# FIT3139 Lab Modelling case-study for week 6

### Objective

Your task this week is to construct, simulate and analyze a simple Pharma-cokinetic model of drug dosage.

# Background

Pharmacokinetics is a branch of pharmacology that studies the effect of substances administered to a living organism. The simplest type of model used in the study of pharmacokinetics is called the *compartment model*. In this model, we are concerned with following the progression of a drug as it enters the intestines (stomach), is absorbed into the blood stream (plasma), and eventually ends up in the urine. As such, we study the amount of drug in three compartments: Intestine, Plasma and Urine.

The purpose of this model is to look at the effect of how a change in the amount of drug (the dose) and the dosing interval affects the amount of drug in the three compartments. We will want to try to stabilize the *plasma concentration* (see glossary below) over a period of about eight days.

#### Glossary of terms

In this case study we will use the following terms:

**Half-life:** The period of time required for the concentration or amount of drug in the body to be reduced to exactly one-half of a given concentration or amount. This is symbolized as  $t_{\frac{1}{2}}$ .

- Volume of distribution: The volume, in an organism, throughout which a drug appears to have been distributed; the volume into which a drug appears to have been dissolved after administration to an organism. Symbolized by  $V_d$ , measured in liters (L). Calculated by amount of drug in the body divided by the concentration in the plasma.
- **Absorption rate constant:** Symbolized as  $k_a$ , the rate at which an orally-dosed drug enters the bloodstream (from intestines).
- **Elimination:** The removal of a drug from the blood stream, usually through the urine.
- Elimination rate constant: Symbolized as  $k_e$ , the rate at which an orally-dosed drug is removed from the bloodstream.
- Plasma concentration: The amount of drug in the plasma divided by the volume of distribution. Concentrations are typically the parameter of most interest to pharmacologists

#### Building the Model:

In this model we are interested in the concentrations of drug in each of the three-compartments, as described above. The assumptions to be made in constructing this model are:

- 1. A specified amount of dosage is delivered *instantaneously* at regular intervals into the intestine compartment.
- 2. The rate of absorption of the drug is proportional to the amount of drug in intestine.
- 3. The rate of elimination of the drug is proportional to the amount of drug in plasma
- 4. Any other parameters that are involved in your model stated without initial values defined (see below) should be treated as variables which you will have to tweak to analyze the problem.

Your task is to build this model (as a script in MATLAB) using the initial values given below, and use it to investigate a number of scenarios by examining plots of Plasma concentration, drug in the intestines, drug in plasma and drug in urine.

# Symbol definitions

I = amount of drug in intestine in mg/L

P = amount of drug in plasma in mg/L

U = amount of drug in urine in mg/L

 $k_a = absorption rate constant$ 

 $k_e = \text{elimination rate constant} = \frac{0.693}{t_{\frac{1}{2}}}$ 

 $C_p = \text{plasma concentration} = \frac{P}{V_d}$ 

#### **Initial values:**

- Initial drug in the intestine or plasma or urine = 0 mg/L
- Absorption rate constant  $(k_a) = 1$  /hour
- Volume of distribution  $(V_d) = 70 \text{ L}$
- Simulation time = 192 hours in 15 minute intervals ( $\Delta t = 0.25$  hour)

#### Scenarios to simulate and examine your Model:

- 1. What is the difference in changing the dosage and the dosing intervals?
- 2. What settings might you use to reach a certain plasma concentration at the peak of the simulation?
- 3. What settings stabilize the plasma concentration? Introduce a minimum value (for the drug to have any effect) and maximum value (before the drug becomes toxic) of plasma concentration for a drug and play with parameters of your model which stabilizes the plasma concentration.