大同大學 106 學年度第 1 學期期中考試試題

科目代號:G1011 科目名稱: 微積分 (一) 班級: XXXX 座號: 姓名: 註: 本次考試不可參考自己的書籍、筆記。不可用計算機、電子辭典。

1. Find the limits.

$$(5\%)(a.) \lim_{x \to 0} \frac{\sin^3(3x)}{x^3}, \qquad (5\%)(b.) \lim_{x \to 0} \frac{x}{\sqrt{4 + 2x} - \sqrt{4 - 2x}}.$$

2. Find the derivative y' of the followings.

$$(5\%)(a.) \ y = 3\sqrt[5]{x} - \frac{3x}{\sqrt{x}} + \frac{4}{x^2},$$
 (5%)(b.) $y = x^6 e^x \cos x,$ (5%)(c.) $y = (3x^3 - 2x^2 + 4)^{12},$ (5%)(d.) $y = \frac{x^3 - 6}{x^6 + 3x}$ (use the Quotient Rule).

- 3. (10%) Find an equation of the tangent line(切線) to the graph of $f(x) = \ln(x^2 + 1)$ when x = -1.
- 4. (10%) Find the maximum(最大値) and minimum(最小値) of $f(x) = \frac{x}{2} \sin x$ on the interval $[0, 2\pi]$.
- 5. (10%) Let $f(x) = -3x^5 + 5x^3 + 5$.
 - (a.) Find the relative extrema(相對極值) of f(x).
 - (b.) Determine the open intervals on which f(x) is increasing(遞增的) or decreasing(遞減的).
- 6. (10%) Let $f(x) = e^{-\frac{1}{8}(x-2)^2}$.
 - (a.) Find the points of inflection(反曲點).
 - (b.) Determine the open intervals on which the graph of f(x) is concave upward(凹口向上) or concave downward(凹口向下).
- 7. Find $\frac{dy}{dx}$ of the followings.

$$(10\%)$$
(a.) $y = \tan^6 e^{4x}$,

$$(10\%)$$
(b.) $y = x^{2x}$,

$$(10\%)$$
(c.) $e^{xy} - \sqrt{x^2 + y^2} = x^3 + 6$.