

# Our Spatial Paper

Your Name

January 15, 2025

## Abstract

Please be concise.

## 1 Project Plan

- Idea Formation and Lit Review Jan 13-17 [together ]
- Theory - Coming up with a Model/Try to meet with Esteban to get feedback? Jan 20-22 [together]
- Theory - Solving the Model Jan 23-24 [Key Person = Henrique]
- Coding (data, estimation, counterfactual, and results) - Jan 27 - Jan 31 [Key Person = ]
  - Inputs are fairly divisible
  - Outputs are less divisible
  - Writing - Feb 4 - 7 (KeyPerson)

## 2 Meeting Notes

1. Could have teams of (2) for various things.
2. There are some tasks that are independent.
3. Decide to break stuff up once we actually have an idea.
4. Henrique: Likes Lit Review / Idea Formation / Likes Writing [let us simplify model if possible]. Prefers the equilibrium part of coding to the early / data cleaning part Less good at Geodata. Very good at polishing and visual details.
5. Jeffrey: Likes Coding / Likes Writing
6. Yulia: Interested in counterfactuals part of coding. Curious about theory. Experience about writing / likes writing.

## 2.1 for next meeting, Jan 17

1. Read model / counterfactuals of Monte et al in detail enough
2. In the Esteban choose your model
3. Map Monte et al to Esteban's choose your model.
4. Look at Jeffrey's ideas.

## 2.2 During next meeting

1. pick idea
2. assign data

## 3 Introduction

Your introduction here.

## 4 Background and Diagnostic

Prompt: Why is the question or policy you want to examine important? Why is a quantitative spatial model the right tool to answer the question? Are there any particular features of the policy/economic environment that are important for the analysis? Feel free to focus on one or a few aspects that you want to study in depth and identify the underlying mechanisms, which will inform you about the key elements to be included in your model.

### 4.1 Brainstorming

#### 4.1.1 Idea 1: Self-driving cars

The original invention of the internal combustion engine radically transformed rents, population density, and the distribution of economic activity.

The rise of self-driving cars is likely to have a similar transformative effect on the spatial distribution of economic activity. Waymo currently operates self-driving cars in Phoenix, Arizona, Los Angeles, CA, and San Francisco, CA.

Our first counterfactual will thus be the introduction of self-driving cars in these three counties, which collectively comprise XYZ share of the US population, and \$PQR share of GDP.

Our second counterfactual will be to introduce self-driving in all counties.

Our third counterfactual, which is most policy-relevant, will be the introduction of self-driving in the top [XXX%] of counties by some measure of regulatory friendliness. This will allow us to study a setting where a sizable chunk of the

US economy has self-driving, and the rest doesn't. This is inspired by the real-world heterogeneity in regulations, compare, e.g. California and Arizona to, e.g., New York.

this will let us speak to distributional effects (welfare, rents, population) of heterogeneity in self-driving car regulation.

Fundamentally, this amounts to what do you mean by "introduction"? 100% use of car trips become this? does any walking or biking or public transit substitute towards this?

With American Time Use Data, which not only reports how much time people spend on various activities, but how much they like or dislike them, we can microfound the cost of commuting (maybe there is another paper we can take this from, instead, too), and building on YYY paper, which compares the cost of commuting by public transit vs. cars, we can back out how the primitives of commuting costs change in XYZ locations.

Important things here:

1. Isn't it obvious that a decline in commuting costs would lead people to spread out? Does it matter that it's self-driving cars causing this decline?
2. Do you model the choice of how to commute, or just reduced-form things?
3. Just reducing  $\kappa_{ni}$  for these places seems a little lazy
4. Might the interesting angle to be quantify how places that are slow-to-allow self driving cars "fall behind", in some sense, those which are faster to allow it?
5. Do we think that (me using a self driving car) has a positive externality on other people?
6. Any pecuniary costs in the counterfactual (e.g. I have to buy a self driving car), or just the commuting costs?
7. Will self-driving have a homogeneous effect on all  $\kappa_{ni}$ ? Probably should only apply to certain node-pairs where people are driving.

#### 4.1.2 Idea 2: Incorporating car ownership

Who owns cars, where, and why?

Is the cost of car ownership incorporated into the indifference conditions of these spatial models: maybe chicago isn't actually much cheaper than e.g. nyc once you add a car payment to your rent [which many more people seem to have / beed in Chicago]

Kind of tricky. Need some heterogeneity to endogenize this choice which already complicates things.

Could have  $\kappa_{ni}^{car}$  ;  $\kappa_{ni}^{no\ car}$  and people choose to pay a fixed cost for a car or not. Then, who gets a car vs. who doesn't? People who have higher preference for space,  $\alpha_i$

Could just have a owning a car as an effective decline in wage (rather than an asset). If we wanted to really get fancy, we could have heterogeneous commuting costs, i.e. weight or power  $\kappa_{ni}$  by something.

#### **4.1.3 Idea 3:**

I wonder if Amazon has impacted car ownership through making it easier to just have a bunch of stuff delivered. And this in turn reduces congestion? Seems second-order, maybe not.

#### **4.1.4 Idea 4: Crime $\rightarrow$ Commuting**

My intuition is that, all else equal, people take public transit less in a city if crime (LA buses, for example, Chicago red line, more recently, NY Subway).

Does this impose a quantitatively important externality on commuting costs, by shifting people to cars?

In a complete paper, we would endogenize crime, by also examining how available commuting influences crime, as well.

#### **4.1.5 Idea 5: Weather, Commuting Costs, and Climate Change**

Climate change may have

distributional consequences on commuting costs: places like Florida may see more precipitation. Places like Chicago may see fewer snowy days [citation needed]

#### **4.1.6 Idea 6: Zoning in car cities vs walkable cities**

#### **4.1.7 Idea 7: Distributional Effects of parking requirements**

Maybe minimum parking requirements in business areas let fewer people live in the city, but lowers commute times for the people that do commute.

#### **4.1.8 Idea 8: Car safety and commuting**

## **5 Model**

### **5.1 Jeff's notes on Monte et al model**

1. It's a bit weird to have this 'E[]' component. WTF. Are we treating it as random which place they commute to? Yes.
2. Amenities are our idiosyncratic term and are parameterized by  $b_{niw}$ , that they can differ by person and where they live / work. Or better, put: they each get  $N^2$  shocks.
3. Goods - standard
4. Closing the land market: landlords own everything.



Figure 1: Deaths per capita in the US from car accidents.

5. People's utility is just in land. So there's no housing being created people just eat  $C$  and  $H$ .
6. When can we use exact hat algebra for counterfactuals? (see Eqn. 24)

Write down the model that directly speaks to the mechanisms you identified in the previous step. You need to specify all the building blocks and solve for the equilibrium (equilibria). Please be clear and concise, and feel free to leave tedious derivations in the appendix or cite any relevant derivations you want to lift from existing papers. You are encouraged to tweak or simplify an existing model, like the one in Monte et al. (2018). If you want to be more creative, feel free to select components from the “menu of quantitative spatial models” in Section 2 of Redding and Rossi-Hansberg (2017). When tweaking an existing model or building a model of your own, make sure you include only the necessary elements related to your proposed mechanisms. Importantly, please be aware of the time and feasibility constraints when specifying your model.

## 5.2 Mapping Monte et al to Redding Rossi Hansberg 2017

1. 2.1 - Preferences: Love of Variety (CES), Single Sector, Exogenous Amenities, Fixed Land (enters into utility), Idiosyncratic Preferences
2. 2.2 - Increasing Returns (kinda. TFP is constant, but there's a fixed cost), Exogenous productivity differences, No input-output linkages, No fixed factors in production (only labor)
3. 2.3 - Variable trade costs (ice berg), asymmetry allowed, economic and geographic frictions (i.e. no stand on what's causing trade costs). Only land is not traded.

4. 2.4 - No knowledge externalities. Exogenous local productivity. No transferability of ideas.
5. 2.5 - No migration costs, Yes commuting costs, No heterogeneity (beyond idiosyncratic preferences), No congestion
6. 2.6 - Homogeneous labor (no skill endowments), Exogenous land, in Counties in the US, No capital
7. 2.7 - Market Structure = Monopolistic Competition, General Eqm, Land ownership: Owned by immobile landlords who spend income locally (no need to “track” workers, but also no externality from moving on other people), Trade Balance: Deficits/Surplus permitted but only exist due to commuting?<sup>1</sup>,
- 8.

### 5.2.1 Simplifications to Monte et al

1. do we need monopolistic competition or would CRS be easier?
2. honestly hard to get a much simpler model than this if you want trade in goods and commuting. Good job Esteban.

### 5.2.2 Monte et al and the Data

We might be able to not know some of these with Exact-Hat magic. I will try to note that if so. I am also sometimes being a little vague when I’m talking about model vs. data, sorry.

Structural parameters

1.  $\alpha$ , Cobb Douglas weight on consumption goods, 60%, taken from the BEA (rest is housing)
2.  $\epsilon$  dispersion of amenities (estimate later, at 3.3)
3.  $\sigma$  CES Elasticity of Substitution = 4 (central value in literature)
4.  $F$  fixed cost of production (maybe? we never seem to actually need this so I guess it gets exact-hatted out or cancels with itself or something)

Calibrated parameters

1. Wages  $w_i$  (totally exogenous in this model, not even calibrated, I think - we just take the county mean from the data and that’s our wage vector)
2.  $d_{ni}$  goods trade cost (compute this as a deterministic function of distance a la Allen Arkolakis 2014)

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<sup>1</sup>Kind of vague on this still? Monte et al explanation “a location’s total workplace income equals total expenditure on the goods that it produces, total residential income can differ from total workplace income (because of commuting).”

3.  $\kappa_{ni}$ , commuting costs
4.  $A_i$  productivity vector
5.  $B_{ni}$  exogenous amenities from living in  $n$  and working in  $i$  (why have this be a matrix? can we simplify this? maybe we're underidentified if so)

Equilibrium objects

Note in this model,  $i$  is where you work,  $n$  is where you live.

1.  $H_n$  housing stock
2.  $L_i$  labor force
3.  $R_n$  residents [note, having an  $R$  distinct from  $L$  is what makes this a commuting model!]

The below can be expressed using all of the above (I would call them “derived equilibrium objects”)

1.  $M_i = L_i/(\sigma F)$  varieties produced
2.  $P_n$  price index
3.  $Q_n$  price of land
4.  $\lambda_{ni}$  probability of working in  $i$  and living in  $n$  (unconditional probability), there are some nice eqm objects
5.  $\pi_{ni}$  share of location  $n$  expenditure on goods produced in  $i$
6.  $\bar{v}_n$  average residential income (differs from wages due to commuting)

### 5.2.3 Taking the model to the data

1. We basically have data on  $R_n$ ,  $L_i$ ,  $\bar{v}_n$ ,
2. While we don't have  $\pi_{ni}$ , we have a 123x123 matrix of CFS regions, and we allocate the deficit for each CFS region across the countries within that region according to their shares of the CFS region's income
3. We are going to calibrate  $A_i$ ,  $d_{ni}$ ,  $\kappa_{ni}$  to match wages, commuting flows, and populations.

Parameterizing  $d_{ni}$  (I say parameterizing because there is no economics here, just geography and math) This is more in the line of Allen Arkolakis 2014 where you calculate trade costs than the Regional Sector Model where you back out trade costs.

1.  $(d_{ni})^{1-\sigma} = \text{dist}_{ni}^{-\psi(1-\sigma)}$  (the  $\tilde{e}$  thing turns out not to matter I think)
2. Since we take  $\sigma$  from the lit. all we need to do is calc  $\psi$  and get some data on distances.

3. we can do that using a gravity regression - of trade flows onto destination and origin fixed effects, and distance. The parameter on distance is going to be  $-(\sigma - 1)\psi$
4. They get  $-1.29 = -(\sigma - 1)\psi$  so  $\psi = 0.43$ . Probably good to make sure we get this same thing with their data !! **Validation Check**
5. Okay, so we have  $d_{ni}$

It's a bit buried, but I believe this means symmetric trade costs! (as long as their distance measure is symmetric)

Solving for  $A_i$

1. Can get a system of  $N$  equations  $N$  unknowns ,eq (16) in the paper, (wages, employment, residents, avg residential income and trade deficits are or computed fairly immediately from data)
2. Computationally, we would like to do a contraction mapping thing right? But I don't know that it is a contraction..They give the excess demand equation in the appendix.

Onto commuting stuff... we can solve for  $\lambda_{ni}$  as  $N^2$  system of equation with same number of unknowns.

The thing we are gonna be solving for is  $\mathcal{B}_{ni} = B_{ni}\kappa_{ni}^{-\epsilon}$  (I am guessing we cannot identify  $\kappa$  (distance) and  $B$  (amenities) separately)

First we need to estimate more parameters though!

We are going to parameterize  $\kappa_{ni}$  as a function of distance  $(dist)^{-\phi}$ , like we did with goods costs before but with another parameter  $\phi$  instead of  $\psi(\sigma - 1)$ . This will let us recover  $\epsilon$  in a 2-step process.

1. Estimate  $\phi$  with a gravity regression (they get  $\phi = 4.43$ ) (B.74 in appendix)
2. Then I guess using  $\phi$  and some features of their model compute  $\epsilon = 3.3$  in another regression (B.75 in appendix)

Then you use  $R_n, H_n, v_n, w_n, \pi_{nn}$  (don't need the whole matrix!),  $L_n$  to solve for  $\lambda_{ni}$ .

#### 5.2.4 How do counterfactuals work / Exact-Hat Notation

(from shock to commuting costs, they say what they assume is held fixed that permits this eqn to work)

$$\hat{U} = \left( \frac{1}{\hat{\lambda}_{ii}} \right)^{\frac{1}{\epsilon}} \left( \frac{1}{\hat{\pi}_{ii}} \right)^{\frac{\alpha}{\sigma-1}} \left( \frac{\hat{w}_i}{\hat{v}_i} \right)^{1-\alpha} \frac{\hat{L}_i^{\frac{\alpha}{\sigma-1}}}{\hat{R}_i^{1-\alpha}} \quad (1)$$



## 6 Data and Estimation

Describe the data you use to estimate the model. What variables do you need? How do you access them? How do you plan to estimate the model? For parameters that you will calibrate, justify your choices. For parameters that you will estimate, explain your strategy.

## 7 Counterfactual

**It seems like this is the area for creativity. We can keep the model itself as in Monte** Carefully describe the counterfactual exercise (i.e., a policy that you want to evaluate) you want to examine. What is your plan for implementing it? Are you going to fully invert the model to back out fundamentals? Are you going to use exact hat algebra to solve the model in changes? For the purpose of this problem set, you can restrict your attention to policies that are local in nature (i.e., policies that target a specific county or a set of counties independently of others). If you are interested in a non-local policy (i.e. a policy like a construction of interstate highways that affect many counties simultaneously), you do not need to compute changes in fundamentals with high level of precision (e.g., changes in commuting costs in each county), a rough approximation will suffice

## 8 Appendix

Painful proofs go here.

## References