

assignment02

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University of Southern California
Marshall School of Business
FBE 506 Quantitative Method in Finance

Assignment 02

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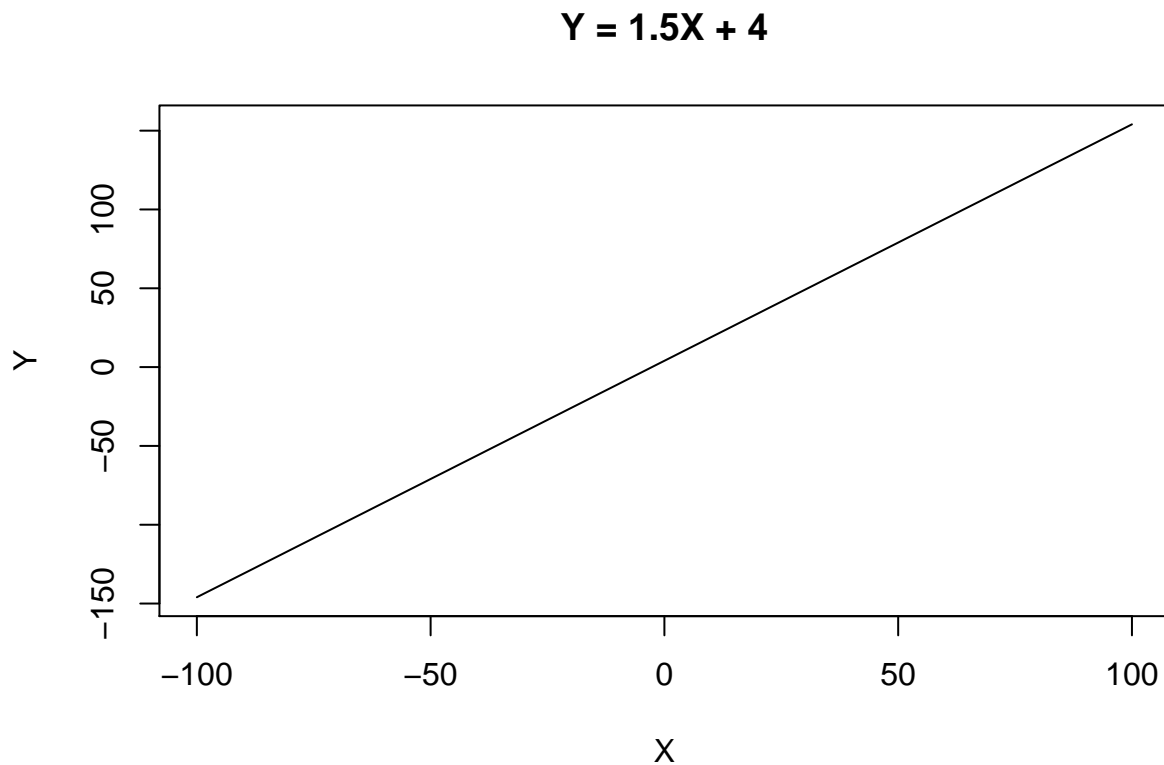
Student ID: 6524885309

Question 1

a. Graph $Y = 1.5X + 4$

The function is a linear function so the graph is a straight line.

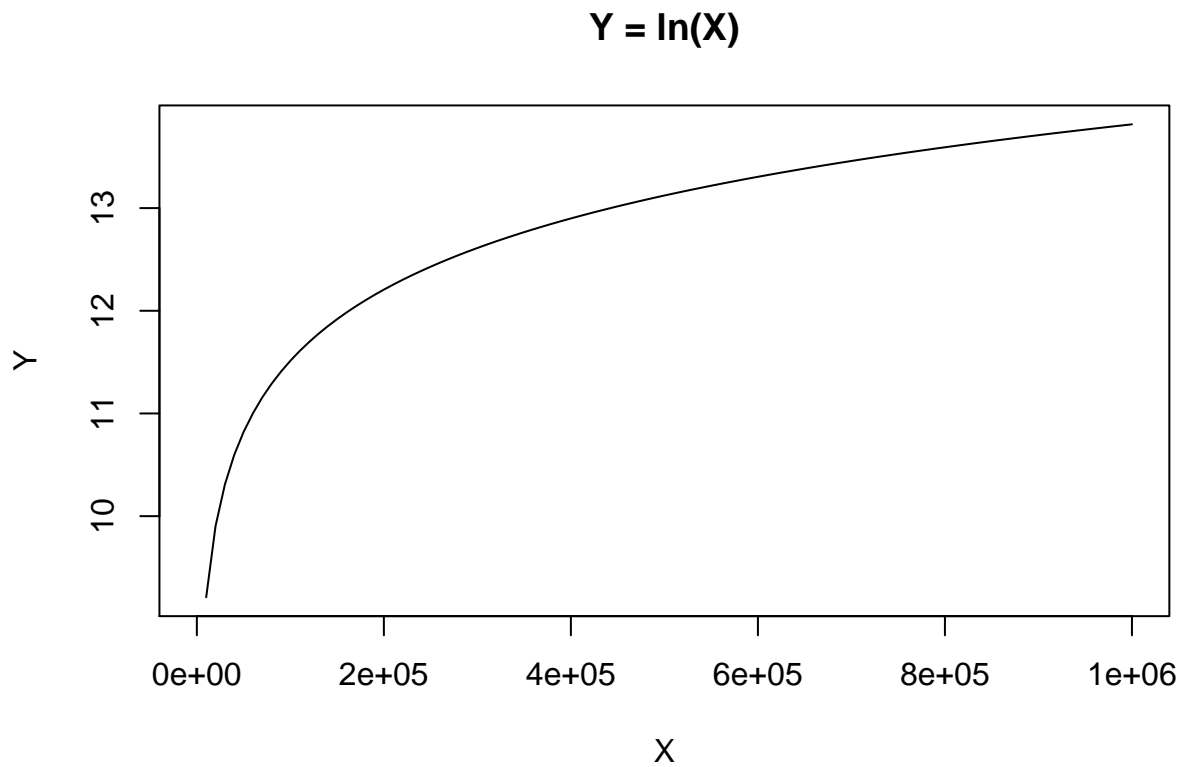
```
# Graph  $Y = 1.5X + 4$   
curve(1.5*x + 4, from = -100, to = 100, ylab = "Y", xlab = "X", main = "Y = 1.5X + 4")
```



b. Graph $Y = \ln(X)$

The function is an inverse function of an exponential function, the graph is a reflection of its related inverse function about the line $Y = X$. Y increases at a decelerated rate as X increases.

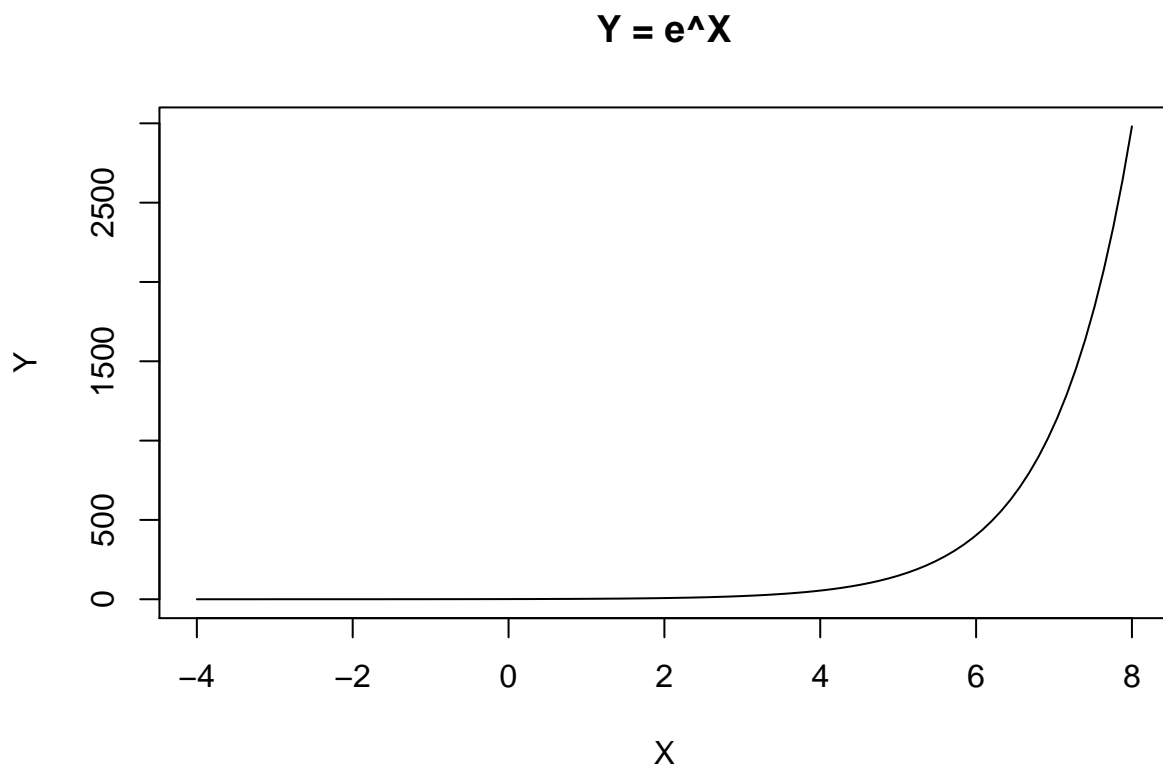
```
# Graph  $Y = \ln(X)$ 
curve(log(x), from = 0, to = 1000000, ylab = "Y", xlab = "X", main = "Y = ln(X)")
```



c. Graph $Y = e^X$

The function is an exponential function, Y value increases at an accelerated rate as X increases.

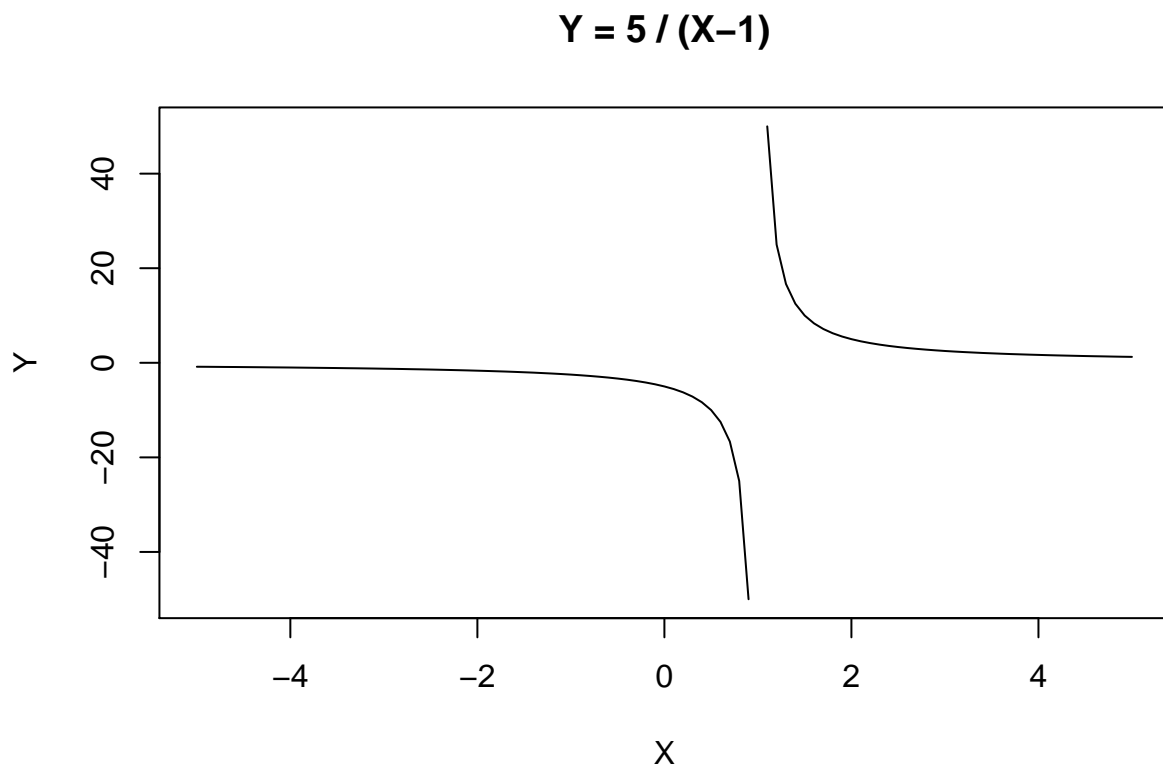
```
# Graph  $Y = e^X$   
curve(exp(x), from = -4, to = 8, ylab = "Y", xlab = "X", main = "Y = e^X")
```



d. Graph $Y = \frac{5}{X-1}$

The function is rational function.

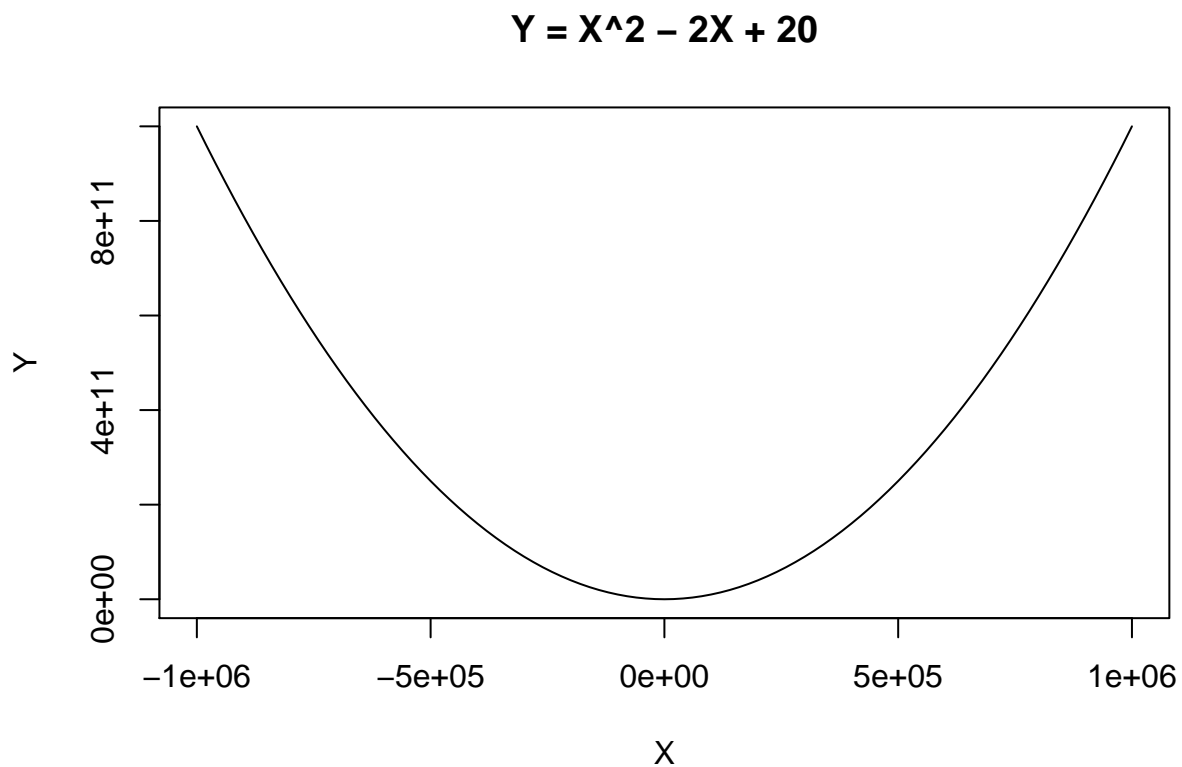
```
# Graph  $Y = \frac{5}{X-1}$ 
curve(5/(x-1), from = -5, to = 5, ylab = "Y", xlab = "X", main = "Y = 5 / (X-1)")
```



e. Graph $Y = X^2 - 2X + 20$

The function is a quadratic function—2nd degree polynomial—, the curve is a parabola,

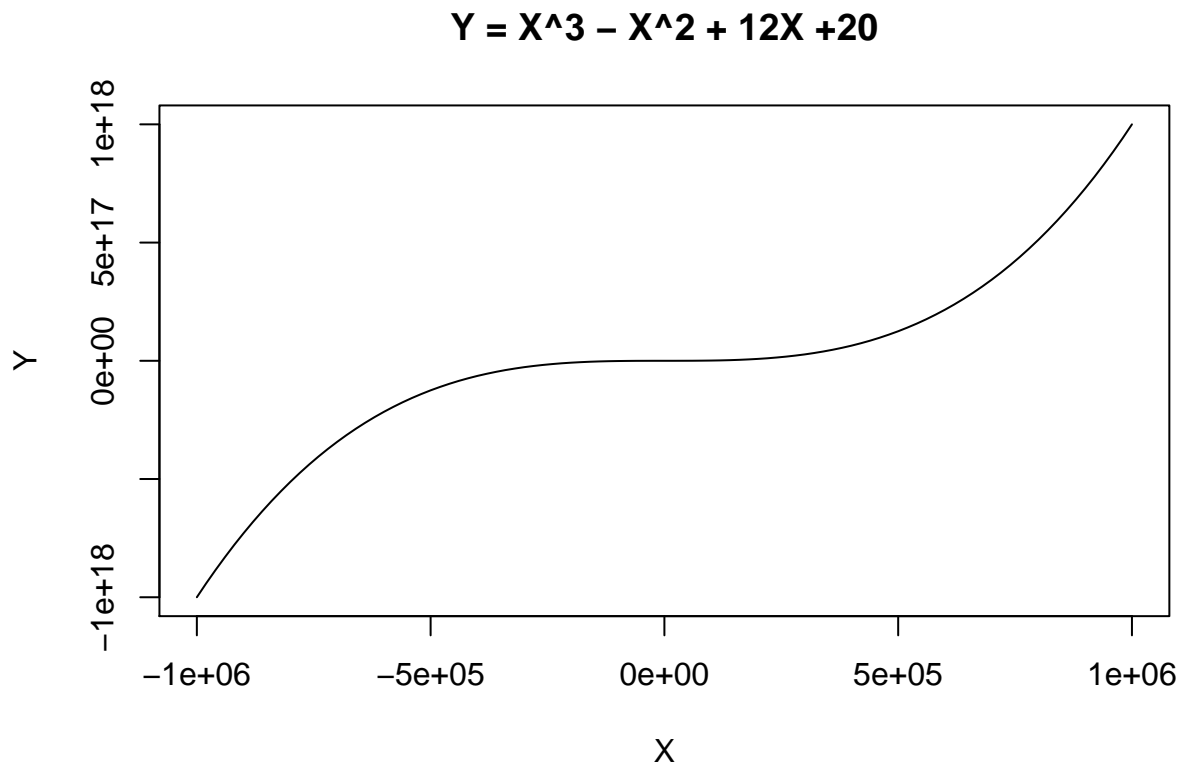
```
# Graph $Y = X^2 - 2X + 20$
curve(x^2 - 2*x + 20, from = -1000000, to = 1000000, ylab = "Y", xlab = "X", main = "Y = X^2 - 2X + 20")
```



f. Graph $Y = X^3 - X^2 + 12X + 20$

The function is a cubic function—3rd degree polynomial.

```
# Graph $Y = X^3 - X^2 + 12X + 20$
curve(x^3 - x^2 + 12*x + 20, from = -1000000, to = 1000000, ylab = "Y", xlab = "X", main = "Y = X^3 - X^2 + 12X + 20")
```

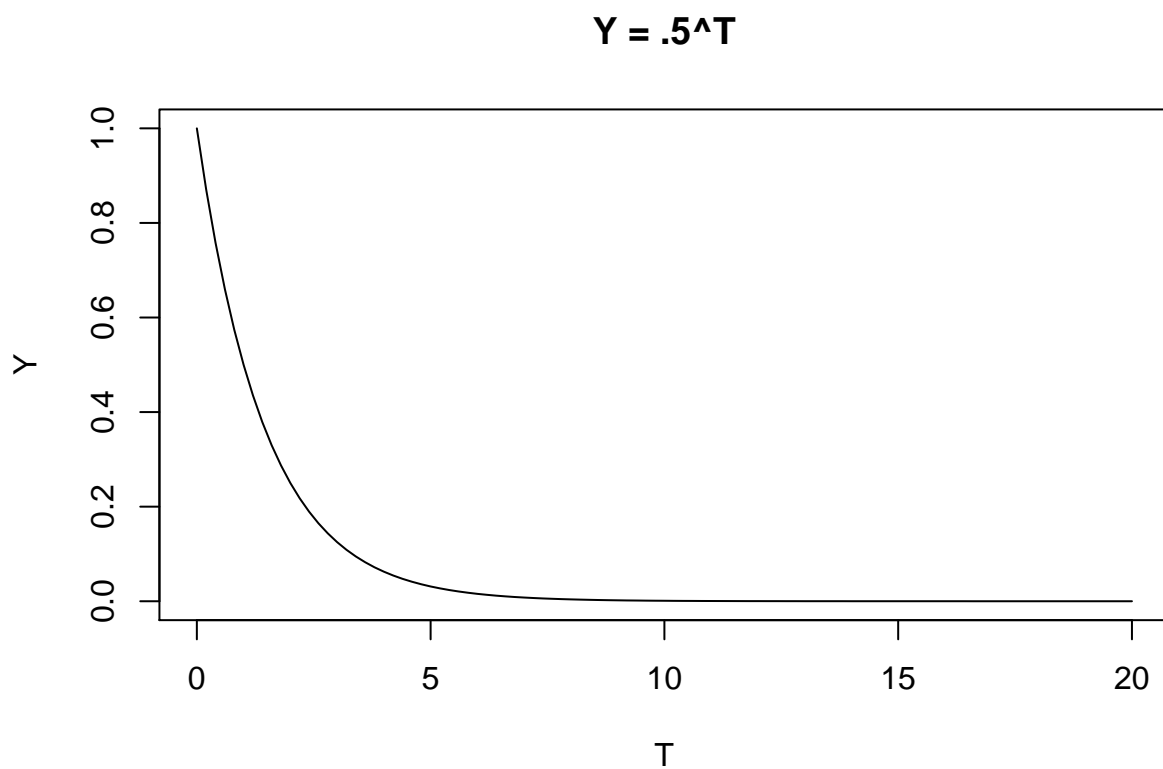


Question 2

a. Graph $Y = .5^T$

The function is an exponential function. The function is strictly decreasing as the base is less than 1.

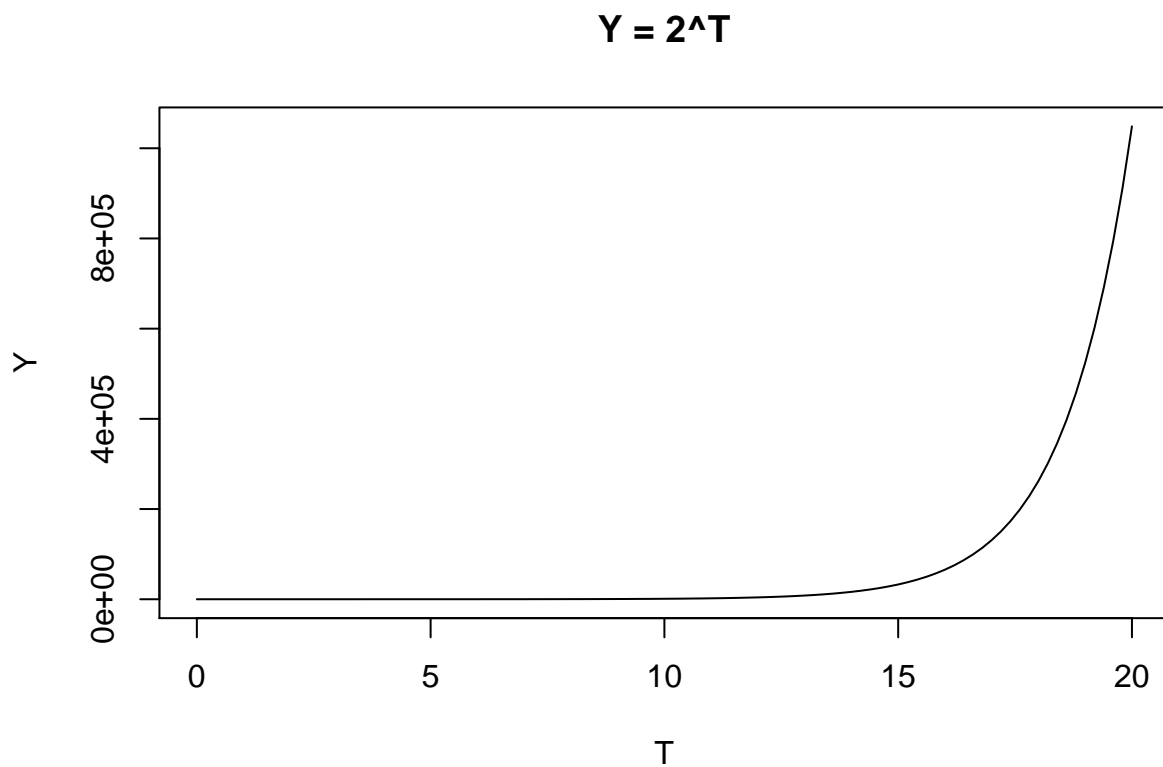
```
# Graph $Y = .5^{T}$
curve(.5^x, from = 0, to = 20, ylab = "Y", xlab = "T", main = "Y = .5^T")
```



b. Graph $Y = 2^T$

The function is an exponential function, the function is strictly increasing as the base is greater than 1.

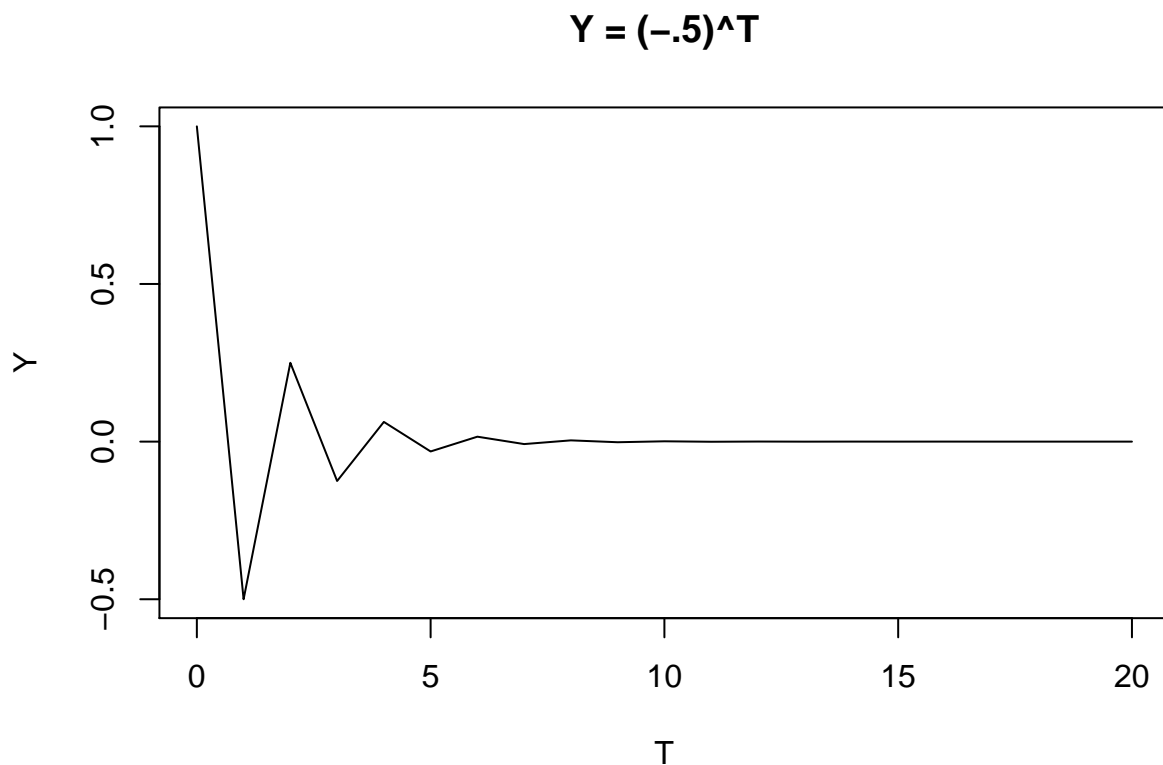
```
# Graph  $Y = 2^T$ 
curve(2^x, from = 0, to = 20, ylab = "Y", xlab = "T", main = "Y = 2^T")
```

c. Graph $Y = (-.5)^T$

The function is an oscillating function.

```
x = c(0:20)
# Graph  $Y = (-.5)^T$ 
plot(x, (-.5)^(x), type = "l", main = "Y = (-.5)^T", xlab = "T", ylab = "Y")
```



Question 3

Install the packages and call the library “quantmod” and download data for S&P 500 (GSPC), Apple (AAPL) from Yahoo and Real Gross Domestic Product (GDPC1) from FRED.

```
# Install the packages and call the library "quantmod"
#install.packages("quantmod") # uncomment to install as neccessary
library(quantmod)
```

```
## Loading required package: xts
```

```
## Loading required package: zoo
```

```
##
```

```
## Attaching package: 'zoo'
```

```
## The following objects are masked from 'package:base':
```

```
##
```

```
## as.Date, as.Date.numeric
```

```
## Loading required package: TTR
```

```
## Registered S3 method overwritten by 'quantmod':
##   method      from
##   as.zoo.data.frame zoo
```

```
## Version 0.4-0 included new data defaults. See ?getSymbols.
```

```
# Get data for S&P500, AAPL
gspc <- getSymbols("~GSPC", src = "yahoo") # S&P500
```

```
## 'getSymbols' currently uses auto.assign=TRUE by default, but will
## use auto.assign=FALSE in 0.5-0. You will still be able to use
## 'loadSymbols' to automatically load data. getOption("getSymbols.env")
## and getOption("getSymbols.auto.assign") will still be checked for
## alternate defaults.
##
## This message is shown once per session and may be disabled by setting
## options("getSymbols.warning4.0"=FALSE). See ?getSymbols for details.
```

```
aapl <- getSymbols("AAPL", src = "yahoo") # AAPL
real_gdpc1 <- getSymbols("GDPC1", src = "FRED") # Real GDP
```

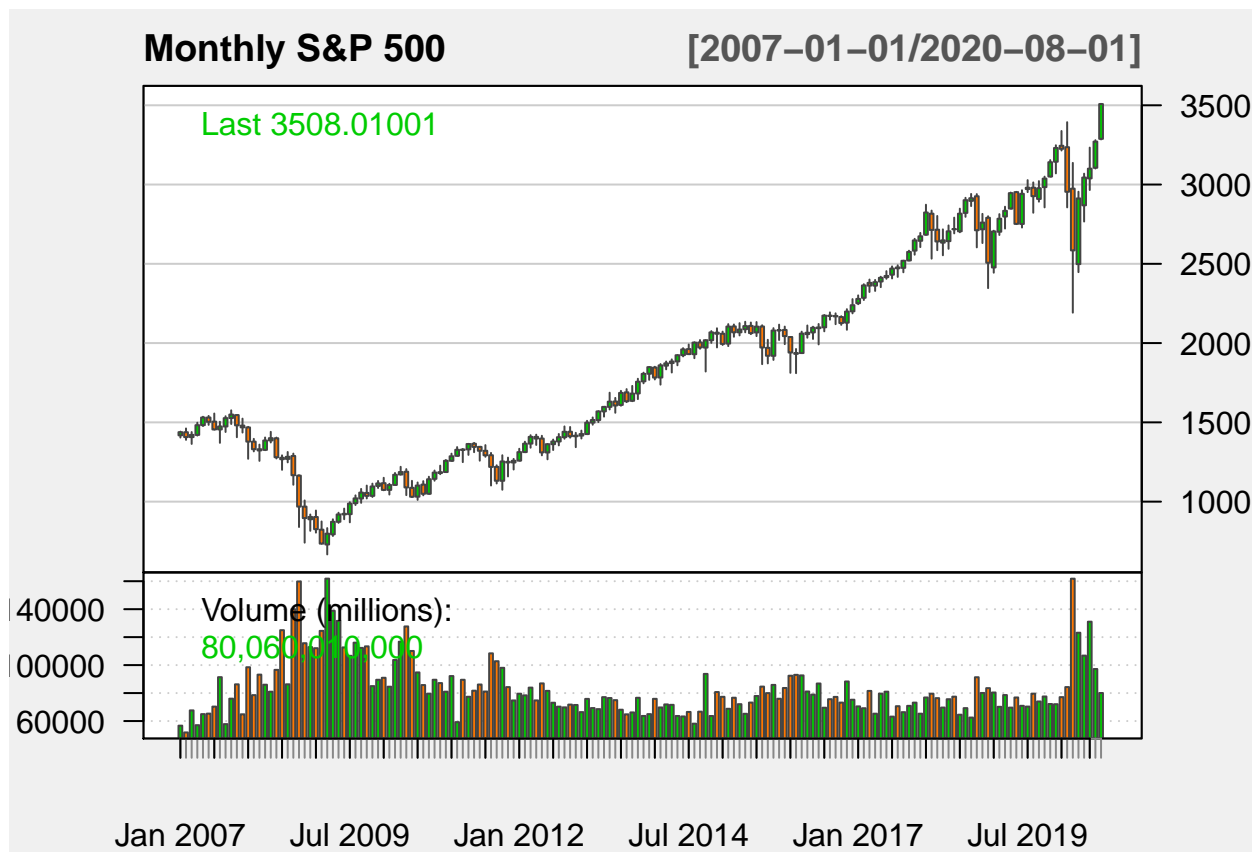
Convert S&P 500 index from daily to monthly and generate returns data.

```
# Convert S&P 500 from daily to monthly
monthly_gspc <- to.monthly(GSPC)

# Convert index to returns
returns_monthly_gspc <- diff(log(GSPC))
```

Graphing monthly S&P 500 index

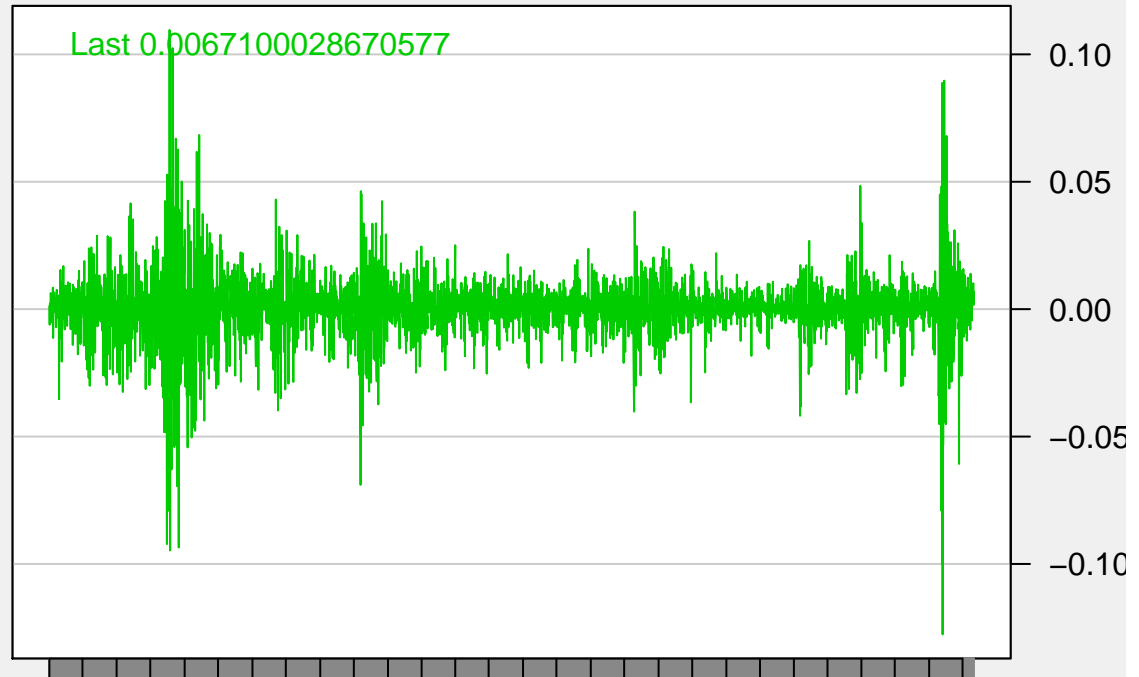
```
# Graphing monthly S&P 500 index
chartSeries(monthly_gspc, name = "Monthly S&P 500", type = "candlesticks", theme = chartTheme("white"))
```



Graphing monthly S&P 500 returns

```
# Graphing monthly S&P 500 returns
chartSeries(returns_monthly_gspc$GSPC.Adjusted, name = "Monthly Returns to S&P 500", type = "candlestick")
```

Monthly Returns to S&P 500 [2007-01-04/2020-08-28]



Jan 04 2007 Jan 04 2010 Jan 02 2013 Jan 04 2016 Jan 02 2019

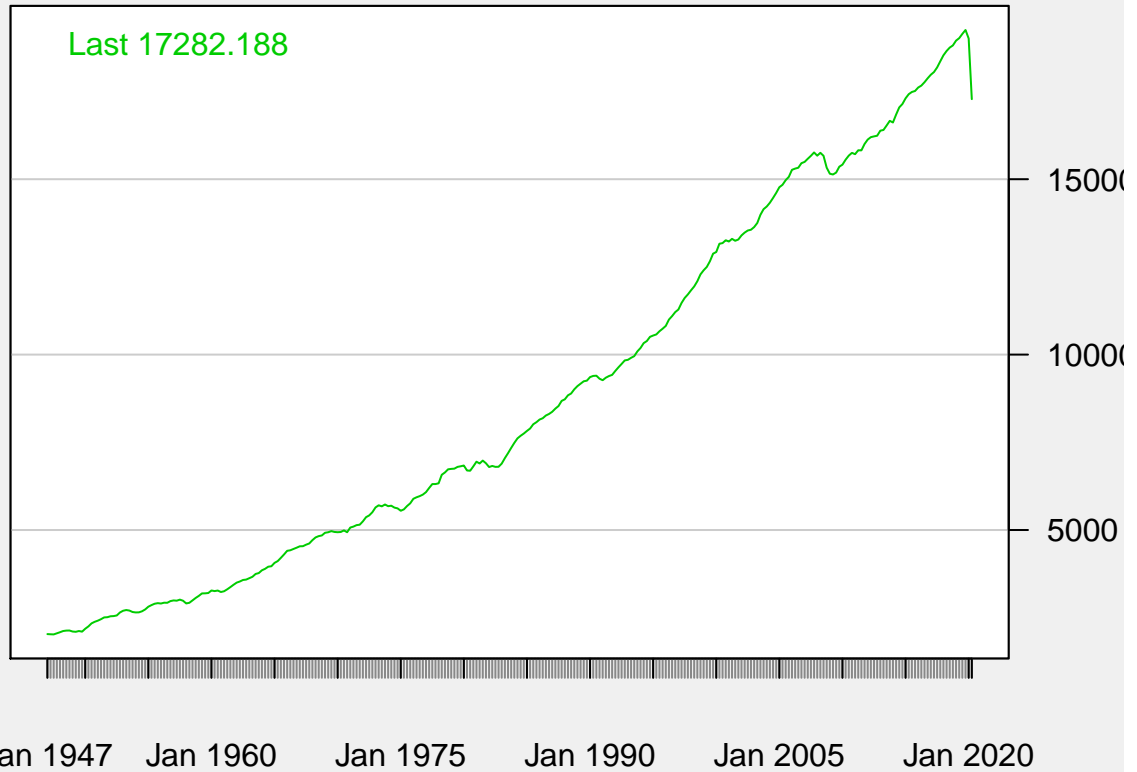
Question 4

Graphing real quarterly GDP

```
# Graphing real quarterly GDP  
chartSeries(GDPC1, name = "Quarterly Real GDP", type = "line", theme = chartTheme("white"))
```

Quarterly Real GDP

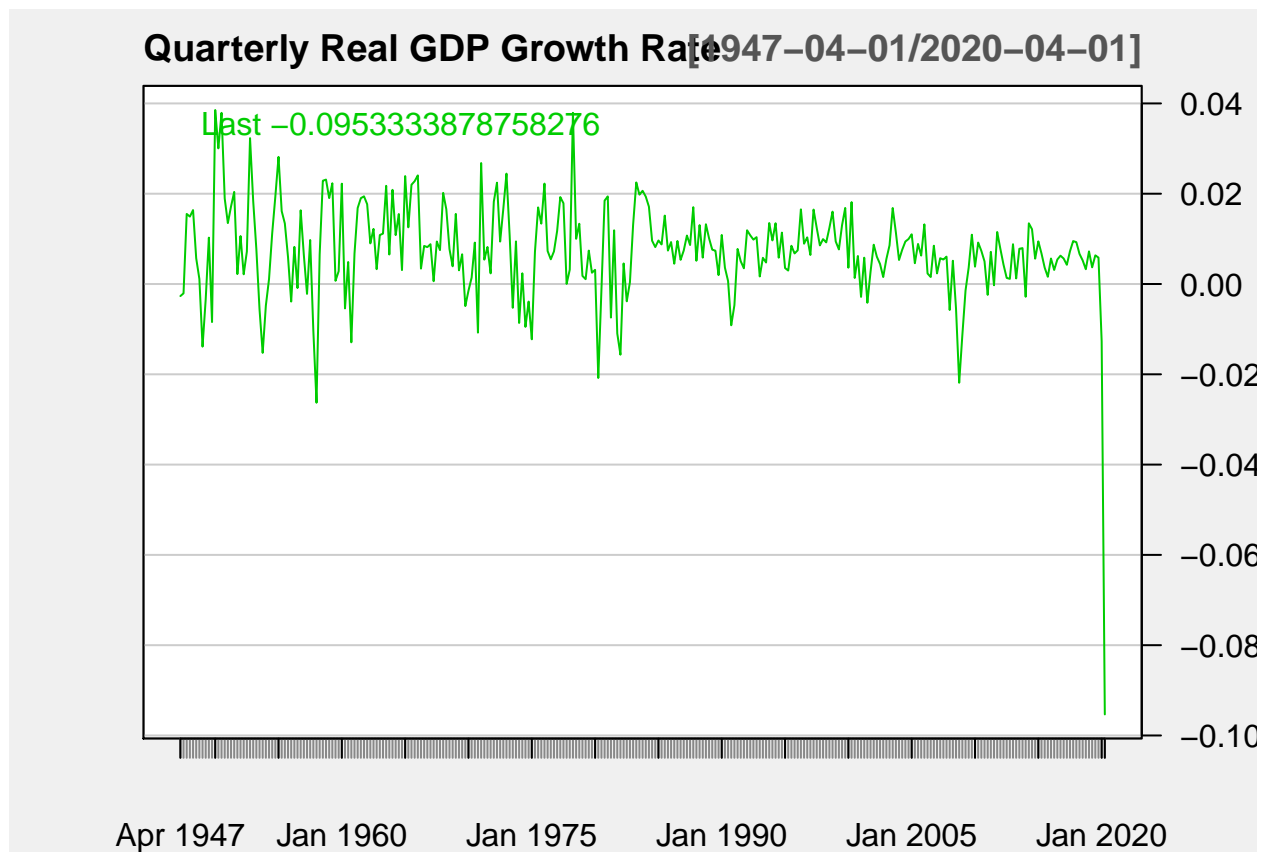
[1947-01-01/2020-04-01]



Convert real GDP to real GDP growth and graph

```
# Convert index to growth  
growth_gdpc1 <- diff(log(GDPC1))
```

```
# Graph real GDP growth  
chartSeries(growth_gdpc1, name = "Quarterly Real GDP Growth Rate", type = "line", theme = chartTheme("w"))
```



Question 5

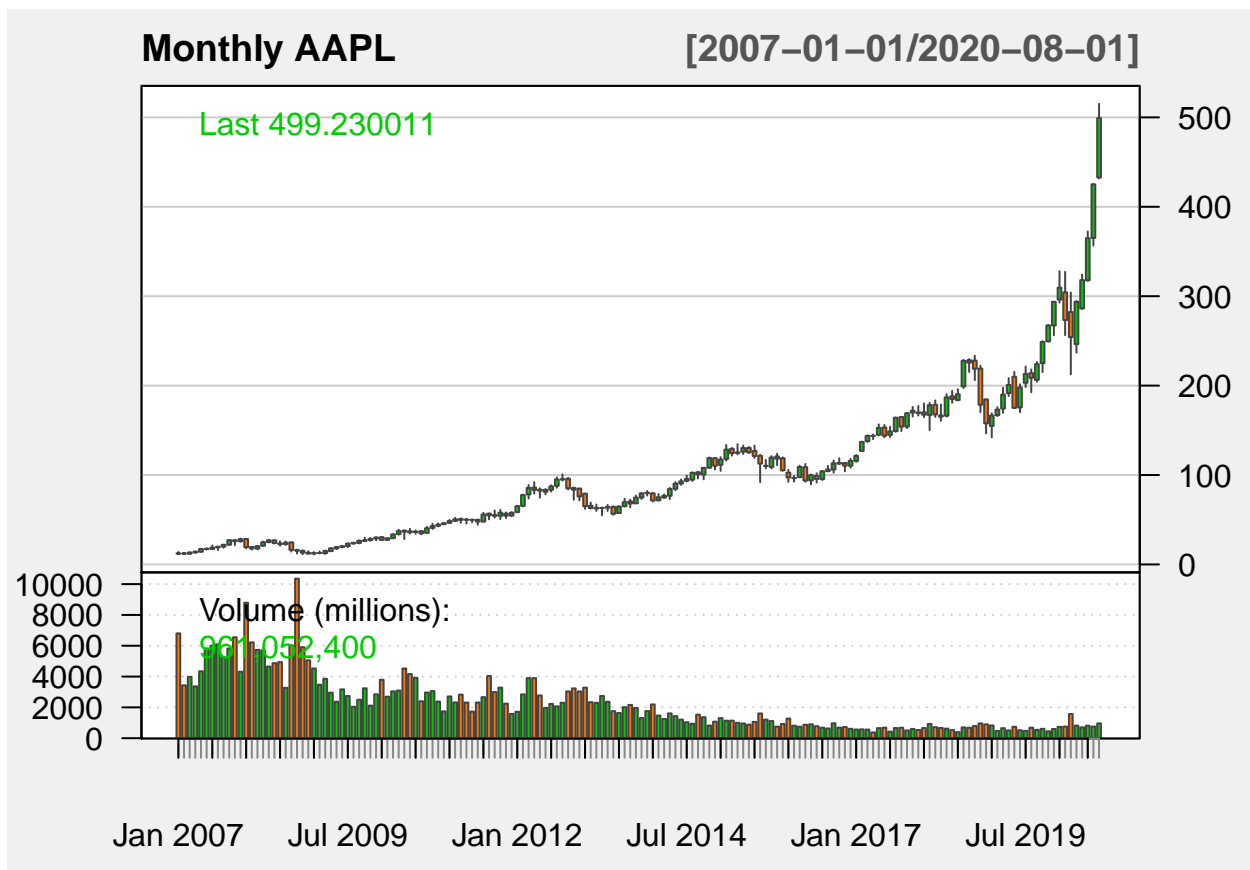
Convert AAPL from daily to monthly and generate returns data.

```
# Convert S&P 500 from daily to monthly
monthly_aapl <- to.monthly(AAPL)

# Convert index to returns
returns_monthly_aapl <- diff(log(AAPL))
```

Graphing monthly AAPL price

```
# Graphing monthly AAPL price
chartSeries(monthly_aapl, name = "Monthly AAPL", type = "candlesticks", theme = chartTheme("white"))
```

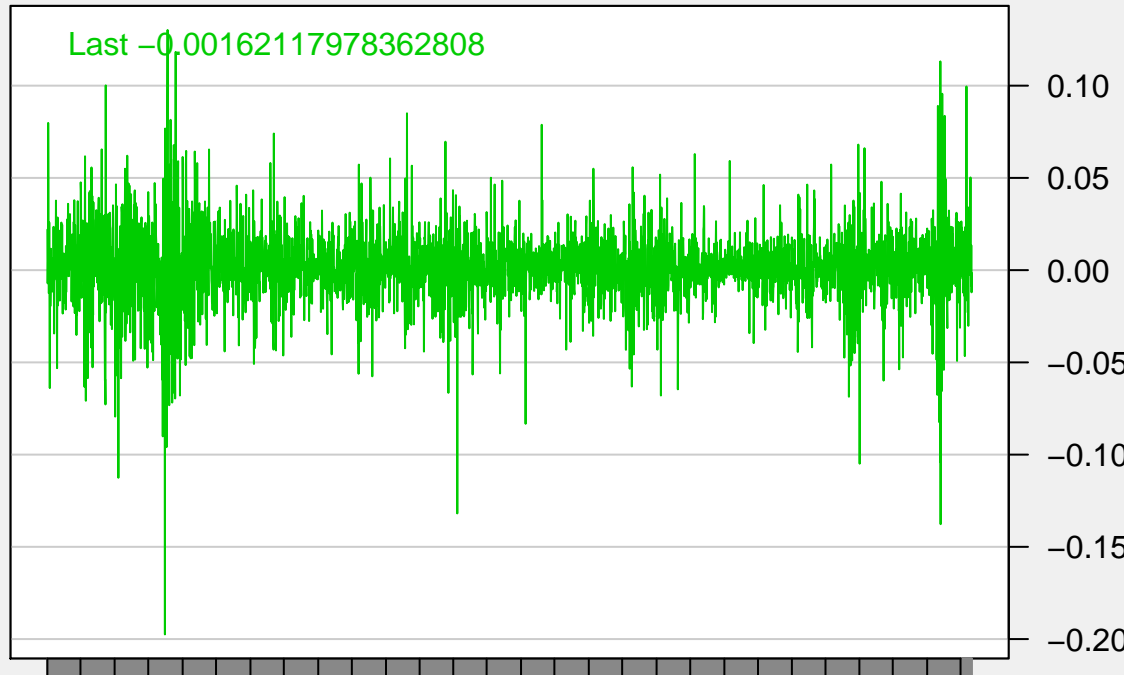


Graphing monthly AAPL returns

```
# Graphing monthly AAPL returns
chartSeries(returns_monthly_aapl$AAPL.Adjusted, name = "Monthly Returns AAPL", type = "candlesticks", t
```


Monthly Returns AAPL

[2007-01-04/2020-08-28]



Jan 04 2007 Jan 04 2010 Jan 02 2013 Jan 04 2016 Jan 02 2019

Question 6

Graph monthly AAPL and monthly S&P500 on one coordinate system:

```
# Initialize xts objects contain adjusted price for S&P 500 and AAPL and merge
gspc_xts <- as.xts(monthly_gspc[, "GSPC.Adjusted"])
aapl_xts <- as.xts(monthly_aapl[, "AAPL.Adjusted"])
price_compare <- merge.xts(gspc_xts, aapl_xts)

# Graph monthly AAPL and monthly S&P500 on one coordinate system
# Plot S&P 500
plot(as.zoo(price_compare[, "GSPC.Adjusted"]), screens = 1, main = "S&P 500 and APPL Adjusted Price Over",
     xlab = "Year", ylab = "Price", col = "Red")

# Keep working on the same plot
par(new = TRUE)

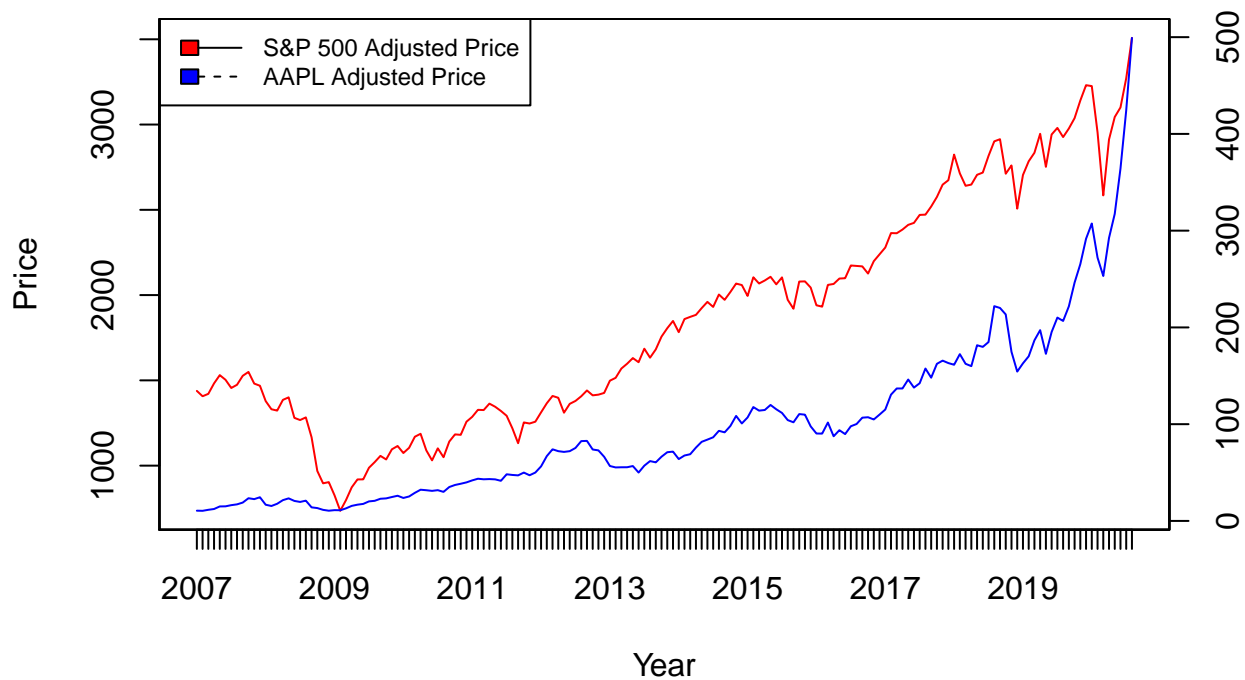
# Plot AAPL and suppress axis value
plot(as.zoo(price_compare[, "AAPL.Adjusted"]), screens = 1, xaxt = "n", yaxt = "n", xlab = "", ylab = "")

# Add right-handed axis to display AAPL price
axis(4)

# Add legend
```

```
legend("topleft", c("S&P 500 Adjusted Price", "AAPL Adjusted Price"), lty = 1:3, cex = 0.75, fill = c("red", "blue"))
```

S&P 500 and APPL Adjusted Price Overlay



Observations from the overlay chart above regarding S&P 500 and AAPL: 1. Seasonal Trend: Both display similar seasonal trend with up and down spikes in price. 2. Cyclical Trend: Both is affected by business cycle, S&P 500 more so than AAPL (most noticably during the Great Recession of '07 where S&P 500 experienced sharp downturn compare to AAPL) 3. Auto-correlation: Both behave similar in this regard where both rises for some times when they rise and vice versa. 4. Randomness: Price of both is unpredictable. 5. Time: Both follows similar time trend.

Question 7

Graph monthly AAPL and monthly S&P500 on one coordinate system:

```
# Initialize xts objects contain close price returns for S&P 500 and AAPL and merge
returns_gspc_xts <- as.xts(returns_monthly_gspc[, "GSPC.Adjusted"])
returns_aapl_xts <- as.xts(returns_monthly_aapl[, "AAPL.Adjusted"])
returns_compare <- merge.xts(returns_gspc_xts, returns_aapl_xts)

# Graph monthly AAPL and monthly S&P 500 returns on one coordinate system
# Plot S&P 500 monthly returns
plot(as.zoo(returns_compare[, "GSPC.Adjusted"]), screens = 1, main = "S&P 500 and APPL Adjusted Price Overlay",
     xlab = "Year", ylab = "Returns", col = "Red")

# Keep working on the same plot
```

```

par(new = TRUE)

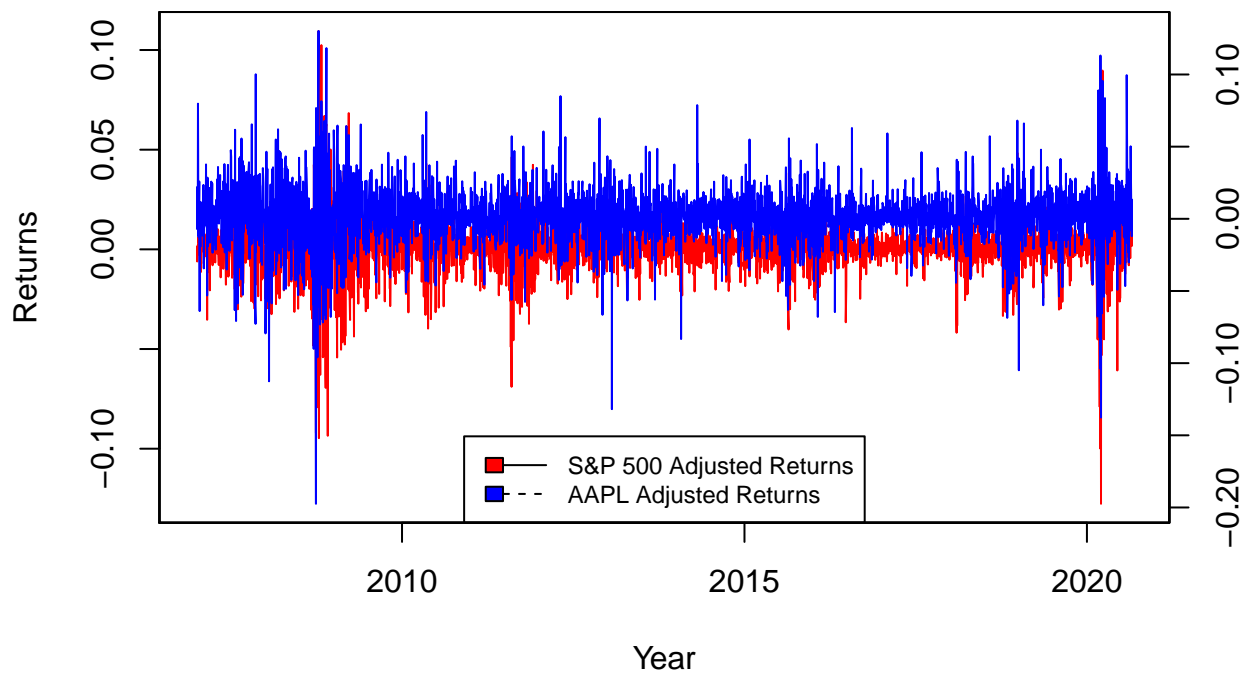
# Plot AAPL monthly returns and suppress axis value
plot(as.zoo(returns_compare[, "AAPL.Adjusted"]), screens = 1, xaxt = "n", yaxt = "n",
     xlab = "", ylab = "", col = "Blue")

# Add right-handed axis to display AAPL price
axis(4)

# Add legend
legend("bottom", c("S&P 500 Adjusted Returns", "AAPL Adjusted Returns"), lty = 1:3, cex = 0.75, fill = c(

```

S&P 500 and APPL Adjusted Price Overlay



In addition to the trends as commented above, AAPL and S&P 500 returns do not always trend in the same direction. This could be attributed to fluctuations in stock price experienced by single companies based on their quarterly earnings season performance, whereas the indices such as the S&P 500 is more or less insulated from these fluctuations.

Furthermore, based on investor's sentiments, single companies' stocks could experience larger upswing or drawdown. This can be observed in 2020 period. With the COVID-19 pandemic, tech stocks such as AAPL retreated less compared the S&P 500 in March 2020 (longer red line drawdown on the graph) with worldwide lockdown in effects, yet they recovered quickly and outperformed the index in the following months (longer blue line upswing on the graph)