully consider which biodiversity processes need to preserved in the prioritisation, and what spatial data can be used to map these processes. To assist in the selection of appropriate demand points, the R package provides several routines for generating demand points (see the `make.DemandPoints` function). These routines essentially use the distribution of a feature in the attribute space to define a polygon. Demand points are then generated as random points within the polygon. A kernel is then fit to the distribution of the feature in the space (using Blonder *et al.* 2014; Duong 2015), and the demand points are weighted based on the estimated density of the feature at the demand points' coordinates.

The `rapr` R package could be further extended to identify more effective prioritisations. First, the formulation of fragmentation used in this package may be too simplistic in some cases (eg. exercises involving multiple species with different dispersal capabilities), and more realistic measures of fragmentation (eg. those used in Zonation) could be used to identify more effective prioritisations. Second, the problem does not consider temporal dynamics. Here, conservation actions are assumed to be implemented simultaneously in all selected planning units and assumed to remain implemented for all time. As a consequence, this R package is not useful for scenarios where actions are implemented during multiple discrete periods in time (eg. actions are made adue to annual funding cycles), or scenarios involving threatening processes that vary across space and time (reviewed in Pressey *et al.* 2007). Future research may look into incorporating such elements into this R package.

To maximise the long-term persistence of biodiversity–the stated goal of conservation–decision makers need to identify prioritisations that preserve existing patterns of biodiversity and the processes that support them. To achieve this, conservation planners need a decision support tool that can explicitly accommodate biodiversity patterns and processes. Here, we developed the `rapr` R package to fill this void. By exploring the functiontality of this package using several simulated species, we found that including space-based targets can radically change a prioritisation for the simplest of species.

Acknowledgements

References

Ball, I., Possingham, H., Watts, M. E. (2009) Marxan and relatives: software for spatial conservation prioritisation. In: *Spatial conservation prioritisation: Quantitative methods & computational tools* (eds A. Moilanen, K. A. Wilson, & H. Possingham) pp. 185–189 Oxford University Press, Oxford, UK.

Beyer, H. L., Dujardin, Y., Watts, M. (2015) Solving conservation planning problems with integer linear programming. *In prep.*

Blonder, B., Lamanna, C., Violle, C., Enquist, B. J. (2014) The n-dimensional hypervolume. *Global Ecology and Biogeography.* **23**, 595–609.

Carvalho, S. B., Brito, J. C., Crespo, E. J., Possingham, H. P. (2011) Incorporating evolutionary processes into conservation planning using species distribution data: a case study with the western Mediterranean herpetofauna. *Diversity & Distributions*. **17**, 408–421.

Ciarleglio, M., Wesley Barnes, J., Sarkar, S. (2009) ConsNet: new software for the selection of conservation area networks with spatial and multi-criteria analyses. *Ecography*. **32**, 205–209.

Cowling, R. M., Pressey, R. L., Rouget, M., Lombard, A. T. (2003) A conservation plan for a global biodiversity hotspot - the Cape Floristic Region, South Africa. *Biological Conservation*. **112**, 191–216.

Crandall, K. A., Bininda-Emonds, O. R. P., Mace, G. M., Wayne, R. K. (2000) Considering evolutionary processes in conservation biology. *Trends in Ecology & Evolution*. **15**, 290–295.

Cui, T. T., Ouyang, Y. F., Shen, Z. J. M. (2010) Reliable facility location design under the risk of disruptions. *Operations Research*. **58**, 998–1011.

Duong, T. (2015) *ks: Kernel Smoothing.*

Faith, D. P. (2003) Environmental diversity (ED) as surrogate information for species-level biodiversity. *Ecography*. **26**, 374–379.

Faith, D. P., Walker, P. A. (1996) Environmental diversity: on the best-possible use of surrogate data for assessing the relative biodiversity of sets of areas. *Biodiversity & Conservation*. **5**, 399–415.

Faith, D., Minchin, P., Belbin, L. (1987) Compositional dissimilarity as a robust measure of ecological distance. *Vegetatio*. **69**, 57–68.

Fernández, E., Landete, M. (2015) Fixed-Charge Facility Location Problems. In: *Location Science* (eds G. Laporte, S. Nickel, & F. Saldanha da Gama) pp. 47–77 Springer International Publishing.

Ferrier, S., Manion, G., Elith, J., Richardson, K. (2007) Using generalized dissimilarity modelling to analyse and predict patterns of beta diversity in regional biodiversity assessment. *Diversity and Distributions*. **13**, 252–264.

Fitzpatrick, M. C., Keller, S. R. (2015) Ecological genomics meets community-level modelling of biodiversity: mapping the genomic landscape of current and future environmental adaptation. *Ecology Letters*. **18**, 1–16.

Hendry, A. P., Lohmann, L. G., Conti, E., Cracraft, J., Crandall, K. A., Faith, D. P., Hauser, C., Joly, C. A., Kogure, K., Larigauderie, A., Magallon, S., Moritz, C., Tillier, S., Zardoya, R., Prieur-Richard, A. H., Walther, B. A., Yahara, T., Donoghue, M. J. (2010) Evolutionary biology in biodiversity science, conservation, and policy: A call to action. *Evolution*. **64**, 1517–1528.

Hijmans, R. J., Cameron, S. E., Parra, J. L., Jones, P. G., Jarvis, A. (2005) Very high resolution interpolated climate surfaces for global land areas. *International Journal of Climatology*. **25**, 1965–1978.

Kleiman, D. G. (1989) Reintroduction of captive mammals for conservation. *BioScience*. **39**, 152–161.

Klein, C., Wilson, K., Watts, M., Stein, J., Berry, S., Carwardine, J., Smith, M. S., Mackey, B., Possingham, H. (2009) Incorporating ecological and evolutionary processes into continental-scale conservation planning. *Ecological applications*. **19**, 206–217.

MacKenzie, D. I., Nichols, J. D., Lachman, G. B., Droege, S., Andrew Royle, J., Langtimm, C. A. (2002) Estimating site occupancy rates when detection probabilities are less than one. *Ecology*. **83**, 2248–2255.

Mahalanobis, P. C. (1936) On the generalized distance in statistics. *Proceedings of the National Institute of Sciences, Calcutta.*

Margules, C. R., Pressey, R. L. (2000) Systematic conservation planning. *Nature.* **405**, 243–253.

McNeely, J. A. (1994) Protected areas for the 21st-century: Working to provide benefits to society. *Biodiversity and Conservation.* **3**, 390–405.

Moilanen, A. (2007) Landscape Zonation, benefit functions and target-based planning: unifying reserve selection strategies. *Biological Conservation.* **134**, 571–579.

Moritz, C. (2002) Strategies to protect biological diversity and the evolutionary processes that sustain it. *Systematic Biology.* **51**, 238–254.

Ponce-Reyes, R., Clegg, S. M., Carvalho, S. B., McDonald-Madden, E., Possingham, H. P. (2014) Geographical surrogates of genetic variation for selecting island populations for conservation. *Diversity & Distributions.* **20**, 640–651.

Pressey, R. L., Cabeza, M., Watts, M. E., Cowling, R. M., Wilson, K. A. (2007) Conservation planning in a changing world. *Trends in Ecology & Evolution.* **22**, 583–592.

Pressey, R. L., Watts, M. E., Barrett, T. W., Ridges, M. J. (2009) The C-Plan conservation planning system: origins, applications, and possible futures. In: *Spatial conservation prioritisation: Quantitative methods & computational tools* (eds A. Moilanen, K. A. Wilson, & H. Possingham) pp. 211–34 Oxford University Press, Oxford, UK.

Rouget, M., Cowling, R. M., Pressey, R. L., Richardson, D. M. (2003) Identifying spatial components of ecological and evolutionary processes for regional conservation planning in the Cape Floristic Region, South Africa. *Diversity & Distributions.* **9**, 191–210.

Sanderson, E. W., Segan, D. B., Watson, J. E. M. (2015) Global status of and prospects for protection of terrestrial geophysical diversity. *Conservation Biology.* **29**, 649–656.

Sherali, H., Alameddine, A. (1992) A new reformulation-linearization technique for bilinear programming problems. *Journal of Global Optimization.* **2**, 379–410.

Snyder, L. V., Daskin, M. S. (2005) Reliability models for facility location: the expected failure cost case. *Transportation Science.* **39**, 400–416.

Stan Development Team (2015) RStan: The R interface to Stan, Version 2.8.0.

Thomassen, H. A., Cheviron, Z. A., Freedman, A. H., Harrigan, R. J., Wayne, R. K., Smith, T. B. (2010) Spatial modelling and landscape-level approaches for visualizing intra-specific variation. *Molecular Ecology.* **19**, 3532–3548.