

# Daily Research Report

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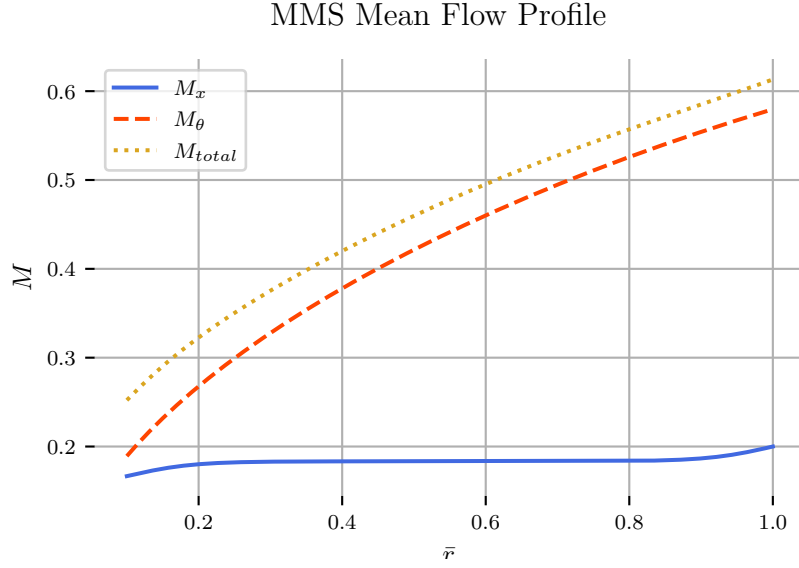


Figure 1: The manufactured mean flow test case using a summation of Tangents for  $A$  and  $M_x$

## 1 Current Research Direction

## 2 Research Performed

### 2.1 Results

Hypothesis 1:

By using a composite trapezoidal rule numerical integration technique, the speed of sound is approximated using the tangential mach number. A second order convergence for the approximated speed of sound is expected (Refer to analysis). To obtain the radial derivatives, second and fourth order central differencing schemes were used and the order of accuracy will also be computed using the four system of equations for the LEE.

Why is this my hypothesis?: As the grid spacing gets smaller from one iteration to the next, the computed order of accuracy is expected to approach a known value, which is the leading error term of the truncated term in the Taylor series used to derive the scheme, which in this case is the composite trapezoidal rule. By using the MMS, a computed order of accuracy was found.

The  $L2_{norm}$  error of the two grids  $\epsilon_{grid_i}$  and  $\epsilon_{grid_{i+1}}$

## 3 Issues and Concerns

There is an issue with the data I am data I am looking for the Source Terms. The figure that I have for the source term error should have a magnitude of near zero. I will also double check the python output and the fortran output to make sure that the perturbation variables without fairing functions  $v_x v_{theta}$

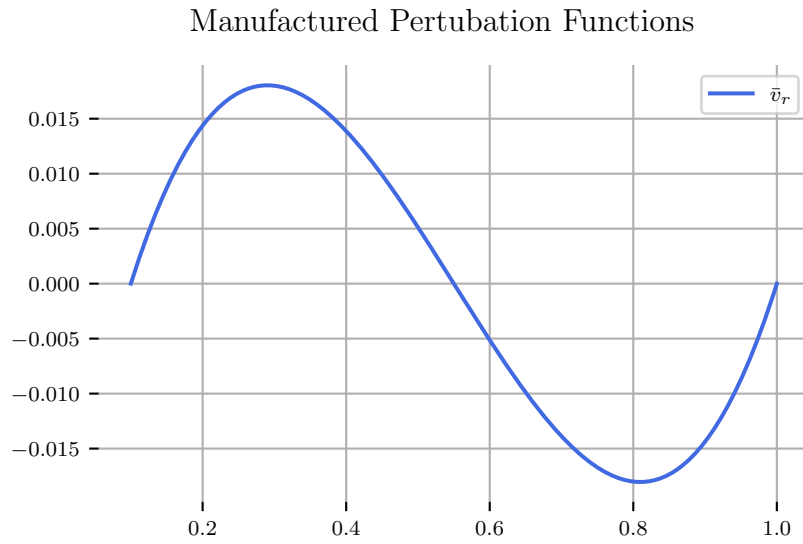


Figure 2: The manufactured perturbation functions  $\bar{v}_r$

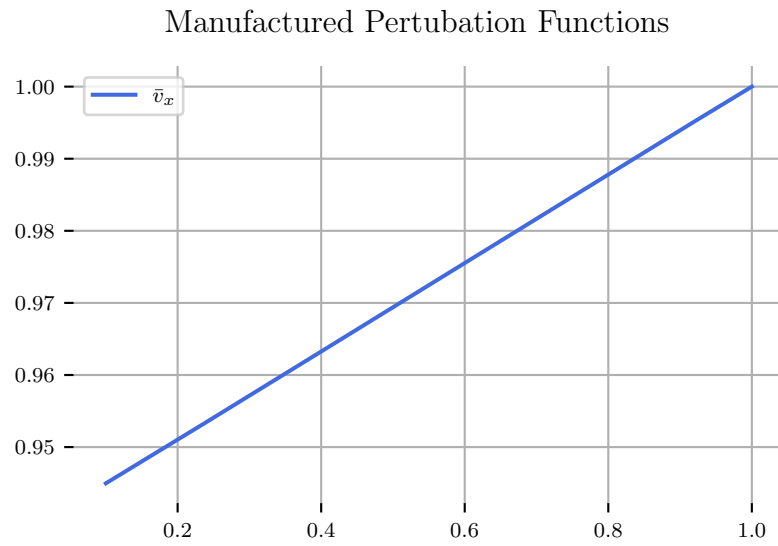


Figure 3: The manufactured perturbation functions  $\bar{v}_x$

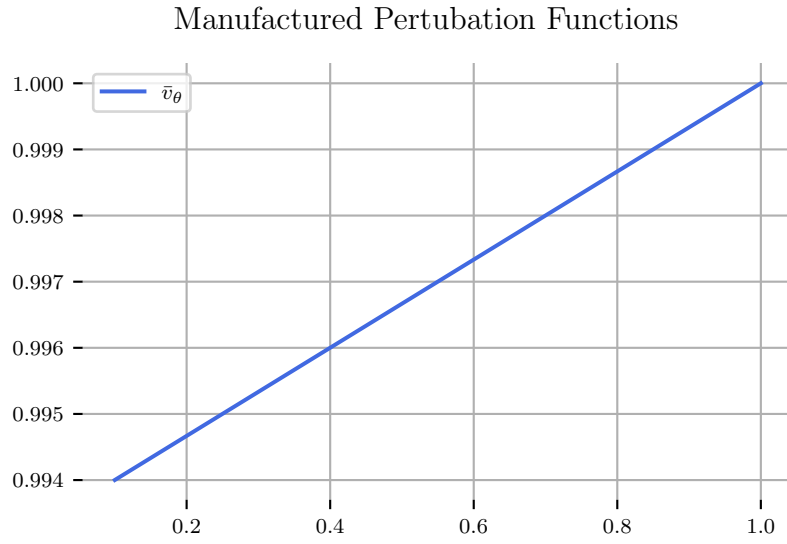


Figure 4: The manufactured perturbation functions  $\bar{v}_\theta$

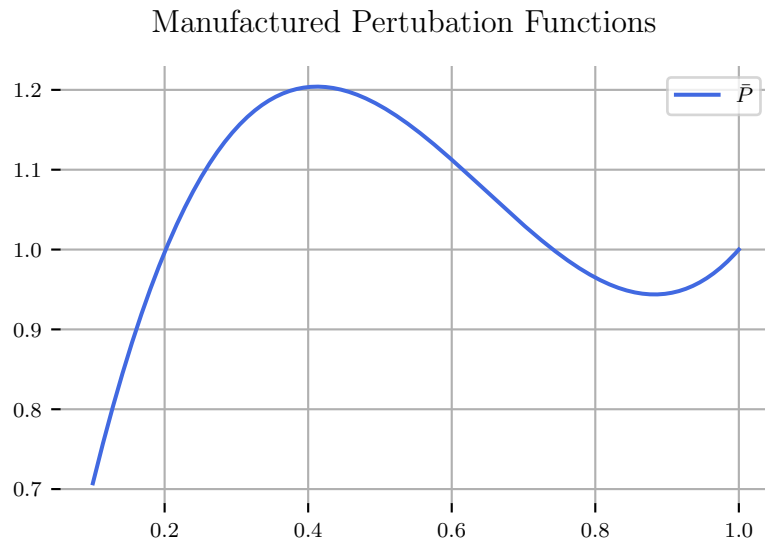


Figure 5: The manufactured perturbation functions  $\bar{P}$

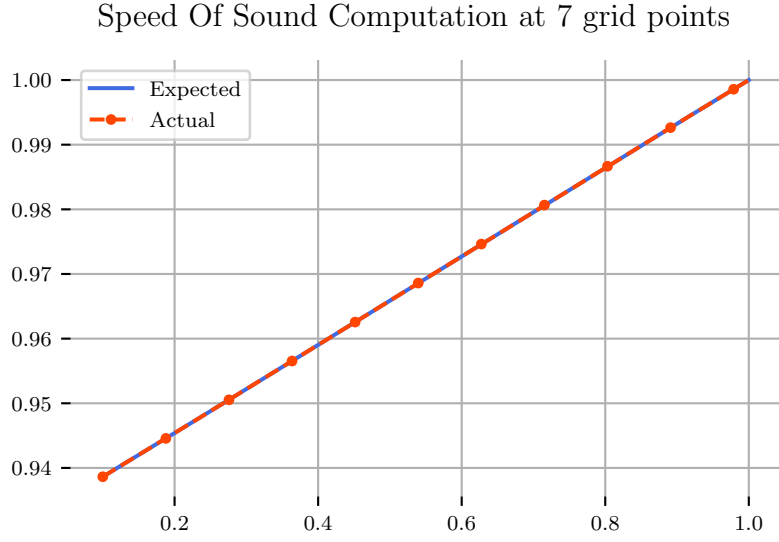


Figure 6: A comparison of the speed of sound, expected vs actual at the lowest grid to show similarities in solution

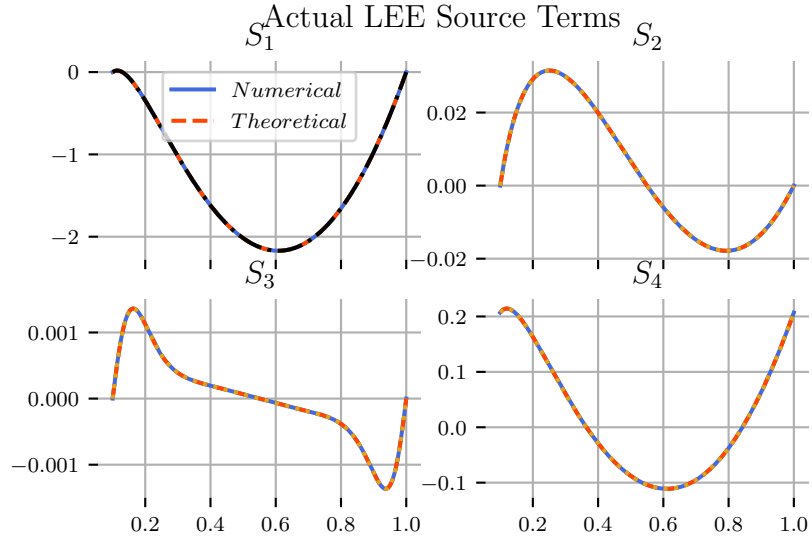


Figure 7: LEE Source Terms

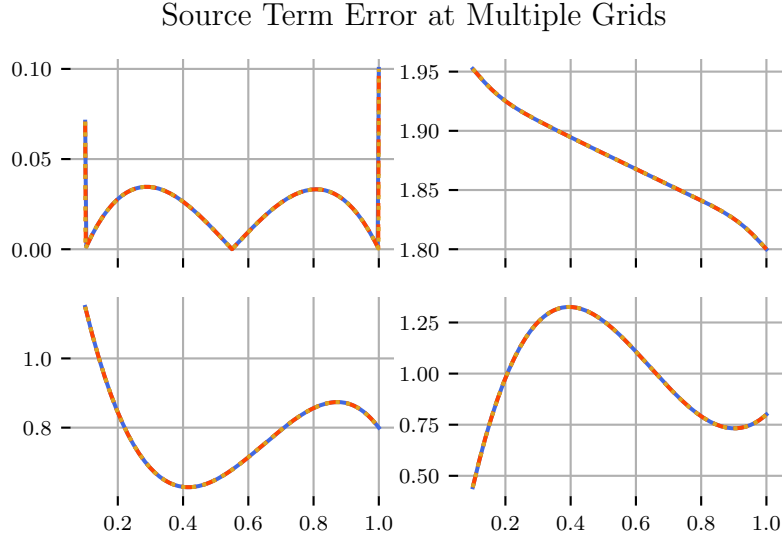


Figure 8: LEE Source Term Error

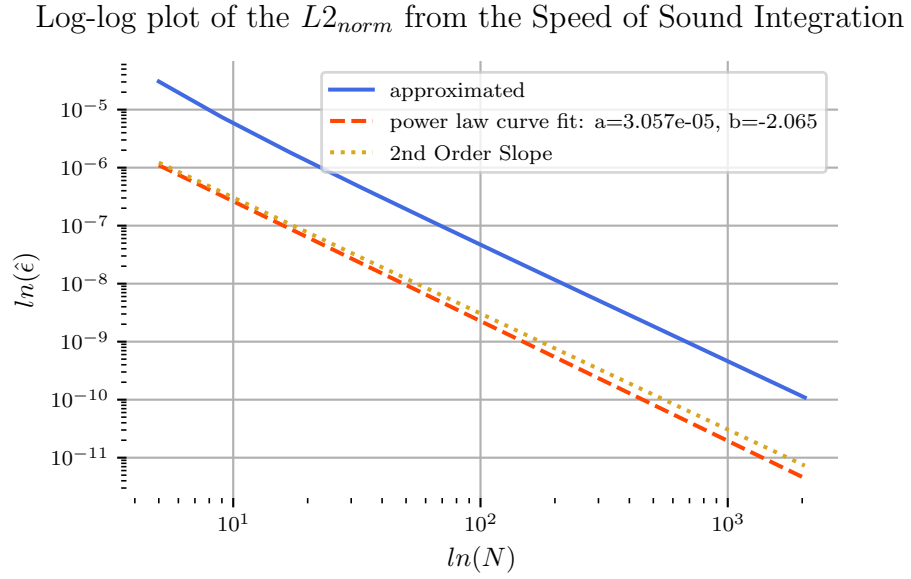


Figure 9: L2 Norm comparison for the speed of sound integration for the compound trapezoidal rule

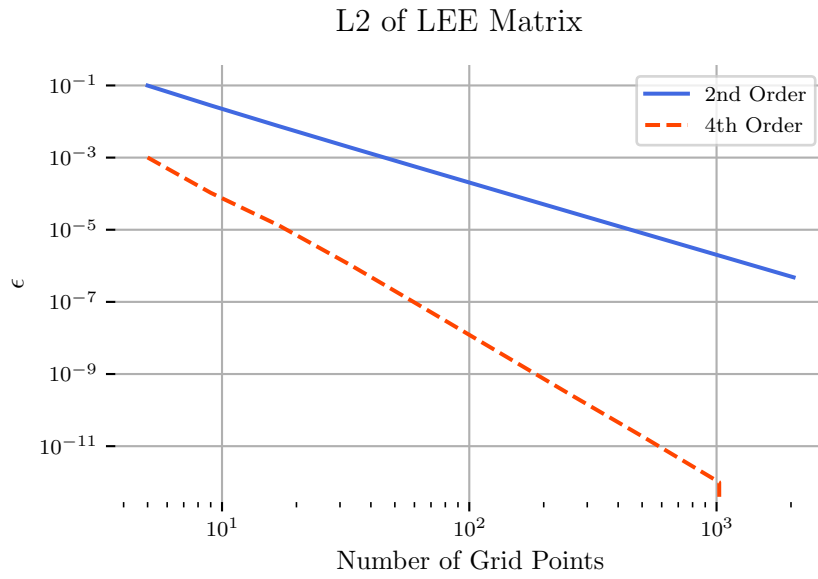


Figure 10: ROC for the speed of sound integration for the compound trapezoidal rule

Figure 11:

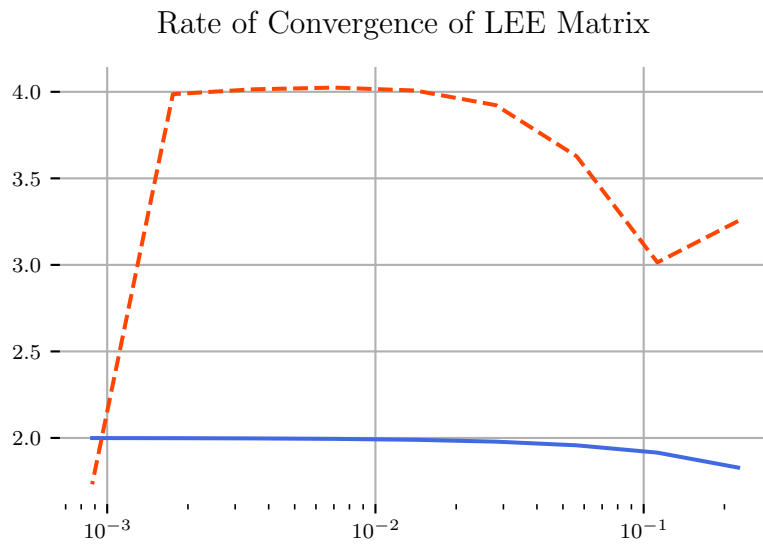


Figure 12:

Figure 13: ROC for the speed of sound integration for the compound trapezoidal rule

## 4 Planned Research

Update Captions and labels Discuss the ROC and the choice of scheme and number of grid points for the MMS. Discuss the L2 procedure in detail and make sure this data is what I think it is.