assignment 05

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Regression Analysis on impact of COVID-19 on a 5-stock portfolio. Ngoc Son (Jeff) Nguyen University of Southern California Marshall School of Business FBE 506 Quantitative Method in Finance Fall 2020 Directed by Professor Mohammad Safarzadeh

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Abstract

Introduction

We selected the following 5 securities to base our analysis of impact of COVID-19 on a CAPM model of 5 stocks upon.

Ticker	Security	Sector	Industry	Founded	Full Time Employees
MSFT	Microsoft Corporation	Technology	Software- Infrastructure	1975	163,000
GWPH	GW Pharmaceuticals PLC	Healthcare	Drug Manufacturers- General	1998	901
DIS	The Walt Disney Company	Communication Services	Entertainment	1923	223,000
CAT	Caterpillar INC	Industrials	Farm & Heavy Construction Machinery	1925	102,300
AMZN	Twitter INC	Consumer Cyclical	Internet Retail	1994	1,125,300

All information and data related to the securities are obtained from Yahoo Finance: MSFT, GWPH, DIS, CAT, and AMZN.

The objective of the study of the study is using the Modern Portfolio Theory to model a portfolio of five securities from different industries using adjusted closing price data from January 02, 2014 to December 31,

2018 to achieve the following:

- 1) Estimated the CAPM for the five securities portfolio.
- 2) Understand the impact of COVID-19 on the alpha and market risk of the CAPM model.
- 3) Compare the MPT portfolio to a similarly diversified portfolio (State Street's SPDR S&P 500 Trust ETF).
 - 4) Use the CAPM model to forecast the returns on the portfolio.

Data Analysis

- 1) Estimated the CAPM for the five securities portfolio
- 1. Select at least five stocks from different industries (for the list of the firms in different industries see, https://biz.yahoo.com/p/sum_conameu.html).

```
library(quantmod)
## Loading required package: xts
## Loading required package: zoo
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
## Loading required package: TTR
## Registered S3 method overwritten by 'quantmod':
##
    method
                       from
     as.zoo.data.frame zoo
## Version 0.4-0 included new data defaults. See ?getSymbols.
# Set start date and end date of data
start_date <- "2014-01-01"
end_date <- "2018-12-31"
# Get data
getSymbols("MSFT", src = "yahoo", from = start_date, to = end_date)
## 'getSymbols' currently uses auto.assign=TRUE by default, but will
## use auto.assign=FALSE in 0.5-0. You will still be able to use
## 'loadSymbols' to automatically load data. getOption("getSymbols.env")
## and getOption("getSymbols.auto.assign") will still be checked for
## alternate defaults.
##
## This message is shown once per session and may be disabled by setting
## options("getSymbols.warning4.0"=FALSE). See ?getSymbols for details.
```

```
## [1] "MSFT"
getSymbols("GWPH", src = "yahoo", , from = start_date, to = end_date)
## [1] "GWPH"
getSymbols("DIS", src = "yahoo", , from = start_date, to = end_date)
## [1] "DIS"
getSymbols("CAT", src = "yahoo", , from = start_date, to = end_date)
## [1] "CAT"
getSymbols("AMZN", src = "yahoo", , from = start_date, to = end_date)
## [1] "AMZN"
getSymbols("GSPC", src = "yahoo", , from = start_date, to = end_date) # SEP 500
## [1] "^GSPC"
getSymbols("^TNX", src = "yahoo", from = start_date, to = end_date) # TNX (10-year T-bill)
## Warning: ^TNX contains missing values. Some functions will not work if objects
## contain missing values in the middle of the series. Consider using na.omit(),
## na.approx(), na.fill(), etc to remove or replace them.
## [1] "^TNX"
# Adjusted Prices
adjMSFT <- MSFT$MSFT.Adjusted
adjGWPH <- GWPH$GWPH.Adjusted
adjDIS <- DIS$DIS.Adjusted
adjCAT <- CAT$CAT.Adjusted
adjAMZN <- AMZN$AMZN.Adjusted
# Get adjusted returns data
rMSFT <- diff(log(to.monthly(MSFT)$MSFT.Adjusted))</pre>
rGWPH <- diff(log(to.monthly(GWPH) $GWPH.Adjusted))
rDIS <- diff(log(to.monthly(DIS) DIS.Adjusted))
rCAT <- diff(log(to.monthly(CAT)$CAT.Adjusted))
rAMZN <- diff(log(to.monthly(AMZN)$AMZN.Adjusted))
rGSPC <- diff(log(to.monthly(GSPC) $GSPC.Adjusted))
rTNX <- (to.monthly(TNX)$TNX.Adjusted) / 1200 # Using monthly rate
## Warning in to.period(x, "months", indexAt = indexAt, name = name, ...): missing
## values removed from data
```

```
# Calculate statistics
MSFT_return_mean <- mean(rMSFT, na.rm = TRUE)</pre>
GWPH_return_mean <- mean(rGWPH, na.rm = TRUE)</pre>
DIS_return_mean <- mean(rDIS, na.rm = TRUE)</pre>
CAT_return_mean <- mean(rCAT, na.rm = TRUE)</pre>
AMZN_return_mean <- mean(rAMZN, na.rm = TRUE)
GSPC_return_mean <- mean(rGSPC, na.rm = TRUE)</pre>
TNX_return_mean <- mean(rTNX, na.rm = TRUE)</pre>
MSFT_return_var <- var(rMSFT, na.rm = TRUE)</pre>
GWPH_return_var <- var(rGWPH, na.rm = TRUE)</pre>
DIS_return_var <- var(rDIS, na.rm = TRUE)</pre>
CAT_return_var <- var(rCAT, na.rm = TRUE)</pre>
AMZN_return_var <- var(rAMZN, na.rm = TRUE)
GSPC_return_var <- var(rGSPC, na.rm = TRUE)</pre>
# Excess Returns
reMSFT <- rMSFT - rTNX
reGWPH <- rGWPH - rTNX
reDIS <- rDIS - rTNX
reCAT <- rCAT - rTNX
reAMZN <- rAMZN - rTNX
# Information Tables:
pricTabl <- data.frame(MSFT, GWPH, DIS, CAT, AMZN)</pre>
# Creates data frame of asset prices
retTabl <- data.frame(rMSFT, rGWPH, rDIS, rCAT, rAMZN)</pre>
# Creates data frame of returns
EretTabl <- data.frame(reMSFT, reGWPH, reDIS, reCAT, reAMZN)</pre>
# Excess return data frame
retTabl <- retTabl[-1,] # remove missing data due to lagging</pre>
EretTabl <- EretTabl[-1,] # remove missing data due to lagging</pre>
priceMat <- matrix(c(MSFT, GWPH, DIS, CAT, AMZN), nrow= length(MSFT), ncol=5, byrow=TRUE) # creates a
# Variance/Covariance Matrix
asset.names <- c("MSFT", "GWPH", "DIS", "CAT", "AMZN")
# Create a list of row and col names for the var/cov matrix
VCV <- matrix(c(cov(retTabl)), nrow=5, ncol = 5, byrow=TRUE) # create a var/cov matrix by finding cov o
dimnames(VCV) <- list(asset.names, asset.names) # assigns asset.names to the VCV matrix</pre>
#Calculate Returns
rm <- matrix(colMeans(retTabl, na.rm=TRUE)) # creates an average return matrix, omitting missing value
erm <- matrix(colMeans(EretTabl, na.rm=TRUE)) # creates an average excess return matrix, omitting miss
tnxy = mean((rTNX)[-1,]) # calculates the average bond yield excluding Jan (risk free rate)
#Create Return Table
retmat <- matrix(c(rm, erm), ncol=2)</pre>
dimnames(retmat) = list(asset.names, c("Return ", "Excess Return"))
```

First we want to look at the data statistics

Instruments	Mean Returns	Variance of Returns	Beta (5Y Monthly)
MSFT	0.0185744	0.0035553	.87
GWPH	0.0090021	0.0293563	1.96
DIS	0.0078206	0.0026173	1.08
CAT	0.0076711	0.0057854	.98
AMZN	0.024	0.006961	1.3

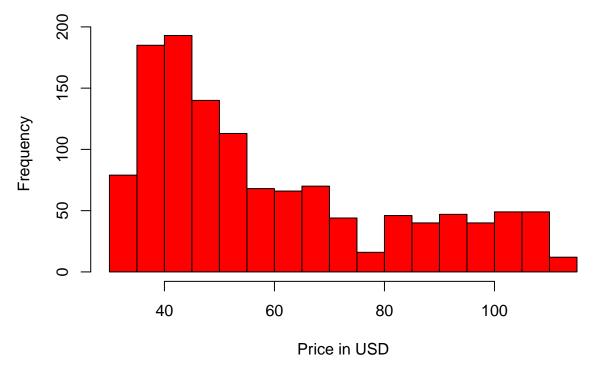
Parameters of indices:

Instruments	Mean Returns	Variance of Returns	Beta
S&P 500	0.0056356	0.0010169	N/A
10-Year T-bill	0.0019378	0	N/A

We look at distribution of adjusted closing prices for each security:

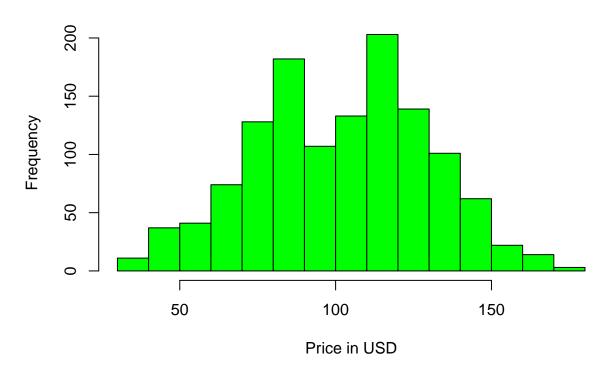
```
hist(adjMSFT,
    main='Daily Adjusted Closing Prices for MSFT',
    xlab='Price in USD',
    col='red',
)
```

Daily Adjusted Closing Prices for MSFT



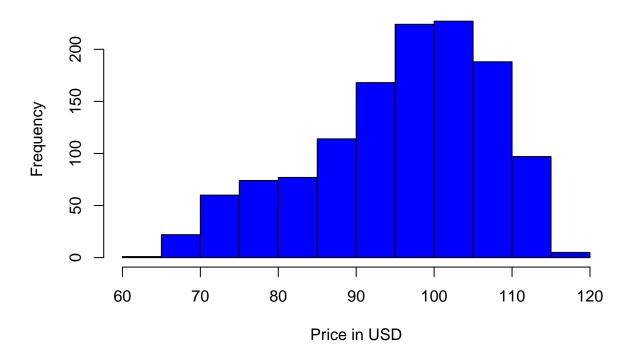
```
hist(adjGWPH,
    main='Daily Adjusted Closing Prices for GWPH',
    xlab='Price in USD',
    col='green',
)
```

Daily Adjusted Closing Prices for GWPH



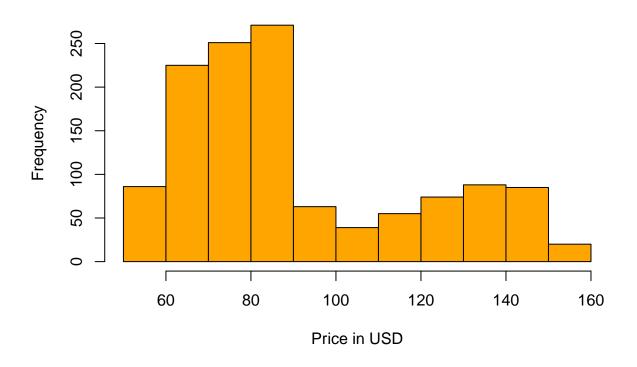
```
hist(adjDIS,
    main='Daily Adjusted Closing Prices for DIS',
    xlab='Price in USD',
    col='blue',
)
```

Daily Adjusted Closing Prices for DIS



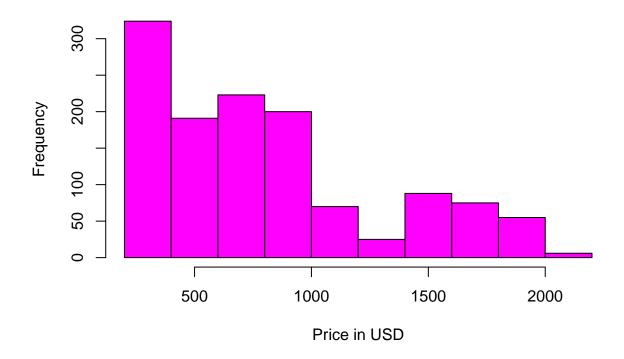
```
hist(adjCAT,
    main='Daily Adjusted Closing Prices for CAT',
    xlab='Price in USD',
    col='orange',
)
```

Daily Adjusted Closing Prices for CAT



```
hist(adjAMZN,
    main='Daily Adjusted Closing Prices for AMZN',
    xlab='Price in USD',
    col='magenta',
)
```

Daily Adjusted Closing Prices for AMZN



CAPM Portfolio Construction

Question covered: 2,3,4,5

Methodology

- 2a) Find the optimum weights using MPT.
- 2b) Allocate \$100.00 among the selected stocks using adjusted closing prices at 2018M12. 2019M1 will have a value of 100 as an index.
- 2c) Using the adjusted closing prices from 2018M12 to 2020M8 calculate the holding values of the portfolio (assume fixed holdings with no re-balancing taking place over time).
 - 3) Find the tangency point of the Capital Allocation Line (CAL) and the efficient frontier.
 - 4) Calculate the CAL equation and graph CAL and the efficient frontier.
- 5) Estimate CAPM for your portfolio and graph the estimated β of the CAPM and the average return of your portfolio as a point relative to SML.

2a) Find the optimum weights using MPT

Since the investor's objective is to minimize risk subjected to a minimum return of the risk free asset–US Treasury Bill, in this case–we solve the constrained optimization problem.

Let x_i denotes the weight of the investment in asset i (i = 1, 2, 3, 4, 5), and assume all money is invested in i, meaning $\sum x_i = x_1 + x_2 + x_3 + x_4 + x_5 = 1$.

The returns of the portfolio is:

$$R_{p,x} = x_1 * r_1 + x_2 * r_2 + x_3 * r_3 + x_4 * r_4 + x_5 * r_5$$

The expected returns on the portfolio is:

$$\mu_{p,x} = E[R_{p,x}]$$

$$= x_1 * \mu_1 + x_2 * \mu_2 + x_3 * \mu_3 + x_4 * \mu_4 + x_5 * \mu_5$$
(1)

The variance of the portfolio returns is:

$$\sigma_{p,x}^2 = var(R_{p,x})$$

Formulating the Markowitz portfolio problem:

The investor's objective is:

$$max \quad \mu_p = w' * \mu \quad \text{s.t.}$$

$$\sigma_p^2 = w' * (\sum) * w \quad \text{and} \quad w' * I = 1$$

where:

w = matrix of asset weights in the portfolio

w' = transpose matrix of asset weights in the portfolio

 $\mu = -$ matrix of mean returns of asset in the portfolio

 \sum = Variance-covariance matrix of asset returns in the portfolio

 $w' * I = \sum_{i=1}^{n} w_i$ or the sum weights of the asset in the portfolio, I is notation for identity matrix

(2)

Let $\mu_{p,0}$ denotes a target expected return level. Formulate the problem:

min
$$\sigma_{p,w}^2 = w' * (\sum) * w$$
 s.t.
 $\mu_p = w' * \mu = \mu_{p,0}, \text{ and } w' * I = 1$ (3)

To solve this, form the Lagrangian function:

$$L(w, \lambda_1, \lambda_2) = w' * \sum *w + \lambda_1 * (w' * \mu - \mu_{p,0}) + \lambda_2 * (w' * I - 1)$$
(4)

Because there are two constraints $(w' * \mu = \mu_{p,0} \text{ and } w'1 = 1)$ there are two Langrange multipliers λ_1 and λ_2 . The first order condition for a minimum are the linear equations:

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial w} = \frac{\partial (\sum *w^2)}{\partial w} + \frac{\partial (\lambda_1 * (w' * \mu - \mu_{p,0}))}{\partial w} + \frac{\lambda_2 * (w' * I - 1)}{\partial w} = 0$$

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial \lambda_1} = 0$$

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial \lambda_2} = 0$$
(5)

Simplify, we have:

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial w} = 2 * \sum *w + \lambda_1 * \mu + \lambda_2 * I = 0$$

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial \lambda_1} = w' * \mu - \mu_{p,0} = 0$$

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial \lambda_2} = w' * I - 1 = 0$$
(6)

Rewrite in matrix form:

$$\begin{pmatrix} 2 * \sum & \mu & I \\ \mu' & 0 & 0 \\ I' & 0 & 0 \end{pmatrix} * \begin{pmatrix} w \\ \lambda_1 \\ \lambda_2 \end{pmatrix} = \begin{pmatrix} 0 \\ \mu_{p,0} \\ I \end{pmatrix}$$
 (7)

or

where
$$A = \begin{pmatrix} 2 * \sum & \mu & I \\ \mu' & 0 & 0 \\ I' & 0 & 0 \end{pmatrix}$$

$$z_w = \begin{pmatrix} w \\ \lambda_1 \\ \lambda_2 \end{pmatrix}$$

$$b_0 = \begin{pmatrix} 0 \\ \mu_{p,0} \\ I \end{pmatrix}$$
(8)

The solution for z_w is:

$$z_w = A^{-1} * b_0 (9)$$

The variance-covariance matrix is as follow:

VCV

```
## MSFT 0.003555316 0.001599836 0.001128235 0.002042991 0.002538589

## GWPH 0.001599836 0.029356292 0.002528779 0.005980634 0.005396791

## DIS 0.001128235 0.002528779 0.002617304 0.001243413 0.001405934

## CAT 0.002042991 0.005980634 0.001243413 0.005785368 0.002040476

## AMZN 0.002538589 0.005396791 0.001405934 0.002040476 0.006961024
```

 $A * z_w = b_0$

The monthly risk-free rate is: 0.001933

```
# Optimum Portfolio
ZOPT <- solve(VCV,erm) # multiply inverse of VCV to excess return to find z
WOPT <- ZOPT/sum(ZOPT) # calculates weights
dimnames(WOPT) <- list(asset.names, "Weights") #label the weight matrix
# Calculate stats</pre>
```

```
ROPT <- t(WOPT)%*%rm  # calculate optimal portfolio's return

VOPT <- t(WOPT)%*%VCV%*%WOPT  # calculate optimal portfolio's variance

SDOPT <- VOPT^0.5  # calculate optimal portfolio's std dev

SRatio <-(ROPT-tnxy)/(SDOPT)  # calculate optimal portfolio's Sharpe ratio

# Create Optimal Stats Table

PTBL <- matrix(c(ROPT, VOPT, SDOPT, SRatio), nrow = 4)  # create a matrix of return, variance, std dev, optstat.names <- c("Return", "Variance", "Std Dev", "Sharpe")  # labels for PTBL matrix

dimnames(PTBL) <- list(optstat.names, "Opt. Portfolio")  # label the optimal portfolio matrix values
```

The optimal portfolio weights are as follow:

```
WOPT
```

```
## Weights
## MSFT 0.75172435
## GWPH -0.03902504
## DIS 0.01785490
## CAT -0.18682397
## AMZN 0.45626977
```

The statistics of the optimal portfolio is:

PTBL

```
## Opt. Portfolio
## Return 0.02326846
## Variance 0.00436794
## Std Dev 0.06609039
## Sharpe 0.32282226
```

2b) Allocate \$100.00 among the selected stocks using adjusted closing prices at 2018M12. 2019M1 will have a value of 100 as an index.

```
# Set start date and end date of data
start_date1 <- "2018-12-01"
end_date1 <- "2020-08-31"

# Get data
getSymbols("MSFT", src = "yahoo", from = start_date1, to = end_date1)

## [1] "MSFT"

getSymbols("GWPH", src = "yahoo", , from = start_date1, to = end_date1)

## [1] "GWPH"</pre>
```

```
getSymbols("DIS", src = "yahoo", , from = start_date1, to = end_date1)
## [1] "DIS"
getSymbols("CAT", src = "yahoo", , from = start_date1, to = end_date1)
## [1] "CAT"
getSymbols("AMZN", src = "yahoo", , from = start_date1, to = end_date1)
## [1] "AMZN"
getSymbols("GSPC", src = "yahoo", , from = start_date1, to = end_date1) # SEP 500
## [1] "^GSPC"
getSymbols("^TNX", src = "yahoo", from=start_date1, to=end_date1) # TNX (10-year T-bill)
## Warning: ^TNX contains missing values. Some functions will not work if objects
## contain missing values in the middle of the series. Consider using na.omit(),
## na.approx(), na.fill(), etc to remove or replace them.
## [1] "^TNX"
rMSFT1 <- diff(log(to.monthly(MSFT)$MSFT.Adjusted))
rGWPH1 <- diff(log(to.monthly(GWPH)$GWPH.Adjusted))
rDIS1 <- diff(log(to.monthly(DIS) DIS.Adjusted))
rCAT1 <- diff(log(to.monthly(CAT) CAT.Adjusted))
rAMZN1 <- diff(log(to.monthly(AMZN)$AMZN.Adjusted))
rGSPC1 <- diff(log(to.monthly(GSPC)$GSPC.Adjusted))
rTNX1 <- to.monthly(TNX)$TNX.Adjusted /1200 # Using monthly rate
## Warning in to.period(x, "months", indexAt = indexAt, name = name, ...): missing
## values removed from data
rTNX1 <- rTNX1[-1,] # remove missing data due to lagging
mean_rTNX1 <- mean(rTNX1, na.rm=TRUE)</pre>
# Adjusted Prices
adjMSFT1 <- MSFT$MSFT.Adjusted</pre>
adjGWPH1 <- GWPH$GWPH.Adjusted
adjDIS1 <- DIS$DIS.Adjusted
adjCAT1 <- CAT$CAT.Adjusted
adjAMZN1 <- AMZN$AMZN.Adjusted
investedAmount <- 100
sharesMSFT <- as.numeric(investedAmount * WOPT[1] / adjMSFT1[1])</pre>
```

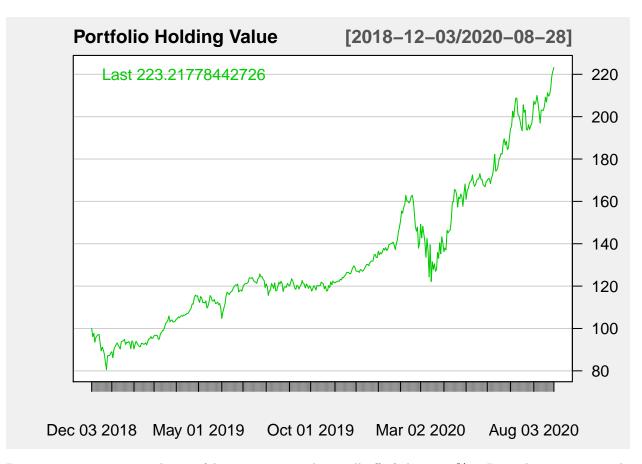
Based on the optimal weighting, to allocate \$100 to the portfolio, we would be purchase the following amount of each security:

Ticker	Weights	Stock to purchase
MSFT	0.7517244	0.6859734
GWPH	-0.039025	-0.0309109
DIS	0.0178549	0.0157364
CAT	-0.186824	-0.1424304
AMZN	0.4562698	0.0257436

2c) Using the adjusted closing prices from 2018M12 to 2020M8 calculate the holding values of the portfolio (assume fixed holdings with no re-balancing taking place over time).

We can then observe the fluctuations in the holding value of the portfolio from the period starting December 01 2018 to August 31, 2020 as follow.

```
chartSeries(holdings, name="Portfolio Holding Value", type="line", theme=chartTheme("white"))
```



By inspection we can see the portfolio experience a sharp sell off of almost 20% in December 2018, coincide with the broad U.S.market selloff due to a combination of the FED hiking the federal funds rate by 25 basis points to a targeted range of 2.25% to 2.5% (JeffCoxCNBCcom) and corporations followed suit by cutting profit forecasts and try temper expectations for earnings growth in 2019 after a big 2018 (Moyer).

The second visibly sharp sell off of the portfolio holding value also coincides with the broad market sell off in the mid March 2020 with investors raising cash in a risk-on environment when COVID-19 lockdowns started going into effects in the U.S.

3) Find the tangency point of the Capital Allocation Line (CAL) and the efficient frontier.

The tangency point of the Capital Allocation Line is the point where the weights of the portfolio is optimal, represented by the point (σ_p, r_p) which is (0.0660904, 0.0232685).

4) Calculate the CAL equation and graph CAL and the efficient frontier.

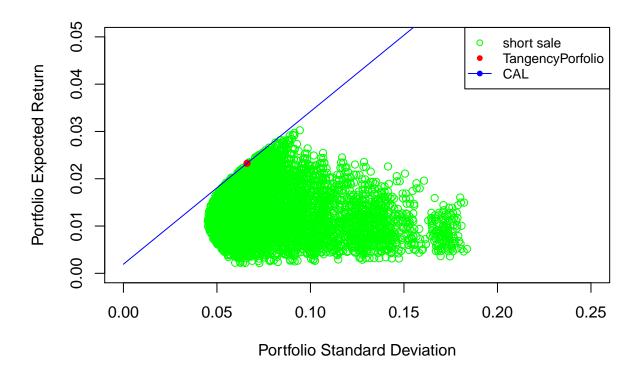
The efficient frontier is the portfolio possibility curve represented by the equation: $CAL = 0.001933 + 0.3228223 * \sigma_p$

```
# Efficient Frontier and CAL
j <- 0  # set value for iterative loop variable t
return_p <- rep(0, 50000)
sd_p <- rep(0, 50000)
# create a matrix of 0 to fill later with sd of different weights</pre>
```

```
vect_0 \leftarrow rep(0, 50000)
# create a matrix of O
fractions <- matrix(vect_0, 10000, 5)</pre>
# create a matrix of 0 to fill with weights
# iterate through weights for asset 1-5 from -20% to 100% by 10%
for (a in seq(-.2, 1, 0.1))
  {
  for (b in seq(-.2, 1, 0.1))
    for (c in seq(-.2, 1, 0.1))
      for (d in seq(-.2, 1, 0.1))
        for (e in seq(-.2, 1, 0.1))
          #test that the weights are equal to 1
          if (a+b+c+d+e==1)
            # increment j by 1 if a+b+c+d+e is equal to 1 (valid weights)
            # load a,b,c,d,e values into row j of the matrix
            fractions[j,] \leftarrow c(a,b,c,d,e)
            # calculate the std dev of the portfolio at a given weight of assets
            sd_p[j] <- (t(fractions[j,])%*%VCV%*%fractions[j,])^.5</pre>
            # calculate the return of the portfolio at a given weight of assets
            return_p[j] <- fractions[j,]%*%rm</pre>
          }
        }
      }
    }
 }
# assign filled vector spots in return_p to the R_p matrix to omit empty spots
Rport <- return_p[1:j]</pre>
# assign filled vector spots in sd_p to the sigma_p matrix to omit empty spots
StdDev_p <- sd_p[1:j]</pre>
# Create Capital Asset Line
# Create x-coordinates for CAL points
f \leftarrow seq(0,.24,.24)
# Calculate corresponding y-coordinates
CAL <- tnxy + SRatio * f
```

Warning in SRatio * f: Recycling array of length 1 in array-vector arithmetic is deprecated.
Use c() or as.vector() instead.

```
#Plot the portfolio possibilities curve:
plot(StdDev_p, Rport, col="green1", xlab="Portfolio Standard Deviation", ylab= "Portfolio Expected Returned Portfolio Expected Portfol
```



5) Estimate CAPM for your portfolio and graph the estimated β of the CAPM and the average return of your portfolio as a point relative to SML.

The expected risk premium of the portfolio based on the CAPM model is given as:

$$E(R_a - R_f) = \beta * (R_m - R_f)$$
or
$$R_a = R_f + \beta * (R_m - R_f)$$

$$R_a - R_f = \alpha_{Jensen} + \beta * (R_m - R_f)$$
or
$$Y = \alpha_{Jensen} + \beta * X + epsilon$$
with
$$Y = R_a - R_f$$

$$X = R_m - R_f$$

$$\beta = \text{Market risk or systematic risk}$$

$$\epsilon = \text{stochastic error term}$$
(10)

Here, the risk premium of the S&P 500 is the independent variable and the expected risk premium of the portfolio is the dependent variable.

Hypothesis for regression:

$$H_0: \alpha = 0$$
 $H_a: \alpha \neq 0$
and
 $H_0: \beta = 0$
 $H_a: \beta \neq 0$

```
# Calculate and normalized the CAPM holdings
ra <- diff(log(to.monthly(holdings)[,1]))

Y <- na.omit(ra - rTNX1)
names(Y)[1] <- "Portfolio Risk Premium" # Rename column
Y_bar <- mean(Y)
Y_bar</pre>
```

[1] 0.03515135

```
X <- na.omit(rGSPC1 - rTNX1)
mean_X <- mean(X)

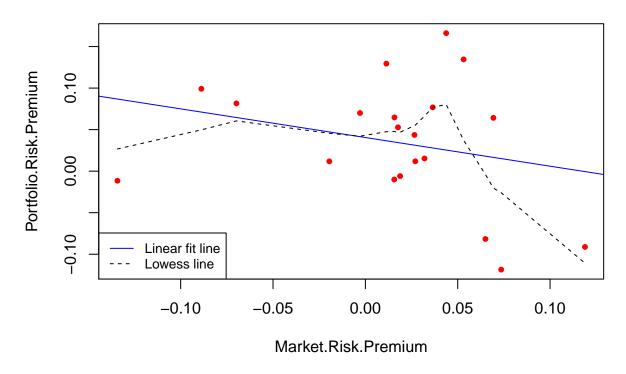
names(X)[1] <- "Market Risk Premium" # Rename column
data1 <- data.frame(X, Y)

plot(data1, col='red', main="Relationship Between Market & Portfolio Risk Premium", pch=20, cex=1)

# Add fit lines
abline(lm(Y~X), col="blue") # Regression line Y ~ X
lines(lowess(X,Y), col="black", lty=2) # Lowess line (X,Y)

legend("bottomleft",c("Linear fit line", "Lowess line"), cex=.8, col=c("blue", "black"), lty=1:2)</pre>
```

Relationship Between Market & Portfolio Risk Premium



Through inspection, we observe the cluster observation scattering in a big range from left to right. This implies a weak linear relationship between the Market Portfolio Risk Premium (the independent X variable on the x-axis) and the CAPM Portfolio Risk Premium (the dependent Y variable on the y-axis).

Next, we attempts to fit an equation of a line: $Y = \alpha_{Jensen} + \beta * X + \epsilon$

```
fit1 <- lm(Y~X, data=data1)
summary(fit1)</pre>
```

```
##
## Call:
  lm(formula = Y ~ X, data = data1)
##
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
## -0.13365 -0.04123
                      0.01465
                               0.03414
                                         0.14071
##
##
   Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
##
               0.04050
                           0.01728
                                      2.343
                                              0.0308 *
  (Intercept)
## X
               -0.34504
                           0.29305
                                     -1.177
                                              0.2544
##
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 0.07458 on 18 degrees of freedom
## Multiple R-squared: 0.07151,
                                     Adjusted R-squared:
## F-statistic: 1.386 on 1 and 18 DF, p-value: 0.2544
```

The estimated equation is Y = .04050 - .34504 * X, where the p_{value} for the intercept .0308 < .05.

Therefore, we reject the null hypothesis at 95% confidence level that the intercept α_{Jensen} statistically is no different from zero. Thus, we reject the null hypothesis $H_0: \alpha = 0$ and accept the null hypothesis $H_a: \alpha \neq 0$.

The coefficient $\beta = 1.07468$ represents the increase in portfolio risk premium relative to increase in the market portfolio risk premium. The p_{value} for β is .2544 > .05, implying that the coefficient β statistically is insignificant at 95% or more, and we accept the null hypothesis $H_0: \beta = 0$ and reject the alternative hypothesis $H_a: \beta \neq 0$.

Goodness of Fit:

Through inspection, we observe the $R^2 = .07151$ value to not be close to 1 at all. $R^2 = .07151$ implies that 7.15 of the variations in the portfolio risk premium is explained by the market risk premium.

Standard Error of Regression:

We can see that the Standard Error of Regression is S.E. = .07458.

From this, we can calculate the forecasting efficiency statistic to be:

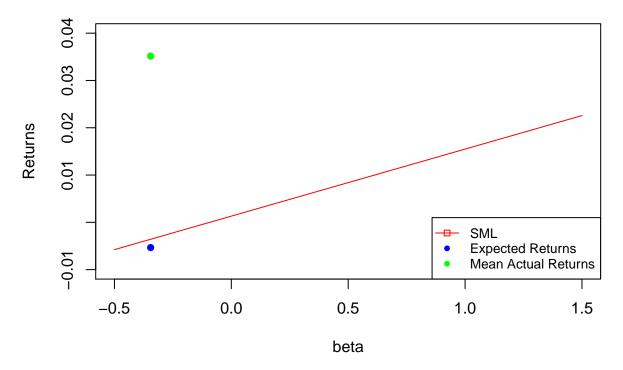
$$\frac{S.E.}{\overline{Y}} = \frac{.05618}{0.0351514}
= 212.17\% > 10\%$$
(12)

This statistic implies that this is not a good forecasting model.

Thus, upon exploring the goodness of fit and standard error of regression, we confirm our initial observation that the portfolio risk premium and the market portfolio risk premium has a weak linear relationship.

The Security Market Line:

CAPM portfolio beta relative to the Security Market Line



The Security Market Line pass through the point $(0, \overline{R_f})$ and $(1, \overline{X})$, which are (0, 0.0013135) and (1, 0.0154876).

Relative to its market risk of beta = -.34504, the expected return is -0.0053439 and the average return is 0.0351514. We can observe that at this estimated β , the expected return is below the security market line and the actual average return is above the security market line.

2) Understand the impact of COVID-19 on the alpha and market risk of the CAPM model.

Question covered: 6).

Methodology Test whether the closing of the economy due to COVID-19 had any effect on Jensen alpha and the market risk of the CAPM model. (6)

We run regression for the model to see if the pandemic has any effect on Jensen alpha:

 $Y = \alpha_{Jensen} + \beta * X + \beta_1 * D + \epsilon$

where:

 $Y = \text{Portfolio Risk Premium } R_a - R_f$

 $\beta = \text{Estimated } \beta \text{ of the CAPM}$

 $X = Market portfolio risk premium <math>R_m - R_f$

 β_1 = Coefficient representing the relationship of the portfolio risk premium with the pandemic factor

D = Dummy variable representing the pandemic factor

 $\epsilon =$ Standard Error of Regression

(13)

Hypothesis for regression:

$$H_0: \alpha = 0$$

$$H_a: \alpha \neq 0$$
and
$$H_0: \beta_1 = 0$$

$$H_a: \beta_1 \neq 0$$
(14)

We examine the potential relationship between the pandemic variable and the portfolio risk premium by plotting a scatter plot as follow:

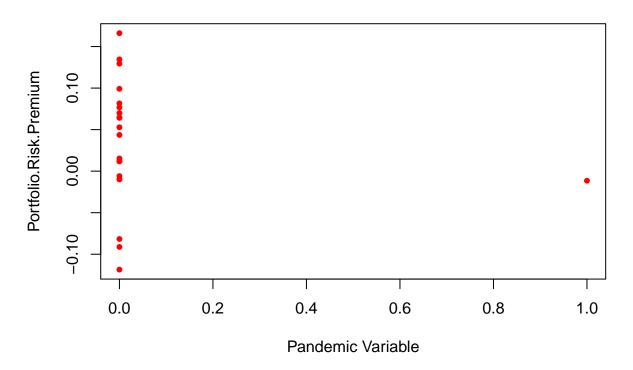
```
# Generating the dummy variable
D <- rep(0, 20)
D[15] <-1
D</pre>
```

```
## [1] 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0
```

```
data2 <- data.frame(D, Y)
names(data2)[1] <- "Pandemic Variable"

plot(data2, col='red', main="Relationship Between Pandemic & Portfolio Risk Premium", pch=20, cex=1)</pre>
```

Relationship Between Pandemic & Portfolio Risk Premium



```
# Add fit lines #abline(lm(Y\sim D), col="blue") # Regression line Y ~ X #lines(lowess(D,Y), col="black", lty=2) # Lowess line (X,Y) #legend("bottomleft",c("Linear fit line", "Lowess line"), cex=.8, col=c("blue", "black"), lty=1:2)
```

Through inspection, we can see there is not much of a linear relationship between these variables. Let's assume linearity, we run regression on $Y = \alpha_{Jensen} + \beta * X + \beta_1 * D$ as hypothesized above.

```
fit2 <- lm(Y~X+D)
summary(fit2)</pre>
```

```
##
## Call:
## lm(formula = Y \sim X + D)
##
## Residuals:
##
                    1Q
                          Median
## -0.119935 -0.048422 -0.008044 0.028370 0.143203
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.05447
                           0.01806
                                      3.017 0.00778 **
## X
               -0.72150
                           0.34667 -2.081 0.05284 .
```

The estimated equation is Y = .05447 - .72150*X - .16285*D, where the p_{value} for the intercept .00778 < .05. Therefore, we reject the null hypothesis at 95% confidence level that the intercept α_{Jensen} statistically is no different from zero. Thus, we reject the null hypothesis $H_0: \alpha = 0$ and accept the null hypothesis $H_a: \alpha \neq 0$. In addition, the coefficient $\beta_1 = -.16285$ represents the increase in portfolio risk premium relative to increase in the pandemic variable. The p_{value} for β_1 is .08979 > .05, implying that the coefficient β_1 statistically is insignificant at 95% or more, and we accept the null hypothesis $H_0: \beta_1 = 0$ and reject the alternative hypothesis $H_a: \beta_1 \neq 0$.

Goodness of Fit:

Through inspection, we observe the $R^2 = .22$ value to not be close to 1 at all. $R^2 = .22$ implies that 22 of the variations in the portfolio risk premium is explained by the pandemic variable.

Standard Error of Regression:

We can see that the Standard Error of Regression is S.E. = .07034.

From this, we can calculate the forecasting efficiency statistic to be:

$$\frac{S.E.}{\overline{Y}} = \frac{.07034}{0.0351514}
= 200.11\% > 10\%$$
(15)

This statistic implies that this is not a good forecasting model.

Now, we want to explore the affect of the pandemic lockdowns on market risk. Thus, we want to explore the following regression model:

$$Y = \alpha_{Jensen} + \beta * X + \beta_1 * D + \beta_2 * D * X + \epsilon_1$$

where:

 $Y = \text{Portfolio Risk Premium } R_a - R_f$

 $\beta = \text{Estimated } \beta \text{ of the CAPM}$

 $X = Market portfolio risk premium <math>R_m - R_f$

 β_1 = Coefficient representing the relationship of the portfolio risk premium with the pandemic factor

D = Dummy variable representing the pandemic factor

 β_2 = Coefficient representing the relationship of the market risk premium with the pandemic factor

D*X =Slope dummy variable representing the pandemic factor correlation with market risk premium

 $\epsilon_1 = \text{Standard Error of Regression}$

(16)

Hypothesis for regression:

$$H_0: \alpha = 0$$

$$H_a: \alpha \neq 0$$
and
$$H_0: \beta_2 = 0$$

$$H_a: \beta_2 \neq 0$$
(17)

```
# Generate the new variable dx = D*X
DX <- D*X
fit3 <- lm(Y~X+D+DX)
summary(fit3)</pre>
```

```
##
## Call:
## lm(formula = Y \sim X + D + DX)
## Residuals:
##
                    1Q
                          Median
  -0.119935 -0.048422 -0.008044
                                  0.028370
                                            0.143203
##
## Coefficients: (1 not defined because of singularities)
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.05447
                           0.01806
                                     3.017
                                            0.00778 **
## X
               -0.72150
                           0.34667
                                    -2.081
                                            0.05284 .
## D
               -0.16285
                           0.09052
                                    -1.799
                                            0.08979 .
## DX
                     NA
                                NA
                                        NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.07034 on 17 degrees of freedom
## Multiple R-squared:
                         0.22, Adjusted R-squared: 0.1282
## F-statistic: 2.398 on 2 and 17 DF, p-value: 0.121
```

The estimated equation is Y = .05447 - .72150 * X - .16285 * D * X

We see $\beta_2 = NA$ implying that the slope dummy is an unnecessary predictor. The coefficient β_2 is not estimated.

Let's run the regression with the slope dummy separately, so the equation of the regression becomes:

$$Y = \alpha_{Jensen} + \beta * X + \beta_2 * D * X + \epsilon_2$$
 where:
$$Y = \text{Portfolio Risk Premium } R_a - R_f$$

$$\beta = \text{Estimated } \beta \text{ of the CAPM}$$

$$X = \text{Market portfolio risk premium } R_m - R_f$$

$$D = \text{Dummy variable representing the pandemic factor}$$

$$\beta_2 = \text{Coefficient representing the relationship of the market risk premium with the pandemic factor}$$

$$D * X = \text{Slope dummy variable representing the pandemic factor correlation with market risk premium}$$

$$\epsilon_1 = \text{Standard Error of Regression}$$
 (18)

Again, stating the hypothesis for regression:

$$H_0: \alpha = 0$$

$$H_a: \alpha \neq 0$$
and
$$H_0: \beta_2 = 0$$

$$H_a: \beta_2 \neq 0$$
(19)

```
# Generate the new variable dx = D*X
fit4 <- lm(Y~X+DX)
summary(fit4)</pre>
```

```
##
## Call:
## lm(formula = Y ~ X + DX)
##
## Residuals:
##
        Min
                   1Q
                         Median
                                        3Q
                                                 Max
## -0.119935 -0.048422 -0.008044 0.028370 0.143203
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.05447
                           0.01806
                                     3.017 0.00778 **
## X
               -0.72150
                           0.34667
                                   -2.081
                                           0.05284 .
                1.21306
## DX
                           0.67427
                                     1.799
                                           0.08979 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.07034 on 17 degrees of freedom
## Multiple R-squared:
                        0.22, Adjusted R-squared: 0.1282
## F-statistic: 2.398 on 2 and 17 DF, p-value: 0.121
```

The estimated equation is Y = .05447 - .72150 * X - 1.21306 * D, where the p_{value} for the intercept .00778 < .05.

Therefore, we reject the null hypothesis at 95% confidence level that the intercept α_{Jensen} statistically is no different from zero. Thus, we reject the null hypothesis $H_0: \alpha=0$ and accept the null hypothesis $H_a: \alpha\neq 0$. In addition, the coefficient $\beta_2=1.21306$ represents the increase in market risk premium relative to increase in the pandemic variable. The p_{value} for β_2 is .08979 > .05, implying that the coefficient β_1 statistically is insignificant at 95% or more, and we accept the null hypothesis $H_0: \beta_1=0$ and reject the alternative hypothesis $H_a: \beta_1\neq 0$.

Goodness of Fit:

Through inspection, we observe the $R^2 = .22$ value to not be close to 1 at all. $R^2 = .22$ implies that 22 of the variations in the portfolio risk premium is explained by the pandemic variable.

Standard Error of Regression:

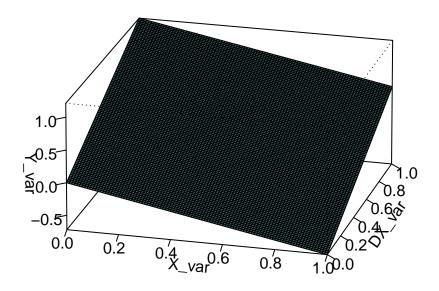
We can see that the Standard Error of Regression is S.E. = .07034. From this, we can calculate the forecasting efficiency statistic to be:

$$\frac{S.E.}{\overline{Y}} = \frac{.07034}{0.0351514}$$

$$= 200.11\% > 10\%$$
(20)

This statistic implies that this is not a good forecasting model.

To visualize:



3) Compare the CAPM portfolio to a diversified State Street's SPDR S&P 500 Trust ETF portfolio (7,8,9)

Questions covered: 7,8,9.

Methodology

- 7) Calculate CV, Sharpe, Treynor, and Sortino ratios for your portfolio and compare them to a similarly diversified portfolio of Vanguard, Fidelity, or any other similar portfolio.
- 8) Calculate 2% and 3% VaRs as a percentage of the mean return of your portfolio when the risk horizon is one year, six months, and one month. Calculate the same VaRs for the selected portfolio in item 6. Compare the VaRs of your portfolio to the ones of the market portfolios.
- 9) Graph the scatter diagram of your portfolio and comment on trends, outliers, structural breaks and any other special features. Graph the scatter diagram of your portfolio and S&P 500 on the same coordinate system and compare the trends.
- 7) Calculate CV, Sharpe, Treynor, and Sortino ratios for your portfolio and compare them to a similarly diversified portfolio of Vanguard, Fidelity, or any other similar portfolio.

```
# Calculate statistics
MSFT1_return_mean <- mean(rMSFT1, na.rm = TRUE)
GWPH1_return_mean <- mean(rGWPH1, na.rm = TRUE)
DIS1_return_mean <- mean(rDIS1, na.rm = TRUE)
CAT1_return_mean <- mean(rCAT1, na.rm = TRUE)</pre>
```

```
AMZN1_return_mean <- mean(rAMZN1, na.rm = TRUE)
GSPC1_return_mean <- mean(rGSPC1, na.rm = TRUE)</pre>
TNX1_return_mean <- mean(rTNX1, na.rm = TRUE)</pre>
MSFT1_return_var <- var(rMSFT1, na.rm = TRUE)</pre>
GWPH1_return_var <- var(rGWPH1, na.rm = TRUE)</pre>
DIS1_return_var <- var(rDIS1, na.rm = TRUE)</pre>
CAT1 return var <- var(rCAT1, na.rm = TRUE)
AMZN1_return_var <- var(rAMZN1, na.rm = TRUE)
GSPC1_return_var <- var(rGSPC1, na.rm = TRUE)</pre>
# Excess Returns
reMSFT1 <- rMSFT1 - rTNX1
reGWPH1 <- rGWPH1 - rTNX1
reDIS1 <- rDIS1 - rTNX1
reCAT1 <- rCAT1 - rTNX1
reAMZN1 <- rAMZN1 - rTNX1
# Information Tables:
#pricTabl1 <- data.frame(MSFT, GWPH, DIS, CAT, AMZN)</pre>
# Creates data frame of asset prices
retTabl1 <- data.frame(rMSFT1, rGWPH1, rDIS1, rCAT1, rAMZN1)</pre>
# Creates data frame of returns
EretTabl1 <- data.frame(reMSFT1, reGWPH1, reDIS1, reCAT1, reAMZN1)</pre>
# Excess return data frame
retTabl1 <- retTabl1[-1,] # remove missing data due to lagging</pre>
EretTabl1 <- EretTabl1[-1,] # remove missing data due to lagging</pre>
priceMat1 <- matrix(c(MSFT, GWPH, DIS, CAT, AMZN), nrow= length(MSFT), ncol=5, byrow=TRUE) # creates a
# Variance/Covariance Matrix
asset.names <- c("MSFT", "GWPH", "DIS", "CAT", "AMZN")
# Create a list of row and col names for the var/cov matrix
VCV1 <- matrix(c(cov(retTabl1)), nrow=5, ncol = 5, byrow=TRUE) # create a var/cov matrix by finding cov
dimnames(VCV1) <- list(asset.names, asset.names) # assigns asset.names to the VCV matrix
#Calculate Returns
rm1 <- matrix(colMeans(retTabl1, na.rm=TRUE)) # creates an average return matrix, omitting missing val
erm1 <- matrix(colMeans(EretTabl1, na.rm=TRUE)) # creates an average excess return matrix, omitting mi
tnxy1 = mean((rTNX1)[-1,]) # calculates the average bond yield excluding Jan (risk free rate)
#Create Return Table
retmat1 <- matrix(c(rm1, erm1), ncol=2)</pre>
dimnames(retmat1) = list(asset.names, c("Return ", "Excess Return"))
# Calculate stats
ROPT1 <- t(WOPT)%*%rm1 # calculate optimal portfolio's return
VOPT1 <- t(WOPT) ** VCV1 ** WOPT # calculate optimal portfolio's variance
SDOPT1 <- VOPT1^0.5 # calculate optimal portfolio's std dev
SRatio1 <-(ROPT1-tnxy1)/(SDOPT1) # calculate optimal portfolio's Sharpe ratio
```

```
mean_Holdings1 <- as.numeric(colMeans(holdings[1])) # Mearn</pre>
sd_Holdings1 <- as.numeric(sqrt(var(holdings)))</pre>
CV1 <- sd Holdings1 / mean Holdings1
                                       # calculate portfolio's coefficient of variation
TrRatio1 <- (ROPT1 - tnxy1)/ -0.34504 # calculate portfolio's Treynor Ratio
# Calculating downside deviation using lower partial moment of order 2
mar <- tnxy1 # Assuming the 10 year T-bill returns as minimum acceptable returns MAR
rHoldings <- diff(log(holdings[,1])) # calculate portfolio holding returns data
dev_rHoldings_mar <- na.omit(rHoldings - mar) # Deviation from MAR, this is a data frame, remove NA va
devNegative_rHoldings_mar <- subset(dev_rHoldings_mar, dev_rHoldings_mar < 0) # Get the subset of nega
downsideDev_Holdings <- var(devNegative_rHoldings_mar) # Calculate the Lower Partial Moment
sd_downsideDev_Holdings <- sqrt(downsideDev_Holdings) # Downside deviation</pre>
SoRatio1 <- (ROPT1 - tnxy1) / sd_downsideDev_Holdings # calculate portfolio Sortino Ratio
# Create Optimal Stats Table
PTBL1 <- matrix(c(CV1, SRatio1, TrRatio1, SoRatio1), nrow = 4) # create a matrix of return, variance,
optstat.names <- c("CV", "Sharpe", "Treynor", "Sortino") # labels for PTBL matrix
dimnames(PTBL1) <- list(optstat.names, "Holdings") # label the optimal portfolio matrix values
# Get data
getSymbols("SPY", src = "yahoo", from = start_date1, to = end_date1)
## [1] "SPY"
rSPY1 <- na.omit(diff(log(to.monthly(SPY) $SPY.Adjusted)))
mean_rSPY1 <- mean(rSPY1)</pre>
var_rSPY1 <- var(rSPY1)</pre>
sd_rSPY1 <- sqrt(var_rSPY1)</pre>
adjSPY1 <- SPY$SPY.Adjusted
mean_adjSPY1 <- mean(adjSPY1)</pre>
var_adjSPY1 <- var(adjSPY1)</pre>
sd_adjSPY1 <- sqrt(var_adjSPY1)</pre>
SRatioSPY1 <- (mean_rSPY1-tnxy1) / sd_rSPY1 # calculate optimal portfolio's Sharpe ratio
CVSPY1 <- sd_adjSPY1 / mean_adjSPY1 # calculate portfolio's coefficient of variation
TrRatioSPY1 <- (mean_rSPY1 - tnxy1)/ 1 # calculate portfolio's Treynor Ratio
# Calculating downside deviation using lower partial moment of order 2
marSPY1 <- tnxy1 # Assuming the 10 year T-bill returns as minimum acceptable returns MAR
dev_rSPY1_mar <- na.omit(rSPY1 - mar) # Deviation from MAR, this is a data frame, remove NA values
devNegative_rSPY1_mar <- subset(dev_rSPY1_mar, dev_rSPY1_mar < 0) # Get the subset of negative values
downsideDev_SPY1 <- var(devNegative_rSPY1_mar) # Calculate the Lower Partial Moment
sd_downsideDev_SPY1 <- sqrt(downsideDev_SPY1) # Downside deviation</pre>
SoRatioSPY1 <- (mean_rSPY1 - tnxy1) / sd_downsideDev_SPY1 # calculate portfolio Sortino Ratio
# Create Optimal Stats Table
SPYTBL1 <- matrix(c(CVSPY1, SRatioSPY1, TrRatioSPY1, SoRatioSPY1), nrow = 4) # create a matrix of retu
```

```
optstat.names <- c("CV", "Sharpe", "Treynor", "Sortino") # labels for PTBL matrix

dimnames(SPYTBL1) <- list(optstat.names, "SPY") # label the optimal portfolio matrix values

SPY_PTBL1 <- data.frame(PTBL1, SPYTBL1)
```

Compare the key financial ratio of the portfolio to that of the State Street's SPDR S&P 500 Trust ETF portfolio (SPY), we see:

```
SPY_PTBL1
```

```
## Holdings SPY
## CV 0.2475044 0.08583704
## Sharpe 0.7609424 0.29444966
## Treynor -0.1369133 0.01710602
## Sortino 2.8067889 0.32133508
```

Remarks: Coefficient of Variations: The SPY has extremely low dispersion of value (based on Adjusted Closing Price) compared to that of the holding portfolio. This implies the holding portfolio carry significantly more volatility in comparison to the SPY.

Sharpe Ratio: The holding portfolio has higher Sharpe ratio compare to the SPY. Assuming returns are normally distributed, this implies the holding portfolio generates significantly higher returns than the SPY. Treynor Ratio: The SPY has a higher and positive Treynor Ratio compared to a lower and negative Treynor Ratio. This implies that the SPY is much better at generating excess returns per unit of risk that it takes on. Compared to the holding portfolio, the SPY is a more suitable investment.

Sortino Ratio: The holding portfolio has significantly higher Sortino Ratio compared to the SPY. This implies that it is earning returns more efficiently than the SPY given downside deviations: earning more turns per unit of the bad risk it is taking on.

8) Calculate 2% and 3% VaRs as a percentage of the mean return of your portfolio when the risk horizon is one year, six months, and one month. Compare the VaRs of your portfolio to the ones of the market portfolios.

```
# 2% VaR Holding Portfolio
VaR_threshold <- 2

# Set scaling factor based on the period of evaluation
# In this example: {1: '1 year', 1/2: '6 months', 1/12: '1 month', 1/250: '1 day'}

# 2% 1 year VAR
scalingFactor <- 1
z_stat <- qnorm(VaR_threshold/100, 0, 1, lower.tail = TRUE)
VaR_1year_p_2percent <- ROPT1*scalingFactor + SDOPT1*sqrt(scalingFactor) * z_stat
VaR_1year_SPY_2percent <- mean_rSPY1*scalingFactor + sd_rSPY1*sqrt(scalingFactor) * z_stat

# 2% 6 month VAR
scalingFactor <- 1/2
VaR_6month_p_2percent <- ROPT1*scalingFactor + SDOPT1*sqrt(scalingFactor) * z_stat
VaR_6month_SPY_2percent <- mean_rSPY1*scalingFactor + sd_rSPY1*sqrt(scalingFactor) * z_stat
VaR_6month_SPY_2percent <- mean_rSPY1*scalingFactor + sd_rSPY1*sqrt(scalingFactor) * z_stat</pre>
```

```
scalingFactor <- 1/12
VaR_1month_p_2percent <- ROPT1*scalingFactor + SDOPT1*sqrt(scalingFactor) * z_stat</pre>
VaR_1month_SPY_2percent <- mean_rSPY1*scalingFactor + sd_rSPY1*sqrt(scalingFactor) * z_stat
# 3% VaR Holding Portfolio
VaR_threshold <- 3
# Set scaling factor based on the period of evaluation
# In this example: {1: '1 year', 1/2: '6 months', 1/12: '1 month', 1/250: '1 day'}
# 3% 1 year VAR
scalingFactor <- 1
z_stat <- qnorm(VaR_threshold/100, 0, 1, lower.tail = TRUE)</pre>
VaR_1year_p_3percent <- ROPT1*scalingFactor + SDOPT1*sqrt(scalingFactor) * z_stat</pre>
VaR_1year_SPY_3percent <- mean_rSPY1*scalingFactor + sd_rSPY1*sqrt(scalingFactor) * z_stat</pre>
# 3% 6 month VAR
scalingFactor <- 1/2</pre>
VaR_6month_p_3percent <- ROPT1*scalingFactor + SDOPT1*sqrt(scalingFactor) * z_stat</pre>
VaR_6month_SPY_3percent <- mean_rSPY1*scalingFactor + sd_rSPY1*sqrt(scalingFactor) * z_stat</pre>
# 3% 1 month VAR
scalingFactor <- 1/12</pre>
VaR_1month_p_3percent <- ROPT1*scalingFactor + SDOPT1*sqrt(scalingFactor) * z_stat</pre>
VaR_1month_SPY_3percent <- mean_rSPY1*scalingFactor + sd_rSPY1*sqrt(scalingFactor) * z_stat</pre>
# Generate comparison table
VaR_stat_p <- matrix(c(VaR_1year_p_2percent, VaR_6month_p_2percent, VaR_1month_p_2percent,</pre>
                       VaR_1year_p_3percent, VaR_6month_p_3percent, VaR_1month_p_3percent), nrow = 6)
VaR_stat_SPY <- matrix(c(VaR_1year_SPY_2percent, VaR_6month_SPY_2percent, VaR_1month_SPY_2percent,
                       VaR_1year_SPY_3percent, VaR_6month_SPY_3percent, VaR_1month_SPY_3percent), nrow
optstat.names <- c("2% 1yr", "2% 6mth", "2% 1month",
                   "3% 1yr", "3% 6mth", "3% 1month")
dimnames(VaR_stat_p) <- list(optstat.names, "Holdings")</pre>
dimnames(VaR_stat_SPY) <- list(optstat.names, "SPY")</pre>
VaR_stat <- data.frame(VaR_stat_p, VaR_stat_SPY)</pre>
```

The VaR statistics is as follow:

VaR_stat

```
## 3% 1month -0.02966421 -0.03001085
```

xlab = "Year", ylab = "SPY Price", col = "Red")

Through inspection, we observe that on shorter time horizon (1 month), both the holding and SPY portfolio has comparable value at risk. When the time horizon increase, the value at risk for the SPY portfolio starts to increase more than that of the holding portfolio.

9) Graph the scatter diagram of your portfolio and comment on trends, outliers, structural breaks and any other special features. Graph the scatter diagram of your portfolio and S&P 500 on the same coordinate system and compare the trends.

plot(as.zoo(adjSPY1[, "SPY.Adjusted"]), main = "SPY and Portfolio Holdings Value Overlay",

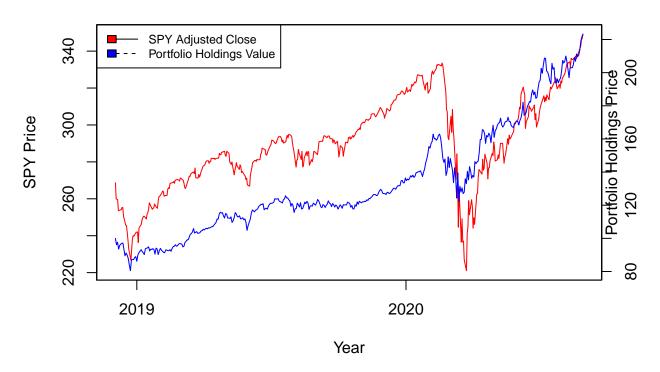
```
par(new=TRUE)
plot(holdings[, 1], type="line", xaxt="n", yaxt = "n", xlab = "", ylab = "", col = "Blue")

## Warning in plot.xy(xy, type, ...): plot type 'line' will be truncated to first
## character

axis(4)
mtext("Portfolio Holdings Price", side = 4)

# Add legend
legend("topleft", c("SPY Adjusted Close", "Portfolio Holdings Value"), lty = 1:3, cex = 0.75, fill = c(
```

SPY and Portfolio Holdings Value Overlay



Remarks

1. Seasonal Trend:

Both display similar seasonal trend with up and down spikes in price days after days.

2. Cyclical Trend:

Both is affected by business cycle with similar peaks and troughs. SPY has more prominent troughs compared to that of the portfolio holdings. Especially during the period of March 2020 with the COVID-19 lockdowns started rolling across the countries.

3. Auto-correlation:

Both behave similar in this regard where both rises for some times when they rise and vice versa.

4. Randomness:

Price of both is unpredictable via inspection.

5. Time:

Both follows similar time trend.

6. Structural Break:

Both does not experience any structural break during this time frame. During the COVID-19 March sell-off, price recovered quickly in a V-shaped fashion.

7. Outliers:

SPY looks to have several outliers corresponded to the March 2020 sell-off when the indicies retreated 30% in a short period of a few weeks before quickly recovered.

4) Forecast the returns of the portfolio CATsed on the CAPM model (10,11,12)

10) Using the CAPM equation of your portfolio do two periods ex-post forecasting of the returns to your portfolio and compare your forecast to the actual returns. Find the accuracy statistics of your forecast and report them.

- 11) Do two-periods ex-ante forecasting of returns to your portfolio assuming that the monthly risk premiums to S&P 500 will be 1.10% in 2020M9 and 1.25 in 2020M10.
- 12) Do forecasting of the returns to your portfolio for the period 2014M1-2020M8. Find the accuracy statistics of your forecast. Do a naïve forecasting of the returns to your portfolio for the period 2014M1-2020M8. Find the accuracy statistics of your forecast. Compare the forecasting accuracy criterion for the two forecasting methods. Which one results in a better forecasting outcome?

Citations

"Amazon.com, Inc. (AMZN) Stock Price, News, Quote & History." Yahoo! Finance, Yahoo!, 14 Nov. 2020, ca.finance.yahoo.com/quote/amzn/?p=amzn.

"Caterpillar, Inc. (CAT) Stock Price, News, Quote & History." Yahoo! Finance, Yahoo!, 13 Nov. 2020, ca.finance.yahoo.com/quote/CAT/?p=CAT.

"GW Pharmaceuticals Plc (GWPH) Stock Price, News, Quote & History." Yahoo! Finance, Yahoo!, 13 Nov. 2020, ca.finance.yahoo.com/quote/GWPH/?p=GWPH.

Moyer, Liz. "We're Finding out Now Why the Stock Market Tanked in December." CNBC, CNBC, 9 Jan. 2019, www.cnbc.com/2019/01/09/markets-december-tumble-may-have-hinted-at-profit-revisions-to-come.html.

"Microsoft Corporation (MSFT) Stock Price, News, Quote & History." Yahoo! Finance, Yahoo!, 14 Nov. 2020, ca.finance.yahoo.com/quote/msft/?p=msft.

"Walt Disney Company (The) (DIS) Stock Price, News, Quote & History." Yahoo! Finance, Yahoo!, 14 Nov. 2020, ca.finance.yahoo.com/quote/dis/?p=dis.