

Nuclear  
Energy is  
important,  
old, new, and  
complicated

Jeffrey  
Seifried

About Me

Nuclear energy  
... is important  
... is old  
... is new

Simulations

The neutron  
transport  
equation  
The Bateman  
equations

Summary

# Nuclear Energy is important, old, new, and complicated

Jeffrey Seifried

Ad Delivery Team, Yelp

Applied Learning Group, 2015-03-16

# Outline

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- 1) Spend a decade in nuclear energy
- 2) Data Miner at Yelp    3) ???    4) Profit!

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- BSNE at University of Maryland, College Park
  - Became a nuclear reactor operator
  - Spent 4 summers + 1 semester at the U.S. Nuclear Regulatory Commission
- PhDNE at UC, Berkeley and Lawrence Livermore Lab
  - Developed reactor simulations
  - Propagated uncertainties through them
  - Helped design a hybrid fusion-fission reactor
- 2 year postdoc
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  - Taught a course on nuclear reactor physics
  - Helped design a thorium-fueled breed and burn reactor

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**"Dear future generations: Please accept our apologies, we were roaring drunk on petroleum."**

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- Climate change is just getting ramped up
  - Coal particulates cause 10 thousand deaths annually in the US
  - One quarter of California air pollution is from China
  
- Global energy use will increase by a third by 2040
- Natural gas and oil just got a lot cheaper
- Coal is and always will be cheap

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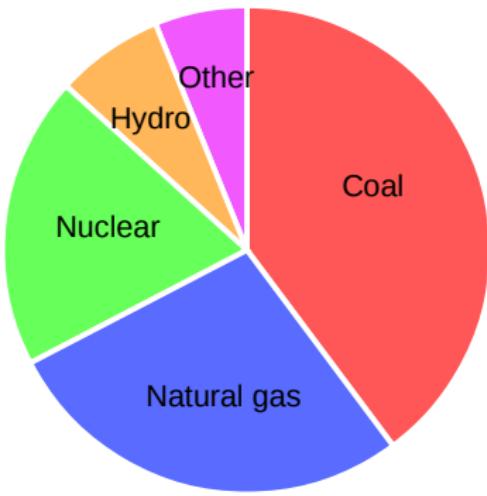
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US electricity sources (2014)

- Fossil Fuels generate 66%
- Nuclear generates 20%
- ... and 60% of carbon-free electricity
- Hydroelectric is shrinking
- Renewables ("other") are not ready

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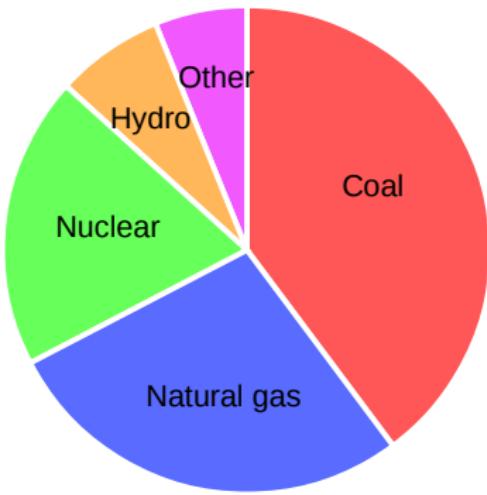
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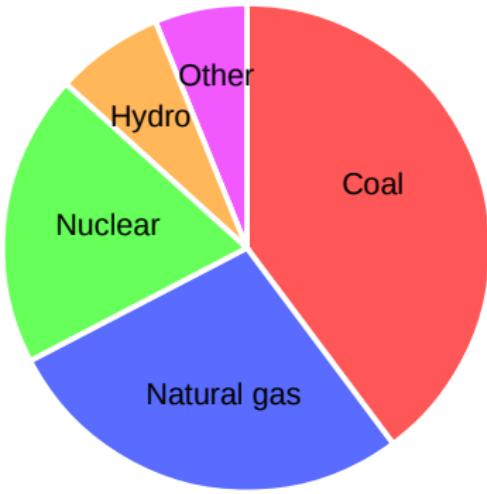
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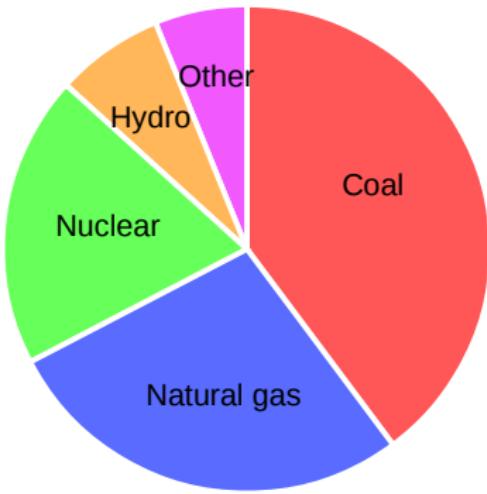
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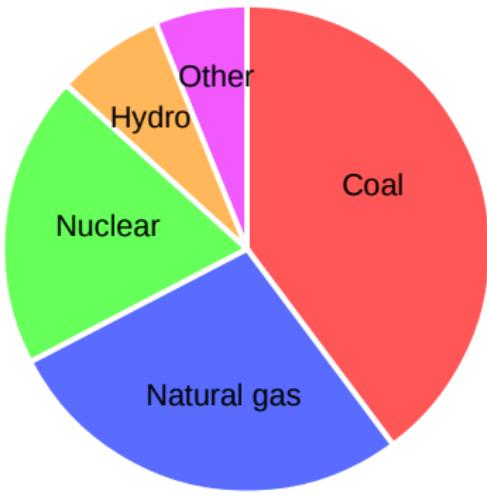
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# The fission chain reaction is at the heart of nuclear energy

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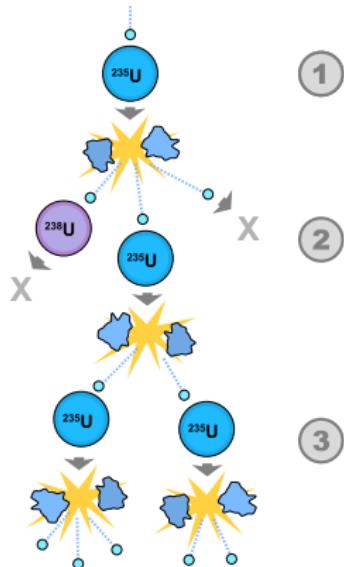
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- 1 A neutron tickles a uranium nucleus
- 2 ... which splits into garbage, energy, and 2-3 neutrons
- 3 ... on average, 1-2 neutrons leak from the system or are consumed in a non-fission reaction
- 4 ... and 1 survives to cause another fission



The fission chain reaction

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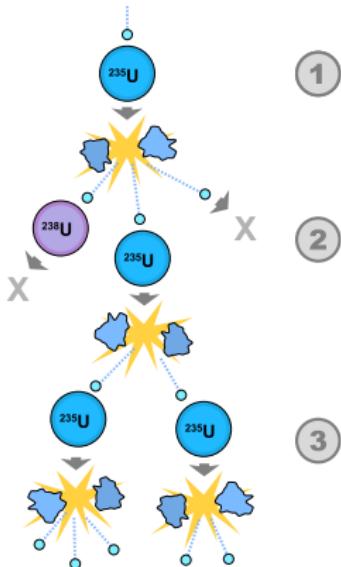
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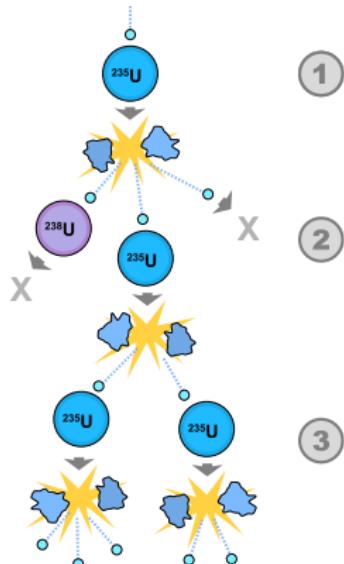
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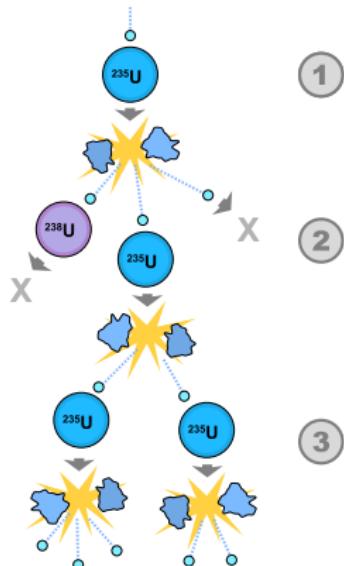
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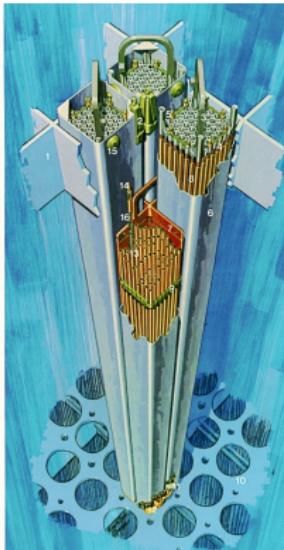
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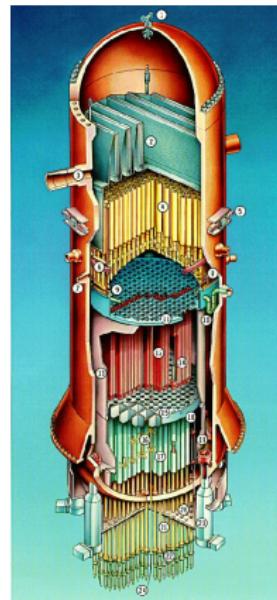
BWR/6 FUEL ASSEMBLIES & CONTROL ROD MODULE

- 1.TOP FUEL CHANNEL
- 2.CHANNEL SUPPORT
- 3.UPPER TIE PLATE
- 4.EXPANSION SPRING
- 5.LOCKING TAB
- 6.FUEL CHANNEL
- 7.CONTROL ROD
- 8.FUEL ROD
- 9.SPRINGER
- 10.CORE PLATE ASSEMBLY
- 11.MIDDLE TIE PLATE
- 12.FUEL SUPPORT
- 13.CORE
- 14.END PLUG
- 15.BEAM SPACER
- 16.PLUMIN SPRING

GENERAL ELECTRIC



An LWR fuel assembly



An LWR core

# Nuclear reactors power 1800's era steam engines just like coal, oil, and some natural gas

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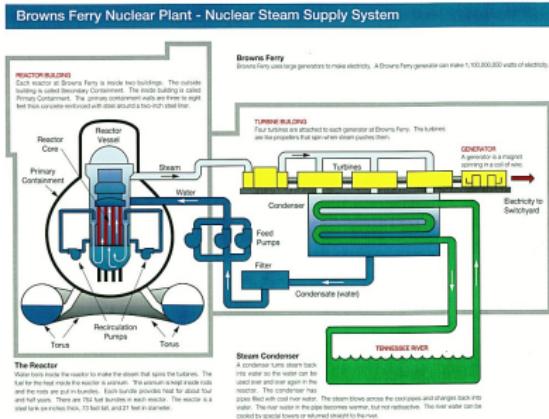
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## Neutrons to electrons

- Fission chain reaction releases heat
  - ... which boils water
  - ... which turns a turbine
  - ... which rotates a generator
  - ... which generates electricity!
- Only one third of heat energy is converted to electricity

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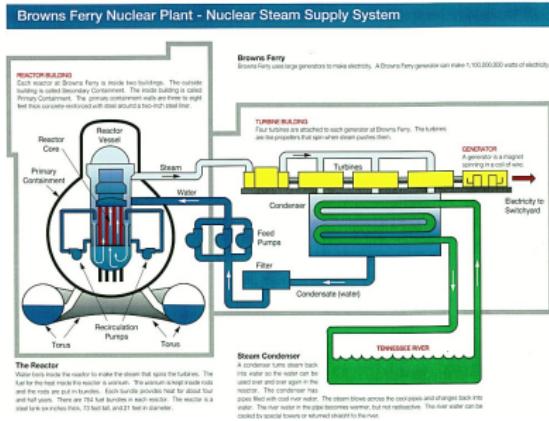
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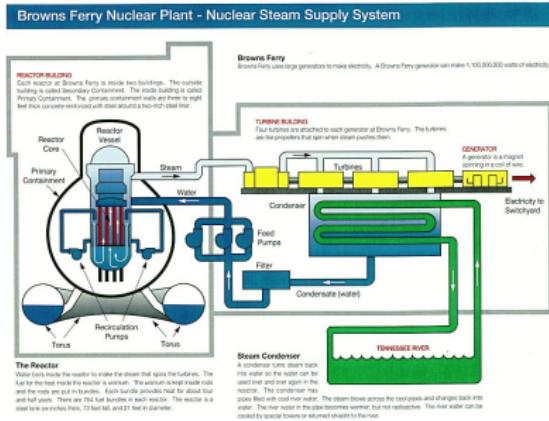
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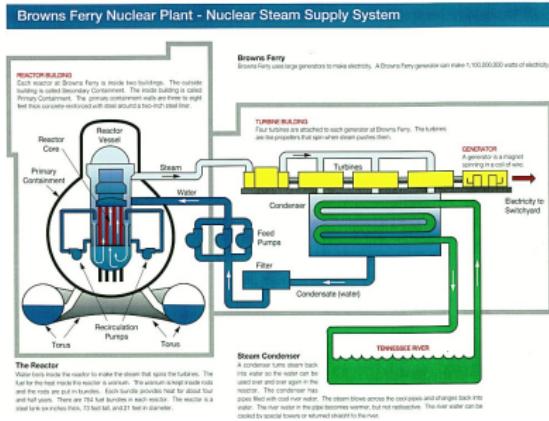
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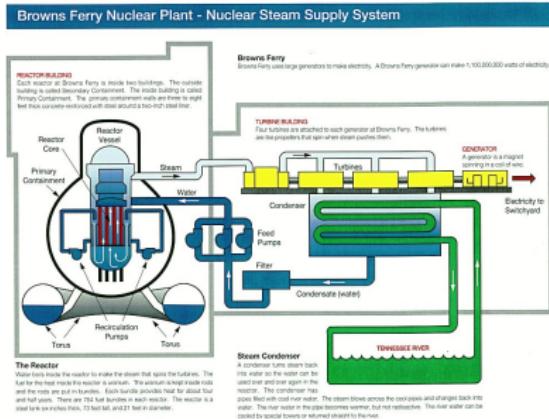
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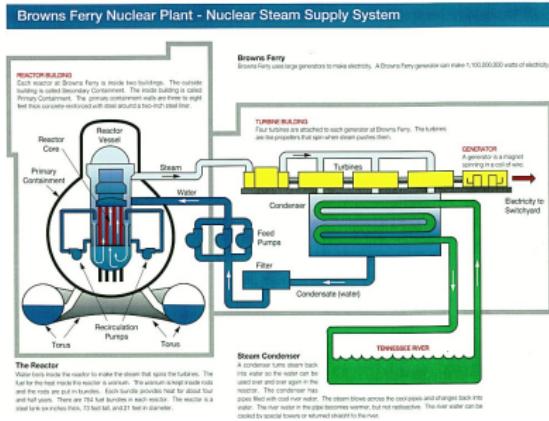
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  - ... its construction began in 1978
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- Spent nuclear fuel is waiting for disposal
  - The core needs to be actively cooled
  - The fuel can melt
  - The water must be at high pressures
  - Two-thirds of energy is lost

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# Sodium-cooled Fast reactors (SFR) consume nuclear waste, recycle it, and consume it again

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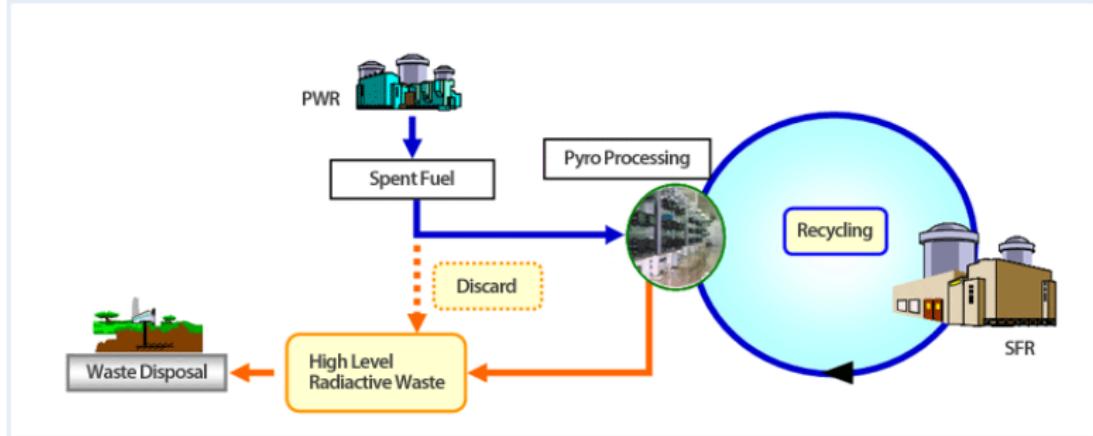
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Traveling wave reactors (TWR; Breed & Burn reactors) breed their own fuel without recycling

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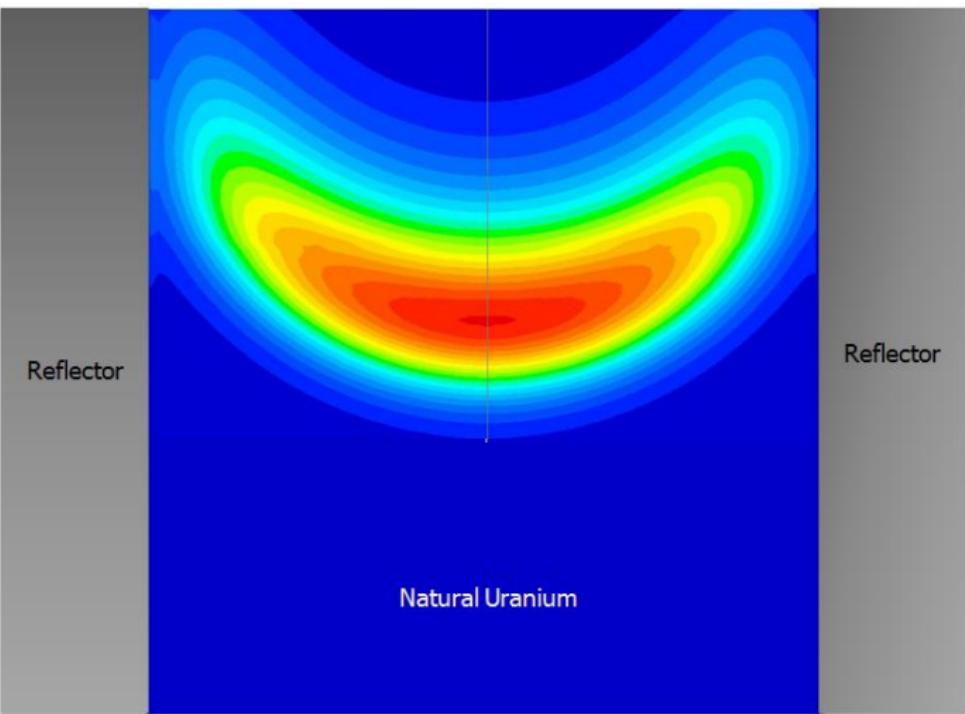
## About Me

- ... is important
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- The neutron transport equation
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## Summary



# Fluoride-salt high-temperature reactors (FHR) can be passively cooled with ambient air

Nuclear Energy is important, old, new, and complicated

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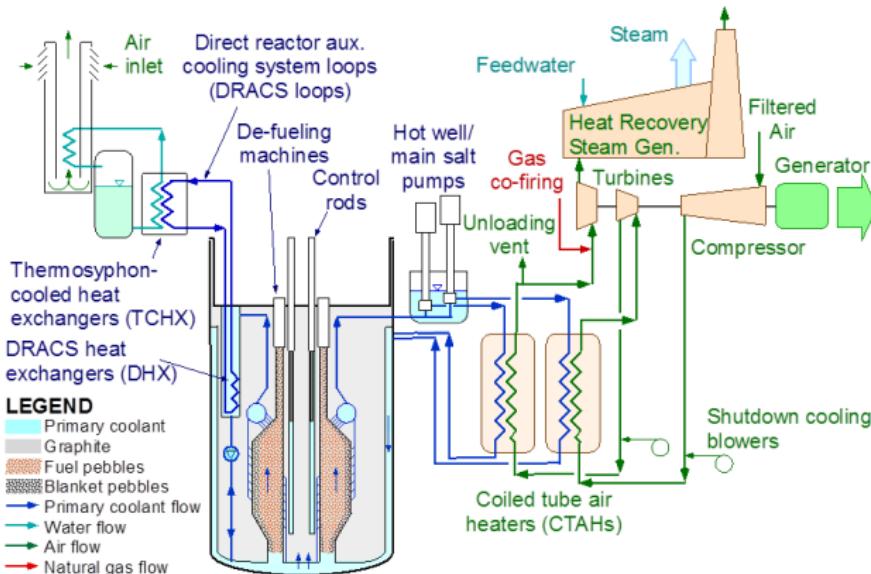
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## Mk1 PB-FHR Flow Schematic



FHR's use coated particle fuel which cannot melt

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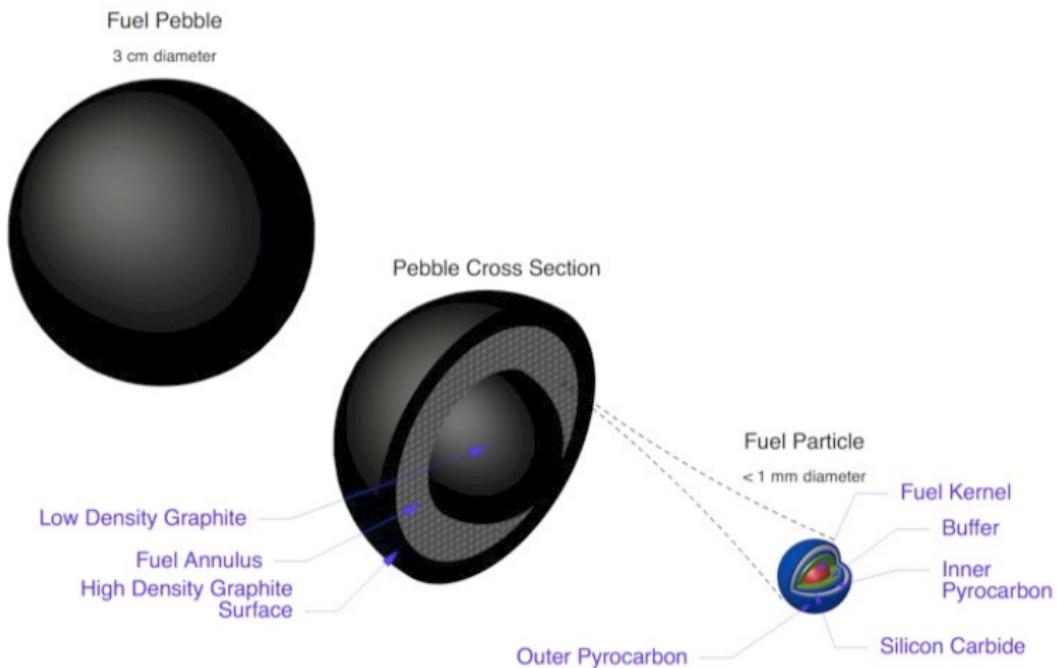
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# FHR's replace water with fluoride salts which boil at 1430°C

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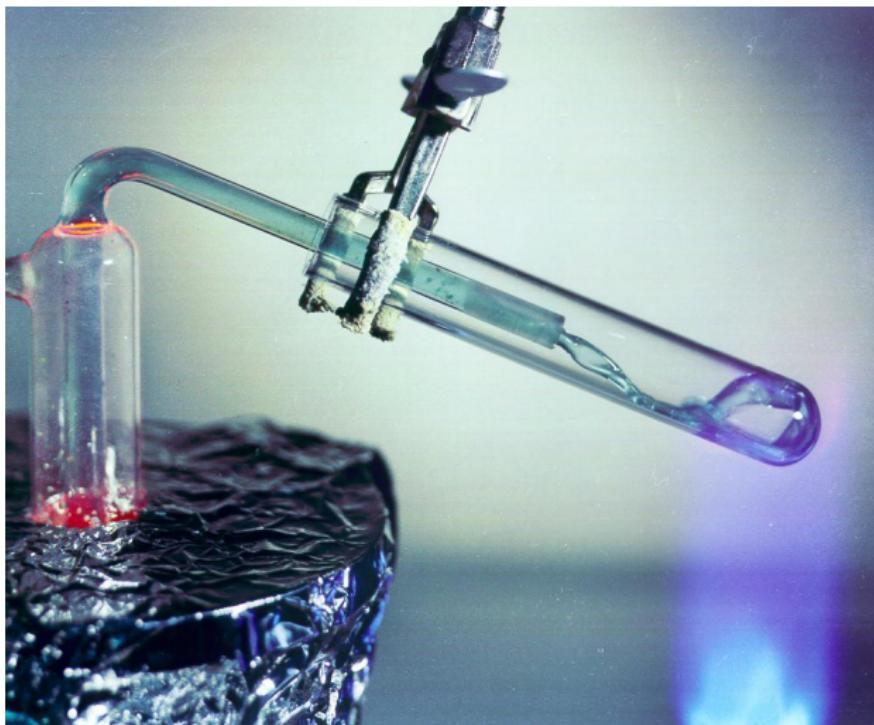
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# FHR's use modern air turbines which are efficient and offer load following

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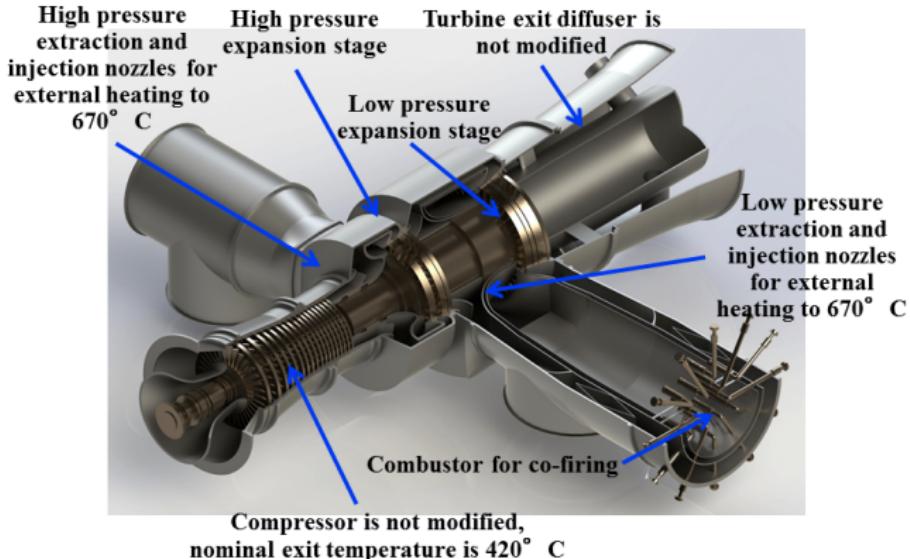
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The GE 7FB turbine design has been  
modified to implement nuclear heating



# Fusion energy is star power on earth! It produces no nuclear waste!

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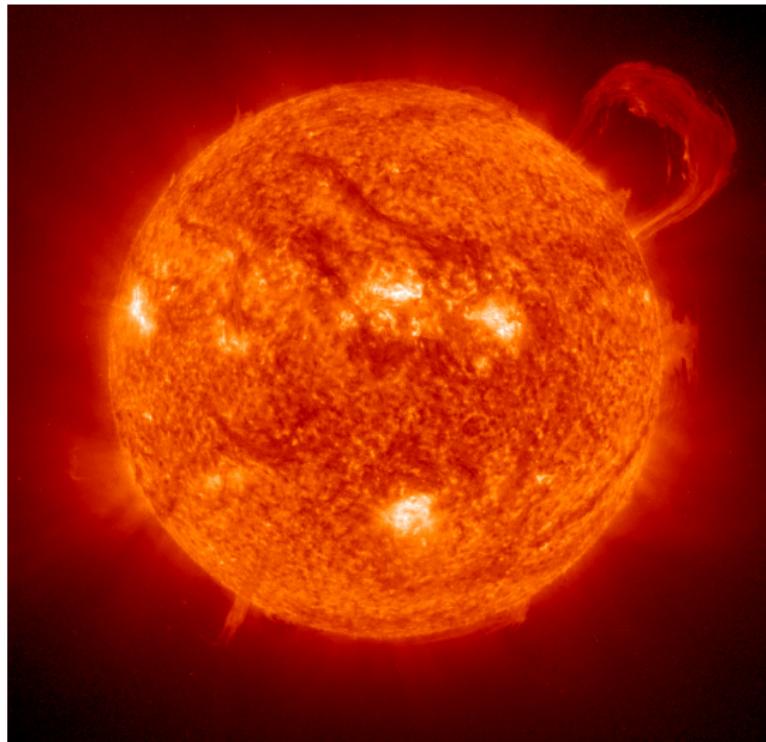
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There is enough fusion fuel in the ocean to power humanity until the earth spins into the sun.

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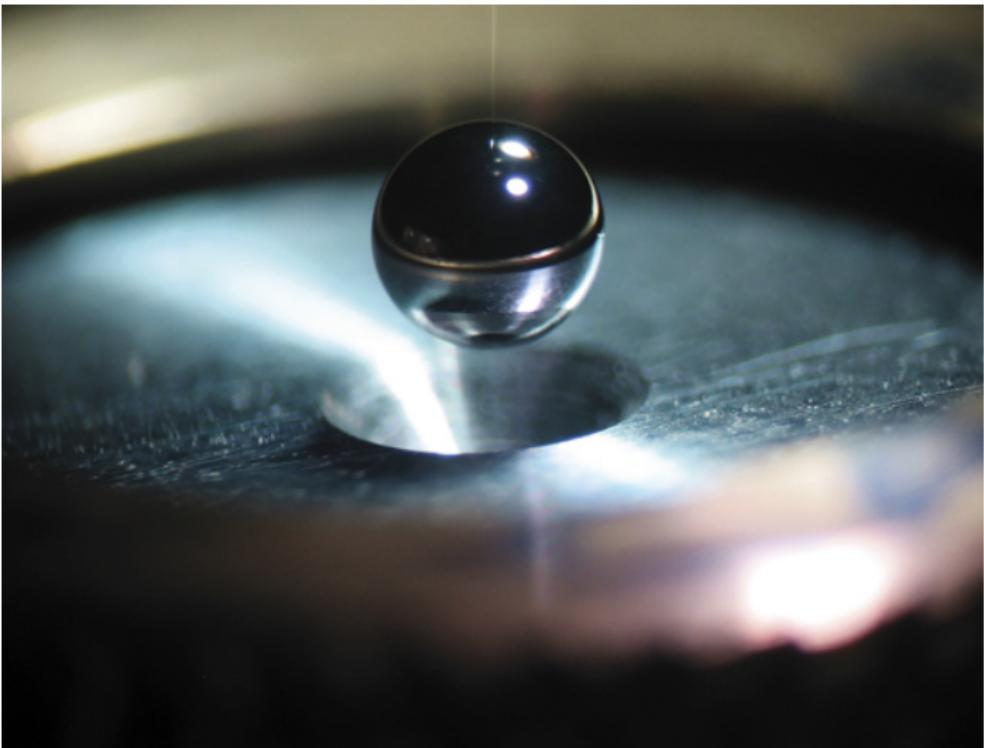
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However, controlled fusion is really difficult. The NIF experiment at LLNL came close to break-even

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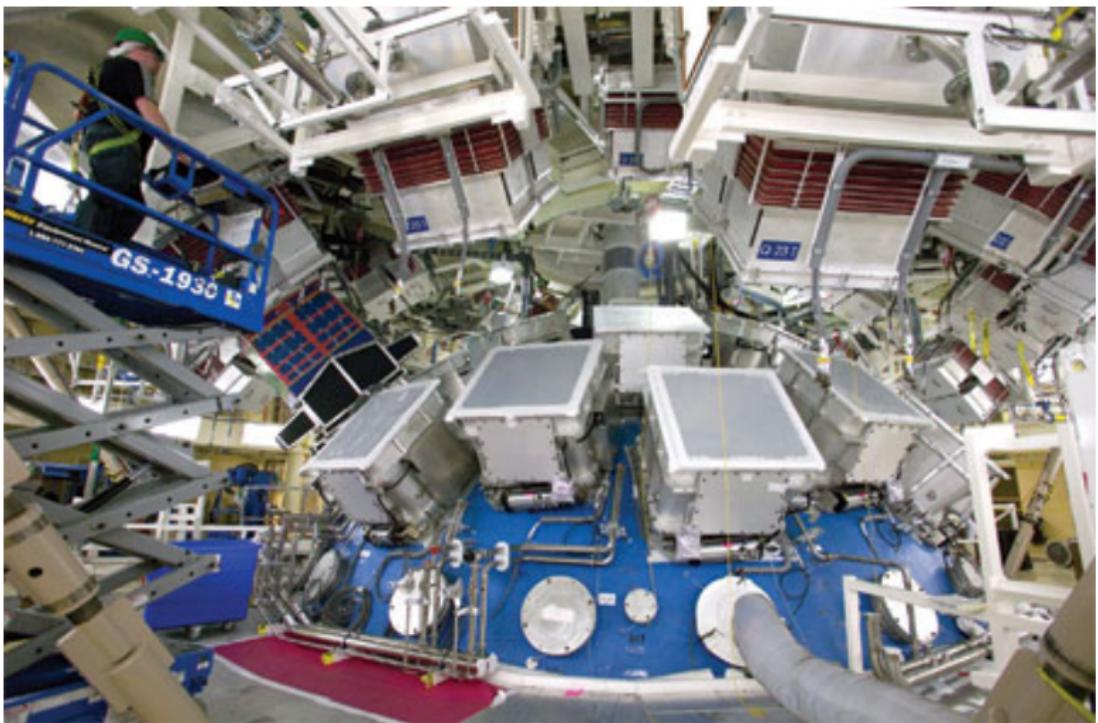
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Hybrid fusion-fission reactors will be an economic stepping stone until fusion energy is perfected

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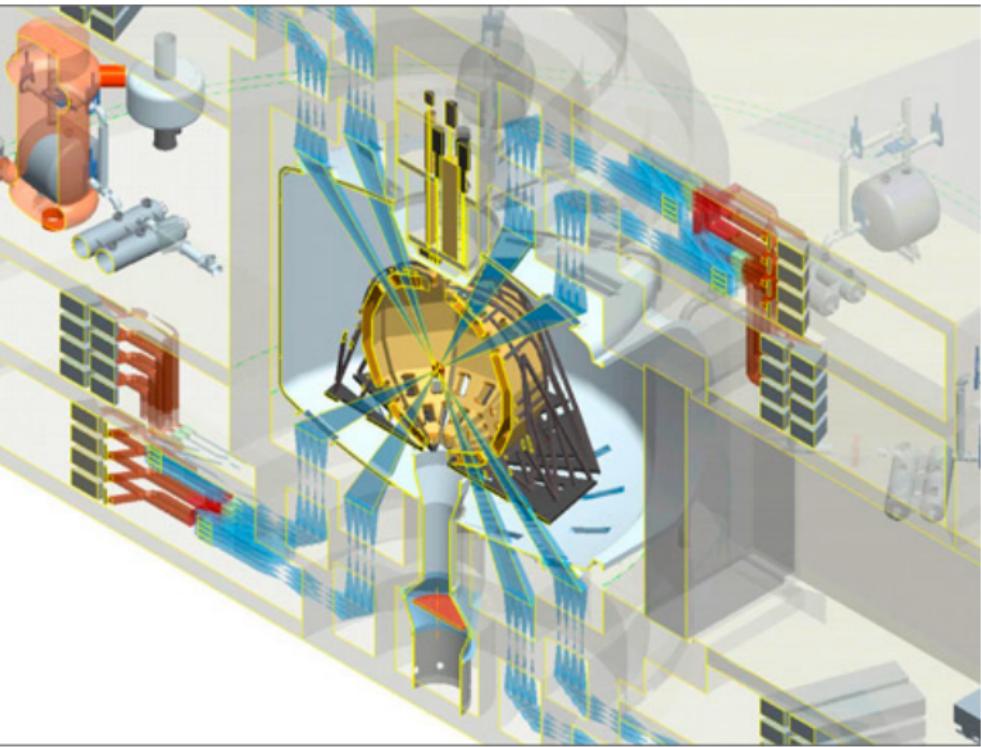
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# Accurate simulation of neutron fields requires their description 7-dimensional neutron phase space

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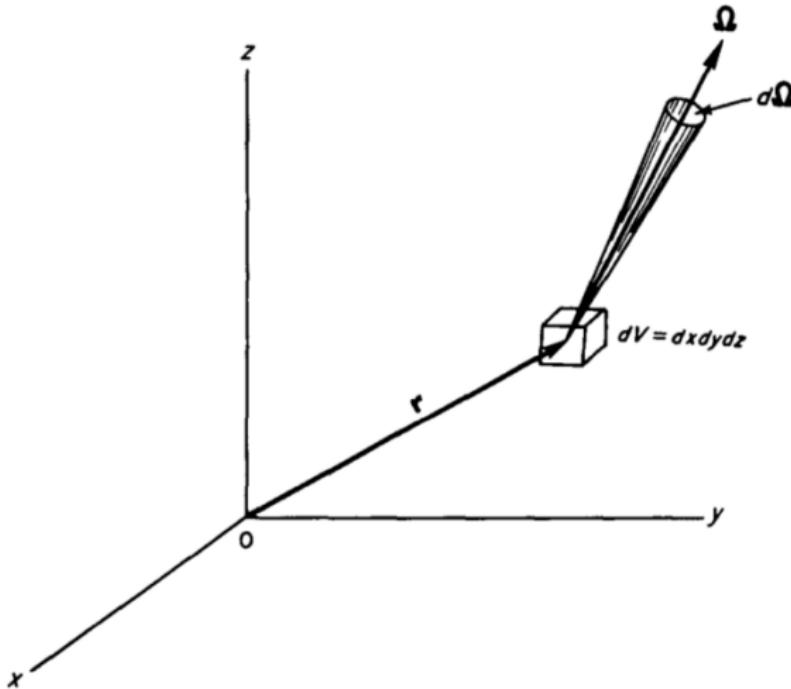


FIG. 1.2 THE VOLUME ELEMENT  $dV$  AND THE DIRECTIONAL ELEMENT  $d\Omega$ .

# Spatial distributions ( $\vec{r}$ ) can be complicated

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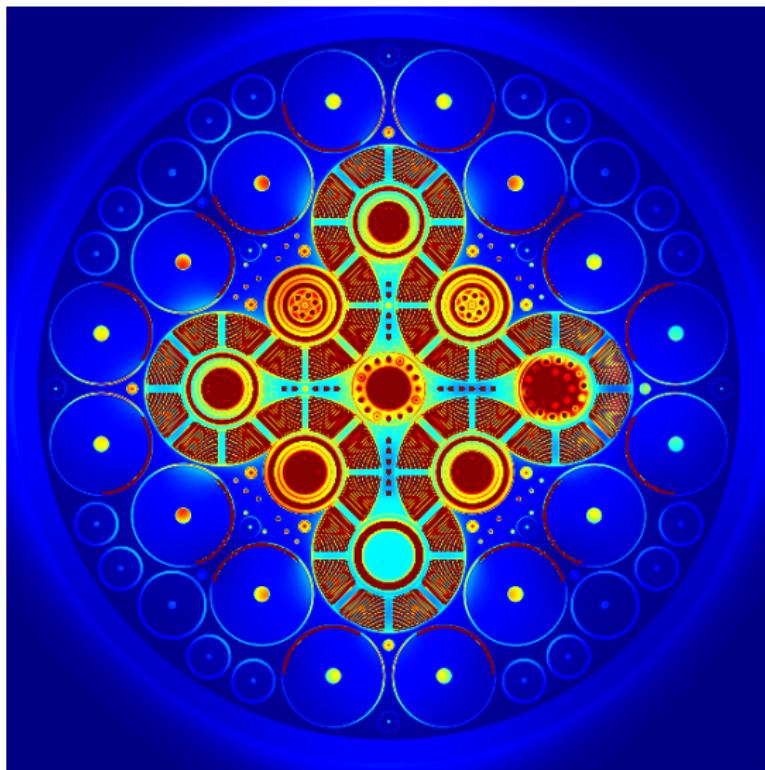
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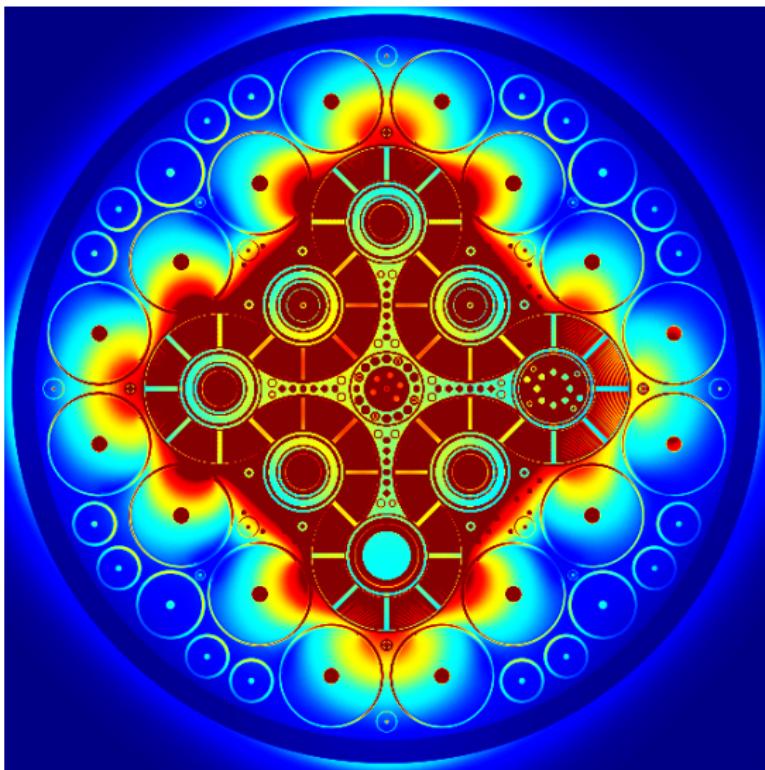
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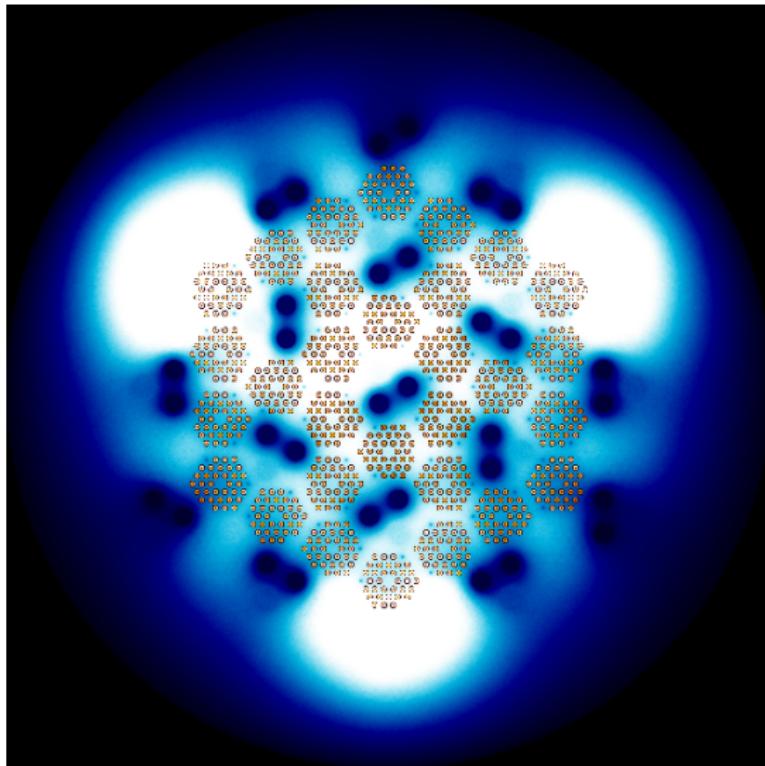
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# Energy distributions ( $E$ ) can be complicated

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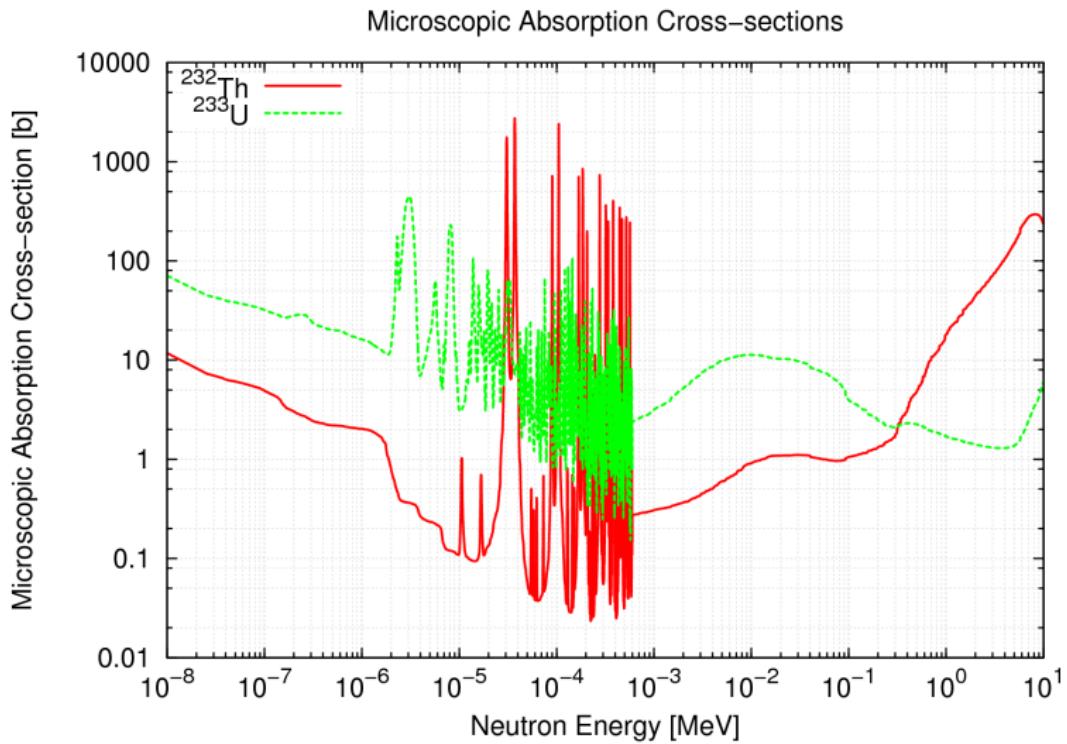
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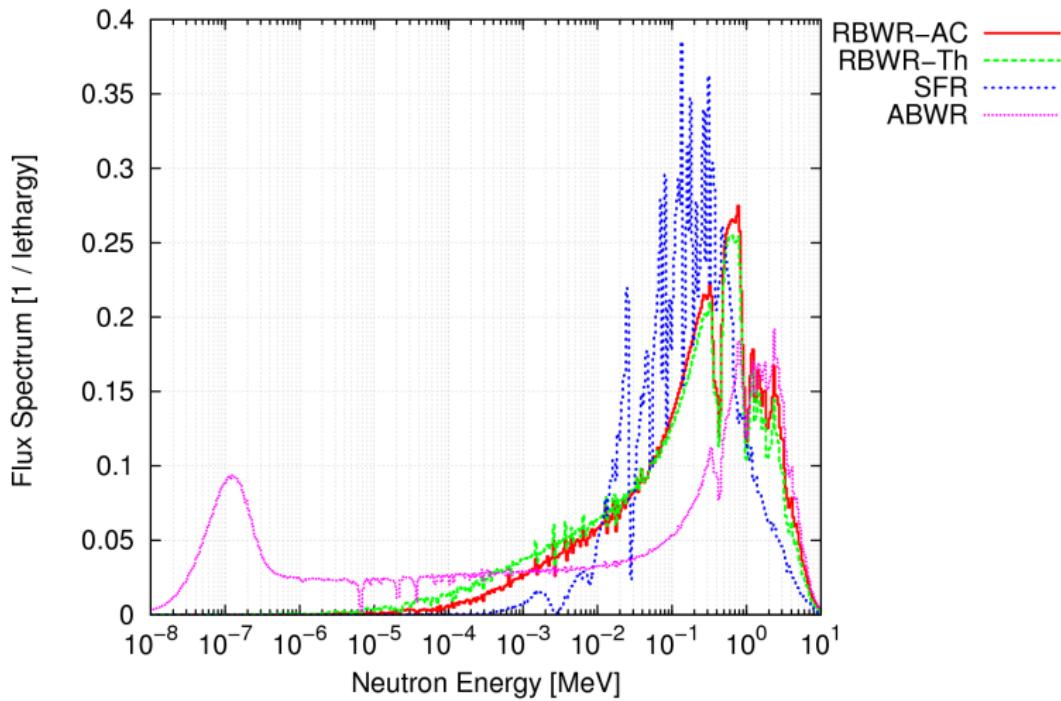
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# The neutron transport equation (NTE) balances sources and sinks within neutron phase space

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$$\vec{\Omega} \cdot \vec{\nabla}_{\vec{r}, E, \vec{\Omega}} \psi(\vec{r}, E, \vec{\Omega}) + \sigma_{total}(\vec{r}, E) N(\vec{r}) \psi(\vec{r}, E, \vec{\Omega}) = \int_0^{\infty} dE \int_{4\pi} d\vec{\Omega}' \sigma_{scatter}(\vec{r}, E' \rightarrow E, \vec{\Omega}' \cdot \vec{\Omega}) N(\vec{r}) \psi(\vec{r}, E', \vec{\Omega}') + \frac{\chi(E)}{4\pi} \int_0^{\infty} dE'' \nu(E'') \sigma_{fission}(\vec{r}, E'') N(\vec{r}) \psi(\vec{r}, E'', \vec{\Omega}'') + S_{ext}(\vec{r}, E, \vec{\Omega})$$

# The easiest approach is simplification

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Summary

## ■ Ignore energy dependence

- Assume directional dependence is isotropic or linearly anisotropic
- Approximate the system as a smeared homogeneous lump
- Assume the spatial/spectral/directional dependencies are separable (e.g.,  $\psi(\vec{r}, E, \vec{\Omega}) = \mathcal{R}(\vec{r})\mathcal{E}(r)\mathcal{W}(\vec{\Omega})$ ) and solve them independently
- You can get creative!
- Also, garbage in, garbage out!

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# The next approach is discretization

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Summary

- 1 Divide spatial regions into cubes or tetrahedra, with interfaces
- 2 Divide the energy axis into hundreds or thousands of bins
- 3 Expand directional dependence in spherical harmonics
- 4 Consider at pseudo-steady-state snapshots in time
- 5 Write an enormous linear system and iterate until convergence
- 6 Sweep through the solution in a manner which mimics the physical path of neutrons

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# The accurate approach is Monte Carlo neutron transport – following neutrons one-at-a-time

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Summary

- 1 Assume a source distribution
- 2 Sample a neutron from it ( $\vec{r}, E, \vec{\Omega}$ )
- 3 Sample how far the neutron travels before a leak or collision
- 4 Sample the collision type (e.g., scatter, fission, capture)
- 5 Sample the collision outcome ( $\vec{r}, E, \vec{\Omega}$ )
- 6 Iterate until the source distribution converges
- 7 Consider accelerating with the simpler models above

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# The NTE often depends upon other fields, so models need to be solved simultaneously

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## ■ Fluids flow (Navier-Stokes)

- Heat spreads (heat equation) and expands things (equation of state of the material)
- Boiling water behaves differently from liquid water (closure relations)
- Solve each one independently – holding the rest constant – and iterate!
- Choose a smart path and consider relaxation for acceleration or stability

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old, new, and  
complicated

Jeffrey  
Seifried

About Me

Nuclear energy  
... is important  
... is old  
... is new

Simulations

The neutron  
transport  
equation  
The Bateman  
equations

Summary

## 1 About Me

### 2 Nuclear energy

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## 3 Simulations

- The neutron transport equation
- The Bateman equations

# Isotope depletion, breeding, and decay can be complicated

Nuclear Energy is important, old, new, and complicated

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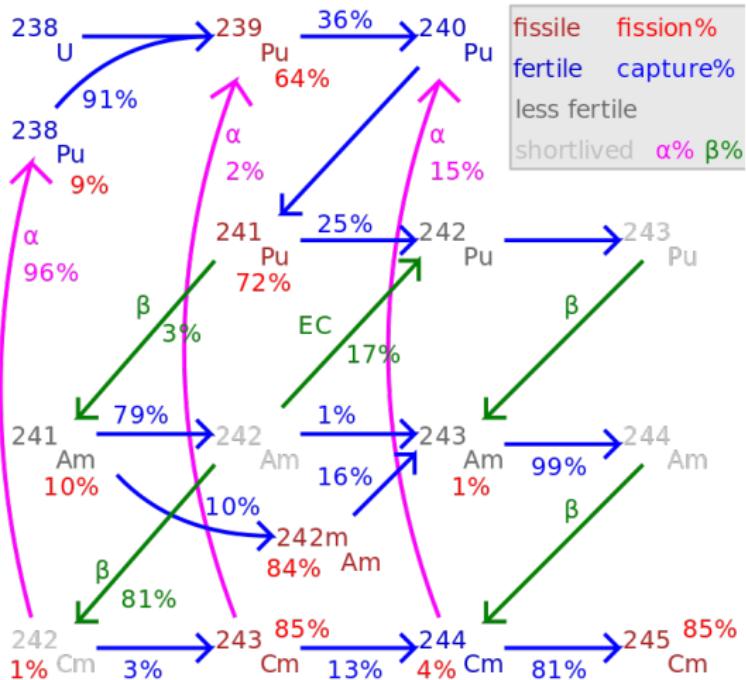
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# The Bateman equations describe the time-evolution of isotopes during decay and irradiation

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$$\begin{aligned} & \frac{\partial N_i(\vec{r}, t)}{\partial t} \\ & + \lambda_i \ N_i(\vec{r}, t) \\ & + \int_0^\infty dE \ \sigma_{absorption,i}(\vec{r}, E) \ \int_{4\pi} d\vec{\Omega} \ \psi(\vec{r}, E, \vec{\Omega}) \ N_i(\vec{r}, t) \\ & = \sum_j [b_{j \rightarrow i} \ \lambda_j \ N_j(\vec{r}, t)] \\ & + \sum_k \left[ b_{k \rightarrow i} \int_0^\infty dE \ \sigma_{absorption,k}(\vec{r}, E) \ \int_{4\pi} d\vec{\Omega} \ \psi(\vec{r}, E, \vec{\Omega}) \ N_k(\vec{r}, t) \right] \end{aligned}$$

# If you take the Laplacian an analytical solution exists!

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$$N_n(t) = \prod_{j=1}^{n-1} \lambda_j \sum_{i=1}^n \sum_{j=1}^n \left( \frac{N_i(0) e^{-\lambda_j t}}{\prod_{p=i, p \neq j} (\lambda_p - \lambda_j)} \right)$$

- The formulation is numerically unstable in real cases
- So, in practice, it is solved numerically

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# The ODE is homogeneous so it can be written as a linear system

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$$\frac{\partial \vec{N}}{\partial t} = \mathbb{T} \vec{N}$$

$$\vec{N}(t) = \vec{N}_0 e^{\mathbb{T}t}$$

$$\vec{N}(t) \approx \mathbb{I} + \mathbb{T}t + \frac{(\mathbb{T}t)^2}{2!} + \dots$$

- $\mathbb{T}$  is large and ill-conditioned in real cases
- So, in practice many of the less relevant terms are zeroed and collapsed

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# Thank you!

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