# rapr: Representative and Adequate Prioritisations in R

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#### Abstract

A central aim in conservation is to maximise the long-term persistence of biodiversity. To fulfil this aim, reserve networks are used to safeguard biodiversity patterns (eg. species, populations) and processes (eg. evolutionary processes that underpin genetic variation). Reserve selection is often formulated as an optimisation problem to identify cost-effective prioritisations. However, most existing decision support tools are based on formulations that are well suited for preserving biodiversity patterns, but not biodiversity processes. To fill this gap in the conservation planning toolbox, we developed the exttt{rapr R} package. This exttt{R} package provides a toolkit to guide reserve selection using novel formulations of this problem. Here, we explore the functionality of this R package using simulated species and a conservation planning exercise in Queensland, Australia as a case-study. We demonstrate how explicitly considering biodiversity processes can alter a prioritisation. In most cases, we found that only a few additional planning units are required to sufficiently preserve of biodiversity processes.

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## Introduction

The overarching aim of conservation is to maximise the long-term persistence of biodiversity (McNeely 1994; Margules and Pressey 2000). To achieve this, conservation actions must preserve biodiversity patterns (eg. species, populations) and the processes that sustain them. One of the major tangible achievements of modern conservation has been the act of setting aside areas for preservation (Sanderson et al. 2015). Reserve networks buffer species from threatening processes (eg. urbanisation; Margules and Pressey 2000) and set the stage for direct management interventions (eg. captive breeding and reintroduction programs; Kleiman 1989). However, the resources available for conservation action are limited, and so reserve networks must be sited in places that satisfy conservation objectives for minimum cost (Margules and Pressey 2000). To achieve this, reserve selection is often formulated as an optimisation problem and then solved to identify cost-effective candidate reserve systems (prioritisations; Margules and Pressey 2000).

To fulfil the overarching aims of conservation, reserve networks must preserve both ecological and evolutionary processes (Crandall et al. 2000; Margules and Pressey 2000). Ecological processes, such as predator-prey interactions, pollination, and decomposition, are required for biodiversity to persist over short time-scales. Typically, they operate over small geographic domains—with exceptions such as migration and refugial habitats—and can be preserved using suitably large planning units (Ciarleglio et al. 2009) that each contain a discrete unit of habitat (Klein et al. 2009). On the other hand, evolutionary processes are required for biodiversity to persist over long time-scales, and they typically operate over large geographic domains. Adaptive evolutionary processes can be preserved by securing populations with different adaptations and/or along selection pressure gradients (eg. environmental gradients; Moritz 2002; Crandall et al. 2000; Rouget et al. 2003; Cowling et al. 2003). Neutral evolutionary processes can be preserved by securing populations with different evolutionary histories and/or with limited gene flow (Moritz 2002; Carvalho et al. 2011; Ponce-Reves et al. 2014). Due to advances in technology in recent decades, a wealth of data on biodiversity processes has become freely available to conservation planners. Yet this data is only rarely used to guide conservation planning exercises (Hendry et al. 2010). Existing decision support tools focus primarily on preserving biodiversity patterns or occasionally processes—but not both.

Many tools have been developed to assist conservation planners in preserving biodiversity patterns (eg. C-Plan, Pressey et al. 2009; ConsNet, Ciarleglio et al. 2009; Marxan, Ball et al. 2009; Zonation, Moilanen 2007). They use targets (eg. Marxan) or weights (eg. Zonation) to identify prioritisations that contain an adequate amount of individuals or habitat for a set of species (features). To accommodate information on biodiversity processes, conservation planners can split features into sub-features as a pre-processing step (eg. Carvalho et al. 2011). However, this approach is limited because data on biodiversity processes is often continuous and hyper-dimensional (eg. bioclimatic data; Hijmans et al. 2005), and therefore they often cannot be reduced to a few categories without significant information loss (Faith and Walker 1996). Additionally, these problem formulations cannot accommodate variation within sub-features, and nor can they account for relationships between sub-features (Faith and Walker 1996).

Very few tools have been developed with a specific focus on biodiversity processes. The DIVERSITY decision support tool (Faith 2003) uses continuous data to site reserves in places that secure a representative sample of variation across a study area (eg. environmental variation). Originally, this tool was developed to identify prioritisations that secure a comprehensive set of environmental variation without requiring any species-level data. The effectiveness of this approach has been highly contested (Araújo et al. 2001, 2003; Faith 2011). However, this tool has been a unique part

of the the decision maker's toolket, because it can be used to secure a representative sample of a continuous variable.

Today, one of the key issues preventing decision makers from explicitly considering both biodiversity patterns and processes in the reserve selection process is the lack of a decision support tool that can simultaneously accommodate data on both in a multi-species context. To fill this void, we present the rapr R package. This R package provides decision makers with the tools to identify prioritisations that preserve biodiversity patterns and processes. These prioritisations are generated by solving novel formulations of the reserve selection problem that use adequacy- and representation-based targets. We also provide a tutorial showcasing the functionality of this R package using simulated species and a case-study conservation planning scenario in Queensland, Australia.

## Problem formulations

The rapr R package uses two novel formulations of the reserve selection problem to identify cost-effective prioritisations. These formulations share many constraints and variables. For brevity, the variables used by both formulations will be defined. Biodiversity features are defined as the entity(s) that the prioritisation is required to preserve (eg. species, populations). Spatial attributes are defined as the intra-feature variation that the prioritisation is required to sample. These attributes are related to the biodiversity processes that the prioritisation needs to represent (eg. environmental variation, and genetic variation).

Each attribute is conceptualised as a space. This space is termed an attribute space. Each planning unit is thought to occupy a single point inside each space. For example, a decision maker may require a prioritisation that preserves populations along climatic gradients. To achieve this, the decision maker might use an "climatic" attribute space with dimensions relating to mean annual temperature (°C) and precipitation (mm). Any given combination of temperature and precipitation may be conceived as a point in this environmental space. By associating planning units with climatic data, they can be mapped from geographic space to this environmental attribute space.

Demand points are points that also exist in an attribute space. They are designated by the decision maker to indicate regions of the attribute space that should be preserved in the prioritisation. The amount of variation in the attribute space that a prioritisation secures is a function of the distance between each demand point and each planning unit in the attribute space. The shorter the distances between the demand points and the planning units; the better the prioritisation is at securing the variation in the spatial attribute. To convert these amounts to a proportion—a meaningful unit for a decision maker—the distances between the selected planing units and the demand points are scaled by the distances between the demand points to the centroid of the demand points. In any attribute space there may exist points that are impossible (eg. mean annual rainfall -5 mm), do not occur in the study area (eg. mean annual temperature 30°C in Antarctica), or are undesirable (eg. conditions known to be outside the physiological tolerance of a species). By placing demand points in desirable regions of an attribute space, the decision maker can ensure that prioritisations secure desirable values of a spatial attribute.

To illustrate these concepts, we will briefly describe a conservation planning scenario example involving attribute spaces and demand points. A decision maker may wish to develop a prioritisation for a single species. This species has four populations in the study area. These populations are in the process of divergent evolution, with different populations inhabiting different environmental conditions and accruing different adaptations. However, the decision maker can only afford to

preserve three of the populations. The decision maker needs to select a set of populations that will secure the most of intra-specific variation. To describe this intra-specific variation—given that no genetic data was available—the decision maker obtained data on the environmental conditions (rainfall (ml) and temperature (°C)) where each population was found. The decision maker then used this environmental data to construct a two-dimensional environmental attribute space. Next, the decision maker generated demand points as equi-distant points between the range of values where the populations were found ( $\pm$  20% to avoid edge effects; Faith and Walker 1996). By comparing the distribution of the demand points to the distribution of the populations in the attribute space, the decision maker can identify a suitable prioritisation (Figure 1). We can see that if the decision maker preserves both populations A and A0, they will effectively "double-up" on the same environmental characteristics, and in turn their waste resources. Instead, a more representative sample of the intra-specific variation could be preserved by securing populations A1, A2, and A3. This example demonstrates how the inclusion of biodiversity processes can guide the reserve selection process.

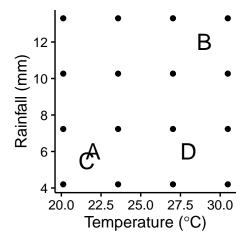


Figure 1 Example of an attribute space. This environmental attribute space has dimensions relating to annual temperature (°C)and rainfall (ml) values. Letters denote the environmental conditions associated with the geographic locations where four hypothetical populations are found. Points represent demand points. In this space, populations closer to each other are considered more similar to each other.

The problem formulations used to guide reserve selection in the rapr R package are based on a combination of the Marxan reserve selection problem and uncapacitated facility location problems (Cornuéjols et al. 1990). All mathematical terms defined hereafter are described in Table S1 for convenience. For convenience, the cardinality of sets will be denoted using the same symbol used to denote the variable. Define F to be the set of features (indexed by f). Let J be a set of planning units (indexed by j). Also, let  $A_j$  denote the area, and  $C_j$  denote the cost of preserving planning unit  $j \in J$ . To assess the extent to which each feature is secured in a given prioritisation, let  $q_{fj}$  denote the probability of feature f occupying planning unit j. The level of fragmentation associated with a prioritisation is parametrised as the net exposed boundary length. Let the shared boundary length between each planning unit  $j \in J$  and  $k \in J$  be  $b_{jk}$ . In any real-world problem, some planning units will have edges that are not associated with any neighbouring planning units (eg. edges along coastlines), these cases will be denoted using  $b_{jj}$  for  $j \in J$ .

Let S denote a set of attribute spaces (indexed by s). Each  $j \in J$  is associated with spatially explicit data that represent coordinates for each attribute space  $s \in S$ . Let  $I_{fsi}$  denote a set of demand points (indexed by i) for each feature  $f \in F$  and each attribute space  $s \in S$ . Let  $\lambda_{fsi}$  denote the

weighting for each demand point  $i \in I$ ,  $f \in F$  and  $s \in S$ . Let  $d_{fsij}$  denote the distance between each demand point  $i \in I$  and each planning unit  $j \in J$  for each feature  $f \in F$  and attribute space  $s \in S$ . Let  $\bar{d}_{fsi}$  denote the distance between each demand point  $i \in I$  and the centroid of the demand points. Demand points with greater weight  $\lambda_{fsi}$  are more important, and the optimal solution will be likely to select planning units close to highly weighted demand points. As a consequence, the decision maker will need to choose an appropriate weighting for each demand point. The decision maker will also need to choose an appropriate distance metric for each attribute space. For example, Euclidean, Mahalanobis (Mahalanobis 1936), Bray-Curtis, or other distance metrics may be appropriate given the nature of the attribute space (evaluated in Faith et al. 1987).

Targets are used to ensure that prioritisations adequately preserve each species. Amount-based targets are used to ensure that the total amount of habitat preserved is sufficient. Let  $\hat{T}_f$  denote the expected amount of area that needs to be preserved for each feature  $f \in F$ . Space-based targets are ensure that a sufficient proportion of the intra-specific variation is secured. Let  $\bar{T}_{fs}$  denote the space-based targets for feature  $f \in F$  and attribute space  $a \in A$ . For convenience, these both types of targets are expressed as proportions in the R package.

The R package provides two formulations for reserve selection. They are based on the unreliable (Cornuéjols et al. 1990) and reliable uncapacitated facility location (Cui et al. 2010) problems. The key difference between them is that the reliable formulation explicitly considers the probability that the planning units are occupied when calculating the proportion of variation that a given solution secures, whereas the unreliable formulation does not.

## Unreliable formulation

In the unreliable formulation, the control variables are the BLM,  $\hat{t}_s$ , and  $\bar{t}_{sa}$  variables.

$$\hat{T}_s = \text{amount target for feature } f$$
 (1b)

$$\bar{T}_{sa}$$
 = representation target for feature  $f$  in attribute space  $a$  (1c)

$$BLM =$$
boundary length modifier: penalises overly fragmented solutions (1d)

The decision variables are the  $X_j$  and  $Y_{fsi}$  variables.

$$X_j = \begin{cases} 1, & \text{if planning unit } j \text{ is selected for conservation action} \\ 0, & \text{otherwise} \end{cases}$$
 (1a)

$$Y_{fsi} = \begin{cases} 1, & \text{if planning unit } i \text{ is assigned to planning unit } j \text{ for feature } f \text{ in space } s \\ 0, & \text{otherwise} \end{cases}$$
 (1e)

The unreliable formulation (URAP) is a defined as a multi-objective optimisation problem.

$$(\text{URAP}) \qquad \text{Min } \sum_{j=0}^{J-1} C_j + BLM \times \sum_{j=0}^{J-1} \sum_{k=j}^{J-1} X_j (1 - X_k) \, b_{jk} + \qquad (2a)$$

$$BLM \times \sum_{j=0}^{J-1} x_j b_{jj}$$

$$\text{s.t. } \sum_{j=0}^{J-1} A_j q_{jf} \ge \bar{T}_f \qquad \forall 0 \le f \le F - 1 \qquad (2b)$$

$$1 - \frac{\sum_{i=0}^{I-1} \sum_{j=0}^{J-1} (\lambda_{fsi} d_{fsij} Y_{fsij})^2}{\sum_{i=0}^{I-1} (\lambda_{fsi} \hat{d}_{fsi})^2} \ge \hat{T}_{fs} \qquad \forall 0 \le f \le F - 1, \qquad (2c)$$

$$0 \le s \le S - 1$$

$$\sum_{j=0}^{J-1} Y_{fsij} = 1 \qquad \forall 0 \le f \le F - 1, \qquad (2d)$$

$$0 \le s \le S - 1, \qquad 0 \le i \le I - 1$$

$$Y_{fsij} \le X_j \qquad \forall 0 \le f \le F - 1, \qquad (2e)$$

$$0 \le s \le S - 1, \qquad 0 \le i \le I - 1, \qquad 0 \le j \le J - 1$$

$$X_j, Y_{fsij} \in 0, 1 \qquad \forall 0 \le f \le F - 1, \qquad (2f)$$

$$0 \le s \le S - 1, \qquad 0 \le S \le S - 1, \qquad$$

The objective function (2a) determines the utility of a given prioritisation: a combination of the total cost of a prioritisation and how fragmented it is. Constraints (2b–2c) ensure that all the amount-based and space-based targets are met. Constraints (2d) ensure that only one planning unit is assigned to each demand point. Constraints (2e) ensure that demand points are only assigned to selected planning units. Constraints (2f) ensure that the X and Y variables are binary.

## Reliable formulation

The reliable formulation explicitly considers the probability that the planning units are inhabited. As a consequence, it may deliver prioritisations that will sufficiently represent an attribute space even if the features do not inhabit several of the planning units when the prioritisation is implemented. This behaviour is achieved by siting back-up planning units near selected planning units with low occupancy probabilities in the attribute space(s). To ensure that prioritisations are robust against multiple planning units being uninhabited, the problem assigns planning units at multiple backup levels.

Backup levels levels are defined as r-levels (similar to failure levels in Snyder and Daskin 2005). The first backup r-level is used to calculate the level of representation when all of the selected planning

units are occupied by all  $f \in F$ . For this scenario, the closest selected planning unit to each demand point i for attribute space s is assigned at r-level = 0. This scenario essentially represents  $Y_{fsij}$  in the unreliable formulation. The second backup r-level is used to assess the level of representation when the closest planning unit to each demand point i is unoccupied. For this scenario, the second closest planning units are assigned at r-level = 1. The third backup r-level is used to assess representation when the first two closest planning units are unoccupied. The third closest planning units are assigned at r-level = 2. Continuing on, in this manner, the selected planning units in a prioritisation are assigned to each demand point  $i \in I$ , attribute space  $s \in S$ , and each feature  $f \in F$  at an r-level.

A final backup r-level when r = R is used to assess the level of representation when the features  $f \in F$  do not occupy any selected planning units in a prioritisation. Each demand point  $i \in I$  for each  $s \in S$  and  $f \in F$  is assigned to an "imaginary" planning unit j = J at r = R. The distance variables associated with this imaginary planning unit  $d_{fsiJ}$  denote the loss of biological value associated with failing to secure a representative sample of feature f in attribute space s. However, the d variables are in distance units which are meaningless in this context. Thus these variables are calculated using a failure multiplier (M) and the maximum distance between the planning units and the demand points for  $f \in F$ ,  $s \in S$  (3).

$$d_{fsiJ} = M \times \max_{0 \le i \le I - 1, 0 \le j \le J - 1} d_{fsij} \qquad \forall 0 \le f \le F - 1,$$

$$0 < s < S - 1$$

$$(3)$$

Moderately-sized conservation planning problems often include several thousand planning units. It is currently not be feasible to solve this problem when considering all possible failure scenarios. As a consequence, the R variable can be any  $1 \le R \le J-1$ . For instance, when R=3 only 2 backup levels are considered in addition to the final backup level. Cui et al. (2010) found that R=5 yields similar solutions to R=J when J>>5. However, depending on the number of features, demand points, attribute spaces, and planning units, decision makers will likely be limited to R=1 to obtain prioritisations in a feasible amount of time.

In the reliable formulation, the control variables are the BLM,  $\hat{t}_s$ ,  $\bar{t}_{sa}$ , R, and M variables. The decision variables are the  $X_j$ ,  $Y_{fsijr}$ ,  $P_{fsijr}$  variables.

$$(1a-1d)$$
 $R = \text{number of failure levels}$  (4a)

$$M = \text{failure multiplier}$$
 (4b)

$$P_{fsijr} = \frac{\text{probability that demand point } i \text{ is assigned to planning}}{\text{unit } j \text{ at back-up level } r \text{ for feature } f \text{ and space } s}$$
(4c)

The reliable formulation (RRAP) is a multi-objective optimisation problem.

$$(RRAP) \quad \text{Min (2a)} \quad \text{s.t. (2b)} \quad 1 - \frac{\sum_{i=0}^{I-1} \sum_{j=0}^{J-1} \left( \lambda_{fsi} d_{fsij} P_{fsijr} Y_{fsij} \right)^2}{\sum_{i=0}^{I-1} \left( \lambda_{fsi} \bar{d}_{fsi} \right)^2} \ge \hat{T}_{fs} \quad \forall 0 \le f \le F-1, \qquad (5a)$$

$$0 \le s \le S-1$$

$$0 \le s \le S-1$$

$$0 \le s \le S-1, \quad 0 \le i \le I-1, \quad 0 \le r \le R$$

$$\sum_{r=0}^{R} Y_{fsijr} = 1 \quad \forall 0 \le f \le F-1, \quad (5b)$$

$$0 \le s \le S-1, \quad 0 \le i \le I-1, \quad 0 \le r \le R$$

$$\sum_{r=0}^{R-1} Y_{fsijr} \le X_j \quad \forall 0 \le f \le F-1, \quad (5c)$$

$$0 \le s \le S-1, \quad 0 \le i \le I-1, \quad 0 \le j \le J$$

$$\sum_{r=0}^{R-1} Y_{fsijr} \le X_j \quad \forall 0 \le f \le F-1, \quad (5d)$$

$$0 \le s \le S-1, \quad 0 \le i \le I-1, \quad 0 \le j \le J-1$$

$$Y_{fsiJR} = 1 \quad \forall 0 \le f \le F-1, \quad (5e)$$

$$0 \le s \le S-1, \quad 0 \le i \le I-1, \quad 0 \le j \le I-1$$

$$0 \le s \le S-1, \quad 0 \le i \le I-1, \quad 0 \le j \le J-1$$

$$P_{fsij0} = q_{fj} \quad \forall 0 \le f \le F-1, \quad (5f)$$

$$0 \le s \le S-1, \quad 0 \le i \le I-1, \quad 0 \le j \le J$$

$$P_{fsijr} = (1-) \sum_{k=0}^{J-1} \frac{1-q_k}{q_k} P_{f,s,i,k,r-1} Y_{f,s,i,k,r-1} \quad \forall 0 \le f \le F-1, \quad (5g)$$

$$0 \le s \le S-1, \quad 0 \le i \le I-1, \quad 0 \le j \le J, \quad 1 \le r \le R$$

$$X_j, Y_{fsijr} \in 0, 1 \quad \forall 0 \le f \le F-1, \quad (5h)$$

$$0 \le s \le S-1, \quad 0 \le i \le I-1, \quad 0 \le j \le J, \quad 1 \le I-1, \quad 0 \le j \le J, \quad 1 \le I-1, \quad 0 \le j \le J, \quad 1 \le I-1, \quad 0 \le J \le J, \quad 1 \le I-1, \quad 0 \le J \le J-1, \quad 0 \le J \le$$

 $0 \le r \le R$ 

The objective function for the reliable formulation is the same as for the unreliable formation (2a). Similar to the unreliable formulation, constraints (2b) and (5a) ensure that the amount-based and space-based targets are met. Constraint (5b–5c) ensure that each planning unit is only assigned to one backup r-level for  $i \in I$ . Constraints (5d) ensure that only selected planning units are assigned to demand points  $i \in I$ . Constraints (5e) ensure that the imaginary planning unit is always assigned to the highest backup r-level. Constraints (5f–5g) determine the probability that planning unit j will be used to sample demand point  $i \in I$  for  $s \in S$  and  $f \in F$  (Cui et al. 2010). Constraints (5h) ensure that the X and Y variables are binary.

## Optimisation

The unreliable and reliable formulations are non-linear. However, the non-linear components can be linearised using existing techniques. First, the expression  $X_jX_k$  in (2a) can be linearised using methods described by Beyer et al. (2016). Second, the expression  $P_{fsijr}Y_{jsijr}$  in (5a) can be linearised using techniques described by Sherali and Alameddine (1992) as implemented in Cui et al. (2010). Linearised versions of the problems can be solved using commercial exact algorithm solvers.

The rapr R package provides functions to express conservation planning data as an optimisation problems using linearised versions of the unreliable and reliable formulations. These optimisation problems can then be solved to generate prioritisations using the commercial Gurobi software suite (http://www.gurobi.com). Note that academics can obtain a license at no cost from the Gurobi website. After installing the Gurobi software suite, users will need to install the Gurobi R package. This R package can be installed on Windows, Mac OSX, and Linux operating systems.

## Package overview

To load the rapr R package and learn more about the package, type the following code into R.

```
# load rapr R package
library(rapr)

# show package overview
?rapr
```

The rapr R package uses a range of S4 classes to store conservation planning data, parameters, and prioritisations (Table 1).

Table 1: Main classes in the rapr R package

Class name	Description
ManualOpts	place-holder class for manually specified solutions
GurobiOpts	stores parameters for solving optimisation problems using Gurobi
RapUnreliableOpts	stores control variables parameters for the unreliable problem formulation $$
RapReliableOpts	stores control variables for the reliable problem formulation

Class name	Description
SimplePoints	represents coordinates in an $n$ -dimensional space
DemandPoints	stores the coordinates and weights for a given species and attribute space
AttributeSpace	stores the coordinates for planning units and the demand points for each species
RapData	stores the all the planning unit, species, and attribute space data
RapUnsolved	stores all the data, control variables, and parameters needed to generate prioritisations
RapResults	stores the prioritisations and summary statistics generated after solving a problem
RapSolved	stores the input data and output results

## Package tutorial

This tutorial is designed to provide users with an understanding of how to use the rapr R package to generate and compare solutions. This tutorial uses several additional packages, so first we will run the following code to load them.

```
# load packages for tutorial
library(plyr)
library(ggplot2)
library(RandomFields)
library(rgeos)

# set seed for reproducibility
set.seed(500)
```

## Simple simulated species

## Data

To investigate the behaviour of the problem, we will generate prioritisations for three simulated species. We will use the unreliable formulation of the problem to understand the basics, and later move onto the reliable formulation. The first species (termed 'uniform') will represent a hyper-generalist. This species will inhabit all areas with equal probability. The second species (termed 'normal') will represent a species with a single range core. The third species (termed 'bimodal') will represent a species with two distinct ecotypes, each with their own range core. To reduce computational time for this example, we will use a  $10 \times 10$  grid of square planning units.

```
# make planning units
sim_pus <- sim.pus(100L)

# simulate species distributions
sim_spp <- lapply(
    c('uniform', 'normal', 'bimodal'),
    sim.species,
n=1,
    x=sim_pus,
    res=1
)</pre>
```

Let's see what these species' distributions look like.

```
# plot species
plot(
    stack(sim_spp),
    main=c('Uniform species','Normal species','Bimodal species'),
    addfun=function(){lines(sim_pus)},
    nc=3
)
```

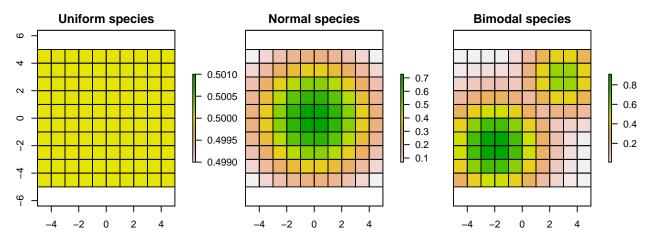


Figure 2 Distribution of three simulated species. Each square represents a planning unit. The colour of each square denotes the probability that individuals from each species occupy it.

Next, we will generate a set of demand points. To understand the effects of probabilities and weights on the demand points, we will generate the demand points in geographic space. These demand points will be the centroids of the planning units. Additionally, we will use the same set of demand points for each species and only vary the weights of the demand points between species. **Note that we are only using the same distribution of demand points for different species for teaching purposes. It is strongly recommended to use different demand points for different species in real-world conservation planning exercises.** See the case-study section of this tutorial for examples on how to generate suitable demand points.

```
# generate coordinates for pus/demand points
pu_coords <- gCentroid(sim_pus, byid=TRUE)</pre>
# calculate weights
sim_dps <- lapply(</pre>
    sim_spp,
    function(x) {
        return(extract(x, pu_coords))
    }
# create demand point objects
sim_dps <- lapply(</pre>
    sim_dps,
    function(x) {
        return(
             DemandPoints(
                 SimplePoints(pu_coords@coords),
             )
        )
    }
)
```

Now, we will construct a RapUnsolved object to store our input data and parameters. This contains all the information to generate prioritisations.

```
## create RapUnreliableOpts object
# this stores parameters for the unreliable formulation problem (ie. BLM)
sim_ro <- RapUnreliableOpts()</pre>
## create RapData object
# create data.frame with species info
species <- data.frame(</pre>
 name=c('uniform', 'normal', 'bimodal')
)
## create data.frame with species and space targets
# amount targets at 20% (denoted with target=0)
# space targets at 20% (denoted with target=1)
targets <- expand.grid(</pre>
  species=1:3,
 target=0:1,
 proportion=0.2
)
# calculate probability of each species in each pu
```

```
pu probabilities <- calcSpeciesAverageInPus(sim_pus, stack(sim_spp))</pre>
## create AttributeSpace object
# this stores the coordinates of the planning units in an attribute space
# and the coordinates and weights of demand points in the space
attr_space <- AttributeSpace(</pre>
  SimplePoints(pu_coords@coords),
  sim dps
)
# generate boundary data information
boundary <- calcBoundaryData(sim_pus)</pre>
## create RapData object
# this stores all the input data for the prioritisation
sim_rd <- RapData(</pre>
  sim_pus@data,
 species,
 targets,
 pu_probabilities,
 list(attr_space),
 boundary,
  SpatialPolygons2PolySet(sim_pus)
)
## create RapUnsolved object
# this stores all the input data and parameters needed to generate prioritisations
sim_ru <- RapUnsolved(sim_ro, sim_rd)</pre>
```

## Single-species prioritisations

Amount-based targets

To investigate the effects of space-based targets, we will generate a prioritisation for each species using only amount-based targets and compare them to prioritisations generated using amount- and space-based targets. To start off, we will generate a prioritisation for the uniform species using amount-based targets. To do this, we will generate a new sim\_ru object by subsetting out the data for the uniform species from the sim\_ru object. Then, we will update the targets in the new object. Finally, we will solve the object to generate a prioritisation that fulfills the targets for minimal cost.

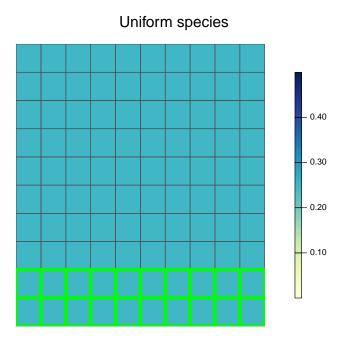
```
# create new object with just the uniform species
sim_ru_s1 <- spp.subset(sim_ru, 'uniform')

# update amount targets to 20% and space targets to 0%
sim_ru_s1 <- update(sim_ru_s1, amount.target=0.2, space.target=NA, solve=FALSE)</pre>
```

```
# solve problem to identify prioritisation
sim_rs_s1_amount <- solve(sim_ru_s1)</pre>
## Optimize a model with 1 rows, 100 columns and 100 nonzeros
## Coefficient statistics:
##
    Matrix range
                     [5e-01, 5e-01]
     Objective range [1e+00, 1e+00]
##
                     [1e+00, 1e+00]
##
     Bounds range
     RHS range
                     [1e+01, 1e+01]
##
## Found heuristic solution: objective 20
## Presolve removed 1 rows and 100 columns
## Presolve time: 0.00s
## Presolve: All rows and columns removed
## Explored O nodes (O simplex iterations) in 0.00 seconds
## Thread count was 1 (of 2 available processors)
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.000000000000e+01, gap 0.0%
## Warning in validityMethod(object): object@space.held contains values less
## than 0, some species are really poorly represented
## show summary
# note the format for this is similar to that used by Marxan
# see ?rapr::summary for details on this table
summary(sim_rs_s1_amount)
##
     Run_Number Status Score Cost Planning_Units Connectivity_Total
## 1
              1 MANUAL
                          20
                               20
                                                                  220
##
     Connectivity_In Connectivity_Edge Connectivity_Out
## 1
                  42
                                   168
##
     Connectivity_In_Fraction
## 1
                    0.1909091
# show amount held
amount.held(sim_rs_s1_amount)
##
    uniform
## 1
         0.2
# show space held
space.held(sim_rs_s1_amount)
    uniform (Space 1)
##
## 1
           -0.2363636
```

Now that we have generated a prioritisation, let's see what it looks like. We can use the spp.plot method to see how the prioritisation overlaps with the uniform species' distribution. Note that since all planning units have equal probabilities for this species, all planning units have the same fill colour.

```
# plot the prioritisation and the uniform species' distribution
spp.plot(sim_rs_s1_amount, 1, main='Uniform species')
```



**Figure 3** A prioritisation for the uniformly distributed species generated using amount-based targets (20%). Squares represent planning units. Planning units with a green border are selected for prioritisation, and their colour denotes the probability they are inhabited by the species.

The prioritisation for the uniform species appears to be just a random selection of planning units. This behavior is due to the fact that any prioritisation with 20 planning units is optimal. By relying on just amount targets, this solution may preserve a section of the species' range core, or just focus on the range margin, or some random part of its range—no emphasis is directed towards preserving different parts of the species' range. This behavior highlights a fundamental limitation of just using amount-based targets. In the absence of additional criteria, conventional reserve selection problems do not contain any additional information to identify the most effective prioritisation.

Now, we will generate a prioritisation for the normally distributed species using amount-based targets. We will use a similar process to what we used for the uniformly distributed species, but for brevity, we will use code to generate solutions immediately after updating the object.

```
# create new object with just the normal species
sim_ru_s2 <- spp.subset(sim_ru, 'normal')</pre>
```

```
# update amount targets to 20% and space targets to 0% and solve it
sim_rs_s2_amount <- update(sim_ru_s2, amount.target=0.2, space.target=NA, solve=TRUE)
## Optimize a model with 1 rows, 100 columns and 100 nonzeros
## Coefficient statistics:
    Matrix range
                     [7e-02, 7e-01]
##
     Objective range [1e+00, 1e+00]
##
                     [1e+00, 1e+00]
##
     Bounds range
                     [7e+00, 7e+00]
     RHS range
##
## Found heuristic solution: objective 27
## Presolve removed 0 rows and 86 columns
## Presolve time: 0.00s
## Presolved: 1 rows, 14 columns, 14 nonzeros
## Variable types: 0 continuous, 14 integer (0 binary)
## Presolved: 1 rows, 14 columns, 14 nonzeros
##
##
## Root relaxation: objective 9.864476e+00, 6 iterations, 0.00 seconds
##
       Nodes
                     Current Node
                                            Objective Bounds
##
                Ι
                                                                  Work
                                      1
    Expl Unexpl | Obj Depth IntInf | Incumbent
##
                                                     BestBd
                                                              Gap | It/Node Time
##
##
        0
              0
                   9.86448
                              0
                                        27.00000
                                                    9.86448 63.5%
                                                                             0s
        0
## H
              0
                                      10.0000000
                                                    9.86448 1.36%
                                                                             0s
##
## Explored O nodes (6 simplex iterations) in 0.02 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 1.000000000000e+01, best bound 1.00000000000e+01, gap 0.0%
# show summary
summary(sim_rs_s2_amount)
##
     Run_Number Status Score Cost Planning_Units Connectivity_Total
## 1
              1 MANUAL
                          10
                                                                  220
                               10
                                               10
##
     Connectivity_In Connectivity_Edge Connectivity_Out
## 1
                                    192
                  12
##
     Connectivity_In_Fraction
## 1
                   0.05454545
# show amount held
amount.held(sim_rs_s2_amount)
##
        normal
```

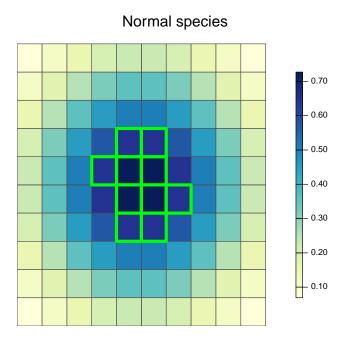
## 1 0.2026153

```
# show space held
space.held(sim_rs_s2_amount)
```

```
## normal (Space 1)
## 1 0.6519926
```

Now let's visualise the prioritisation we made for the normal species.

```
# plot the prioritisation and the normal species' distribution
spp.plot(sim_rs_s2_amount, 1, main='Normal species')
```



**Figure 4** A prioritisation for the normally distributed species generated using amount-based targets (20%). See Figure 3 caption for conventions.

The amount-based prioritisation for the normal species focuses only on the species' range core. This prioritisation fails to secure any peripheral parts of the species' distribution. As a consequence, it may miss out on populations with novel adaptations to environmental conditions along the species' range margin.

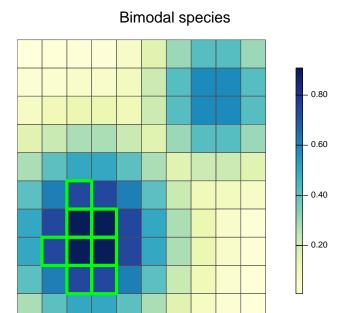
Now, let's generate an amount-based target for the bimodally distributed species view it.

```
# create new object with just the bimodal species
sim_ru_s3 <- spp.subset(sim_ru, 'bimodal')</pre>
```

```
# update amount targets to 20% and space targets to 0% and solve it
sim_rs_s3_amount <- update(sim_ru_s3, amount.target=0.2, space.target=NA)</pre>
```

```
## Optimize a model with 1 rows, 100 columns and 100 nonzeros
## Coefficient statistics:
                     [7e-03, 9e-01]
##
     Matrix range
##
     Objective range [1e+00, 1e+00]
     Bounds range
                     [1e+00, 1e+00]
##
     RHS range
                     [7e+00, 7e+00]
##
## Found heuristic solution: objective 21
## Presolve removed 0 rows and 75 columns
## Presolve time: 0.00s
## Presolved: 1 rows, 25 columns, 25 nonzeros
## Variable types: 0 continuous, 25 integer (0 binary)
## Presolved: 1 rows, 25 columns, 25 nonzeros
##
##
## Root relaxation: objective 7.919039e+00, 18 iterations, 0.00 seconds
##
##
       Nodes
                     Current Node
                                            Objective Bounds
                                                                        Work
##
   Expl Unexpl |
                   Obj Depth IntInf | Incumbent
                                                     BestBd
                                                              Gap | It/Node Time
##
##
        0
              0
                   7.91904
                              0
                                   1
                                       21.00000
                                                    7.91904
                                                             62.3%
                                                                             0s
                                       8.0000000
## H
        0
              0
                                                    7.91904
                                                            1.01%
                                                                             0s
##
## Explored O nodes (18 simplex iterations) in 0.00 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 8.000000000000e+00, best bound 8.00000000000e+00, gap 0.0%
```

```
# plot the prioritisation and the bimodal species' distribution
spp.plot(sim_rs_s3_amount, 1, main='Bimodal species')
```



**Figure 5** A prioritisation for the bimodally distributed species generated using amount-based targets (20%). See Figure 3 caption for conventions.

```
# show summary
summary(sim_rs_s3_amount)
##
     Run_Number Status Score Cost Planning_Units Connectivity_Total
## 1
              1 MANUAL
                                                                  220
##
     Connectivity_In Connectivity_Edge Connectivity_Out
## 1
##
     Connectivity_In_Fraction
## 1
                   0.04090909
# show amount held
amount.held(sim_rs_s3_amount)
##
       bimodal
## 1 0.2018391
# show space held
space.held(sim_rs_s3_amount)
     bimodal (Space 1)
##
             0.2829105
## 1
```

The amount-based prioritisation for the bimodally distributed species only selects planning units in the bottom left corner of the study area. This prioritisation only preserves individuals belonging to one of the two ecotypes. As a consequence, this prioritisation may fail to preserve a representative sample of the genetic variation found inside this species.

## Amount-based and space-based targets

Now that we have generated a prioritisation for each species using only amount-based targets, we will generate a prioritisations using both amount-based and space-targets. To do this we will update the space targets in our amount-based prioritisations to 85%, and store the new prioritisations in new objects.

First, let's do this for the uniform species.

```
# make new prioritisation
sim_rs_s1_space <- update(sim_rs_s1_amount, amount.target=0.2, space.target=0.85)
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 10102 rows, 10100 columns and 40000 nonzeros
## Coefficient statistics:
##
                     [2e-01, 4e+01]
     Matrix range
     Objective range [1e+00, 1e+00]
##
##
     Bounds range
                     [1e+00, 1e+00]
                     [1e+00, 6e+01]
     RHS range
## Found heuristic solution: objective 89
## Presolve removed 36 rows and 0 columns
## Presolve time: 3.68s
## Presolved: 10066 rows, 10100 columns, 40104 nonzeros
## Variable types: 0 continuous, 10100 integer (10100 binary)
## Presolved: 10066 rows, 10100 columns, 40104 nonzeros
##
## Presolve removed 10066 rows and 10100 columns
## Root relaxation: objective 2.000000e+01, 621 iterations, 0.24 seconds
##
                     Current Node
##
       Nodes
                                           Objective Bounds
                                                                        Work
   Expl Unexpl | Obj Depth IntInf | Incumbent
                                                     BestBd
                                                              Gap | It/Node Time
##
## *
        0
                                     20.0000000
                                                   20.00000
                                                             0.00%
                                                                            4s
##
## Explored 0 nodes (1086 simplex iterations) in 4.08 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.00000000000e+01, gap 0.0%
# show summary
summary(sim_rs_s1_space)
```

## Run\_Number Status Score Cost Planning\_Units Connectivity\_Total

```
## 1
              1 MANUAL
                           20
                                20
                                                                   220
##
     Connectivity_In Connectivity_Edge Connectivity_Out
## 1
                   18
                                    147
                                                        55
##
     Connectivity_In_Fraction
## 1
                   0.08181818
# show amount held
amount.held(sim_rs_s1_space)
##
     uniform
## 1
         0.2
# show space held
space.held(sim_rs_s1_space)
     uniform (Space 1)
##
             0.8793939
## 1
```

Let's take a look at the prioritisation for the uniform species with amount-based and space-based targets. Then, let's compare the solutions for the amount-based prioritisation with the new prioritisation using both amount and space targets.

```
# plot the prioritisation and the uniform species' distribution
spp.plot(sim_rs_s1_space, 'uniform', main='Uniform species')
```

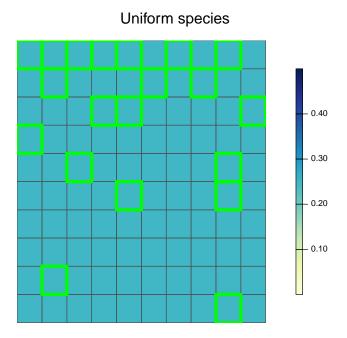
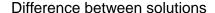


Figure 6 A prioritisation for the uniformly distributed species generated using amount-based targets (20%) and space-based targets (85%). See Figure 3 caption for conventions.

```
# plot the difference between old and new prioritisations
plot(sim_rs_s1_amount, sim_rs_s1_space, 1, 1, main='Difference between solutions')
```



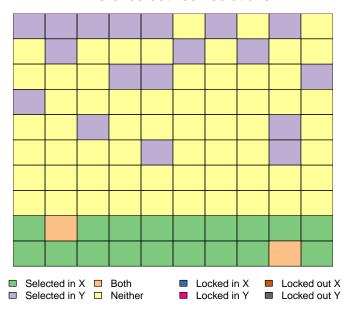


Figure 7 Difference between two prioritisations for the uniformly distributed species. Prioritisation X was generated using just amount-based targets (20%), and prioritisation Y was generated using an additional space-based target (85%).

Here we can see that by including a space-target, the prioritisation is spread out evenly across the species' distribution. Unlike the amount-based prioritisation, this prioritisation samples all the different parts of the species' distribution.

Now, let's generate a prioritisation for the normally distributed species that considers amount-based and space-based targets. Then, let's visualise the new prioritisation and compare it to the old amount-based prioritisation.

```
# make new prioritisation
sim_rs_s2_space <- update(sim_rs_s2_amount, amount.target=0.2, space.target=0.85)</pre>
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 10102 rows, 10100 columns and 40000 nonzeros
## Coefficient statistics:
                     [5e-03, 3e+01]
##
     Matrix range
##
     Objective range [1e+00, 1e+00]
##
     Bounds range
                     [1e+00, 1e+00]
##
     RHS range
                     [1e+00, 2e+01]
## Found heuristic solution: objective 87
## Presolve removed 1176 rows and 192 columns (presolve time = 5s) ...
```

```
## Presolve removed 1178 rows and 192 columns (presolve time = 10s) ...
## Presolve removed 1178 rows and 192 columns
## Presolve time: 10.37s
## Presolved: 8924 rows, 9908 columns, 55525 nonzeros
## Variable types: 0 continuous, 9908 integer (9908 binary)
## Presolve removed 1 rows and 0 columns
## Presolved: 8923 rows, 9908 columns, 55510 nonzeros
## Presolve removed 8923 rows and 9908 columns
## Root simplex log...
##
                Objective
                                Primal Inf.
                                               Dual Inf.
                                                               Time
## Iteration
               1.0000000e+02
                               0.000000e+00
                                              1.000000e+02
##
                                                                11s
##
       3156
               1.2049877e+01
                               0.000000e+00
                                              0.000000e+00
                                                                11s
##
       3156
               1.2049877e+01
                               0.000000e+00
                                              0.000000e+00
                                                                11s
##
## Root relaxation: objective 1.204988e+01, 3156 iterations, 0.87 seconds
##
##
       Nodes
                     Current Node
                                           Objective Bounds
##
   Expl Unexpl | Obj Depth IntInf | Incumbent
                                                     BestBd
                                                              Gap | It/Node Time
##
##
                  12.04988
                              0 409
                                       87.00000
                                                   12.04988
                                                             86.1%
                                                                           11s
## H
              0
                                     13.0000000
                                                   12.04988 7.31%
                                                                           12s
##
## Explored 0 nodes (3431 simplex iterations) in 12.43 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 1.30000000000e+01, best bound 1.30000000000e+01, gap 0.0%
# show summary
summary(sim_rs_s2_space)
##
     Run_Number Status Score Cost Planning_Units Connectivity_Total
## 1
              1 MANUAL
                          13
                               13
                                                                 220
##
     Connectivity_In Connectivity_Edge Connectivity_Out
## 1
                   7
                                   175
                                                      38
##
     Connectivity_In_Fraction
## 1
                   0.03181818
# show amount held
amount.held(sim_rs_s2_space)
```

##

normal

## 1 0.2122983

```
# show space held
space.held(sim_rs_s2_space)
     normal (Space 1)
##
## 1
            0.8523318
# plot the prioritisation and the normal species' distribution
spp.plot(sim_rs_s2_space, 'normal', main='Normal species')
```

# Normal species

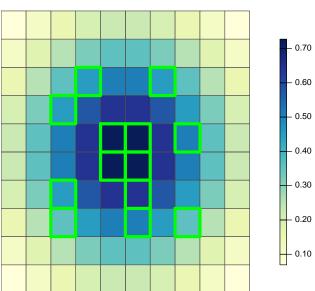


Figure 8 A prioritisation for the normally distributed species generated using amount-based targets (20%) and space-based targets (85%). See Figure 3 caption for conventions.

```
# plot the difference between old and new prioritisations
plot(sim_rs_s2_amount, sim_rs_s2_space, 1, 1, main='Difference between solutions')
```

## Difference between solutions

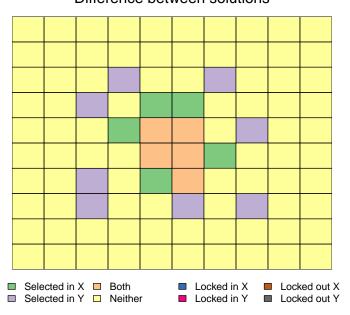


Figure 9 Difference between two prioritisations for the normally distributed species. See Figure 7 caption for conventions.

We can see by using both amount-based and space-based targets we can obtain a prioritisation that secures both the species' range core and parts of its range margin. As a consequence, it may capture any novel adaptations found along the species' range margin—unlike the amount-based prioritisation.

Finally, let's generate a prioritisation for the bimodal species using amount-based and space-based targets.

```
# make new prioritisation
sim rs s3 space <- update(sim rs s3 amount, amount.target=0.2, space.target=0.85)
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 10102 rows, 10100 columns and 40000 nonzeros
## Coefficient statistics:
                     [6e-05, 8e+01]
##
    Matrix range
     Objective range [1e+00, 1e+00]
##
                     [1e+00, 1e+00]
##
     Bounds range
     RHS range
                     [1e+00, 3e+01]
##
## Found heuristic solution: objective 83
## Presolve removed 817 rows and 184 columns (presolve time = 5s) ...
## Presolve removed 817 rows and 184 columns
## Presolve time: 7.45s
## Presolved: 9285 rows, 9916 columns, 50895 nonzeros
## Variable types: 0 continuous, 9916 integer (9916 binary)
## Presolve removed 2 rows and 0 columns
## Presolved: 9283 rows, 9916 columns, 50869 nonzeros
```

```
##
## Presolve removed 9283 rows and 9916 columns
## Root simplex log...
##
                Objective
                                Primal Inf.
                                                Dual Inf.
                                                               Time
## Iteration
##
               1.0000000e+02
                                0.000000e+00
                                               1.000000e+02
                                                                  8s
                                0.000000e+00
##
       9465
               8.1205830e+00
                                               0.000000e+00
                                                                  9s
##
       9465
               8.1205830e+00
                               0.000000e+00
                                               0.000000e+00
                                                                  9s
##
## Root relaxation: objective 8.120583e+00, 9465 iterations, 2.01 seconds
##
       Nodes
                     Current Node
##
                                            Objective Bounds
                                                                         Work
   Expl Unexpl | Obj Depth IntInf | Incumbent
                                                     BestBd
                                                              Gap | It/Node Time
##
##
##
        0
                   8.12058
                                 207
                                        83.00000
                                                    8.12058 90.2%
                                                                             9s
## H
        0
                                       9.0000000
                                                    8.12058 9.77%
                                                                             9s
##
## Explored O nodes (9665 simplex iterations) in 9.88 seconds
## Thread count was 1 (of 2 available processors)
## Optimal solution found (tolerance 5.00e-02)
## Best objective 9.000000000000e+00, best bound 9.00000000000e+00, gap 0.0%
# show summary
summary(sim_rs_s3_space)
##
     Run_Number Status Score Cost Planning Units Connectivity Total
## 1
              1 MANUAL
                           9
                                                                  220
     Connectivity_In Connectivity_Edge Connectivity_Out
##
## 1
##
     Connectivity_In_Fraction
## 1
                   0.04090909
# show amount held
amount.held(sim_rs_s3_space)
##
      bimodal
## 1 0.219729
# show space held
space.held(sim_rs_s3_space)
     bimodal (Space 1)
## 1
             0.8813757
```

```
# plot the prioritisation and the bimodal species' distribution
spp.plot(sim_rs_s3_space, 'bimodal', main='Bimodal species')
```

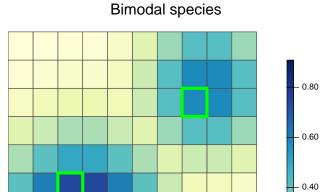


Figure 10 A prioritisation for the normally distributed species generated using amount-based targets (20%) and space-based targets (85%). See Figure 3 caption for conventions.

- 0.20

```
# plot the difference between old and new prioritisations
plot(sim_rs_s3_amount, sim_rs_s3_space, 1, 1, main='Difference between solutions')
```



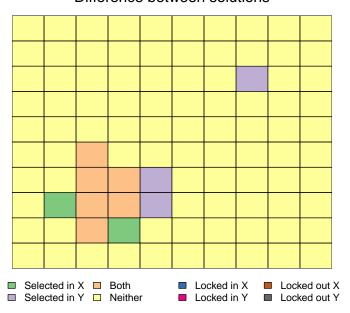


Figure 11 Difference between two prioritisations for the bimodally distributed species. See Figure 7 caption for conventions.

Earlier we found that the amount-based prioritisation only preserved individuals from a single ecotype, and would have failed to adequately preserve the intra-specific variation for this species. However, here we can see that by including space-based targets, we can develop prioritisations that secure individuals belonging to both ecotypes. This new prioritisation is much more effective at sampling the intra-specific variation for this species.

Overall, these results demonstrate that under the simplest of conditions, the use of space-based targets can improve prioritisations. However, these prioritisations were each generated for a single species. Prioritisations generated using multiple species may do a better job at preserving the intra-specific variation for individuals species by preserving them in different parts of their range. We will investigate this in the next section.

## Multi-species prioritisations

Effects of including space-based targets

So far we have generated prioritisations using only a single species at a time. However, real world prioritisations are often generated using multiple species to ensure that they preserve a comprehensive set of biodiversity. Here, we will generate multi-species prioritisations that preserve all three of the simulated species. First, we will generate a prioritisation using amount-based targets that only aims to preserve 20% of the area they occupy. Then, we will generate a prioritisation that also incoperate space-based targets to also preserve 85% of their geographic distribution. We will then compare the two prioritisations.

```
# make prioritisations
sim_mrs_amount <- update(
    sim_ru,</pre>
```

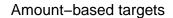
```
amount.target=c(0.2,0.2,0.2),
    space.target=c(0,0,0)
)
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 30306 rows, 30100 columns and 120000 nonzeros
## Coefficient statistics:
##
    Matrix range
                     [6e-05, 8e+01]
##
     Objective range [1e+00, 1e+00]
##
     Bounds range
                     [1e+00, 1e+00]
##
     RHS range
                     [1e+00, 4e+02]
## Found heuristic solution: objective 99
## Presolve removed 0 rows and 0 columns (presolve time = 5s) ...
## Presolve time: 5.82s
## Presolved: 30306 rows, 30100 columns, 120000 nonzeros
## Variable types: 0 continuous, 30100 integer (30100 binary)
## Presolved: 30306 rows, 30100 columns, 120000 nonzeros
##
## Presolve removed 30306 rows and 30100 columns
## Root simplex log...
##
                                                Dual Inf.
## Iteration
                Objective
                                Primal Inf.
                                                               Time
##
          0
               1.0000000e+02
                               0.000000e+00
                                               1.000000e+02
                                                                 7s
               2.1441200e+01
                               0.000000e+00
##
       1961
                                               1.675003e+05
                                                                10s
##
       3319
               2.0000000e+01
                               0.000000e+00
                                               0.000000e+00
                                                                12s
       3319
               2.0000000e+01
                               0.000000e+00
##
                                               0.000000e+00
                                                                12s
##
## Root relaxation: objective 2.000000e+01, 3319 iterations, 6.48 seconds
##
                                            Objective Bounds
##
                     Current Node
                                                                        Work
   Expl Unexpl | Obj Depth IntInf | Incumbent
                                                     BestBd
                                                              Gap | It/Node Time
##
                                      20.0000000
## *
        0
                                                   20.00000
                                                            0.00%
                                                                            12s
##
## Explored O nodes (4618 simplex iterations) in 12.57 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.00000000000e+01, gap 0.0%
sim_mrs_space <- update(</pre>
    sim_ru,
    amount.target=c(0.2,0.2,0.2),
    space.target=c(0.85, 0.85, 0.85)
)
```

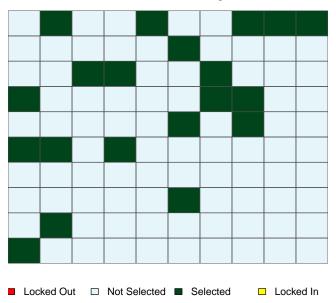
```
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 30306 rows, 30100 columns and 120000 nonzeros
## Coefficient statistics:
    Matrix range
                     [6e-05, 8e+01]
##
##
     Objective range [1e+00, 1e+00]
                     [1e+00, 1e+00]
##
     Bounds range
     RHS range
                     [1e+00, 6e+01]
## Found heuristic solution: objective 99
## Presolve removed 1362 rows and 376 columns (presolve time = 5s) ...
## Presolve removed 1391 rows and 376 columns (presolve time = 10s) ...
## Presolve removed 1595 rows and 376 columns (presolve time = 15s) ...
## Presolve removed 1636 rows and 376 columns (presolve time = 20s) ...
## Presolve removed 1636 rows and 376 columns (presolve time = 25s) ...
## Presolve removed 1636 rows and 376 columns
## Presolve time: 26.40s
## Presolved: 28670 rows, 29724 columns, 137500 nonzeros
## Variable types: 0 continuous, 29724 integer (29724 binary)
## Presolved: 28670 rows, 29724 columns, 137500 nonzeros
##
## Presolve removed 28670 rows and 29724 columns
## Root simplex log...
                                Primal Inf.
                                               Dual Inf.
## Iteration
                Objective
                                                               Time
##
               1.0000000e+02
                               0.000000e+00
                                              1.000000e+02
                                                                28s
          0
##
       4026
               2.0991859e+01
                               0.000000e+00
                                              1.342700e+04
                                                                30s
       4125
               2.0000000e+01
                               0.000000e+00
                                              0.000000e+00
##
                                                                30s
##
       4125
               2.0000000e+01
                               0.000000e+00
                                              0.000000e+00
                                                                30s
##
## Root relaxation: objective 2.000000e+01, 4125 iterations, 3.67 seconds
##
##
                     Current Node
                                     Objective Bounds
                                                                        Work
##
    Expl Unexpl | Obj Depth IntInf | Incumbent
                                                    BestBd
                                                              Gap | It/Node Time
##
##
        0
              0
                  20.00000
                              0
                                       99.00000
                                                  20.00000
                                                            79.8%
                                                                           30s
## H
        0
              0
                                     20.0000000
                                                  20.00000
                                                            0.00%
                                                                           30s
## Explored 0 nodes (5947 simplex iterations) in 30.85 seconds
## Thread count was 1 (of 2 available processors)
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.00000000000e+01, gap 0.0%
# show summaries
```

## Run\_Number Status Score Cost Planning\_Units Connectivity\_Total

summary(sim mrs amount)

```
## 1
              1 MANUAL
                          20
                                20
                                                                  220
     Connectivity_In Connectivity_Edge Connectivity_Out
## 1
                  17
                                    147
##
     Connectivity_In_Fraction
## 1
                   0.07727273
summary(sim_mrs_space)
     Run_Number Status Score Cost Planning_Units Connectivity_Total
##
## 1
              1 MANUAL
                          20
                                                                  220
                                20
##
     Connectivity_In Connectivity_Edge Connectivity_Out
## 1
                   7
                                    142
##
     Connectivity_In_Fraction
## 1
                   0.03181818
# show amount held for each prioritisation
amount.held(sim_mrs_amount)
     uniform
               normal
                        bimodal
##
         0.2 0.201559 0.2012952
## 1
amount.held(sim_mrs_space)
##
     uniform
                normal
                         bimodal
## 1
         0.2 0.2185579 0.2232897
# show space held for each prioritisation
space.held(sim_mrs_amount)
     uniform (Space 1) normal (Space 1) bimodal (Space 1)
## 1
             0.8593939
                              0.8205165
                                                 0.8866593
space.held(sim_mrs_space)
     uniform (Space 1) normal (Space 1) bimodal (Space 1)
## 1
             0.9321212
                              0.8805152
                                                 0.9261063
# plot multi-species prioritisation with amount-based targets
plot(sim_mrs_amount, 1, main='Amount-based targets')
```





**Figure 12** A multi-species prioritisation for the uniformly, normally, and bimodally distributed species generated using just amount-based targets (20%). Squares represent planning units. Dark green planning units are selected for preservation.

# plot multi-species prioritisation with amount- and space-based targets
plot(sim\_mrs\_space, 1, main='Amount and space-based targets')



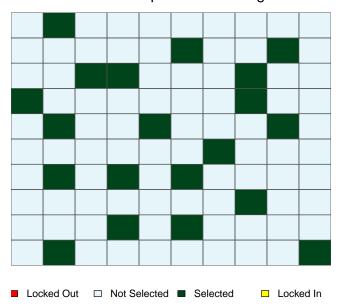


Figure 13 A multi-species prioritisation for the uniformly, normally, and bimodally distributed species generated using amount-based targets (20%) and space-based targets (85%). See Figure 12 caption for conventions.

```
# difference between the two prioritisations
plot(sim_mrs_amount, sim_mrs_space, 1, 1, main='Difference between solutions')
```



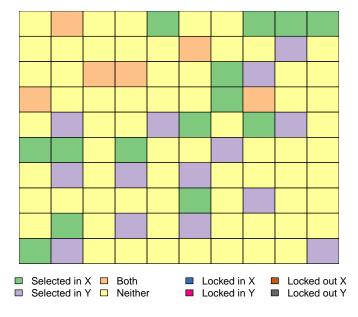


Figure 14 Difference between two multi-species prioritisations. See Figure 7 caption for conventions.

Here we can see that the inclusion of space-based targets changes which planning units are selected for prioritisation, but also the number of planning units that are selected. The amount-based prioritisation is comprised of 20 units, and the space-based prioritisation is comprised of 20 units. This result suggests that an adequate and representative prioritisation can be achieved for only a minor increase in cost.

## Uncertainty in species' distributions

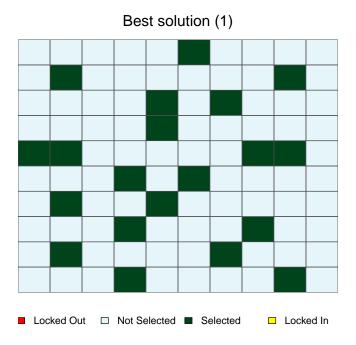
The unreliable formulation does not consider the probability that the planning units are occupied by features when calculating how well a given solution secures a representative sample of an attribute space. Thus solutions identified using the unreliable formulation may select regions of an attribute space for a species using planning units that only have a small chance of being inhabited. As a consequence, if the prioritisation is implemented, it may fail to secure regions of an attribute space if individuals do not inhabit these planning units, and ultimately fail to fulfil the space-based targets.

A simple solution to this issue would be to ensure that planning units cannot be assigned to demand points if they have a low probability of occupancy. This can be achieved by setting a probability threshold for planning units, such that planning units with a probability of occupancy below the threshold are effectively set to zero.

```
# make new prioritisation with probability threshold of 0.5 for each species
sim_mrs_space2 <- solve(
    prob.subset(
        sim_mrs_space,
        species=1:3,
        threshold=c(0.1,0.1,0.1)
    )
)</pre>
```

```
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 27706 rows, 27500 columns and 109600 nonzeros
## Coefficient statistics:
##
    Matrix range
                     [3e-04, 8e+01]
##
     Objective range [1e+00, 1e+00]
    Bounds range
                     [1e+00, 1e+00]
##
    RHS range
                     [1e+00, 6e+01]
## Found heuristic solution: objective 99
## Presolve removed 1197 rows and 270 columns (presolve time = 5s) ...
## Presolve removed 1219 rows and 270 columns (presolve time = 10s) \dots
## Presolve removed 1365 rows and 270 columns (presolve time = 15s) ...
## Presolve removed 1366 rows and 270 columns (presolve time = 20s) ...
## Presolve removed 1366 rows and 270 columns
## Presolve time: 23.67s
## Presolved: 26340 rows, 27230 columns, 125602 nonzeros
## Variable types: 0 continuous, 27230 integer (27230 binary)
## Presolve removed 30 rows and 0 columns
## Presolved: 26310 rows, 27230 columns, 125523 nonzeros
##
## Presolve removed 26310 rows and 27230 columns
```

```
##
## Root simplex log...
##
## Iteration
                Objective
                               Primal Inf.
                                              Dual Inf.
                                                               Time
##
               1.0000000e+02
                               0.000000e+00
                                              1.000000e+02
                                                                26s
          0
##
       4330
               2.0000000e+01
                               0.000000e+00
                                              0.000000e+00
                                                                29s
##
       4330
               2.0000000e+01
                               0.000000e+00
                                              0.000000e+00
                                                                29s
##
## Root relaxation: objective 2.000000e+01, 4330 iterations, 5.04 seconds
## Total elapsed time = 30.12s
##
##
                                     Objective Bounds
       Nodes
                     Current Node
                                                                        Work
   Expl Unexpl | Obj Depth IntInf | Incumbent
                                                    BestBd
                                                              Gap | It/Node Time
##
##
              0
                  20.00000
                              0 364
##
                                       99.00000
                                                   20.00000
                                                            79.8%
                                                                           30s
                                                  20.00000 9.09%
## H
        0
              0
                                     22.0000000
                                                                           31s
## H
        0
              0
                                     20.0000000
                                                   20.00000 0.00%
                                                                           31s
##
## Explored O nodes (7172 simplex iterations) in 31.69 seconds
## Thread count was 1 (of 2 available processors)
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.00000000000e+01, gap 0.0%
# show summary
summary(sim_mrs_space2)
     Run_Number Status Score Cost Planning_Units Connectivity_Total
## 1
              1 MANUAL
                          20
                               20
                                                                 220
##
     Connectivity_In Connectivity_Edge Connectivity_Out
## 1
                                   143
     Connectivity_In_Fraction
##
## 1
                   0.03181818
# plot prioritisation
plot(sim_mrs_space2, 1)
```



**Figure 15** A multi-species prioritisation for the uniformly, normally, and bimodally distributed species generated using amount-based targets (20%) and space-based targets (85%). This priorititisation was generated to be robust against low occupancy probabilities, by preventing planning units with low probabilities from being used to represent demand points. See Figure 12 caption for conventions.

# difference between prioritisations that use and do not use thresholds
plot(sim\_mrs\_space2, sim\_mrs\_space, 1, 1, main='Difference between solutions')

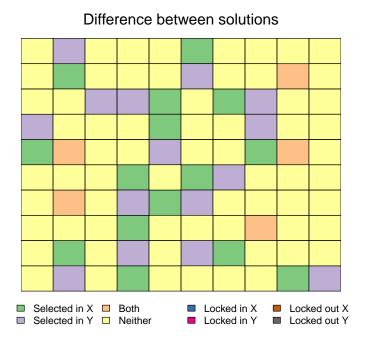


Figure 16 Difference between two multi-species prioritisations. See Figure 7 caption for conventions.

But this method requires setting somewhat arbitrary thresholds. A more robust solution to this issue is to actually use the probability that species occupy planning units to generate the prioritisations. This is what the reliable formulation does. First we will try and generate a solution using existing targets and the reliable formulation. To reduce computational time, we will set the maximum backup R-level to 1.

```
# make new prioritisation using reliable formulation
sim mrs_space3 <- try(update(sim_mrs_space, formulation='reliable', max.r.level=1L))</pre>
## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 364206 rows, 181900 columns and 3847200 nonzeros
## Coefficient statistics:
     Matrix range
                     [6e-05, 1e+02]
##
     Objective range [1e+00, 1e+00]
##
     Bounds range
                     [1e+00, 1e+00]
##
                     [7e-03, 6e+01]
     RHS range
##
## Presolve removed 349813 rows and 90706 columns
## Presolve time: 3.98s
##
## Explored O nodes (O simplex iterations) in 6.76 seconds
## Thread count was 1 (of 2 available processors)
##
## Model is infeasible
## Best objective -, best bound -, gap -
## Try setting lower space-based targets.
   Below are the maximum targets for each species and space.
##
     Proportion
                           Target
      -1.97000 uniform (Space 1)
## 1
## 2 -12.67570 normal (Space 1)
## 3 -21.69092 bimodal (Space 1)
```

However, this fails. The reason why we cannot generate a prioritisation that fulfills these targets is because even the solution that contains all the planning units is still insufficient when we consider probabilities. The negative maximum targets printed in the error message indicate that planning units have low probabilities of occupancy. To fulfill the targets, we must obtain more planning units with higher probabilities of occupancy. We also could attempt resolving the problem using a higher R-level. Instead, we will set lower targets and generate solution.

```
# make new prioritisation using reliable formulation and reduced targets
sim_mrs_space3 <- update(
    sim_mrs_space,
    formulation='reliable',
    max.r.level=1L,
    space.target=-25
)</pre>
```

## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored

```
## Optimize a model with 364206 rows, 181900 columns and 3847200 nonzeros
## Coefficient statistics:
                     [6e-05, 1e+02]
##
    Matrix range
     Objective range [1e+00, 1e+00]
##
##
     Bounds range
                     [1e+00, 1e+00]
                     [7e-03, 1e+04]
     RHS range
## Presolve removed 333501 rows and 90800 columns (presolve time = 5s) ...
## Presolve removed 333701 rows and 151600 columns (presolve time = 10s) ...
## Presolve removed 333701 rows and 151600 columns (presolve time = 109s) ...
## Presolve removed 333701 rows and 151600 columns (presolve time = 110s) \dots
## Presolve removed 333701 rows and 151600 columns
## Presolve time: 112.26s
## Presolved: 30505 rows, 30300 columns, 129690 nonzeros
## Variable types: 200 continuous, 30100 integer (30100 binary)
## Found heuristic solution: objective 64.0000000
## Presolved: 30505 rows, 30300 columns, 129690 nonzeros
## Presolve removed 30103 rows and 11814 columns
##
## Root simplex log...
##
## Iteration
              Objective
                                Primal Inf.
                                               Dual Inf.
                                                               Time
##
          0
               0.000000e+00
                               2.865759e+01
                                              5.535568e+08
                                                               117s
        177
               2.0000000e+01
                               0.000000e+00
                                              0.000000e+00
##
                                                               117s
##
        177
               2.0000000e+01
                               0.000000e+00
                                              0.000000e+00
                                                               117s
##
## Root relaxation: objective 2.000000e+01, 177 iterations, 1.27 seconds
##
##
                     Current Node
                                     Objective Bounds
    Expl Unexpl | Obj Depth IntInf | Incumbent
                                                    BestBd
                                                              Gap | It/Node Time
##
##
## *
                                     20.0000000
                                                  20.00000
                                                            0.00%
                                                                       - 117s
##
## Explored O nodes (179 simplex iterations) in 117.18 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 2.000000000000e+01, best bound 2.00000000000e+01, gap 0.0%
## Warning in validityMethod(object): object@space.held contains values less
## than 0, some species are really poorly represented
# show summary
summary(sim_mrs_space3)
##
    Run_Number Status Score Cost Planning_Units Connectivity_Total
```

20

220

## 1

1 MANUAL

20

20

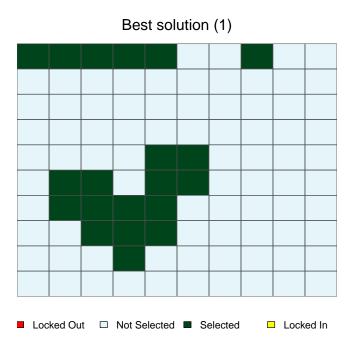


Figure 17 A multi-species prioritisation for the uniformly, normally, and bimodally distributed species generated using amount-based targets (20%) and space-based targets (85%). This priorititisation was generated to be robust against low occupancy probabilities, by explicitly using the probability of occupancy data when deriving a solution. See Figure 12 caption for conventions.

# difference between prioritisations based on unreliable and reliable formulation
plot(sim\_mrs\_space3, sim\_mrs\_space, 1, 1, main='Difference between solutions')

# Difference between solutions

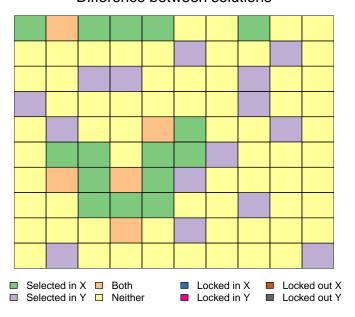


Figure 18 Difference between two multi-species prioritisations. See Figure 7 caption for conventions.

An additional planning unit was selected using the reliable formulation. The prioritisation based on the unreliable formulation had 20 planning units, but the prioritisation based on the reliable formulation has 20 planning units. This difference occurs because the reliable formulation needs to ensure that all selected planning units with a low chance of being occupied have a suitable backup planning unit. While the reliable formulation can deliver more robust prioritisations, it takes much longer to solve conservation planning problems expressed using this formulation than the unreliable formulation. As a consequence, the reliable formulation is only feasible for particularly small problems, such as those involving few features and less than several hundred planning units.

# Fragmentation

Fragmentation is an important consideration in real-world planning situations. Up until now, we haven't considered the effects of fragmentation on the viability of the prioritisation. As a consequence, our prioritisations have tended to contain planning units without any neighbours. We can use the BLM parameter to penalise fragmented solutions.

Let's generate a new prioritisation that heavily penalises fragmentation. Here, we will update the sim\_mrs\_amount object with BLM of 100.

```
# update prioritisation
sim_mrs_amount_blm <- update(sim_mrs_amount, BLM=100)

## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored
## Optimize a model with 30666 rows, 30280 columns and 120720 nonzeros
## Coefficient statistics:
## Matrix range [6e-05, 8e+01]
## Objective range [1e+02, 4e+02]</pre>
```

```
##
                      [1e+00, 1e+00]
     Bounds range
                      [1e+00, 4e+02]
##
     RHS range
## Found heuristic solution: objective 4299
## Presolve removed 0 rows and 0 columns (presolve time = 5s) ...
## Presolve time: 5.96s
## Presolved: 30666 rows, 30280 columns, 120720 nonzeros
## Variable types: 0 continuous, 30280 integer (30280 binary)
## Presolved: 30666 rows, 30280 columns, 120720 nonzeros
## Presolve removed 30666 rows and 30280 columns
##
## Root simplex log...
##
##
  Iteration
                Objective
                                 Primal Inf.
                                                 Dual Inf.
                                                                 Time
##
          0
               2.2100000e+04
                                0.000000e+00
                                                4.010000e+04
                                                                   7s
##
       2093
               1.1941697e+03
                                0.000000e+00
                                                3.921985e+05
                                                                  10s
##
       5768
               6.4673127e+02
                                0.000000e+00
                                                2.068700e+05
                                                                  15s
##
       7117
               4.644444e+02
                                0.000000e+00
                                                0.000000e+00
                                                                  18s
##
       7117
               4.644444e+02
                                0.000000e+00
                                                0.000000e+00
                                                                  18s
##
## Root relaxation: objective 4.644444e+02, 7117 iterations, 12.18 seconds
##
##
                      Current Node
                                       Objective Bounds
                                                                          Work
##
    Expl Unexpl |
                   Obj Depth IntInf | Incumbent
                                                      BestBd
                                                                Gap | It/Node Time
##
##
        0
                 464.44444
                               0 1725 4299.00000
                                                   464.44444
                                                               89.2%
              0
                                                                              18s
        0
              0
                                                               76.2%
                                                                             45s
## H
                                     1953.0000000
                                                   464.44444
##
        0
                 523.81679
                               0 1561 1953.00000
                                                   523.81679
                                                               73.2%
                                                                             48s
##
        0
              0
                 523.81679
                               0 1560 1953.00000
                                                   523.81679
                                                               73.2%
                                                                             48s
##
        0
                 571.01549
                               0 1811 1953.00000
                                                   571.01549
                                                               70.8%
                                                                             51s
        0
##
              0
                 571.01549
                               0 1827 1953.00000
                                                   571.01549
                                                               70.8%
                                                                             51s
##
        0
              0
                 571.01549
                               0 1832 1953.00000
                                                   571.01549
                                                               70.8%
                                                                             53s
##
        0
              0
                 571.01549
                               0 1831 1953.00000
                                                   571.01549
                                                               70.8%
                                                                             54s
        0
                                                               70.8%
##
              0
                 571.01549
                               0 1676 1953.00000
                                                   571.01549
                                                                             59s
##
        0
                               0 1684 1953.00000
                                                               70.8%
                                                                             60s
              0
                 571.01549
                                                   571.01549
##
        0
              0
                 571.01549
                               0 1636 1953.00000
                                                   571.01549
                                                               70.8%
                                                                              62s
##
        0
                 571.01549
                               0 1651 1953.00000
                                                   571.01549
                                                               70.8%
                                                                              63s
        0
                               0 1625 1953.00000
                                                               70.8%
                                                                              67s
##
              0
                 571.01549
                                                   571.01549
##
        0
              0
                 571.01549
                               0 1631 1953.00000
                                                   571.01549
                                                               70.8%
                                                                             67s
                 571.01549
##
        0
                               0 1606 1953.00000
                                                               70.8%
                                                                             71s
              0
                                                   571.01549
        0
                                                                             71s
##
              0
                 571.01549
                               0 1611 1953.00000
                                                   571.01549
                                                               70.8%
##
        0
              0
                 571.01549
                               0 1556 1953.00000
                                                   571.01549
                                                               70.8%
                                                                             75s
        0
                                                               70.8%
                                                                             76s
##
              0
                 571.01549
                               0 1559 1953.00000
                                                   571.01549
        0
##
                 571.01549
                               0 1561 1953.00000
                                                   571.01549
                                                               70.8%
                                                                             78s
##
        0
              0 571.01549
                               0 1562 1953.00000
                                                               70.8%
                                                                             79s
                                                   571.01549
##
        0
                 571.01549
                               0 1584 1953.00000
                                                   571.01549
                                                               70.8%
                                                                             82s
##
        0
              0
                 571.01549
                               0 1539 1953.00000
                                                   571.01549
                                                               70.8%
                                                                             84s
## H
        0
              0
                                    1435.0000000 571.01549
                                                               60.2%
                                                                             97s
```

```
## H
                                       1332.0000000
                                                                                 109s
        0
               0
                                                      571.01549
                                                                   57.1%
##
         0
               2
                   572.12289
                                 0 1506 1332.00000
                                                      572.12289
                                                                   57.0%
                                                                                 109s
##
        2
               4
                                 2 1168 1332.00000
                                                                   56.8%
                                                                          2933
                                                                                 110s
                   592.61930
                                                      575.86532
                   702.77417
                                10 1108 1332.00000
                                                                   56.8%
##
       10
              12
                                                      575.86532
                                                                           1568
                                                                                 117s
                                                                           1287
##
       17
              19
                   770.00000
                                17
                                    708 1332.00000
                                                      575.86532
                                                                   56.8%
                                                                                 120s
##
  Η
       22
              22
                                       1227.0000000
                                                      575.86532
                                                                   53.1%
                                                                           1170
                                                                                 123s
##
       27
              29 1070.00000
                                26
                                     81 1227.00000
                                                      575.86532
                                                                   53.1%
                                                                           1020
                                                                                 125s
## H
       28
              28
                                       1121.0000000
                                                      575.86532
                                                                   48.6%
                                                                            984
                                                                                 127s
##
       41
              33
                                38
                                       1120.0000000
                                                      575.86532
                                                                   48.6%
                                                                            702
                                                                                 127s
##
       45
              35
                   666.15385
                                 3 1604 1120.00000
                                                      585.46465
                                                                   47.7%
                                                                            721
                                                                                 130s
                                                                   47.7%
##
       58
              48
                   860.00000
                                    919 1120.00000
                                                                            689
                                                                                 135s
                                16
                                                      585.46465
                                                                   47.7%
##
       66
              55 1104.37500
                                24
                                    586 1120.00000
                                                      585.46465
                                                                            687
                                                                                 140s
##
                                    992 1120.00000
                                                                   46.9%
                                                                                 145s
       91
              68
                  826.38298
                                11
                                                      594.82736
                                                                            589
                                                                   46.9%
##
      110
              87 1100.00000
                                28
                                    376 1120.00000
                                                      594.82736
                                                                            570
                                                                                 150s
##
      122
              91
                   806.59044
                                10 1057 1120.00000
                                                      604.26637
                                                                   46.0%
                                                                            596
                                                                                 155s
##
                                    932 1120.00000
                                                                   46.0%
      127
              96
                  989.04762
                                15
                                                      604.26637
                                                                            631
                                                                                 160s
##
      140
             101
                   695.00000
                                   1519 1120.00000
                                                      613.10042
                                                                   45.3%
                                                                            650
                                                                                 166s
                                 6
##
                   702.99776
                                 7
                                   1479 1120.00000
                                                                   45.3%
                                                                            706
      141
             102
                                                      613.10042
                                                                                 171s
##
                                    926 1120.00000
                                                                   45.3%
      151
             112
                   853.33333
                                17
                                                      613.10042
                                                                            697
                                                                                 175s
##
             121
                   678.62069
                                   1293 1120.00000
                                                      621.72786
                                                                   44.5%
                                                                            697
                                                                                 180s
      167
                                 5
##
      180
             134
                   970.00000
                                18
                                    625 1120.00000
                                                      621.72786
                                                                   44.5%
                                                                            687
                                                                                 185s
                                                                   44.2%
##
      201
             150
                   779.67391
                                 8 1008 1120.00000
                                                      625.00000
                                                                            662
                                                                                 190s
##
      210
             159 1038.75000
                                17
                                    623 1120.00000
                                                      625.00000
                                                                   44.2%
                                                                            671
                                                                                 195s
                                                                                 200s
##
      228
             161 1086.66667
                                21
                                    575 1120.00000
                                                      625.00000
                                                                   44.2%
                                                                            646
##
      242
             166
                  882.79070
                                    995 1120.00000
                                                      641.89958
                                                                   42.7%
                                                                            647
                                                                                 205s
                                15
                                                                   42.7%
##
      251
             172 1086.66667
                                23
                                    390 1120.00000
                                                      641.89958
                                                                            654
                                                                                 210s
##
                                                                   42.0%
      254
             171
                  744.59580
                                 3
                                   1572 1120.00000
                                                      650.00000
                                                                            671
                                                                                 215s
##
      259
             176 1063.92292
                                 8
                                    589 1120.00000
                                                      650.00000
                                                                   42.0%
                                                                            679
                                                                                 220s
                                                                   42.0%
##
      266
             175
                      cutoff
                                12
                                         1120.00000
                                                      650.00000
                                                                            690
                                                                                 227s
##
      278
             179
                  822.43902
                                12
                                    963 1120.00000
                                                      654.29758
                                                                   41.6%
                                                                            681
                                                                                 230s
      289
             149
                                       1021.0000000
                                                                   35.9%
                                                                                 235s
## H
                                                      654.29758
                                                                            676
## H
      353
             149
                                       1020.0000000
                                                      654.29758
                                                                   35.9%
                                                                            561
                                                                                 238s
##
      358
             149
                   766.22267
                                 7 1282 1020.00000
                                                      655.58472
                                                                   35.7%
                                                                            565
                                                                                 240s
##
                                   1348 1020.00000
                                                                   35.4%
      379
             163
                   721.02078
                                                      658.46154
                                                                            557
                                                                                 245s
##
      391
             175
                   876.36364
                                    983 1020.00000
                                                      658.46154
                                                                   35.4%
                                                                                 250s
                                18
                                                                            562
##
      411
             182
                   887.56757
                                11
                                    889 1020.00000
                                                      660.85511
                                                                   35.2%
                                                                            559
                                                                                 256s
##
      418
             189
                   928.69565
                                13
                                    844 1020.00000
                                                      660.85511
                                                                   35.2%
                                                                            576
                                                                                 261s
##
      429
             191
                   826.76895
                                   1510 1020.00000
                                                      663.02381
                                                                   35.0%
                                                                            576
                                                                                 265s
                                 3
##
      456
             210
                   769.70930
                                10
                                    983 1020.00000
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                                                                   34.9%
                                                                            562
                                                                                 270s
##
      461
             215
                   932.00000
                                15
                                    934 1020.00000
                                                      663.90244
                                                                   34.9%
                                                                            568
                                                                                 275s
##
             233
                                   1580 1020.00000
                                                                   33.5%
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      498
                   855.52632
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##
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      505
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                   912.30769
                                                      678.06452
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##
             245
                   834.28571
                                16 1539 1020.00000
                                                      678.06452
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                                                                                 307s
      511
                                                                            547
##
      513
             246
                   691.48733
                                   1725 1020.00000
                                                      678.06452
                                                                   33.5%
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##
      514
             247
                   920.00000
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                                                      678.06452
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                                                                            544
                                                                                 352s
##
      515
             248
                   885.51724
                                21 1613 1020.00000
                                                      678.06452
                                                                   33.5%
                                                                            543
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##
      516
             248
                   842.44898
                                15 1500 1020.00000
                                                      678.06452
                                                                   33.5%
                                                                            542
                                                                                 378s
##
      517
             249
                                 3 1504 1020.00000
                                                      678.06452
                                                                   33.5%
                                                                                 380s
                   792.39116
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```

```
##
             250
                   898.94737
                                16 1594 1020.00000
                                                       678.06452
                                                                   33.5%
                                                                                  387s
      519
                                                                            539
##
      520
             251
                   882.50000
                                12 1486 1020.00000
                                                       678.06452
                                                                   33.5%
                                                                            538
                                                                                  397s
##
      521
             252
                                 6 1563 1020.00000
                                                       678.06452
                                                                   33.5%
                                                                            537
                                                                                  401s
                   803.27125
##
             252
                                10 1562 1020.00000
                                                                   33.5%
                                                                                  405s
      522
                   737.39130
                                                       678.06452
                                                                            536
##
      524
             254
                   943.40426
                                15 1571 1020.00000
                                                       678.06452
                                                                   33.5%
                                                                            534
                                                                                  413s
##
      525
             254
                   898.12500
                                   1532 1020.00000
                                                       678.06452
                                                                   33.5%
                                                                            533
                                                                                  417s
##
      526
             255
                   717.89474
                                   1483 1020.00000
                                                       678.06452
                                                                   33.5%
                                                                            532
                                                                                  427s
##
      528
             256
                   705.00031
                                 4 1439 1020.00000
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                                                                                  439s
##
                                16 1445 1020.00000
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##
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                                 8 1472 1020.00000
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##
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             259
                   718.75000
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                                                                   33.5%
                                                                            526
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                                15 1444 1020.00000
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                                                                                  464s
##
             263
                                   1329 1020.00000
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                                                                   33.5%
                                                                            692
                                                                                  472s
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##
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             265
                   804.93743
                                16 1480 1020.00000
                                                       678.06452
                                                                   33.5%
                                                                            701
                                                                                  476s
##
      541
             267
                   818.18717
                                18 1294 1020.00000
                                                       678.06452
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                                                                            712
                                                                                  480s
##
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                                                                            728
                                                                                  485s
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             268
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##
      559
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                                17 1062 1020.00000
                                                       678.06452
                                                                   33.5%
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                                19 1629 1020.00000
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      563
             268
                   758.61850
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                                21 1429 1020.00000
                                                       678.06452
                                                                   33.5%
                                                                                 505s
##
      567
             270
                                                                            752
      571
             254
                                23
                                        920.0000000
                                                       678.06452
                                                                   26.3%
                                                                            761
                                                                                  510s
##
   *
##
      580
             250
                   784.96446
                                17 1564
                                          920.00000
                                                       689.31692
                                                                   25.1%
                                                                            768
                                                                                  517s
                                                                   25.1%
##
      582
             251
                   827.74784
                                18 1391
                                          920.00000
                                                       689.31692
                                                                            780
                                                                                 521s
##
      584
             253
                   845.67295
                                19 1395
                                          920.00000
                                                       689.31692
                                                                   25.1%
                                                                            787
                                                                                  525s
                                                                                 530s
##
      593
             248
                   787.90042
                                18 1176
                                          920.00000
                                                       691.34181
                                                                   24.9%
                                                                            790
##
             248
                   843.52941
                                19 1122
                                          920.00000
                                                       710.96046
                                                                   22.7%
                                                                            792
                                                                                 535s
      605
##
      607
             249
                   826.25000
                                20
                                     597
                                          920.00000
                                                       710.96046
                                                                   22.7%
                                                                            802
                                                                                  540s
##
                                   1229
                                          920.00000
                                                                   22.7%
      608
             250
                   857.37717
                                                       710.96046
                                                                            812
                                                                                  545s
                                21
##
      612
             248
                   892.72727
                                22
                                     569
                                          920.00000
                                                       710.96046
                                                                   22.7%
                                                                            817
                                                                                  552s
                                                                   22.7%
##
      613
             249
                   900.00000
                                23
                                     547
                                          920.00000
                                                       710.96046
                                                                            819
                                                                                  555s
##
      622
             248
                   790.00000
                                20
                                     941
                                          920.00000
                                                       715.05609
                                                                   22.3%
                                                                            830
                                                                                  562s
##
             249
                                     701
                                          920.00000
                                                                   22.3%
                                                                                  565s
      623
                   853.33333
                                21
                                                       715.05609
                                                                            830
##
      627
             249
                   916.55172
                                23
                                     612
                                          920.00000
                                                       715.05609
                                                                   22.3%
                                                                            832
                                                                                  571s
##
      629
             250
                   896.00000
                                24
                                     610
                                          920.00000
                                                       715.05609
                                                                   22.3%
                                                                            834
                                                                                 575s
##
             245
                                19 1091
                                          920.00000
                                                                   20.5%
      641
                   878.62069
                                                       731.83346
                                                                            832
                                                                                 580s
##
      658
             240
                   827.58226
                                19 1348
                                          920.00000
                                                       732.65856
                                                                   20.4%
                                                                            825
                                                                                  587s
##
      660
             241
                   905.00000
                                21
                                    743
                                          920.00000
                                                       732.65856
                                                                   20.4%
                                                                            829
                                                                                  590s
##
      675
             236
                   782.77632
                                19 1520
                                          920.00000
                                                       782.77632
                                                                   14.9%
                                                                            823
                                                                                  595s
##
      691
             232
                   905.18519
                                     608
                                          920.00000
                                                       782.77632
                                                                   14.9%
                                                                            818
                                                                                  600s
                                34
##
                                22
                                     933
                                          920.00000
                                                                   12.8%
      728
             221
                   888.42105
                                                       801.98120
                                                                            787
                                                                                  606s
##
      732
             218
                   840.82613
                                20 1367
                                          920.00000
                                                       805.11605
                                                                   12.5%
                                                                            794
                                                                                  611s
##
             213
                                33 1323
                                          920.00000
                                                                            788
      746
                   905.24590
                                                       805.11605
                                                                   12.5%
                                                                                 615s
##
                                          920.00000
                                                                   12.5%
                                                                                  620s
      852
             177
                   905.24590
                               139 1322
                                                       805.11605
                                                                            692
##
      880
             167
                   828.68077
                                17 1337
                                          920.00000
                                                                   12.2%
                                                                                  636s
                                                       808.16731
                                                                            681
                                18
##
      885
             164
                      cutoff
                                          920.00000
                                                       808.16731
                                                                   12.2%
                                                                            687
                                                                                  640s
##
      896
             161
                   912.67370
                                25 1087
                                          920.00000
                                                       812.30628
                                                                   11.7%
                                                                            689
                                                                                  645s
##
      909
             157
                   918.12293
                                38 2347
                                          920.00000
                                                       812.30628
                                                                   11.7%
                                                                            686
                                                                                  653s
##
      910
             157
                   918.71776
                                39 1113
                                          920.00000
                                                       812.30628
                                                                   11.7%
                                                                            687
                                                                                  655s
##
      916
                   904.61538
                                     610
                                          920.00000
                                                       818.45124
                                                                   11.0%
                                                                            688
             153
                                24
                                                                                  660s
```

```
142 912.93231
                                                             10.4%
##
      943
                             18 1436 920.00000 824.46334
                                                                     677
                                                                          666s
##
                    cutoff
      952
            139
                             21
                                      920.00000 825.63973
                                                             10.3%
                                                                     681
                                                                          671s
##
      956
            138
                903.87097
                             20
                                 577
                                      920.00000
                                                 828.87080
                                                             9.91%
                                                                     683
                                                                          675s
##
      961
                             21
                                                             9.51%
            133
                 853.33333
                                 581
                                      920.00000
                                                 832.50000
                                                                     684
                                                                          680s
##
      962
            133
                 904.61538
                             22
                                 581
                                      920.00000
                                                 832.50000
                                                             9.51%
                                                                     686
                                                                          685s
      983
                                 767
                                                             8.89%
                                                                          690s
##
            128
                 886.66667
                             22
                                      920.00000
                                                 838.18182
                                                                     677
##
      997
                 902.56002
                             21 1443
                                      920.00000
                                                  845.85831
                                                             8.06%
                                                                     677
                                                                          695s
##
     1001
            117
                 906.36364
                             22
                                 612
                                      920.00000 850.43478 7.56%
                                                                     684
                                                                          704s
##
     1006
                             20 1182 920.00000 853.33333 7.25%
                                                                          705s
            114 882.06897
                                                                     682
##
     1028
            105
                 916.55172
                             39
                                 563
                                      920.00000
                                                 853.33333 7.25%
                                                                     672
                                                                          710s
##
     1038
             98 911.65434
                             19 1677
                                      920.00000
                                                 857.42235 6.80%
                                                                     672
                                                                          715s
##
                                 780
     1052
             94 909.22095
                             21
                                      920.00000
                                                  862.02517
                                                             6.30%
                                                                     670
                                                                          721s
##
     1067
                                 691
                                                             6.30%
                                                                          725s
             89
                909.22095
                             36
                                      920.00000 862.02517
                                                                     666
                                                             5.56%
##
     1123
             70
                902.35294
                             30
                                 439 920.00000
                                                  868.81512
                                                                     639
                                                                          730s
##
     1156
             55
                    cutoff
                             22
                                      920.00000 877.19462 4.65%
                                                                     629
                                                                          735s
##
## Cutting planes:
##
     Gomory: 11
##
     Zero half: 69
##
## Explored 1157 nodes (809290 simplex iterations) in 735.65 seconds
## Thread count was 1 (of 2 available processors)
## Optimal solution found (tolerance 5.00e-02)
## Best objective 9.200000000000e+02, best bound 8.78000000000e+02, gap 4.5652%
# show summary of prioritisation
summary(sim_mrs_amount_blm)
     Run Number Status Score Cost Planning Units Connectivity Total
##
## 1
              1 MANUAL 1420
                               20
                                               20
                                                                 220
##
     Connectivity_In Connectivity_Edge Connectivity_Out
## 1
                  35
                                   171
##
     Connectivity_In_Fraction
## 1
                    0.1590909
# show amount held for each prioritisation
amount.held(sim_mrs_amount_blm)
##
     uniform
                         bimodal
                normal
## 1
         0.2 0.2645832 0.3911267
# show space held for each prioritisation
space.held(sim_mrs_amount_blm)
##
     uniform (Space 1) normal (Space 1) bimodal (Space 1)
## 1
             0.4545455
                              0.4517326
                                                0.6539667
```

```
# plot prioritisation
plot(sim_mrs_amount_blm, 1)
```

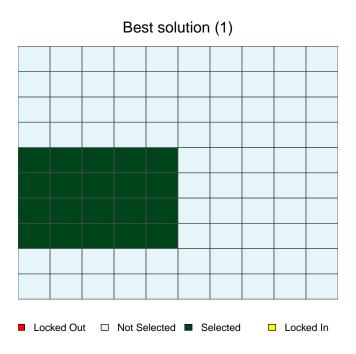
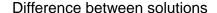


Figure 19 A multi-species prioritisation for the uniformly, normally, and bimodally distributed species generated using only amount-based targets (20%). Additionally, this priorititisation was specified to have high connectivity, by using a high BLM parameter. See Figure 12 caption for conventions.

```
# difference between the two prioritisations
plot(sim_mrs_amount_blm, sim_mrs_amount, 1, 1, main='Difference between solutions')
```



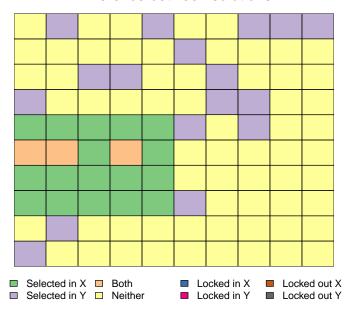


Figure 20 Difference between two multi-species prioritisations. See Figure 7 caption for conventions.

Here we can see that the prioritisation generated using a BLM parameter of 100 is much more clustered than the prioritisation generated using a BLM of 0. In practice, conservation planners will need to try a variety of BLM parameters to find a suitable prioritisation.

# Complex simulated species

### Data

In the previous examples, we have only used Euclidean distances to determine how much of an attribute space is sampled by a prioritisation. However, Euclidean distances can be poor measures of distance for multivariate, binary, or correlated variables (Faith *et al.* 1987). As a consequence this may lead to over- or under-estimates of the quality of a given solution.

The rapr R package provides a suite of distance metrics that can be used to calculate spatial representation (see ?AttributeSpace for available metrics). To illustrate how using different distance metrics can affect the resulting solution, we will generate a new suite of prioritisations using different distance metrics.

First, we will simulate a new species and a three-dimensional attribute space. Note that unlike the previous examples, the attribute space will not be geographic space. Rather, each dimension in the attribute space will have values that map onto geographic space (eg. like climatic variables across the landscape). To add further complexity, we simulate their distributions using Gaussian processes.

```
# set seed for simulations
set.seed(500)
## simulate planning units
```

```
sim_pus <- sim.pus(25L)</pre>
# simulate species
sim_gspp <- sim.species(sim_pus, model=RPgauss(), n=1, res=0.1)</pre>
# simulate space
sim_gspace <- sim.space(sim_pus, model=RMgauss(scale=3), d=3, res=0.1)</pre>
## ...
# increment simulated space values by 100 so there are no negative values
# so we can investigate all distance metrics
sim_gspace <- sim_gspace + 100</pre>
# generate RapUnsolved object containing data to generate prioritisations
sim_ru_gp <- rap(</pre>
    sim_pus, sim_gspp, sim_gspace,
    amount.target=0.2, space.target=0.85,
    n.demand.points=50L, kernel.method='hypervolume',
    include.geographic.space=FALSE, scale=FALSE, solve=FALSE
)
## Choosing repsperpoint=1500 (use a larger value for more accuracy.)
## Evaluating probability density...
## Building tree... done.
## Querying tree... 2.33918e-06 0.0233942 0.046786 0.0701778 0.0935696 0.116961 0.140353
## Finished evaluating probability density.
## Beginning volume calculation... done.
## Quantile requested: 0.20
                               obtained: 0.20
Let's visualise the species' distribution and the distribution of the attribute space across geographic
space.
```

# Simulated species

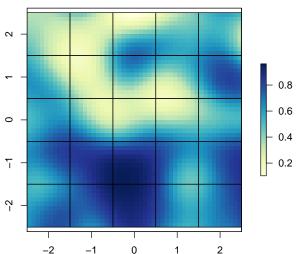


Figure 21 Distribution map of a species simulated using Gaussian processes. See Figure 2 caption for conventions.

```
# plot distribution of each dimension in the attribute space across geographic space
plot(
    sim_gspace,
    main=c('Attribute space (d=1)', 'Attribute space (d=2)', 'Attribute space (d=3)'),
    addfun=function(){lines(sim_pus)},
    nc=3
)
```

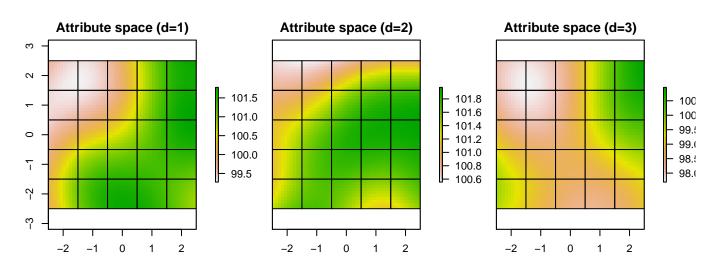


Figure 22 Distribution of spatial variables across the species' geographic range. These variables each represent a dimension of a three-dimensional attribute space.

#### Distance metrics

For each different distance metric, we will update the sim\_gru object with the new distance metric, solve it, and store the solution in a list.

```
# create vector with distance metrics
dist.metrics <- c(</pre>
    'euclidean', 'bray', 'manhattan', 'gower',
    'canberra', 'mahalanobis',
    'jaccard', 'kulczynski'
# generate solutions
solutions <- list()</pre>
for (i in dist.metrics) {
    solutions[[i]] <- update(sim_ru_gp, distance.metric=i)</pre>
}
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
     Matrix range
                     [3e-01, 3e+04]
##
     Objective range [1e+00, 1e+00]
##
                     [1e+00, 1e+00]
##
     Bounds range
     RHS range
                      [1e+00, 5e+03]
## Presolve removed 248 rows and 143 columns
## Presolve time: 0.14s
## Presolved: 1054 rows, 1132 columns, 5329 nonzeros
## Variable types: 0 continuous, 1132 integer (1132 binary)
## Found heuristic solution: objective 19.0000000
## Presolved: 1054 rows, 1132 columns, 5329 nonzeros
## Presolve removed 1054 rows and 1132 columns
##
## Root relaxation: objective 4.583726e+00, 701 iterations, 0.04 seconds
##
##
       Nodes
                     Current Node
                                            Objective Bounds
                                                                         Work
    Expl Unexpl |
                   Obj Depth IntInf | Incumbent
##
                                                     BestBd
                                                               Gap | It/Node Time
##
##
        0
                   4.58373
                                   69
                                        19.00000
                                                     4.58373
                                                              75.9%
                                                                              0s
## H
        0
                                       5.0000000
                                                     4.58373 8.33%
                                                                              0s
##
## Explored O nodes (701 simplex iterations) in 0.21 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.00000000000e+00, gap 0.0%
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
```

```
Matrix range
                     [8e-06, 1e+00]
##
##
     Objective range [1e+00, 1e+00]
     Bounds range
                     [1e+00, 1e+00]
##
                     [4e-02, 3e+00]
##
     RHS range
## Presolve removed 185 rows and 134 columns
## Presolve time: 0.21s
## Presolved: 1117 rows, 1141 columns, 5590 nonzeros
## Variable types: 0 continuous, 1141 integer (1141 binary)
## Found heuristic solution: objective 19.0000000
## Presolve removed 22 rows and 0 columns
## Presolved: 1095 rows, 1141 columns, 5479 nonzeros
##
## Presolve removed 493 rows and 91 columns
##
## Root relaxation: objective 4.419702e+00, 718 iterations, 0.05 seconds
##
##
       Nodes
                     Current Node
                                            Objective Bounds
                                                                        Work
   Expl Unexpl |
                   Obj Depth IntInf | Incumbent
                                                     BestBd
                                                              Gap | It/Node Time
##
##
##
        0
              0
                   4.41970
                              0
                                  43
                                        19.00000
                                                    4.41970
                                                             76.7%
                                                                             0s
## H
                                       5.0000000
        0
              0
                                                    4.41970
                                                             11.6%
                                                                             0s
##
## Explored O nodes (718 simplex iterations) in 0.31 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.00000000000e+00, gap 0.0%
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
##
     Matrix range
                     [3e-01, 9e+04]
     Objective range [1e+00, 1e+00]
##
##
     Bounds range
                     [1e+00, 1e+00]
##
     RHS range
                     [1e+00, 1e+04]
## Presolve removed 236 rows and 134 columns
## Presolve time: 0.14s
## Presolved: 1066 rows, 1141 columns, 5541 nonzeros
## Variable types: 0 continuous, 1141 integer (1141 binary)
## Found heuristic solution: objective 19.0000000
## Found heuristic solution: objective 18.0000000
## Presolved: 1066 rows, 1141 columns, 5541 nonzeros
##
## Presolve removed 1066 rows and 1141 columns
## Root relaxation: objective 4.422638e+00, 738 iterations, 0.04 seconds
##
##
                     Current Node
                                     Objective Bounds
##
    Expl Unexpl | Obj Depth IntInf | Incumbent
                                                     BestBd
                                                              Gap | It/Node Time
##
```

```
4.42264
                                  43
                                       18,00000
                                                    4.42264
                                                             75.4%
##
              0
                              0
                                                                             0s
## H
        0
              0
                                       5.0000000
                                                    4.42264 11.5%
                                                                             0s
##
## Explored O nodes (738 simplex iterations) in 0.21 seconds
## Thread count was 1 (of 2 available processors)
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.00000000000e+00, gap 0.0%
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
                     [5e-02, 1e+03]
##
     Matrix range
     Objective range [1e+00, 1e+00]
##
                     [1e+00, 1e+00]
     Bounds range
##
##
     RHS range
                     [1e+00, 2e+02]
## Presolve removed 223 rows and 123 columns
## Presolve time: 0.15s
## Presolved: 1079 rows, 1152 columns, 5990 nonzeros
## Variable types: 0 continuous, 1152 integer (1152 binary)
## Found heuristic solution: objective 18.0000000
## Presolved: 1079 rows, 1152 columns, 5990 nonzeros
##
## Presolve removed 1079 rows and 1152 columns
## Root relaxation: objective 4.300502e+00, 706 iterations, 0.04 seconds
##
                     Current Node
                                            Objective Bounds
##
       Nodes
                                      ##
   Expl Unexpl |
                   Obj Depth IntInf | Incumbent
                                                     BestBd
                                                              Gap | It/Node Time
##
        0
##
              0
                   4.30050
                              0
                                  70
                                        18.00000
                                                    4.30050
                                                             76.1%
                                                                             0s
## H
        0
              0
                                       5.0000000
                                                    4.30050
                                                             14.0%
                                                                             0s
## Explored O nodes (706 simplex iterations) in 0.23 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.00000000000e+00, gap 0.0%
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
                     [7e-05, 2e+00]
##
     Matrix range
##
     Objective range [1e+00, 1e+00]
     Bounds range
                     [1e+00, 1e+00]
##
                     [3e-01, 3e+00]
##
     RHS range
## Presolve removed 230 rows and 134 columns
## Presolve time: 0.14s
## Presolved: 1072 rows, 1141 columns, 5485 nonzeros
## Variable types: 0 continuous, 1141 integer (1141 binary)
## Found heuristic solution: objective 19.0000000
## Presolve removed 3 rows and 0 columns
```

```
## Presolved: 1069 rows, 1141 columns, 5465 nonzeros
##
## Presolve removed 1042 rows and 626 columns
##
## Root relaxation: objective 4.428373e+00, 571 iterations, 0.04 seconds
##
##
       Nodes
                     Current Node
                                            Objective Bounds
##
   Expl Unexpl | Obj Depth IntInf | Incumbent
                                                     BestBd
                                                              Gap | It/Node Time
##
##
        0
              0
                   4.42837
                              0
                                  43
                                        19.00000
                                                    4.42837
                                                             76.7%
                                                                             0s
        0
              0
                                                                            0s
## H
                                       5.0000000
                                                    4.42837
                                                             11.4%
##
## Explored O nodes (571 simplex iterations) in 0.22 seconds
## Thread count was 1 (of 2 available processors)
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.00000000000e+00, gap 0.0%
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
     Matrix range
                     [3e-01, 5e+04]
##
     Objective range [1e+00, 1e+00]
##
                     [1e+00, 1e+00]
     Bounds range
##
     RHS range
                     [1e+00, 9e+03]
## Presolve removed 415 rows and 381 columns
## Presolve time: 0.12s
## Presolved: 887 rows, 894 columns, 6274 nonzeros
## Variable types: 0 continuous, 894 integer (894 binary)
## Found heuristic solution: objective 21.0000000
## Presolve removed 13 rows and 0 columns
## Presolved: 874 rows, 894 columns, 6203 nonzeros
##
## Presolve removed 874 rows and 894 columns
##
## Root relaxation: objective 9.752283e+00, 244 iterations, 0.03 seconds
##
##
       Nodes
                     Current Node
                                            Objective Bounds
                                                                        Work
    Expl Unexpl |
                   Obj Depth IntInf | Incumbent
                                                     BestBd
                                                              Gap | It/Node Time
##
        0
                   9.75228
                              0
                                        21.00000
##
                                  23
                                                    9.75228
                                                             53.6%
                                                                             0s
## H
        0
              0
                                      10.0000000
                                                    9.75228 2.48%
                                                                             0s
##
## Explored O nodes (244 simplex iterations) in 0.18 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 1.000000000000e+01, best bound 1.00000000000e+01, gap 0.0%
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
```

```
[3e-05, 1e+00]
##
     Matrix range
##
     Objective range [1e+00, 1e+00]
     Bounds range
                     [1e+00, 1e+00]
##
                     [1e-01, 3e+00]
##
     RHS range
## Presolve removed 207 rows and 134 columns
## Presolve time: 0.18s
## Presolved: 1095 rows, 1141 columns, 5597 nonzeros
## Variable types: 0 continuous, 1141 integer (1141 binary)
## Found heuristic solution: objective 19.0000000
## Presolve removed 13 rows and 0 columns
## Presolved: 1082 rows, 1141 columns, 5516 nonzeros
##
## Presolve removed 833 rows and 282 columns
##
## Root relaxation: objective 4.429824e+00, 591 iterations, 0.04 seconds
##
##
       Nodes
                     Current Node
                                            Objective Bounds
                                                                         Work
    Expl Unexpl |
                                                     BestBd
                                                              Gap | It/Node Time
##
                   Obj Depth IntInf | Incumbent
##
##
        0
              0
                   4.42982
                              0
                                   43
                                        19.00000
                                                    4.42982
                                                             76.7%
                                                                             0s
## H
        0
              0
                                      17.0000000
                                                    4.42982
                                                             73.9%
                                                                             0s
## H
        0
              0
                                       5.0000000
                                                    4.42982
                                                             11.4%
                                                                             0s
## Explored O nodes (591 simplex iterations) in 0.27 seconds
## Thread count was 1 (of 2 available processors)
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.00000000000e+00, gap 0.0%
## Optimize a model with 1302 rows, 1275 columns and 5025 nonzeros
## Coefficient statistics:
                     [8e-06, 1e+00]
##
     Matrix range
##
     Objective range [1e+00, 1e+00]
##
     Bounds range
                     [1e+00, 1e+00]
                     [3e-02, 3e+00]
##
     RHS range
## Presolve removed 184 rows and 134 columns
## Presolve time: 0.21s
## Presolved: 1118 rows, 1141 columns, 5819 nonzeros
## Variable types: 0 continuous, 1141 integer (1141 binary)
## Found heuristic solution: objective 19.0000000
## Presolve removed 16 rows and 0 columns
## Presolved: 1102 rows, 1141 columns, 5735 nonzeros
##
## Presolve removed 443 rows and 91 columns
##
## Root relaxation: objective 4.432050e+00, 692 iterations, 0.05 seconds
##
##
       Nodes
                     Current Node
                                            Objective Bounds
                                                                         Work
## Expl Unexpl | Obj Depth IntInf | Incumbent
                                                              Gap | It/Node Time
                                                     BestBd
```

```
##
##
             0
                   4.43205
                              0
                                  43
                                       19.00000
                                                   4.43205 76.7%
                                                                           0s
        0
                                      5.0000000
## H
        0
             0
                                                   4.43205 11.4%
                                                                           0s
##
## Explored O nodes (692 simplex iterations) in 0.30 seconds
## Thread count was 1 (of 2 available processors)
## Optimal solution found (tolerance 5.00e-02)
## Best objective 5.000000000000e+00, best bound 5.00000000000e+00, gap 0.0%
```

Now, let's plot the solutions to see how they differ.

```
# set plotting window
par(mfrow=c(3,3), mar=c(0, 0, 4.1, 0))
## create plots showing the selected planning units (dark green)
for (i in seq_along(solutions)) {
    # plot i'th solution
    plot(
        sim_pus,
        main=dist.metrics[i],
        col=replace(
            rep('#ccece6',nrow(sim_pus@data)),
            which(selections(solutions[[i]])==1),
            '#00441b'
        ),
        axes=FALSE
    )
}
# reset plotting window
par(mfrow=c(1,1), mar=c(5.1, 4.1, 4.1, 2.1))
```

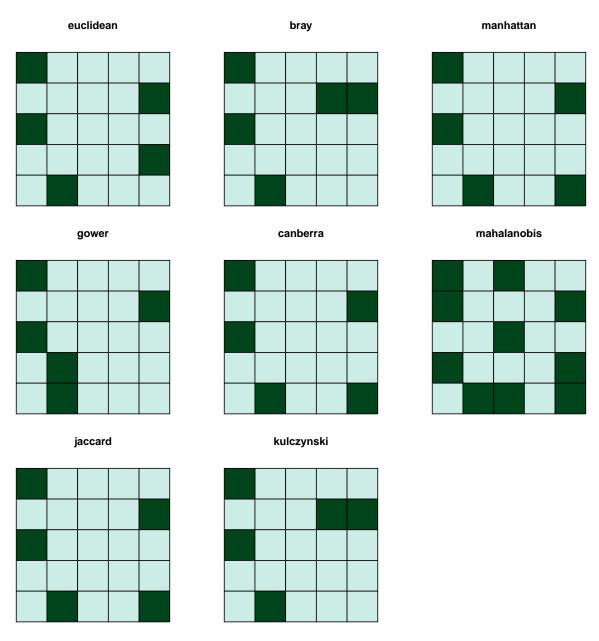


Figure 23 Prioritisations generated using different distance metrics. See Figure 12 for conventions.

It appears that main difference between the solutions is which planning units get selected in the bottom section of the study area. Some solutions tend to select a lot of planning units in this region (eg. Canberra, Euclidean, Gower, and Manhattan), whereas others select fewer planning units (eg. Bray-Curtis, Jaccard, and Kulczynski). Additionally, the Mahalanobis-based solution contains substantially more planning units than any other solution. Conservation planners should think carefully which distance metric is most appropriate for their attribute spaces. See the discussion section below for guidelines on selecting an appropriate distance metric.

### Case-study examples

#### Overview

Here we will investigate how space-based targets can affect prioritisations using a more realistic dataset. We will generate prioritisations for the four bird species—blue-winged kookaburra, brown-backed honeyeater, brown falcon, pale-headed rosella—in Queensland, Australia. This region contains a broad range of different habitats—such as rainforests, woodlands, and deserts—making it ideal for this tutorial. First, we will generate a typical amount-based prioritisation that aims to capture 20% of the species' distributions. Then we will generate a prioritisation that also aims to secure populations in representative parts of the species' distributions in terms of their geographic location and their environmental heterogeneity. To do this we will generate a prioritisation using 20% amount-based targets and 85% space-based targets. Finally, we will compare these prioritisations to Australia's existing protected network.

#### Data

Survey data for the species were obtained from BirdLife Australia. The survey data was rarefied using a 100 km<sup>2</sup> grid, wherein the survey with the greatest number of repeat visits in each grid cell was chosen. To model the distribution of each species, environmental data were obtained at survey location (site). Specifically, climatic data (bio1, bio4, bio15, bio16, bio17) and classifications of the vegetation at the site were used. Occupancy-detection models (MacKenzie et al. 2002) were fit using Stan (Stan Development Team 2015) using manually tuned parameters (adapt deta=0.9, maximum treedepth=20, chains=4, warmup iterations=1000, total iterations=1500) with five-fold cross-validation. In each replicate, data were partitioned into training and test sites. A full model was fit using quadratic terms for environmental variables in the site-component, and an intercept in the detection-component of the model. The full model was then subject to a step-wise backwards term deletion routine. Terms were retained when their inclusion resulted in a model with a greater area under the curve (AUC) value as calculated using the test data. Maps were generated for each species as an average of the predictions from the best model in each best replicate. To further improve the accuracy of these maps, areas well outside of the species' known distributions were set to 0. For each species, this was achieved by masking out biogeographic regions where the species was not observed, and regions that did not have a neighbouring planning unit where the species was observed. The maps were then resampled (10 km<sup>2</sup> resolution) and cropped to the study area. The resulting maps are stored in the cs spp object.

```
# load data
data(cs_spp)

# plot species' distributions
plot(cs_spp, main=c(
    "Blue-winged kookaburra", "Brown-backed honeyeater",
    "Brown falcon", "Pale-headed rosella"
))
```

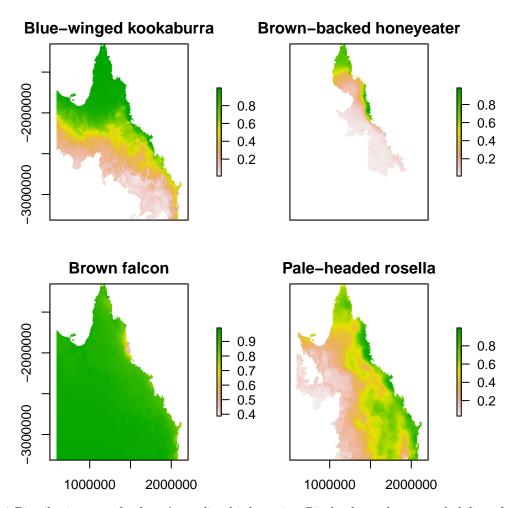


Figure 24 Distribution map for four Australian bird species. Pixel colours denote probability of occupancy.

Planning units (50km² resolution) were generated across Australia, and then clipped to the Queensland state borders and coastline. Note that we are using excessively coarse planning units so that our examples will complete relatively quickly. In a real-world planning exercise, we would use much finer planning units. To compare our prioritisations to Queensland's existing protected area network, this network was intersected with the planning units. Planning units with more than 50% of their area inside a protected area had their status set to 2 (following conventions in Marxan). Since we do not have cost data, the prioritisations will aim to select the minimum number of planning units required to meet the targets. The planning units are stored in the cs\_pu object.

```
# load data
data(cs_pus)

## plot planning units
# convert SpatialPolygons to PolySet for quick plotting
cs_pus2 <- SpatialPolygons2PolySet(cs_pus)

# create vector of colours for planning units</pre>
```

```
# + light green: units not already inside reserve
# + yellow: units already inside reserve
cs_pus_cols <- rep('#c7e9c0', nrow(cs_pus@data))
cs_pus_cols[which(cs_pus$status==2)] <- 'yellow'

# set plotting window
par(mar=c(0.1, 0.1, 4.1, 0.1))

# plot polygons
PBSmapping::plotPolys(
    cs_pus2, col=cs_pus_cols, border='gray30',
    xlab='', ylab='', axes=FALSE,
    main='Case-study planning units',
    cex=1.8
)</pre>
```

# Case-study planning units

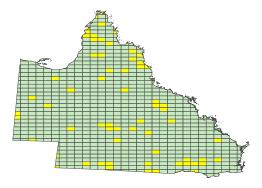


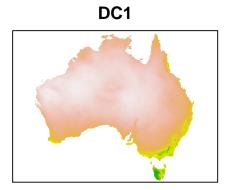
Figure 25 Planning units for the case-study examples. Polygons denote planning units. Yellow units have more than 50% of their area already in a reserve.

```
# reset plotting window
par(mar=c(5.1, 4.1, 4.1, 2.1))
```

To map the distribution of environmental conditions across the species' range, 21 bioclimatic layers were obtained. These layers were cropped to Australia and subject to detrended correspondence analysis to produce two new variables. These layers are stored in the cs\_space object.

```
# load data
data(cs_space)

# plot variables
plot(cs_space, main=c('DC1', 'DC2'), legend=FALSE, axes=FALSE)
```



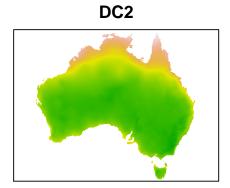


Figure 26 Broad-scale environmental variation across Australia. The variable DC1 describes the transition from wet and cool to dry and hot conditions. The variable DC2 describes the transition from wet and hot to dry and cool conditions.

### Effectiveness of Australia's reserve network compared to optimal prioritisations

To simplify the process of formatting data and generating prioritisations, we can use the rap function. First, we will generate an amount-based prioritisation that aims to capture 20% of the rosella's range. We will use 50 demand points to map the geographic and environmental spaces. Be warned, the examples hereafter can take 5-10 minutes to run.

```
# make amount-based prioritisation,
# and ignore existing protected areas by discarding values in the
# status (third) column of the attribute table
cs_rs_amount <- rap(
    cs_pus[,-2], cs_spp, cs_space,
  amount.target=0.2, space.target=NA, n.demand.points=50L,
  include.geographic.space=TRUE, formulation='unreliable',
  solve=FALSE
)
## Warning in (function (pus, species, spaces = NULL, amount.target = 0.2, :
## argument to pus does not have a 'status' column, creating default with all
## status=0L
# threshold probabilities to 0.1 for space calculations
cs_rs_amount <- prob.subset(cs_rs_amount, species=1:4, threshold=rep(0.1,4))</pre>
# generate prioritisation
cs_rs_amount <- solve(cs_rs_amount)</pre>
## Optimize a model with 4 rows, 762 columns and 2001 nonzeros
## Coefficient statistics:
                     [3e+02, 2e+04]
##
    Matrix range
```

```
##
     Objective range [1e+00, 1e+00]
##
     Bounds range
                     [1e+00, 1e+00]
                     [2e+05, 3e+06]
##
     RHS range
## Found heuristic solution: objective 176
## Presolve time: 0.01s
## Presolved: 4 rows, 762 columns, 2001 nonzeros
## Variable types: 0 continuous, 762 integer (762 binary)
## Presolved: 4 rows, 762 columns, 2001 nonzeros
##
##
## Root relaxation: objective 1.359167e+02, 832 iterations, 0.01 seconds
##
                     Current Node
##
       Nodes
                                     Objective Bounds
                                                                        Work
   Expl Unexpl | Obj Depth IntInf | Incumbent
                                                    BestBd
##
                                                             Gap | It/Node Time
##
##
                135.91668
                                   4 176.00000 135.91668
                                                            22.8%
                                                                            0s
        0
## H
        0
                                    136.0000000 135.91668 0.06%
                                                                            0s
##
## Explored O nodes (832 simplex iterations) in 0.03 seconds
## Thread count was 1 (of 2 available processors)
## Optimal solution found (tolerance 5.00e-02)
## Best objective 1.360000000000e+02, best bound 1.36000000000e+02, gap 0.0%
## Warning in validityMethod(object): object@space.held contains values less
## than 0, some species are really poorly represented
# show summary
summary(cs_rs_amount)
##
     Run_Number Status Score Cost Planning_Units Connectivity_Total
## 1
              1 MANUAL
                         136 136
                                             136
     Connectivity_In Connectivity_Edge Connectivity_Out
##
             9636021
                              81120163
## 1
                                                8126230
     Connectivity_In_Fraction
##
## 1
                   0.09744929
# plot prioritisation
plot(cs rs amount, 1)
```

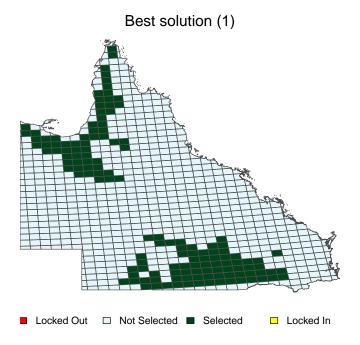


Figure 27 Multi-species prioritisation generated for four bird species using amount-based targets (20%). See Figure 12 captions for conventions.

We can also see how well the prioritisation secures the species' distributions in the geographic and environmental attribute spaces.

```
# plot prioritisation in geographic attribute space
p1 <- space.plot(cs_rs_amount, 1, 2, main='Blue-winged kookaburra')
p2 <- space.plot(cs_rs_amount, 2, 2, main='Brown-backed honeyeater')
p3 <- space.plot(cs_rs_amount, 3, 2, main='Brown falcon')
p4 <- space.plot(cs_rs_amount, 4, 2, main='Pale-headed rosella')
gridExtra::grid.arrange(p1, p2, p3, p4, ncol=2)</pre>
```

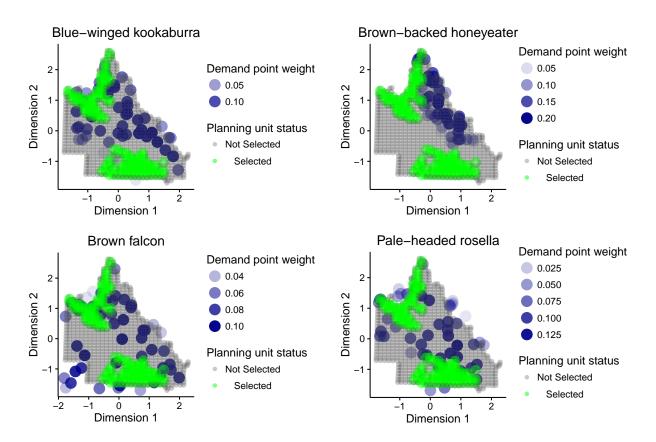
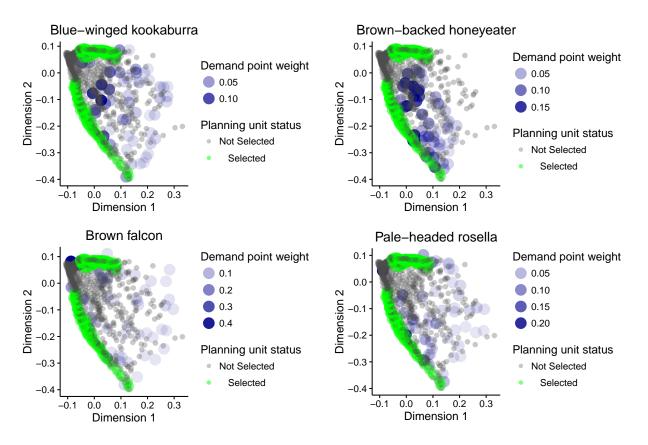


Figure 28 Distribution of amount-based prioritisation in the geographic attribute space. Points denote combinations of environmental conditions. Green and grey points represent planning unit selected for and not selected for prioritisation (respectively). Blue points denote demand points, and their size indicates their weighting.

```
# plot prioritisation in environmental attribute space
p1 <- space.plot(cs_rs_amount, 1, 1, main='Blue-winged kookaburra')
p2 <- space.plot(cs_rs_amount, 2, 1, main='Brown-backed honeyeater')
p3 <- space.plot(cs_rs_amount, 3, 1, main='Brown falcon')
p4 <- space.plot(cs_rs_amount, 4, 1, main='Pale-headed rosella')
gridExtra::grid.arrange(p1, p2, p3, p4, ncol=2)</pre>
```



**Figure 29** Distribution of amount-based prioritisation in the environmental attribute space. See Figure 28 caption for conventions.

Next, let's generate a prioritisation using amount- and space-based targets. This prioritisation will secure 50% of the species distribution in geographic and environmental space.

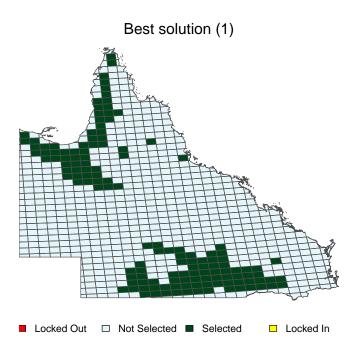
```
# make amount- and space-based prioritisation
cs_rs_space <- update(cs_rs_amount, space.target=0.5)</pre>
## Optimize a model with 200512 rows, 200862 columns and 802401 nonzeros
## Coefficient statistics:
                     [2e-11, 2e+04]
##
     Matrix range
     Objective range [1e+00, 1e+00]
##
                     [1e+00, 1e+00]
##
     Bounds range
##
     RHS range
                     [3e-03, 3e+06]
  Warning: Model contains large matrix coefficient range
##
            Consider reformulating model or setting NumericFocus parameter
##
##
            to avoid numerical issues.
## Presolve removed 537 rows and 493 columns (presolve time = 5s) ...
## Presolve removed 566 rows and 493 columns (presolve time = 10s) ...
## Presolve removed 629 rows and 493 columns (presolve time = 15s) ...
## Presolve removed 657 rows and 493 columns (presolve time = 20s) ...
## Presolve removed 736 rows and 493 columns (presolve time = 25s) ...
```

```
## Presolve removed 786 rows and 493 columns (presolve time = 30s) ...
## Presolve removed 819 rows and 529 columns (presolve time = 35s) ...
## Presolve removed 819 rows and 529 columns (presolve time = 40s) ...
## Presolve removed 893 rows and 529 columns (presolve time = 45s) ...
## Presolve removed 893 rows and 529 columns (presolve time = 50s) ...
## Presolve removed 893 rows and 529 columns (presolve time = 55s) ...
## Presolve removed 893 rows and 529 columns (presolve time = 60s) ...
## Presolve removed 893 rows and 529 columns (presolve time = 65s) ...
## Presolve removed 916 rows and 529 columns (presolve time = 70s) ...
## Presolve removed 937 rows and 529 columns (presolve time = 75s) ...
## Presolve removed 937 rows and 529 columns (presolve time = 80s) ...
## Presolve removed 937 rows and 529 columns (presolve time = 85s) ...
## Presolve removed 1060 rows and 529 columns (presolve time = 90s) ...
## Presolve removed 1083 rows and 529 columns (presolve time = 95s) ...
## Presolve removed 1116 rows and 529 columns (presolve time = 100s) ...
## Presolve removed 1147 rows and 529 columns (presolve time = 105s) ...
## Presolve removed 1147 rows and 529 columns (presolve time = 110s) ...
## Presolve removed 1153 rows and 529 columns (presolve time = 115s) ...
## Presolve removed 1153 rows and 529 columns (presolve time = 120s) ...
## Presolve removed 1179 rows and 529 columns (presolve time = 125s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 130s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 135s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 141s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 145s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 150s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 155s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 160s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 165s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 170s) ...
## Presolve removed 1191 rows and 529 columns (presolve time = 175s) ...
## Presolve removed 1191 rows and 967 columns (presolve time = 180s) ...
## Presolve removed 1191 rows and 967 columns (presolve time = 185s) ...
## Presolve removed 1191 rows and 967 columns (presolve time = 190s) ...
## Presolve removed 1191 rows and 967 columns (presolve time = 195s) ...
## Presolve removed 1591 rows and 967 columns (presolve time = 200s) ...
## Presolve removed 1672 rows and 967 columns (presolve time = 205s) ...
## Presolve removed 1729 rows and 967 columns (presolve time = 210s) ...
## Presolve removed 1765 rows and 967 columns (presolve time = 215s) ...
## Presolve removed 1789 rows and 967 columns (presolve time = 220s) ...
## Presolve removed 1806 rows and 967 columns (presolve time = 225s) ...
## Presolve removed 1806 rows and 967 columns (presolve time = 230s) \dots
## Presolve removed 1806 rows and 967 columns (presolve time = 235s) ...
## Presolve removed 1806 rows and 967 columns (presolve time = 240s) ...
## Presolve removed 1806 rows and 967 columns (presolve time = 245s) ...
## Presolve removed 1806 rows and 967 columns
## Presolve time: 247.81s
## Presolved: 198706 rows, 199895 columns, 802062 nonzeros
## Variable types: 0 continuous, 199895 integer (199895 binary)
```

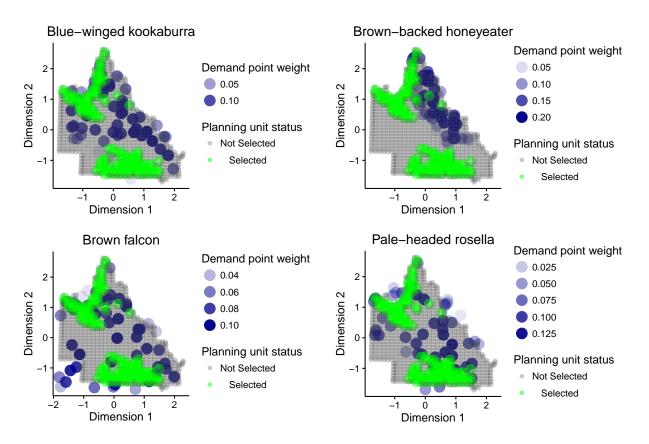
```
## Found heuristic solution: objective 236.0000000
## Presolve removed 246 rows and 0 columns (presolve time = 5s) ...
## Presolve removed 248 rows and 0 columns (presolve time = 10s) ...
## Presolve removed 248 rows and 0 columns (presolve time = 15s) ...
## Presolve removed 248 rows and 0 columns
## Presolved: 198458 rows, 199895 columns, 801255 nonzeros
##
## Presolve removed 195493 rows and 9695 columns
## Root simplex log...
##
## Iteration
                                Primal Inf.
                Objective
                                                Dual Inf.
                                                               Time
                                                               272s
               0.000000e+00
##
          0
                               4.676020e+01
                                               1.178365e+10
##
       6577
               1.3949729e+02
                               0.00000e+00
                                               8.922430e+02
                                                               275s
##
      10952
               1.3796623e+02
                               0.000000e+00
                                               1.033107e+03
                                                               280s
##
      15328
               1.3750019e+02
                               0.000000e+00
                                               1.563778e+03
                                                               285s
##
      19702
               1.3707462e+02
                               0.000000e+00
                                               1.270111e+03
                                                               290s
##
      24562
               1.3689079e+02
                                                               295s
                               0.000000e+00
                                               4.471597e+05
      27479
               1.3634176e+02
                               0.000000e+00
##
                                               1.921086e+03
                                                               300s
##
      32339
               1.3607752e+02
                               0.000000e+00
                                               7.979122e+02
                                                               305s
##
      37442
               1.3602078e+02
                               0.000000e+00
                                               2.325462e+02
                                                               310s
##
      40844
               1.3599476e+02
                               0.000000e+00
                                               6.299705e+01
                                                               315s
##
      41032
               1.3599204e+02
                               0.000000e+00
                                               0.000000e+00
                                                               316s
##
      41032
               1.3599204e+02
                               0.000000e+00
                                               0.000000e+00
                                                               316s
##
## Root relaxation: objective 1.359920e+02, 41032 iterations, 64.68 seconds
##
##
       Nodes
                     Current Node
                                            Objective Bounds
                                                                        Work
##
    Expl Unexpl | Obj Depth IntInf | Incumbent
                                                     BestBd
                                                              Gap | It/Node Time
##
        0
                 135.99204
                              0 189
                                      236.00000
                                                 135.99204
                                                             42.4%
##
              0
                                                                          319s
## H
        0
                                    137.0000000
                                                 135.99204
                                                             0.74%
                                                                          320s
##
## Explored O nodes (53801 simplex iterations) in 320.95 seconds
## Thread count was 1 (of 2 available processors)
##
## Optimal solution found (tolerance 5.00e-02)
## Best objective 1.370000000000e+02, best bound 1.36000000000e+02, gap 0.7299%
# show summary
summary(cs_rs_space)
     Run_Number Status Score Cost Planning_Units Connectivity_Total
##
## 1
              1 MANUAL
                         137
                             137
                                              137
                                                            98882414
     Connectivity_In Connectivity_Edge Connectivity_Out
##
## 1
             9738090
                              80918598
                                                 8225726
     Connectivity_In_Fraction
##
```

## 1 0.09848151

```
# plot prioritisation
plot(cs_rs_space,1)
```



```
# plot prioritisation in geographic attribute space
p1 <- space.plot(cs_rs_space, 1, 2, main='Blue-winged kookaburra')
p2 <- space.plot(cs_rs_space, 2, 2, main='Brown-backed honeyeater')
p3 <- space.plot(cs_rs_space, 3, 2, main='Brown falcon')
p4 <- space.plot(cs_rs_space, 4, 2, main='Pale-headed rosella')
gridExtra::grid.arrange(p1, p2, p3, p4, ncol=2)</pre>
```



**Figure 30** Distribution of the amount- and space-based prioritisation in the geographic attribute space. See Figure 28 caption for conventions.

```
# plot prioritisation in environmental attribute space
p1 <- space.plot(cs_rs_space, 1, 1, main='Blue-winged kookaburra')
p2 <- space.plot(cs_rs_space, 2, 1, main='Brown-backed honeyeater')
p3 <- space.plot(cs_rs_space, 3, 1, main='Brown falcon')
p4 <- space.plot(cs_rs_space, 4, 1, main='Pale-headed rosella')
gridExtra::grid.arrange(p1, p2, p3, p4, ncol=2)</pre>
```

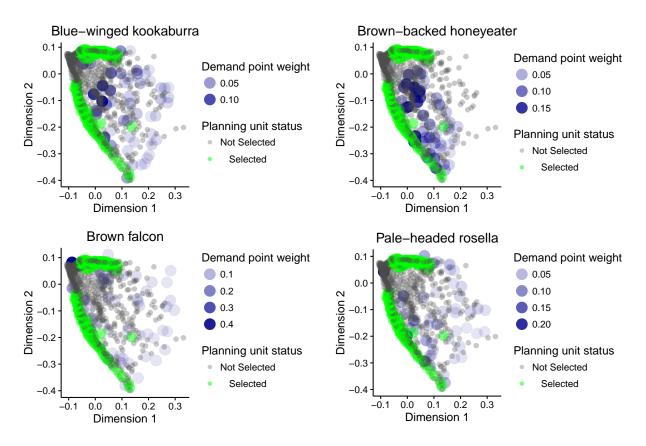


Figure 31 Distribution of the amount- and space-based prioritisation in the environmental attribute space. See Figure 28 caption for conventions.

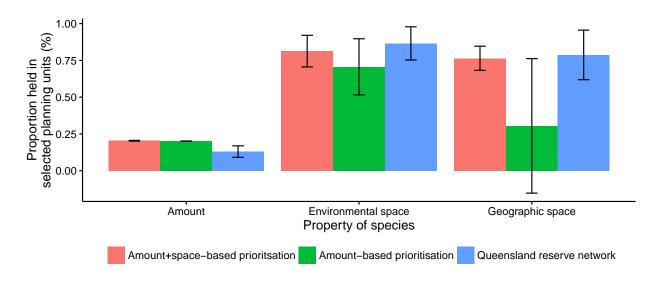
Let's compare these prioritisations with Queensland's existing protected areas system. To do this, we can create update the cs\_rs\_space with manually specified solutions to create a RapSolved object to represent the Queensland's reserve network.

```
# generate vector with Australia's selections
aus_selections <- which(cs_pus$status>0)

# create new object with Australia's network
cs_rs_aus <- update(cs_rs_amount, b=aus_selections)</pre>
```

Now, let's plot the performance metrics for these prioritisations.

```
variable=rep(c('Amount', 'Geographic space', 'Environmental space'), each=12),
    species=colnames(amount.held(cs_rs_amount)),
   value=c(
        amount.held(cs_rs_amount)[1,], amount.held(cs_rs_space)[1,],
            amount.held(cs rs aus)[1,],
        space.held(cs_rs_amount, space=2)[1,], space.held(cs_rs_space, space=2)[1,],
            space.held(cs_rs_aus, space=2)[1,],
        space.held(cs_rs_amount, space=1)[1,], space.held(cs_rs_space, space=1)[1,],
            space.held(cs_rs_aus, space=1)[1,]
) %>% group_by(
   name,
    variable
) %>% summarise(
   mean=mean(value),
   se=se(value)
)
# plot the performance metrics
ggplot(aes(x=variable, y=mean, fill=name), data=cs_results) +
    geom_bar(position=position_dodge(0.9), stat='identity') +
   geom_errorbar(
        aes(ymin=mean-se, ymax=mean+se), position=position dodge(0.9),
        width=0.2
   ) +
   xlab('Property of species') +
   ylab('Proportion held in\nselected planning units (%)') +
   scale_fill_discrete(
       name=''
   ) +
   theme_classic() +
    theme(legend.position='bottom',legend.direction='horizontal')
```



We can see that a greater number of planning units is needed to satisfy the space-based targets. The prioritisation generated using just amount-based targets has 136 planning units, and the prioritisations using amount-based and space-based targets has 137 targets. These results suggest that prioritisations generated using only amount-based targets can obtain a moderately representative sample of the species' geographic distribution and climatic niche.

# Implications and future directions

The rapr R package provides a unified approach to reserve selection. This R package provides decision makers with the tools to generate prioritisations that secure both biodiversity patterns and processes. Additionally, the package contains funcionality to accommodate uncertainty in the distribution of features, and also identify suitably connected reserves. Both the simulated and case-study species suggest that conservation planning exercises need to explicitly consider biodiversity processes during the reserve selection process to capture them.

One of the key advantages of the rapr R package is that it is general enough that any spatial variation could be considered an attribute space, regardless of whether this variation is intrinsic or extrinsic to the feature(s). For example, advances in genomic fields produced high resolution data on genetic information (eg. amplified fragment length polymorphisms, AFLPs; single nucleotide polymorphisms, SNPs). By using geostatistical analysis (eg. generalised dissimilarity modelling GDMs and gradient forests; Ferrier et al. 2007; Ellis et al. 2012), this data has been used to generate maps describing the spatial distribution of genomic variation within a species (Thomassen et al. 2010; Fitzpatrick and Keller 2015). These maps in turn could be used to construct a genomic attribute space, and in turn, could be used to generate prioritisations that secure a representative sample of genomic variation within a species. However, because the problem formulations used in this package are so general, the tools in this package could be misused, and generate poor quality prioritisations.

The degree to which a prioritisation truly secures a representative sample of a feature depends on the attribute spaces and distribution of demand points chosen by the decision maker. Ultimately, the space-based targets are set as a proportion based on the distribution of the demand-points. As a consequence, if the decision maker uses an inappropriate set of spatial variables to construct an attribute space, or an inappropriate set of demand points, then the optimal solution based on this data will not actually be an effective prioritisation. We therefore stress that decision makers must carefully consider which biodiversity processes need to preserved in the prioritisation, and what spatial data can be used to map these processes. To assist in the selection of appropriate demand points, the R package provides several routines for generating demand points (see the make.DemandPoints function). These routines essentially use the distribution of a feature in the attribute space to define a polygon. Demand points are then generated as random points within the polygon. A kernel is then fit to the distribution of the feature in the space (using Blonder et al. 2014; Duong 2015), and the demand points are weighted based on the estimated density of the feature at the demand points' coordinates.

The rapr R package could be further extended to identify more effective prioritisations. First, the formulation of fragmentation used in this package may be too simplistic in some cases (eg. exercises involving multiple species with different dispersal capabilities), and more realistic measures of fragmentation (eg. those used in Zonation) could be used to identify more effective prioritisations. Second, the problem does not consider temporal dynamics. Here, conservation actions are assumed to be implemented simultaneously in all selected planning units and assumed to remain implemented for all time. As a consequence, this R package is not useful for scenarios where actions are implemented during multiple discrete periods in time (eg. actions are made adue to annual funding cycles), or scenarios involving threatening processes that vary across space and time (reviewed in Pressey et al. 2007). Future research may look into incorporating such elements into this R package.

To maximise the long-term persistence of biodiversity—the stated goal of conservation—decision makers need to identify prioritisations that preserve existing patterns of biodiversity and the processes that support them. To achieve this, conservation planners need a decision support tool that can explicitly accommodate biodiversity patterns and processes. Here, we developed the rapr R package to fill this void. By exploring the functiontality of this package using several simulated species, we found that including space-based targets can radically change a prioritisation for the simplest of species.

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