

▼ Resolução Exercício Aula 2

```
1 import numpy as np
2 import random as rnd
```

▼ Criar função znorm:

$$znorm = \frac{x - \min(x)}{\max(x) - \min(x)}$$

```
1 def znorm(x):
2
3     return (x - min(x)) / (max(x) - min(x))
```

▼ criar vetores A e B

```
1 # vetorA = np.arange(1,21) # criando direto com numpy
2 vetorA = np.array(list(range(1,21))) # metodo apresentado na aula
```

```
1 vetorA
array([ 1,  2,  3,  4,  5,  6,  7,  8,  9, 10, 11, 12, 13, 14, 15, 16, 17,
       18, 19, 20])

1 # vetorB = np.random.randint(1, 21, 20) # criando direto pelo numpy
2
3 vetorB = np.array(rnd.sample(range(1,21), 20)) # metodo apresentado na aula

1 vetorB
array([ 2,  9, 12, 15, 19, 16, 10,  5,  1,  6,  4, 13,  3, 11, 20, 14, 17,
       7, 18,  8])
```

▼ Aplicar função

```
1 vetorA_norm = znorm(vetorA)
2 vetorA_norm
array([0.          , 0.05263158, 0.10526316, 0.15789474, 0.21052632,
       0.26315789, 0.31578947, 0.36842105, 0.42105263, 0.47368421,
       0.52631579, 0.57894737, 0.63157895, 0.68421053, 0.73684211,
       0.78947368, 0.84210526, 0.89473684, 0.94736842, 1.        ])

1 vetorB_norm = znorm(vetorB)
2 vetorB_norm
array([0.05263158, 0.42105263, 0.57894737, 0.73684211, 0.94736842,
       0.78947368, 0.47368421, 0.21052632, 0.          , 0.26315789,
       0.15789474, 0.63157895, 0.10526316, 0.52631579, 1.        ,
       0.68421053, 0.84210526, 0.31578947, 0.89473684, 0.36842105])
```

▼ Criar as matrizes

```
1 np.shape(vetorA), np.shape(vetorB)
((20,), (20,))

1 np.shape([vetorA, vetorB])
(2, 20)

1 np.shape(np.transpose([vetorA, vetorB]))
(20, 2)

1 matrizAB = np.transpose([vetorA, vetorB])

1 matrizAB
array([[ 1,  2],
       [ 2,  9],
       [ 3, 12],
       [ 4, 15],
       [ 5, 19],
       [ 6, 16],
       [ 7, 10],
       [ 8,  5],
       [ 9,  1],
       [10,  6],
       [11,  4],
       [12, 13],
       [13,  3],
       [14, 11],
       [15, 20],
       [16, 14],
       [17, 17],
       [18,  7],
```

```
[19, 18],  
[20, 8]])
```

```
1 matrizAB_norm = np.transpose([vetorA_norm, vetorB_norm])
```

```
1 matrizAB_norm
```

```
array([[0.          , 0.05263158],  
       [0.05263158, 0.42105263],  
       [0.10526316, 0.57894737],  
       [0.15789474, 0.73684211],  
       [0.21052632, 0.94736842],  
       [0.26315789, 0.78947368],  
       [0.31578947, 0.47368421],  
       [0.36842105, 0.21052632],  
       [0.42105263, 0.        ],  
       [0.47368421, 0.26315789],  
       [0.52631579, 0.15789474],  
       [0.57894737, 0.63157895],  
       [0.63157895, 0.10526316],  
       [0.68421053, 0.52631579],  
       [0.73684211, 1.        ],  
       [0.78947368, 0.68421053],  
       [0.84210526, 0.84210526],  
       [0.89473684, 0.31578947],  
       [0.94736842, 0.89473684],  
       [1.          , 0.36842105]])
```

▼ Aplicar operações

- operação *

```
1 matrizAB*matrizAB_norm
```

```
array([[ 0.          , 0.10526316],  
       [ 0.10526316, 3.78947368],  
       [ 0.31578947, 6.94736842],  
       [ 0.63157895, 11.05263158],  
       [ 1.05263158, 18.        ],  
       [ 1.57894737, 12.63157895],  
       [ 2.21052632, 4.73684211],  
       [ 2.94736842, 1.05263158],  
       [ 3.78947368, 0.        ],  
       [ 4.73684211, 1.57894737],  
       [ 5.78947368, 0.63157895],  
       [ 6.94736842, 8.21052632],  
       [ 8.21052632, 0.31578947],  
       [ 9.57894737, 5.78947368],  
       [11.05263158, 20.        ],  
       [12.63157895, 9.57894737],  
       [14.31578947, 14.31578947],  
       [16.10526316, 2.21052632],  
       [18.          , 16.10526316],  
       [20.          , 2.94736842]])
```

- Operação dot

```
1 matrizAB.dot(np.transpose(matrizAB_norm))
```

```
5.68421053, 13.57894737, 5.47368421, 12.52631579, 20.42105263,  
15.68421053, 18.52631579, 10.42105263, 20.          , 11.89473684],  
[ 0.52631579, 4.57894737, 6.52631579, 8.47368421, 10.94736842,  
9.73684211, 6.94736842, 4.68421053, 2.94736842, 5.94736842,  
5.26315789, 10.36842105, 5.47368421, 10.05263158, 15.15789474,  
12.36842105, 14.31578947, 9.42105263, 15.57894737, 10.68421053],  
[ 0.26315789, 2.52631579, 3.73684211, 4.94736842, 6.42105263,  
6.05263158, 4.89473684, 4.          , 3.36842105, 5.10526316,  
5.          , 7.78947368, 5.57894737, 8.10526316, 10.89473684,  
9.73684211, 10.94736842, 8.73684211, 12.05263158, 9.84210526],  
[ 0.05263158, 0.89473684, 1.52631579, 2.15789474, 2.84210526,  
3.15789474, 3.31578947, 3.52631579, 3.78947368, 4.52631579,  
4.89473684, 5.84210526, 5.78947368, 6.68421053, 7.63157895,  
7.78947368, 8.42105263, 8.36842105, 9.42105263, 9.36842105],  
[ 0.31578947, 0.85263158, 4.52631579, 6.          , 7.78947368,  
7.36842105, 6.          , 4.94736842, 4.21052632, 6.31578947,  
6.21052632, 9.57894737, 6.94736842, 10.          , 13.36842105,  
12.          , 13.47368421, 10.84210526, 14.84210526, 12.21052632],  
[ 0.21052632, 2.26315789, 3.47368421, 4.68421053, 6.10526316,  
6.05263158, 5.36842105, 4.89473684, 4.63157895, 6.26315789,  
6.42105263, 8.89473684, 7.36842105, 9.63157895, 12.10526316,  
11.42105263, 12.63157895, 11.10526316, 14.          , 12.47368421],  
[ 0.68421053, 6.10526316, 8.78947368, 11.47368421, 14.84210526,  
13.42105263, 9.94736842, 7.15789474, 5.05263158, 9.10526316,
```

```
[ 0.20042105,  0.07420042,  0.9420042,  0. ,  10.42105205,  
10.26315789,  9. ,  8.10526316,  7.57894737,  10.36842105,  
10.57894737,  14.84210526,  12.10526316,  16. ,  20.26315789,  
19. ,  21.05263158,  18.31578947,  23.31578947,  20.57894737],  
[ 0.94736842,  8.57894737,  12.42105263,  16.26315789,  21.05263158,  
19.21052632,  14.52631579,  10.78947368,  8. ,  13.73684211,  
12.84210526,  22.36842105,  13.89473684,  22.47368421,  32.  
,  
27.31578947,  31.15789474,  22.68421053,  34.10526316,  25.63157895],  
[ 0.42105263,  4.42105263,  6.73684211,  9.05263158,  11.78947368,  
11.57894737,  10.10526316,  9.05263158,  8.42105263,  11.57894737,  
11.78947368,  16.63157895,  13.47368421,  17.89473684,  22.73684211,  
21.26315789 ,  23.57894737  20.42105263  26.10526316  22.9473684211]
```

```
1 np.transpose(matrizAB).dot(matrizAB_norm)
```

```
array([[140. , 111.05263158],  
[111.05263158, 140. ]])
```

```
1
```