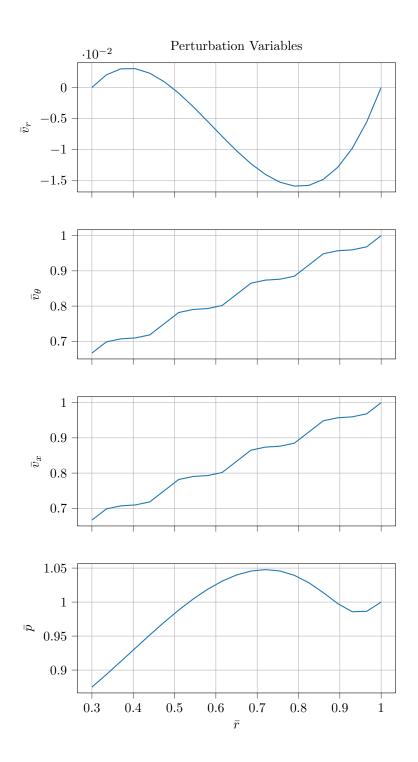


Figure 1: Mach distribution for method of manufactured solution case

## 1 Results

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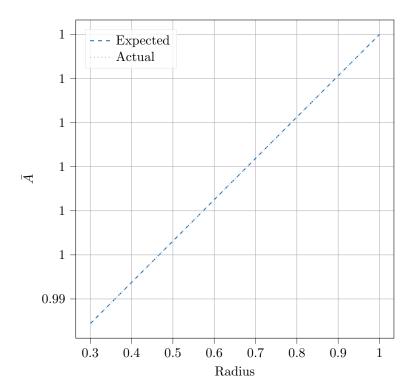
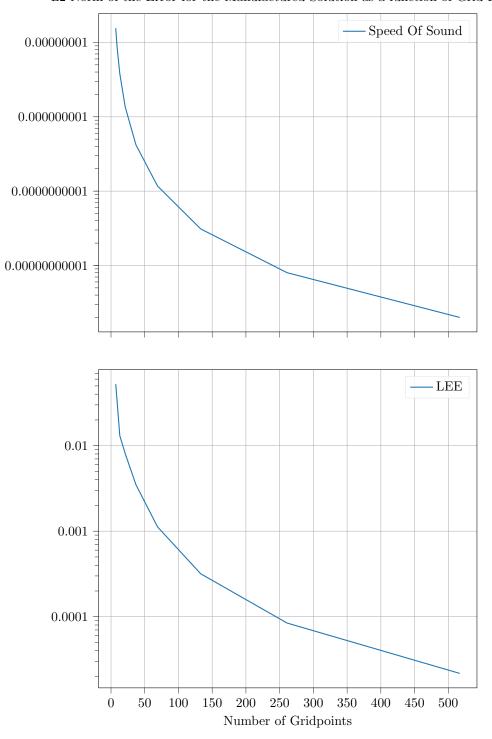


Figure 2: Speed of Sound from Integrating the Tangential Mach Number

L2 Norm of the Error for the Manufactured Solution as a function of Grid Points



 $\label{eq:4} 4$  Figure 3: Speed of Sound Expected vs Actual

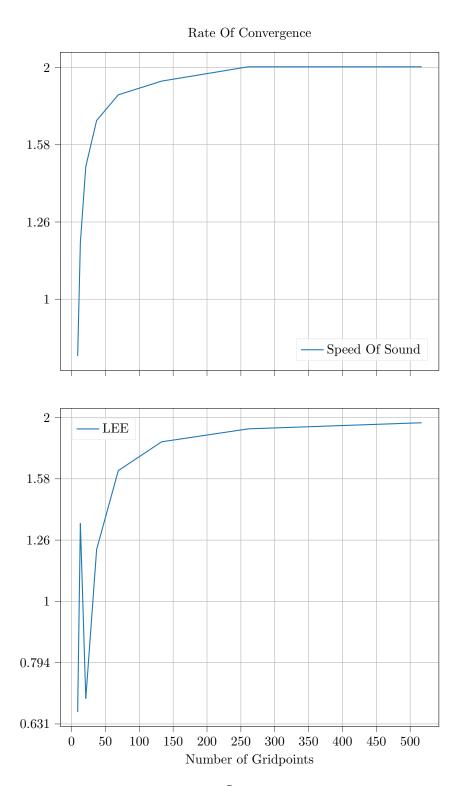


Figure 4: Rate of Convergence for the Speed of Sound Integration

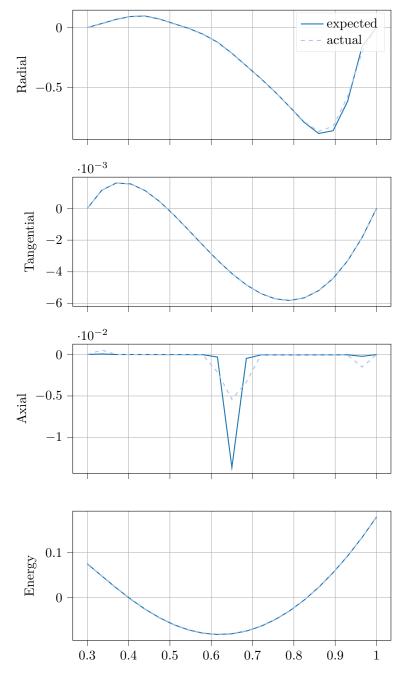
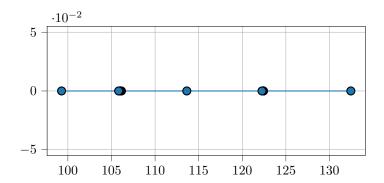


Figure 5: Source Term Error



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                                     Im{gam}
                                                         Re{gam/ak}
                                                                                 Im{gam/ak}
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24

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