

GUIDING PRINCIPLE #1: Focus on Worst-Case Analysis

By focusing on worst-case analysis our running time bound holds for every input of length n .

AVERAGE-CASE ANALYSIS - Evaluate an algorithm's average running time by accounting for relative frequency of different input lengths.
* Requires domain specific knowledge

BENCHMARK ANALYSIS - Evaluate an algorithm's running time to execute a pre-specified/standardized set of inputs the algorithm will most likely see.
* Requires domain specific knowledge.

WORST-CASE ANALYSIS - Evaluate an algorithm as if every time it runs the algorithm will take its maximum amount of time to execute.

Particularly appropriate for "general-purpose" problems in which we do not know what the inputs to the algorithm will be beforehand.

Worst-case is mathematically easier to analyze

GUIDING PRINCIPLE #2: Do not worry about constant factors or lower order terms

JUSTIFICATIONS:

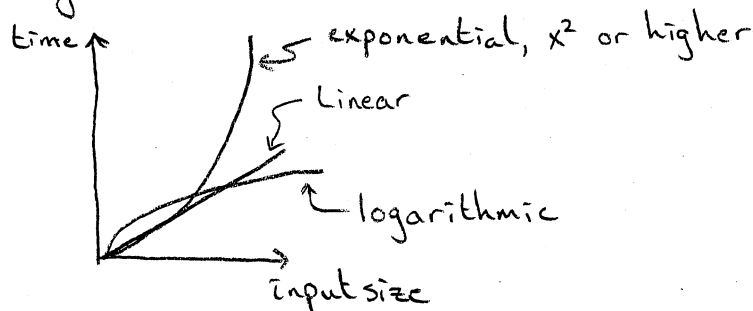
- 1) Much easier mathematically to remove constant factors and lower order terms
- 2) Constant factors will depend on and change based on computer architecture, the computer, programmer, and so on.
- 3) Lose very little predictive power. We lose some granularity of analysis, but overall the higher order terms will give a strong snapshot as to the speed of the algorithm.

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GUIDING PRINCIPLE #3: USE ASYMPTOTIC ANALYSIS

Asymptotic analysis uses large inputs to the algorithm to determine if the algorithm has run-time limits it cannot improve upon.

For example, x^2 and higher order terms grow much more quickly than linear or lower order terms with increasing input size.



Therefore, when n is large an algorithm of runtime n^2 is slower than an algorithm of runtime n .

While there will be instances when a higher order runtime algorithm will perform better than a lower order algorithm these instances will all be when the input size is small ($n < 100$) due to constant factors influencing the higher order terms.

You can optimize a solution to a problem by switching algorithms after reaching a given input size, but this would only be after optimizing for the large number of inputs. Otherwise, the optimization efforts would be premature.

WHAT IS A FAST ALGORITHM?

A fast algorithm is an algorithm whose worst-case running time grows slowly as input size increases.

Quadratic run time better than exponential n^2 vs. 2^n

Linear runtime is better than quadratic n vs n^2

Logarithmic runtime is better than linear $\lg n$ vs n

Constant runtime is better than logarithmic 10 vs $\lg n$