### Spring 2021 Project

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```
library(quantmod)
## Loading required package: xts
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
## Loading required package: TTR
## Registered S3 method overwritten by 'quantmod':
##
     method
     as.zoo.data.frame zoo
## Version 0.4-0 included new data defaults. See ?getSymbols.
library(forecast)
library(aTSA)
##
## Attaching package: 'aTSA'
## The following object is masked from 'package:forecast':
##
##
       forecast
## The following object is masked from 'package:graphics':
##
##
       identify
University of Southern California
Marshall School of Business
FBE 543 Forecasting and Risk Analysis
Spring 2021
Directed by Professor Mohammad Safarzadeh
```

### **Table of Contents**

### Abstract

### Introduction

We selected the following 5 securities to base our analysis of impact of COVID-19 on a CAPM model of 5 stocks upon.

Ticker	Security	Sector	Industry	Founded	Full Time Employees
MSFT	Microsoft Corporation	Technology	Software- Infrastructure	1975	163,000
GWPH	GW Pharma- ceuticals PLC	Healthcare	Drug Manufacturers- General	1998	901
DIS	The Walt Disney Company	Communication Services	Entertainment	1923	223,000
CAT	Caterpillar INC	Industrials	Farm & Heavy Construction Machinery	1925	102,300
AMZN	Amazon.com INC	Consumer Cyclical	Internet Retail	1994	1,125,300

All information and data related to the securities are obtained from Yahoo Finance: MSFT, GWPH, DIS, CAT, and AMZN.

The objective of the study of the study is using the Modern Portfolio Theory to model a portfolio of five securities from different industries using adjusted closing price data from January 01, 2016 to December 31, 2018.

#### Methodology

- 1) Select at least five stocks from different industries.
- 2) Construct a portfolio of the selected stocks and graph the efficient frontier.
- a. Find the optimum weights using MPT.
- b. Using the optimum weights and monthly adjusted closing prices at the end of 2018 allocate \$100.00 among the selected stocks. On 1/1/2019, the portfolio will have a value of 100 as an index.
- c. Using the daily adjusted closing prices from 1/2/2019 to present calculate the holding values of the portfolio. Assume fixed holdings with no re-balancing taking place over time. Calculate the CAL equation and graph the CAL and the efficient frontier.
- 3) Do Naive, MA(5), MA(15), ES, Holt, and Holt-Winters forecasting of your portfolio returns and do a three-period-ahead forecasting of the portfolio returns for each forecast. Estimate the accuracy statistics.

- 4) Start with the regression analysis and forecasting of your portfolio returns. Use the CAPM and three-factor CAPM (Fama-French) models to estimate the coefficients of the models and use them for forecasting. Do a 10-days ex-post forecasting of the portfolio risk premiums and compare the forecasted value to actual ones. Do a three-period-ahead (ex-ante) forecasting of the portfolio risk premiums and write confidence intervals.
- 5) Do an ARIMA model of your portfolio returns and use it for three-period ahead forecasting of the returns to portfolio. Write confidence interval. Estimate the accuracy statistics.
- 6) Test your ARIMA model for the stability of the ARIMA coefficients.
- 7) Test your ARIMA model for the existence of ARCH and GARCH and do proper corrections, if needed.
- 8) Find different time-series measures of volatility for your portfolio returns (see the volatility file posted on Blackboard) and do a three-period ahead forecasting of the portfolio volatility. Compare the different measures of volatility with GARCH.
- 9) Use the accuracy statistics of the different forecasting techniques to decide which technique fits the data best.
- 10) Test whether your portfolio index conforms to the efficient market hypothesis.
- 11) Find 1% and 3% daily and monthly VaR of your portfolio.
- 12) Find 1% and 3% daily and monthly equity EVaR of your portfolio.
- 13) Graph the security Market Line (SML) of your portfolio and test whether you would add a stock of your own choice to the portfolio or not.
- 14) Do an intervention function analysis of the March 15th closing of US economy due to COVID19. Did the event have any effect on return to your portfolio.
- 15) Do a 2-variable VAR between your portfolio index and S&P500 index. Graph the Impulse response function of the VAR and comment on the relationship.

### Data Analysis

1) Select at least five stocks from different industries.

```
# Set start date and end date of data
start_date <- "2016-01-01"
end_date <- "2018-12-31"

# Get data
getSymbols("MSFT", src = "yahoo", from = start_date, to = end_date)

## 'getSymbols' currently uses auto.assign=TRUE by default, but will
## use auto.assign=FALSE in 0.5-0. You will still be able to use
## 'loadSymbols' to automatically load data. getOption("getSymbols.env")
## and getOption("getSymbols.auto.assign") will still be checked for
## alternate defaults.
##
## This message is shown once per session and may be disabled by setting
## options("getSymbols.warning4.0"=FALSE). See ?getSymbols for details.</pre>
```

```
## [1] "MSFT"
getSymbols("GWPH", src = "yahoo", , from = start_date, to = end_date)
## [1] "GWPH"
getSymbols("DIS", src = "yahoo", , from = start_date, to = end_date)
## [1] "DIS"
getSymbols("CAT", src = "yahoo", , from = start_date, to = end_date)
## [1] "CAT"
getSymbols("AMZN", src = "yahoo", , from = start_date, to = end_date)
## [1] "AMZN"
getSymbols("^GSPC", src = "yahoo", , from = start_date, to = end_date)
## [1] "^GSPC"
getSymbols("^TNX", src = "yahoo", from = start_date, to = end_date)
## Warning: ^TNX contains missing values. Some functions will not work if objects
## contain missing values in the middle of the series. Consider using na.omit(),
## na.approx(), na.fill(), etc to remove or replace them.
## [1] "^TNX"
# Adjusted Prices
adjMSFT <- MSFT$MSFT.Adjusted
adjGWPH <- GWPH$GWPH.Adjusted
adjDIS <- DIS$DIS.Adjusted
adjCAT <- CAT$CAT.Adjusted
adjAMZN <- AMZN$AMZN.Adjusted
# Get adjusted returns data
rMSFT <- diff(log(to.monthly(MSFT)$MSFT.Adjusted))</pre>
rGWPH <- diff(log(to.monthly(GWPH)$GWPH.Adjusted))
rDIS <- diff(log(to.monthly(DIS)$DIS.Adjusted))</pre>
rCAT <- diff(log(to.monthly(CAT)$CAT.Adjusted))</pre>
rAMZN <- diff(log(to.monthly(AMZN)$AMZN.Adjusted))
rGSPC <- diff(log(to.monthly(GSPC)$GSPC.Adjusted))
rTNX <- (to.monthly(TNX)$TNX.Adjusted) / 1200 # Using monthly rate
## Warning in to.period(x, "months", indexAt = indexAt, name = name, ...): missing
## values removed from data
```

```
# Calculate statistics
MSFT_return_mean <- mean(rMSFT, na.rm = TRUE)</pre>
GWPH_return_mean <- mean(rGWPH, na.rm = TRUE)</pre>
DIS_return_mean <- mean(rDIS, na.rm = TRUE)</pre>
CAT_return_mean <- mean(rCAT, na.rm = TRUE)</pre>
AMZN_return_mean <- mean(rAMZN, na.rm = TRUE)
GSPC_return_mean <- mean(rGSPC, na.rm = TRUE)</pre>
TNX_return_mean <- mean(rTNX, na.rm = TRUE)</pre>
MSFT_return_var <- var(rMSFT, na.rm = TRUE)</pre>
GWPH_return_var <- var(rGWPH, na.rm = TRUE)</pre>
DIS_return_var <- var(rDIS, na.rm = TRUE)</pre>
CAT_return_var <- var(rCAT, na.rm = TRUE)</pre>
AMZN_return_var <- var(rAMZN, na.rm = TRUE)
GSPC_return_var <- var(rGSPC, na.rm = TRUE)</pre>
# Excess Returns
reMSFT <- rMSFT - rTNX
reGWPH <- rGWPH - rTNX
reDIS <- rDIS - rTNX
reCAT <- rCAT - rTNX
reAMZN <- rAMZN - rTNX
# Information Tables:
pricTabl <- data.frame(MSFT, GWPH, DIS, CAT, AMZN)</pre>
# Creates data frame of asset prices
retTabl <- data.frame(rMSFT, rGWPH, rDIS, rCAT, rAMZN)</pre>
# Creates data frame of returns
EretTabl <- data.frame(reMSFT, reGWPH, reDIS, reCAT, reAMZN)</pre>
# Excess return data frame
retTabl <- retTabl[-1,] # remove missing data due to lagging</pre>
EretTabl <- EretTabl[-1,] # remove missing data due to lagging</pre>
priceMat <- matrix(c(MSFT, GWPH, DIS, CAT, AMZN), nrow= length(MSFT), ncol=5, byrow=TRUE) # creates a
# Variance/Covariance Matrix
asset.names <- c("MSFT", "GWPH", "DIS", "CAT", "AMZN")
# Create a list of row and col names for the var/cov matrix
VCV <- matrix(c(cov(retTabl)), nrow=5, ncol = 5, byrow=TRUE) # create a var/cov matrix by finding cov o
dimnames(VCV) <- list(asset.names, asset.names) # assigns asset.names to the VCV matrix
#Calculate Returns
rm <- matrix(colMeans(retTabl, na.rm=TRUE)) # creates an average return matrix, omitting missing value
erm <- matrix(colMeans(EretTabl, na.rm=TRUE)) # creates an average excess return matrix, omitting miss
tnxy = mean((rTNX)[-1,]) # calculates the average bond yield excluding Jan (risk free rate)
#Create Return Table
retmat <- matrix(c(rm, erm), ncol=2)</pre>
dimnames(retmat) = list(asset.names, c("Return ", "Excess Return"))
```

First we want to look at the data statistics

Instruments	Mean Returns	Variance of Returns	Beta (5Y Monthly)
MSFT	0.0190403	0.0027112	.87
GWPH	0.0183674	0.0299313	1.96
DIS	0.0045494	0.0017214	1.08
CAT	0.0223445	0.0058996	.98
AMZN	0.0263838	0.0062955	1.3

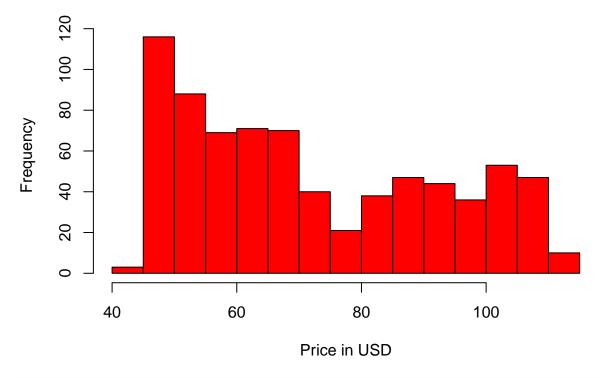
### Parameters of indices:

Instruments	Mean Returns	Variance of Returns	Beta
S&P 500	0.0070788	0.0010008	N/A
10-Year T-bill	0.0019565	0	N/A

We look at distribution of adjusted closing prices for each security:

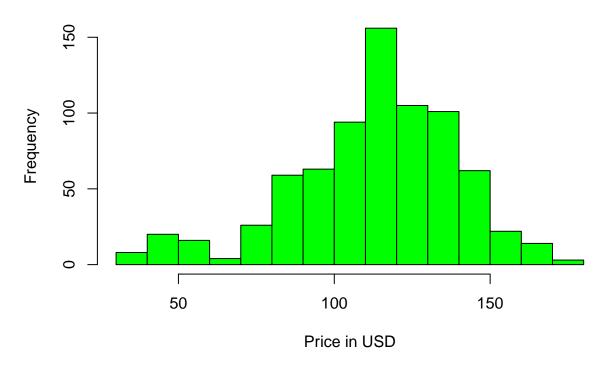
```
hist(adjMSFT,
    main='Daily Adjusted Closing Prices for MSFT',
    xlab='Price in USD',
    col='red',
)
```

## **Daily Adjusted Closing Prices for MSFT**



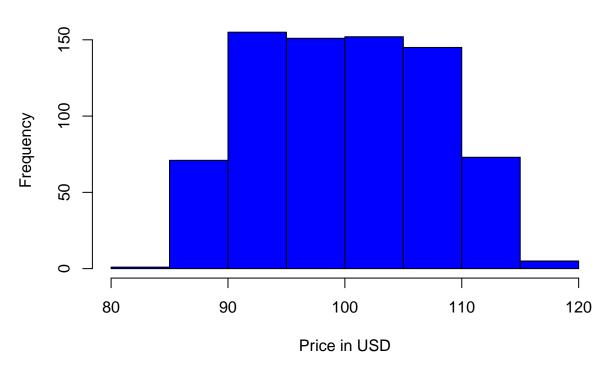
```
hist(adjGWPH,
    main='Daily Adjusted Closing Prices for GWPH',
    xlab='Price in USD',
    col='green',
)
```

# **Daily Adjusted Closing Prices for GWPH**



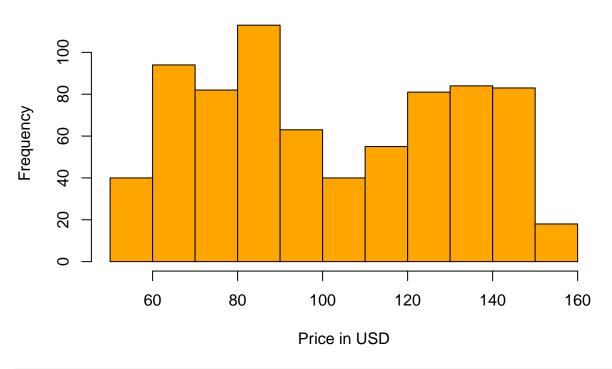
```
hist(adjDIS,
    main='Daily Adjusted Closing Prices for DIS',
    xlab='Price in USD',
    col='blue',
)
```

# **Daily Adjusted Closing Prices for DIS**



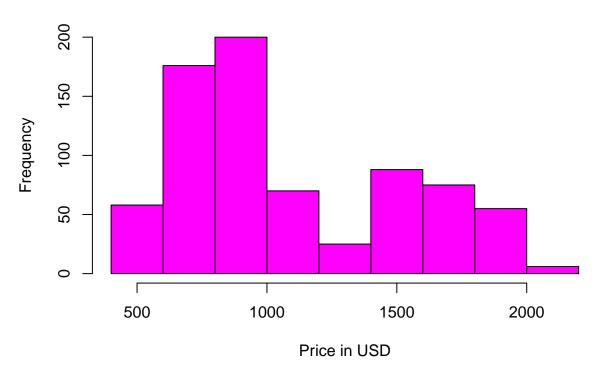
```
hist(adjCAT,
    main='Daily Adjusted Closing Prices for CAT',
    xlab='Price in USD',
    col='orange',
)
```

# **Daily Adjusted Closing Prices for CAT**



```
hist(adjAMZN,
    main='Daily Adjusted Closing Prices for AMZN',
    xlab='Price in USD',
    col='magenta',
)
```

### **Daily Adjusted Closing Prices for AMZN**



### **CAPM Portfolio Construction**

### 2a) Find the optimum weights using MPT

Since the investor's objective is to minimize risk subjected to a minimum return of the risk free asset–US Treasury Bill, in this case–we solve the constrained optimization problem.

Let  $x_i$  denotes the weight of the investment in asset i (i = 1, 2, 3, 4, 5), and assume all money is invested in i, meaning  $\sum x_i = x_1 + x_2 + x_3 + x_4 + x_5 = 1$ .

The returns of the portfolio is:

$$R_{p,x} = x_1 * r_1 + x_2 * r_2 + x_3 * r_3 + x_4 * r_4 + x_5 * r_5$$

The expected returns on the portfolio is:

$$\mu_{p,x} = E[R_{p,x}]$$

$$= x_1 * \mu_1 + x_2 * \mu_2 + x_3 * \mu_3 + x_4 * \mu_4 + x_5 * \mu_5$$
(1)

The variance of the portfolio returns is:

$$\sigma_{p,x}^2 = var(R_{p,x})$$

Formulating the Markowitz portfolio problem:

The investor's objective is:

$$\max \quad \mu_p = w' * \mu \quad \text{s.t.}$$
 
$$\sigma_p^2 = w' * (\sum) * w \quad \text{and} \quad w' * I = 1$$

where:

w = matrix of asset weights in the portfolio

w' = transpose matrix of asset weights in the portfolio

 $\mu = \text{matrix of mean returns of asset in the portfolio}$ 

 $\sum$  = Variance-covariance matrix of asset returns in the the portfolio

 $w' * I = \sum_{i=1}^{n} w_i$  or the sum weights of the asset in the portfolio, I is notation for identity matrix

(2)

Let  $\mu_{p,0}$  denotes a target expected return level. Formulate the problem:

min 
$$\sigma_{p,w}^2 = w' * (\sum) * w$$
 s.t.  
 $\mu_p = w' * \mu = \mu_{p,0}, \text{ and } w' * I = 1$  (3)

To solve this, form the Lagrangian function:

$$L(w, \lambda_1, \lambda_2) = w' * \sum *w + \lambda_1 * (w' * \mu - \mu_{p,0}) + \lambda_2 * (w' * I - 1)$$
(4)

Because there are two constraints  $(w' * \mu = \mu_{p,0} \text{ and } w'1 = 1)$  there are two Langrange multipliers  $\lambda_1$  and  $\lambda_2$ . The first order condition for a minimum are the linear equations:

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial w} = \frac{\partial (\sum *w^2)}{\partial w} + \frac{\partial (\lambda_1 * (w' * \mu - \mu_{p,0}))}{\partial w} + \frac{\lambda_2 * (w' * I - 1)}{\partial w} = 0$$

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial \lambda_1} = 0$$

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial \lambda_2} = 0$$
(5)

Simplify, we have:

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial w} = 2 * \sum *w + \lambda_1 * \mu + \lambda_2 * I = 0$$

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial \lambda_1} = w' * \mu - \mu_{p,0} = 0$$

$$\frac{\partial L(w, \lambda_1, \lambda_2)}{\partial \lambda_2} = w' * I - 1 = 0$$
(6)

Rewrite in matrix form:

$$\begin{pmatrix} 2 * \sum & \mu & I \\ \mu' & 0 & 0 \\ I' & 0 & 0 \end{pmatrix} * \begin{pmatrix} w \\ \lambda_1 \\ \lambda_2 \end{pmatrix} = \begin{pmatrix} 0 \\ \mu_{p,0} \\ I \end{pmatrix}$$
 (7)

or

where
$$A = \begin{pmatrix} 2 * \sum \mu & I \\ \mu' & 0 & 0 \\ I' & 0 & 0 \end{pmatrix}$$

$$z_w = \begin{pmatrix} w \\ \lambda_1 \\ \lambda_2 \end{pmatrix}$$

$$b_0 = \begin{pmatrix} 0 \\ \mu_{p,0} \\ I \end{pmatrix}$$
(8)

The solution for  $z_w$  is:

$$z_w = A^{-1} * b_0 (9)$$

The variance-covariance matrix is as follow:

VCV

```
## MSFT 0.0027112031 0.003255723 0.0004124035 0.0014986841 0.0025785122
## GWPH 0.0032557231 0.029931273 0.0020363050 0.0058326666 0.0064760106
## DIS 0.0004124035 0.002036305 0.0017214342 0.0009435592 0.0005948209
## CAT 0.0014986841 0.005832667 0.0009435592 0.0058996292 0.0023212055
## AMZN 0.0025785122 0.006476011 0.0005948209 0.0023212055 0.0062955209
```

 $A * z_w = b_0$ 

The monthly risk-free rate is: 0.0019664

```
# Optimum Portfolio

ZOPT <- solve(VCV,erm) # multiply inverse of VCV to excess return to find z

WOPT <- ZOPT/sum(ZOPT) # calculates weights

dimnames(WOPT) <- list(asset.names, "Weights") #label the weight matrix

# Calculate stats

ROPT <- t(WOPT)%*%rm # calculate optimal portfolio's return

VOPT <- t(WOPT)%*%VCV%*%WOPT # calculate optimal portfolio's variance

SDOPT <- VOPT^0.5 # calculate optimal portfolio's std dev

SRatio <-(ROPT-tnxy)/(SDOPT) # calculate optimal portfolio's Sharpe ratio

# Create Optimal Stats Table
```

```
PTBL <- matrix(c(ROPT, VOPT, SDOPT, SRatio), nrow = 4) # create a matrix of return, variance, std dev, optstat.names <- c("Return", "Variance", "Std Dev", "Sharpe") # labels for PTBL matrix

dimnames(PTBL) <- list(optstat.names, "Opt. Portfolio") # label the optimal portfolio matrix values
```

The optimal portfolio weights are as follow:

```
WOPT
```

```
## Weights
## MSFT 0.53181762
## GWPH -0.11209776
## DIS -0.08535046
## CAT 0.34599850
## AMZN 0.31963210
```

The statistics of the optimal portfolio is:

```
PTBL
```

```
## Opt. Portfolio
## Return 0.023842999
## Variance 0.003055134
## Std Dev 0.055273268
## Sharpe 0.395790195
```

2b) Allocate \$100.00 among the selected stocks using adjusted closing prices at 2018M12. 2019M1 will have a value of 100 as an index.

```
# Set start date and end date of data
start_date1 <- "2018-12-01"
end_date1 <- "2020-08-31"

# Get data
getSymbols("MSFT", src = "yahoo", from = start_date1, to = end_date1)

## [1] "MSFT"
getSymbols("GWPH", src = "yahoo", , from = start_date1, to = end_date1)

## [1] "GWPH"
getSymbols("DIS", src = "yahoo", , from = start_date1, to = end_date1)

## [1] "DIS"</pre>
```

```
getSymbols("CAT", src = "yahoo", , from = start_date1, to = end_date1)
## [1] "CAT"
getSymbols("AMZN", src = "yahoo", , from = start_date1, to = end_date1)
## [1] "AMZN"
getSymbols("^GSPC", src = "yahoo", , from = start_date1, to = end_date1) # SEP 500
## [1] "^GSPC"
getSymbols("^TNX", src = "yahoo", from=start_date1, to=end_date1) # TNX (10-year T-bill)
## Warning: ^TNX contains missing values. Some functions will not work if objects
## contain missing values in the middle of the series. Consider using na.omit(),
## na.approx(), na.fill(), etc to remove or replace them.
## [1] "^TNX"
rMSFT1 <- diff(log(to.monthly(MSFT)$MSFT.Adjusted))</pre>
rGWPH1 <- diff(log(to.monthly(GWPH)$GWPH.Adjusted))
rDIS1 <- diff(log(to.monthly(DIS)$DIS.Adjusted))
rCAT1 <- diff(log(to.monthly(CAT)$CAT.Adjusted))</pre>
rAMZN1 <- diff(log(to.monthly(AMZN)$AMZN.Adjusted))
rGSPC1 <- diff(log(to.monthly(GSPC)$GSPC.Adjusted))
rTNX1 <- to.monthly(TNX)$TNX.Adjusted /1200 # Using monthly rate
## Warning in to.period(x, "months", indexAt = indexAt, name = name, ...): missing
## values removed from data
rTNX1 <- rTNX1[-1,] # remove missing data due to lagging
mean_rTNX1 <- mean(rTNX1, na.rm=TRUE)</pre>
# Adjusted Prices
adjMSFT1 <- MSFT$MSFT.Adjusted
adjGWPH1 <- GWPH$GWPH.Adjusted
adjDIS1 <- DIS$DIS.Adjusted
adjCAT1 <- CAT$CAT.Adjusted
adjAMZN1 <- AMZN$AMZN.Adjusted
investedAmount <- 100
sharesMSFT <- as.numeric(investedAmount * WOPT[1] / adjMSFT1[1])</pre>
sharesGWPH <- as.numeric(investedAmount * WOPT[2] / adjGWPH1[1])</pre>
sharesDIS <- as.numeric(investedAmount * WOPT[3] / adjDIS1[1])</pre>
sharesCAT <- as.numeric(investedAmount * WOPT[4] / adjCAT1[1])</pre>
sharesAMZN <- as.numeric(investedAmount * WOPT[5] / adjAMZN1[1])</pre>
```

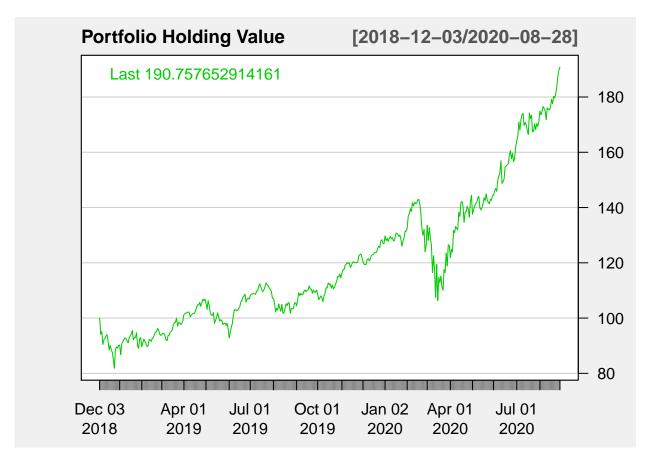
Based on the optimal weighting, to allocate \$100 to the portfolio, we would be purchase the following amount of each security:

Ticker	Weights	Stock to purchase
MSFT	0.5318176	0.4876924
GWPH	-0.1120978	-0.0887903
DIS	-0.0853505	-0.0752235
CAT	0.3459985	0.2651849
AMZN	0.3196321	0.0180343

2c) Using the adjusted closing prices from 2018M12 to 2020M8 calculate the holding values of the portfolio (assume fixed holdings with no re-balancing taking place over time).

We can then observe the fluctuations in the holding value of the portfolio from the period starting December 01 2018 to August 31, 2020 as follow.

```
chartSeries(holdings, name="Portfolio Holding Value", type="line", theme=chartTheme("white"))
```



By inspection we can see the portfolio experience a sharp sell off of almost 20% in December 2018, coincide with the broad U.S.market selloff due to a combination of the FED hiking the federal funds rate by 25 basis points to a targeted range of 2.25% to 2.5% (JeffCoxCNBCcom) and corporations followed suit by cutting profit forecasts and try temper expectations for earnings growth in 2019 after a big 2018 (Moyer).

The second visibly sharp sell off of the portfolio holding value also coincides with the broad market sell off in the mid March 2020 with investors raising cash in a risk-on environment when COVID-19 lockdowns started going into effects in the U.S.

# Find the tangency point of the Capital Allocation Line (CAL) and the efficient frontier.

The tangency point of the Capital Allocation Line is the point where the weights of the portfolio is optimal, represented by the point  $(\sigma_p, r_p)$  which is (0.0552733, 0.023843).

### Calculate the CAL equation and graph CAL and the efficient frontier.

The efficient frontier is the portfolio possibility curve represented by the equation:  $CAL = 0.0019664 + 0.3957902 * \sigma_p$ 

```
# Efficient Frontier and CAL

j <- 0  # set value for iterative loop variable t

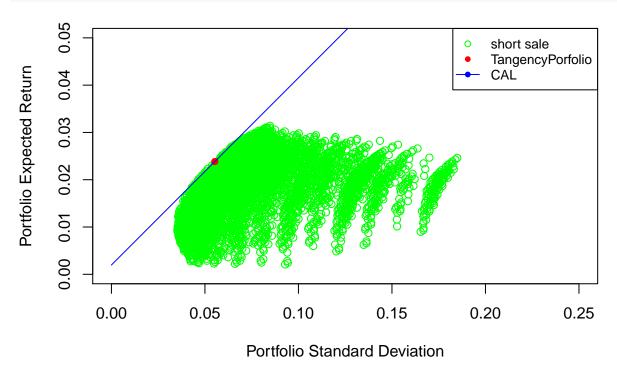
return_p <- rep(0, 50000)

sd_p <- rep(0, 50000)</pre>
```

```
# create a matrix of 0 to fill later with sd of different weights
vect_0 \leftarrow rep(0, 50000)
# create a matrix of O
fractions <- matrix(vect_0, 10000, 5)</pre>
# create a matrix of O to fill with weights
# iterate through weights for asset 1-5 from -20% to 100% by 10%
for (a in seq(-.2, 1, 0.1))
  for (b in seq(-.2, 1, 0.1))
    for (c in seq(-.2, 1, 0.1))
      for (d in seq(-.2, 1, 0.1))
        for (e in seq(-.2, 1, 0.1))
          #test that the weights are equal to 1
          if (a+b+c+d+e==1)
            # increment j by 1 if a+b+c+d+e is equal to 1 (valid weights)
            # load a,b,c,d,e values into row j of the matrix
            fractions[j,] \leftarrow c(a,b,c,d,e)
            # calculate the std dev of the portfolio at a given weight of assets
            sd_p[j] <- (t(fractions[j,])%*%VCV%*%fractions[j,])^.5</pre>
            # calculate the return of the portfolio at a given weight of assets
            return_p[j] <- fractions[j,]%*%rm</pre>
          }
        }
      }
    }
  }
# assign filled vector spots in return_p to the R_p matrix to omit empty spots
Rport <- return_p[1:j]</pre>
# assign filled vector spots in sd_p to the sigma_p matrix to omit empty spots
StdDev_p \leftarrow sd_p[1:j]
# Create Capital Asset Line
# Create x-coordinates for CAL points
f \leftarrow seq(0,.24,.24)
# Calculate corresponding y-coordinates
CAL <- tnxy + SRatio * f
```

## Warning in SRatio \* f: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.

```
#Plot the portfolio possibilities curve:
plot(StdDev_p, Rport, col="green1", xlab="Portfolio Standard Deviation", ylab= "Portfolio Expected Returning Portfolio Expected Returning Portfo
```



Estimate CAPM for your portfolio and graph the estimated  $\beta$  of the CAPM and the average return of your portfolio as a point relative to SML.

The expected risk premium of the portfolio based on the CAPM model is given as:

$$E(R_a - R_f) = \beta * (R_m - R_f)$$
or
$$R_a = R_f + \beta * (R_m - R_f)$$

$$R_a - R_f = \alpha_{Jensen} + \beta * (R_m - R_f)$$
or
$$Y = \alpha_{Jensen} + \beta * X + epsilon$$
with
$$Y = R_a - R_f$$

$$X = R_m - R_f$$

$$\beta = \text{Market risk or systematic risk}$$

$$\epsilon = \text{stochastic error term}$$
(10)

Here, the risk premium of the S&P 500 is the independent variable and the expected risk premium of the portfolio is the dependent variable.

Hypothesis for regression:

```
H_0: \alpha = 0
H_a: \alpha \neq 0
and
H_0: \beta = 0
H_a: \beta \neq 0
```

```
# Calculate and normalized the CAPM holdings
ra <- diff(log(to.monthly(holdings)[,1]))

Y <- na.omit(ra - rTNX1)
names(Y)[1] <- "Portfolio Risk Premium" # Rename column
Y_bar <- mean(Y)
Y_bar</pre>
```

#### ## [1] 0.02665436

```
X <- na.omit(rGSPC1 - rTNX1)
mean_X <- mean(X)

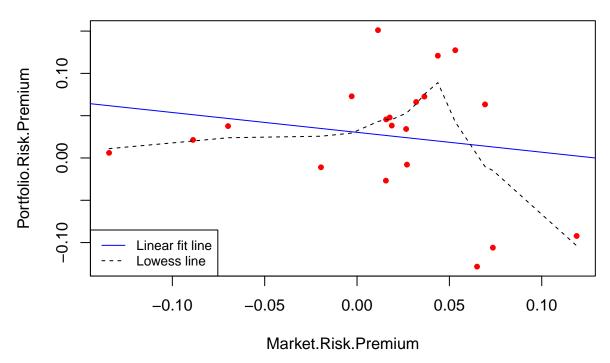
names(X)[1] <- "Market Risk Premium" # Rename column
data1 <- data.frame(X, Y)

plot(data1, col='red', main="Relationship Between Market & Portfolio Risk Premium", pch=20, cex=1)

# Add fit lines
abline(lm(Y~X), col="blue") # Regression line Y ~ X
lines(lowess(X,Y), col="black", lty=2) # Lowess line (X,Y)

legend("bottomleft",c("Linear fit line", "Lowess line"), cex=.8, col=c("blue", "black"), lty=1:2)</pre>
```

### Relationship Between Market & Portfolio Risk Premium



Through inspection, we observe the cluster observation scattering in a big range from left to right. This implies a weak linear relationship between the Market Portfolio Risk Premium (the independent X variable on the x-axis) and the CAPM Portfolio Risk Premium (the dependent Y variable on the y-axis).

Next, we attempts to fit an equation of a line:  $Y = \alpha_{Jensen} + \beta * X + \epsilon$ 

```
fit1 <- lm(Y~X, data=data1)
summary(fit1)</pre>
```

```
##
## Call:
## lm(formula = Y ~ X, data = data1)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
  -0.14347 -0.04775 0.01132
                               0.04489
##
##
##
  Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
  (Intercept) 0.03029
                           0.01735
                                      1.746
                                              0.0979 .
               -0.23470
                           0.29421
                                    -0.798
## X
                                              0.4354
##
## Signif. codes:
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.07488 on 18 degrees of freedom
## Multiple R-squared: 0.03415,
                                     Adjusted R-squared:
## F-statistic: 0.6364 on 1 and 18 DF, p-value: 0.4354
```

The estimated equation is Y = .04050 - .34504 \* X, where the  $p_{value}$  for the intercept .0308 < .05. Therefore, we reject the null hypothesis at 95% confidence level that the intercept  $\alpha_{Jensen}$  statistically is no different from zero. Thus, we reject the null hypothesis  $H_0: \alpha = 0$  and accept the null hypothesis  $H_a: \alpha \neq 0$ .

The coefficient  $\beta = 1.07468$  represents the increase in portfolio risk premium relative to increase in the market portfolio risk premium. The  $p_{value}$  for  $\beta$  is .2544 > .05, implying that the coefficient  $\beta$  statistically is insignificant at 95% or more, and we accept the null hypothesis  $H_0: \beta = 0$  and reject the alternative hypothesis  $H_a: \beta \neq 0$ .

#### Goodness of Fit:

Through inspection, we observe the  $R^2 = .07151$  value to not be close to 1 at all.  $R^2 = .07151$  implies that 7.15 of the variations in the portfolio risk premium is explained by the market risk premium.

#### Standard Error of Regression:

We can see that the Standard Error of Regression is S.E. = .07458.

From this, we can calculate the forecasting efficiency statistic to be:

$$\frac{S.E.}{\overline{Y}} = \frac{.05618}{0.0266544}$$

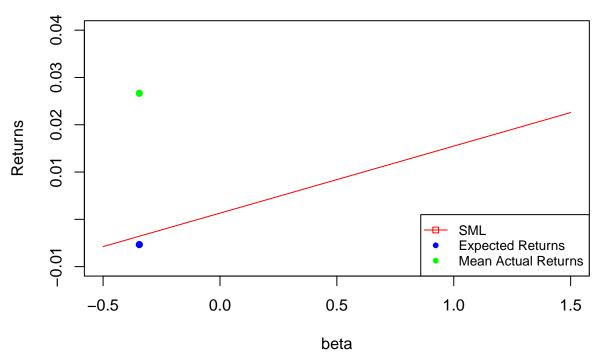
$$= 279.8\% > 10\%$$
(12)

This statistic implies that this is not a good forecasting model.

Thus, upon exploring the goodness of fit and standard error of regression, we confirm our initial observation that the portfolio risk premium and the market portfolio risk premium has a weak linear relationship.

The Security Market Line:

### **CAPM portfolio beta relative to the Security Market Line**



The Security Market Line pass through the point  $(0, \overline{R_f})$  and  $(1, \overline{X})$ , which are (0, 0.0013135) and (1, 0.0154876).

Relative to its market risk of beta = -.34504, the expected return is -0.0053439 and the average return is 0.0266544. We can observe that at this estimated  $\beta$ , the expected return is below the security market line and the actual average return is above the security market line.

### Forecasting of Portfolio

3) Do Naive, MA(5), MA(15), ES, Holt, and Holt-Winters forecasting of your portfolio returns and do a three-period-ahead forecasting of the portfolio returns for each forecast. Estimate the accuracy statistics.

Get the portfolio monthly returns over the period based on its daily closing price:

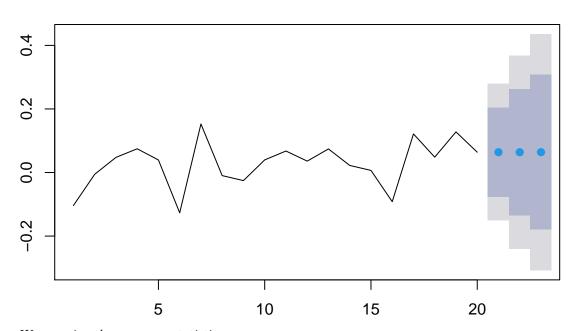
### Naive Foreacsting

```
rwf <- rwf(rHoldings, 3)
rwf

## Point Forecast Lo 80 Hi 80 Lo 95 Hi 95
## 21     0.06395247 -0.07647209 0.2043770 -0.1508084 0.2787133
## 22     0.06395247 -0.13463785 0.2625428 -0.2397652 0.3676701
## 23     0.06395247 -0.17927000 0.3071749 -0.3080242 0.4359291

plot(rwf, main="Portfolio Holdings Monthly Returns Random Walk Forecast")</pre>
```

### Portfolio Holdings Monthly Returns Random Walk Forecast



We examine the accuracy statistics:

```
accuracy(rwf)
```

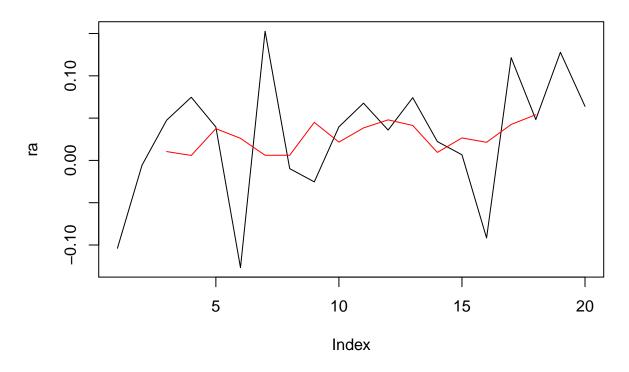
```
## ME RMSE MAE MPE MAPE MASE ACF1
## Training set 0.008831147 0.1095739 0.08400768 7.77391 286.3902 1 -0.5620567
```

### MA(5) Forecast

```
ma5 <- ma(rHoldings, order=5)

plot(ra, main="Portfolio Holdings Monthly Returns MA5 Forecast", type = "1")
lines(ma5, col="red")</pre>
```

## **Portfolio Holdings Monthly Returns MA5 Forecast**

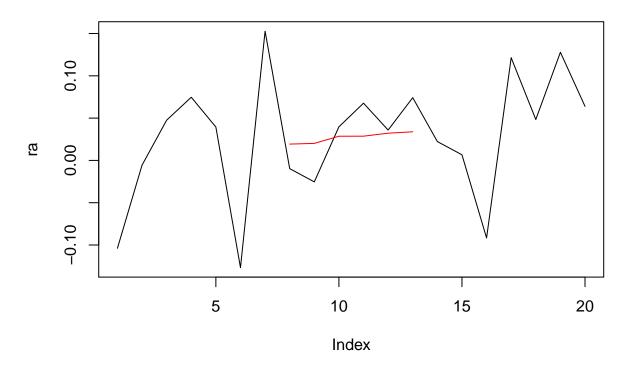


### MA(15) Forecast

```
ma15 <- ma(rHoldings, order=15)

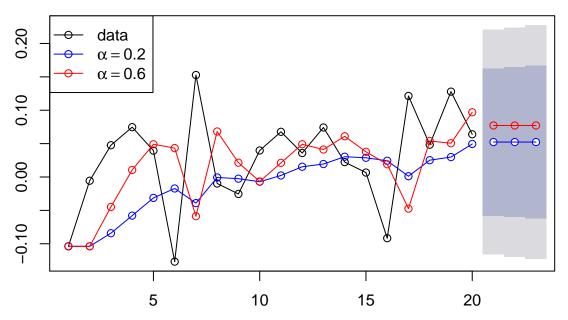
plot(ra, main="Portfolio Holdings Monthly Returns MA15 Forecast", type = "l")
lines(ma15, col="red")</pre>
```

### **Portfolio Holdings Monthly Returns MA15 Forecast**



#### **Exponential Smoothing Forecast**

### Simple Exponential Smoothing of Portfolio Returns



With  $\alpha = .2$ :

#### fit1

```
## Point Forecast Lo 80 Hi 80 Lo 95 Hi 95
## 21 0.05233808 -0.05780525 0.1624814 -0.1161116 0.2207878
## 22 0.05233808 -0.05998652 0.1646627 -0.1194476 0.2241237
## 23 0.05233808 -0.06212623 0.1668024 -0.1227200 0.2273961
```

#### accuracy(fit1)

```
## Training set 0.03904435 0.0859453 0.0678189 -18.61915 193.3179 0.8072941 ## ACF1 ## Training set -0.1934649
```

#### With $\alpha = .6$ :

#### fit2

```
## Point Forecast Lo 80 Hi 80 Lo 95 Hi 95
## 21 0.07714779 -0.03755176 0.1918474 -0.09827004 0.2525656
## 22 0.07714779 -0.05661372 0.2109093 -0.12742279 0.2817184
## 23 0.07714779 -0.07327926 0.2275749 -0.15291054 0.3072061
```

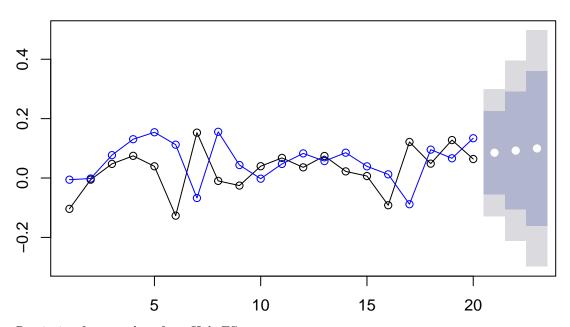
#### accuracy(fit2)

```
## ME RMSE MAE MPE MAPE MASE
## Training set 0.01508226 0.08950054 0.06874322 -21.41817 230.1669 0.8182968
## ACF1
## Training set -0.3748286
```

#### Holt Trend Model Forecast

```
#Holt Trend Model
holt1 <- holt(ra, alpha=0.8, beta=0.2, initial="simple", h=3)
plot(holt1, main="Holt Exponential Smoothing, Portfolio Holdings", fcol="white", type="o")
lines(fitted(holt1), col="blue", type="o")</pre>
```

### Holt Exponential Smoothing, Portfolio Holdings



Retrieving forecast data from Holt ES:

#### holt1\$model\$state

```
## Time Series:
## Start = 0
## End = 20
## Frequency = 1
##
##
   0 -0.103839331
                   0.0982258062
##
   1 -0.084194170
                   0.0825096772
##
   2 -0.004827718
                   0.0818810321
##
   3 0.053470443 0.0771644579
##
      0.085854384 0.0682083545
##
      0.062386741
                   0.0498731550
##
   6 -0.078959888
                   0.0116291983
##
      0.108745804
                   0.0468444969
      0.023328108
                   0.0203920584
##
   9 -0.011577796
                   0.0093324659
      0.031312520 0.0160440359
  10
## 11
      0.063601770 0.0192930788
      0.045271979 0.0117685047
## 12
## 13 0.070751161 0.0145106402
```

```
## 14 0.034876282 0.0044335364
## 15 0.013175438 -0.0007933398
## 16 -0.070872841 -0.0174443275
## 17 0.079475449 0.0161141959
## 18 0.057827285 0.0085617239
## 19 0.115549083 0.0183937388
## 20 0.077950538 0.0071952820
holt1$mean
## Time Series:
## Start = 21
## End = 23
## Frequency = 1
## [1] 0.08514582 0.09234110 0.09953638
accuracy(holt1)
##
                                 RMSE
                                                     MPE
                                                             MAPE
                                                                      MASE
                        ME
                                            MAF.
## Training set -0.02844704 0.1095262 0.0855149 71.01617 225.0103 1.017942
##
                     ACF1
## Training set -0.4120045
```

#### **Holt-Winter Seasonal Method:**

There might not be seasonality in our data to run the Holt-Winter model. The numerical method is shown below.

```
#hws2 <- hw(rHoldings)
#plot(hws2, plot.conf=FALSE, type="o", fcol="white")
#lines(fitted(hws1), col="red", lty=2)</pre>
```

4) Start with the regression analysis and forecasting of your portfolio returns. Use the CAPM model to estimate the coefficients of the models and use them for forecasting. Do a 10-days ex-post forecasting of the portfolio risk premiums and compare the forecasted value to actual ones. Do a three-period-ahead (ex-ante) forecasting of the portfolio risk premiums and write confidence intervals.

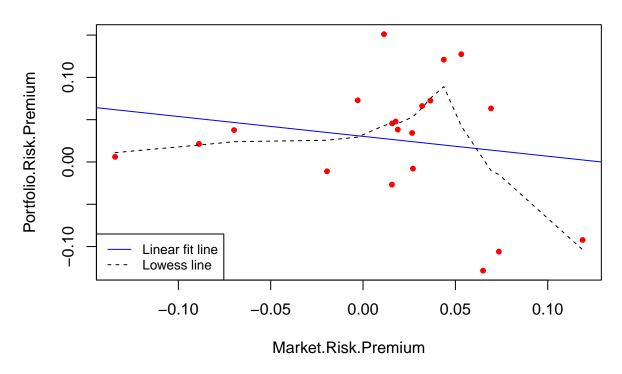
#### Regression of Market Risk Premium and Portfolio Risk Premium

First we run the linear regression and examine its result.

```
# Recall Y is the portfolio risk premium from January 2019 to August 2020
# as calculated above.
# Likewise, rTNX1 is the risk free rate for the same period.
reg <- lm(Portfolio.Risk.Premium ~ Market.Risk.Premium, data=data1)
summary(reg)</pre>
```

```
##
## Call:
## lm(formula = Portfolio.Risk.Premium ~ Market.Risk.Premium, data = data1)
## Residuals:
##
       \mathtt{Min}
                 1Q Median
                                    3Q
                                            Max
## -0.14347 -0.04775 0.01132 0.04489 0.12346
##
## Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                       0.03029
                                  0.01735 1.746 0.0979 .
                                   0.29421 -0.798
## Market.Risk.Premium -0.23470
                                                     0.4354
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 0.07488 on 18 degrees of freedom
## Multiple R-squared: 0.03415,
                                    Adjusted R-squared: -0.01951
## F-statistic: 0.6364 on 1 and 18 DF, p-value: 0.4354
confint(reg)
##
                              2.5 %
                                        97.5 %
## (Intercept)
                       -0.006166892 0.06674557
## Market.Risk.Premium -0.852820785 0.38341716
We can visual the result as follow:
plot(data1, col='red', main="Relationship Between Market & Portfolio Risk Premium", pch=20, cex=1)
# Add fit lines
abline(reg, col="blue") # Regression line Y ~ X
lines(lowess(X,Y), col="black", lty=2) # Lowess line (X,Y)
legend("bottomleft",c("Linear fit line", "Lowess line"), cex=.8, col=c("blue", "black"), lty=1:2)
```

### Relationship Between Market & Portfolio Risk Premium



#### **Ex-post Forecasting**

For ex-post forecasting, since our data is monthly portfolio returns with 20 observations, it makes more sense to do split the data on a 5 months ex-post forecasting instead of 10 days as recommended by the guide. Splitting the data:

```
data1_1 <- data1[1:15,]
data1_2 <- data1[16:20,]</pre>
```

Running regression on the  $data1_1$ :

```
regExPost <- lm(Portfolio.Risk.Premium ~ Market.Risk.Premium, data=data1_1)
summary(regExPost)</pre>
```

```
##
## Call:
## lm(formula = Portfolio.Risk.Premium ~ Market.Risk.Premium, data = data1_1)
##
##
  Residuals:
##
                          Median
         Min
                    1Q
                                         ЗQ
                                                  Max
   -0.127170 -0.037323 -0.000716 0.043271
##
##
  Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        0.01786
                                    0.01817
                                              0.983
                                                       0.344
## Market.Risk.Premium -0.29418
                                    0.32971
                                            -0.892
                                                       0.388
## Residual standard error: 0.07038 on 13 degrees of freedom
```

```
## Multiple R-squared: 0.0577, Adjusted R-squared: -0.01478 ## F-statistic: 0.7961 on 1 and 13 DF, p-value: 0.3885
```

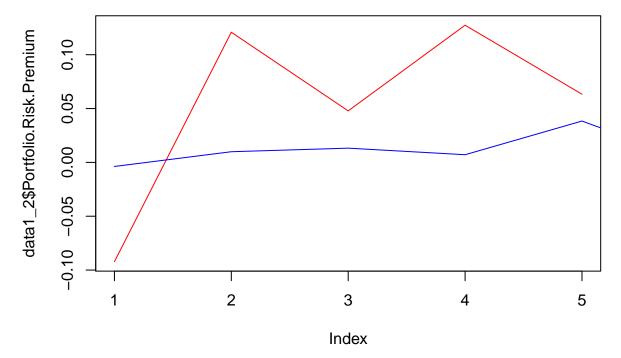
Doing the Ex-Post Forecasting:

```
predExPost <- predict(regExPost, newdata=data1_2, se.fit=TRUE)
predExPost</pre>
```

```
## $fit
##
                    May 2020
                                  Jun 2020
       Apr 2020
                                               Jul 2020
                                                            Aug 2020
## -0.017120773 0.004988486 0.012657516 0.002210383 -0.002531426
##
## $se.fit
     Apr 2020
                May 2020
                           Jun 2020
                                       Jul 2020
##
## 0.04307277 0.02310716 0.01903903 0.02514972 0.02907819
##
## $df
## [1] 13
##
## $residual.scale
## [1] 0.07038464
```

Plotting the results:

```
plot(data1_2$Portfolio.Risk.Premium, type="l", col="red")
lines(regExPost$fitted.values, col="blue")
```



We have the 95% confidence intervals for our forecast as follow:

```
\hat{Y}_t \pm 1.96 \hat{\sigma}_{\epsilon}
-0.017120773 \pm 1.96 * 0.07038
0.004988486 \pm 1.96 * 0.07038
0.012657516 \pm 1.96 * 0.07038
0.002210383 \pm 1.96 * 0.07038
-0.002531426 \pm 1.96 * 0.07038
(13)
```

#### **Ex-ante Forecasting**

Running the regression:

```
regExAnte <- lm(Portfolio.Risk.Premium ~ Market.Risk.Premium, data=data1)
summary(regExAnte)
##
## Call:
## lm(formula = Portfolio.Risk.Premium ~ Market.Risk.Premium, data = data1)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   ЗQ
                                           Max
## -0.14347 -0.04775 0.01132 0.04489 0.12346
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
                       0.03029
                                  0.01735
                                            1.746
                                                    0.0979 .
## (Intercept)
## Market.Risk.Premium -0.23470
                                  0.29421
                                           -0.798
                                                    0.4354
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.07488 on 18 degrees of freedom
## Multiple R-squared: 0.03415, Adjusted R-squared: -0.01951
```

Perform a three-period-ahead ex-ante forecast of portfolio holdings returns:

## F-statistic: 0.6364 on 1 and 18 DF, p-value: 0.4354

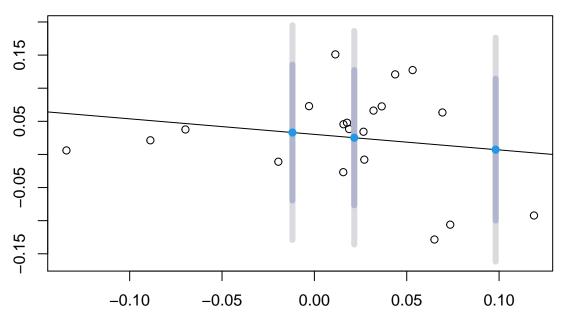
```
predExAnte <- forecast::forecast(regExAnte, newdata=data.frame(Market.Risk.Premium=c(0.021584390, -0.01
predExAnte</pre>
```

```
## Point Forecast Lo 80 Hi 80 Lo 95 Hi 95
## 1 0.025223443 -0.07688333 0.1273302 -0.1360212 0.1864681
## 2 0.033080188 -0.06955968 0.1357201 -0.1290063 0.1951666
## 3 0.007253296 -0.09983073 0.1143373 -0.1618513 0.1763579
```

Graphing the regression and its forecast:

```
plot(predExAnte, type="1")
```

### Forecasts from Linear regression model



We have the 95% confidence interval for our forecast as follow:

$$\hat{Y}_t \pm 1.96 \hat{\sigma}_{\epsilon}$$

$$0.025223443 \pm 1.96 * 0.07488$$

$$0.033080188 \pm 1.96 * 0.07488$$

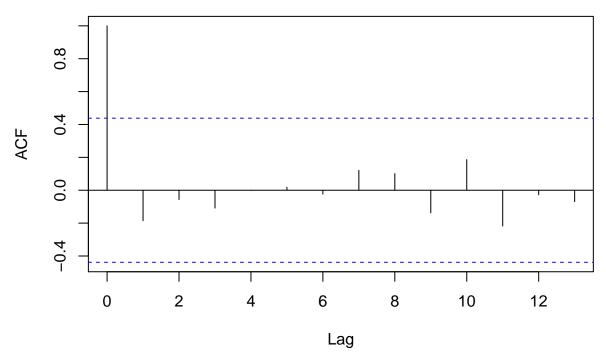
$$0.007253296 \pm 1.96 * 0.07488$$
(14)

5) Do an ARIMA model of your portfolio returns and use it for three-period ahead forecasting of the returns to portfolio. Write confidence interval. Estimate the accuracy statistics.

Review the ACF plot for portfolio holding monthly returns:

acf(rHoldings, main="ACF")

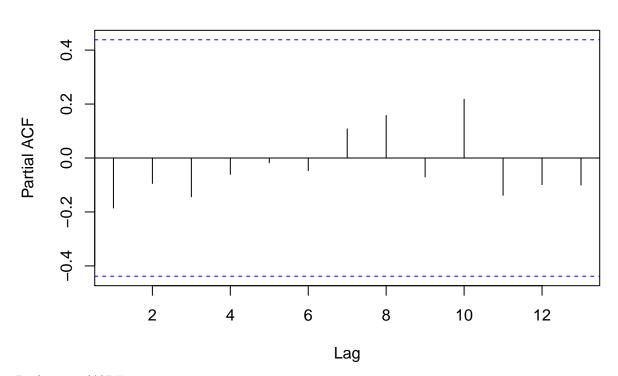




And the PACF:

pacf(rHoldings, main="PACF")

# PACF



Perform an (A)DF Test:

```
adf.test(rHoldings)
## Augmented Dickey-Fuller Test
## alternative: stationary
## Type 1: no drift no trend
       lag ADF p.value
##
## [1,]
        0 -4.44 0.0100
## [2,]
        1 -2.41 0.0191
        2 -1.51 0.1314
## [3,]
## Type 2: with drift no trend
       lag ADF p.value
         0 -5.46 0.0100
## [1,]
## [2,]
        1 -3.72 0.0111
## [3,]
         2 -2.94 0.0574
## Type 3: with drift and trend
       lag ADF p.value
## [1,]
        0 -5.64 0.0100
## [2,]
        1 -3.91 0.0278
## [3,]
         2 -3.27 0.0956
## ----
## Note: in fact, p.value = 0.01 means p.value <= 0.01
Fitting an auto-ARIMA model:
fitAutoARIMA <- auto.arima(rHoldings)</pre>
summary(fitAutoARIMA)
## Series: rHoldings
## ARIMA(0,0,0) with non-zero mean
## Coefficients:
##
           mean
##
         0.0280
## s.e. 0.0161
## sigma^2 estimated as 0.00548: log likelihood=24.2
## AIC=-44.4
             AICc=-43.7
                           BIC=-42.41
## Training set error measures:
                                    RMSE
                                                MAE
                                                         MPE
## Training set -1.470171e-13 0.07215255 0.05578648 93.45528 128.1167 0.6640641
## Training set -0.1851261
Performing a three-period ahead forecasting:
pred_autoARIMA <- forecast::forecast(fitAutoARIMA, h=3)</pre>
pred_autoARIMA
```

Lo 95

Hi 95

Hi 80

Lo 80

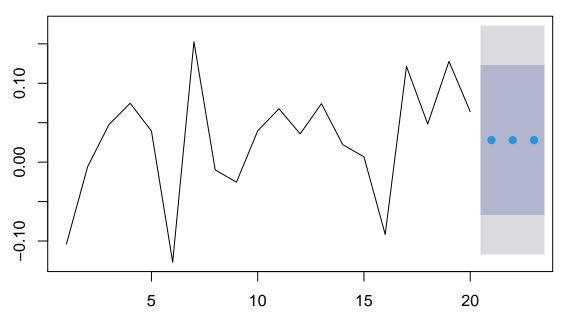
##

Point Forecast

```
## 21 0.02796782 -0.06690154 0.1228372 -0.1171224 0.173058
## 22 0.02796782 -0.06690154 0.1228372 -0.1171224 0.173058
## 23 0.02796782 -0.06690154 0.1228372 -0.1171224 0.173058
```

plot(pred\_autoARIMA)

### Forecasts from ARIMA(0,0,0) with non-zero mean



Review the confidence interval:

$$\hat{Y}_t \pm 1.96 \hat{\sigma}_{\epsilon}$$

$$0.02796782 \pm 1.96 * \sqrt{0.00548}$$

$$0.02796782 \pm 1.96 * \sqrt{0.00548}$$

$$0.02796782 \pm 1.96 * \sqrt{0.00548}$$
(15)

Review the accuracy statistics:

### accuracy(pred\_autoARIMA)

```
## ME RMSE MAE MPE MAPE MASE
## Training set -1.470171e-13 0.07215255 0.05578648 93.45528 128.1167 0.6640641
## ACF1
## Training set -0.1851261
```

### 6) Test your ARIMA model for the stability of the ARIMA coefficients.

To test for stability of the ARIMA coefficients, we split the data in half, applies 2 separate ARIMA models and run an F-test.

```
# Splitting the data
rHoldings1 <- rHoldings[1:10]
rHoldings2 <- rHoldings[11:20]
# Fitting ARIMA models
fitAutoARIMA1 <- auto.arima(rHoldings1)</pre>
fitAutoARIMA2 <- auto.arima(rHoldings2)</pre>
# Review the ARIMA models
summary(fitAutoARIMA1)
## Series: rHoldings1
## ARIMA(0,0,0) with zero mean
## sigma^2 estimated as 0.006193: log likelihood=11.23
## AIC=-20.46 AICc=-19.96 BIC=-20.16
##
## Training set error measures:
                                   RMSE
                                               MAE MPE MAPE
                                                                  MASE
                                                                             ACF1
## Training set 0.008281122 0.07869687 0.0625526 100 100 0.6236386 -0.3443178
summary(fitAutoARIMA2)
## Series: rHoldings2
## ARIMA(0,0,0) with non-zero mean
## Coefficients:
##
           mean
         0.0477
##
## s.e. 0.0187
## sigma^2 estimated as 0.003902: log likelihood=14.07
## AIC=-24.14 AICc=-22.42 BIC=-23.53
## Training set error measures:
                           ME
                                    RMSE
                                               MAE
                                                           MPE
                                                                    MAPE
## Training set 5.550946e-18 0.05926407 0.04350333 -39.64692 113.2025 0.5883591
## Training set -0.09468779
We have the F-stat:
                                         0.006193
                                        =\frac{0.01}{0.003902}
                                                                                          (16)
                                       =1.5871348
                                   F_{crit} = 3.1789
                                    dof = N - 1 = 10 - 1 = 9
                                      \alpha = .05
```

We notice a relative small F-stat, i.e. the differences in variances of two models are fairly insignificant, i.e. the coefficients of the ARIMA model are stable.

- 7) Test your ARIMA model for the existence of ARCH and GARCH and do proper corrections, if needed.
- 8) Find different time-series measures of volatility for your portfolio returns (see the volatility file posted on Blackboard) and do a three-period ahead forecasting of the portfolio volatility. Compare the different measures of volatility with GARCH.
- 9) Use the accuracy statistics of the different forecasting techniques to decide which technique fits the data best.
- 10) Test whether your portfolio index conforms to the efficient market hypothesis.
- 11) Find 1% and 3% daily and monthly VaR of your portfolio.

1% VaR

```
# 1% VaR Holding Portfolio
VaR_threshold <- 1

# Set scaling factor based on the period of evaluation
# In this example: {1: '1 year', 1/2: '6 months', 1/12: '1 month', 1/250: '1 day'}

# 1% 1 month VaR
scalingFactor <- 1/12
z_stat <- qnorm(VaR_threshold/100, 0, 1, lower.tail = TRUE)
VaR_1mo_p_1percent <- ROPT*scalingFactor + SDOPT*sqrt(scalingFactor) * z_stat

# 1% 1 day VaR
scalingFactor <- 1/250
VaR_1day_p_1percent <- ROPT*scalingFactor + SDOPT*sqrt(scalingFactor) * z_stat</pre>
```

The 1% monthly VaR is -0.0351323. The 1% daily VaR is -0.008037.

3% VaR

```
# 1% VaR Holding Portfolio
VaR_threshold <- 3

# Set scaling factor based on the period of evaluation
# In this example: {1: '1 year', 1/2: '6 months', 1/12: '1 month', 1/250: '1 day'}

# 1% 1 month VaR
scalingFactor <- 1/12</pre>
```

```
z_stat <- qnorm(VaR_threshold/100, 0, 1, lower.tail = TRUE)
VaR_1mo_p_3percent <- ROPT*scalingFactor + SDOPT*sqrt(scalingFactor) * z_stat

# 1% 1 day VaR
scalingFactor <- 1/250
VaR_1day_p_3percent <- ROPT*scalingFactor + SDOPT*sqrt(scalingFactor) * z_stat</pre>
```

The 1% monthly VaR is -0.0280231. The 1% daily VaR is -0.0064795.

#### 12) Find 1% and 3% daily and monthly equity EVaR of your portfolio.

Recall that the Risk Adjusted Portfolio or RAP, is the sum weighted values of assets in the portfolio, weighted by the corresponding assets'  $\beta_i$ , i.e.  $\sum \beta_i R_i$ .

Recall the summary statistics of each stock:

Instruments	Mean Returns	Variance of Returns	Beta (5Y Monthly)
MSFT	0.0190403	0.0027112	.87
GWPH	0.0183674	0.0299313	1.96
DIS	0.0045494	0.0017214	1.08
CAT	0.0223445	0.0058996	.98
AMZN	0.0263838	0.0062955	1.3

```
betas <- c(.87, 1.96, 1.08, .98, 1.3)
RAP <- 100*sum(WOPT*betas)
```

We have the Risk Adjusted Portfolio value as 90.5391483'.

Recall that EVaR = RAP \* VaR. Thus:

The 1% monthly EVaR is -3.1808515. The 1% daily VaR is -0.7276675.

Likewise, the 3% monthly EVaR is -2.537184. The 3% daily VaR is -0.586647.

- 13) Graph the security Market Line (SML) of your portfolio and test whether you would add a stock of your own choice to the portfolio or not.
- 14) Do an intervention function analysis of the March 15th closing of US economy due to

COVID19. Did the event have any effect on return to your portfolio.

# 15) Do a 2-variable VAR between your portfolio index and S&P500 index. Graph the Impulse

response function of the VAR and comment on the relationship.

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