

betaDelta: Methods

Ivan Jacob Agaloos Pesigan

1 Multivariate Normal-Theory Approach

```
object <- lm(QUALITY ~ NARTIC + PCTGRT + PCTSUPP, data = nas1982)
```

```
out <- BetaDelta(object, type = "mvn")
str(out)

#> List of 8
#> $ call      : language BetaDelta(object = object, type = "mvn")
#> $ lm        :List of 12
#> ..$ coefficients : Named num [1:4] 10.3592 0.0842 0.216 0.1126
#> .. ..- attr(*, "names")= chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ residuals    : Named num [1:46] -3.068 -0.688 2.675 2.052 4.039 ...
#> .. ..- attr(*, "names")= chr [1:46] "1" "2" "3" "4" ...
#> ..$ effects      : Named num [1:46] -187.4 51.49 27.59 -16.11 4.51 ...
#> .. ..- attr(*, "names")= chr [1:46] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP" ...
#> ..$ rank         : int 4
#> ..$ fitted.values: Named num [1:46] 15.1 23.7 26.3 33.9 40 ...
#> .. ..- attr(*, "names")= chr [1:46] "1" "2" "3" "4" ...
#> ..$ assign       : int [1:4] 0 1 2 3
#> ..$ qr           :List of 5
#> .. ..$ qr        : num [1:46, 1:4] -6.782 0.147 0.147 0.147 0.147 ...
#> .. .. ..- attr(*, "dimnames")=List of 2
#> .. .. ..$ : chr [1:46] "1" "2" "3" "4" ...
#> .. .. ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> .. .. ..- attr(*, "assign")= int [1:4] 0 1 2 3
#> .. ..$ qraux: num [1:4] 1.15 1.04 1.06 1.09
#> .. ..$ pivot: int [1:4] 1 2 3 4
#> .. ..$ tol   : num 1e-07
#> .. ..$ rank  : int 4
#> .. ..- attr(*, "class")= chr "qr"
#> ..$ df.residual : int 42
#> ..$ xlevels     : Named list()
#> ..$ call        : language lm(formula = QUALITY ~ NARTIC + PCTGRT + PCTSUPP, data = nas1982)
#> ..$ terms       :Classes 'terms', 'formula' language QUALITY ~ NARTIC + PCTGRT + PCTSUPP
```

```

#> .. ..- attr(*, "variables")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
#> .. ..- attr(*, "factors")= int [1:4, 1:3] 0 1 0 0 0 0 1 0 0 0 ...
#> .. ..- attr(*, "dimnames")=List of 2
#> .. ..$ : chr [1:4] "QUALITY" "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..- attr(*, "term.labels")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..- attr(*, "order")= int [1:3] 1 1 1
#> .. ..- attr(*, "intercept")= int 1
#> .. ..- attr(*, "response")= int 1
#> .. ..- attr(*, ".Environment")=<environment: 0x560bc2dae260>
#> .. ..- attr(*, "predvars")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
#> .. ..- attr(*, "dataClasses")= Named chr [1:4] "numeric" "numeric" "numeric" "numeric"
#> .. ..- attr(*, "names")= chr [1:4] "QUALITY" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ model : 'data.frame': 46 obs. of 4 variables:
#> ..$ QUALITY: int [1:46] 12 23 29 36 44 21 40 42 24 30 ...
#> ..$ NARTIC : int [1:46] 14 61 68 49 130 65 79 187 32 50 ...
#> ..$ PCTGRT : int [1:46] 8 3 13 63 53 29 35 40 19 8 ...
#> ..$ PCTSUPP: int [1:46] 16 67 66 52 64 59 81 65 87 43 ...
#> ..- attr(*, "terms")=Classes 'terms', 'formula' language QUALITY ~ NARTIC + PCTGRT + PCTSUPP
#> .. ..- attr(*, "variables")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
#> .. ..- attr(*, "factors")= int [1:4, 1:3] 0 1 0 0 0 0 1 0 0 0 ...
#> .. ..- attr(*, "dimnames")=List of 2
#> .. ..$ : chr [1:4] "QUALITY" "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..- attr(*, "term.labels")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..- attr(*, "order")= int [1:3] 1 1 1
#> .. ..- attr(*, "intercept")= int 1
#> .. ..- attr(*, "response")= int 1
#> .. ..- attr(*, ".Environment")=<environment: 0x560bc2dae260>
#> .. ..- attr(*, "predvars")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
#> .. ..- attr(*, "dataClasses")= Named chr [1:4] "numeric" "numeric" "numeric" "numeric"
#> .. ..- attr(*, "names")= chr [1:4] "QUALITY" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..- attr(*, "class")= chr "lm"
#> $ lm_process:List of 19
#> ..$ x : num [1:46, 1:4] 12 23 29 36 44 21 40 42 24 30 ...
#> .. ..- attr(*, "dimnames")=List of 2
#> .. ..$ : chr [1:46] "1" "2" "3" "4" ...
#> .. ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..- attr(*, "assign")= int [1:4] 0 1 2 3
#> ..$ dims : int [1:2] 46 4
#> ..$ n : int 46
#> ..$ k : int 4
#> ..$ p : num 3
#> ..$ q : num 10
#> ..$ df : int 42

```

```

#> ..$ pinv_of_dcap          : num [1:10, 1:16] 1 0 0 0 0 0 0 0 0 0 ...
#> ..$ varnames              : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ xnames                 : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ sigmacap               : num [1:4, 1:4] 101 455 129 138 455 ...
#> ..$- attr(*, "dimnames")=List of 2
#> ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ vechsigmacap           : num [1:10] 101 455 129 138 3507 ...
#> ..$ sigma                  : Named num [1:4] 10.1 59.2 18.3 23.5
#> ..$- attr(*, "names")= chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ sigmacap_consistent    : num [1:4, 1:4] 99.2 444.7 125.9 135 444.7 ...
#> ..$- attr(*, "dimnames")=List of 2
#> ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ vechsigmacap_consistent: num [1:10] 99.2 444.7 125.9 135 3430.9 ...
#> ..$ rhocap                  : num [1:4, 1:4] 1 0.762 0.7 0.582 0.762 ...
#> ..$- attr(*, "dimnames")=List of 2
#> ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ betastar                : Named num [1:3] 0.495 0.391 0.263
#> ..$- attr(*, "names")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ beta                    : Named num [1:3] 0.0842 0.216 0.1126
#> ..$- attr(*, "names")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ theta                   : Named num [1:10] 8.42e-02 2.16e-01 1.13e-01 2.12e+01 3.51e+03 ...
#> ..$- attr(*, "names")= chr [1:10] "NARTIC" "PCTGRT" "PCTSUPP" "" ...
#> $ type                      : chr "mvn"
#> $ gamma                     : num [1:10, 1:10] 20579 92227 26100 28001 413321 ...
#> $ est                        : Named num [1:3] 0.495 0.391 0.263
#> ..$- attr(*, "names")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> $ vcov                       : num [1:3, 1:3] 0.00575 -0.00336 -0.00217 -0.00336 0.00593 ...
#> ..$- attr(*, "dimnames")=List of 2
#> ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> $ acov                       : num [1:3, 1:3] 0.2647 -0.1546 -0.0996 -0.1546 0.2729 ...
#> ..$- attr(*, "dimnames")=List of 2
#> ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> - attr(*, "class")= chr [1:2] "betadelta" "list"

BetaDelta(object, type = "mvn")

#> Call:
#> BetaDelta(object = object, type = "mvn")
#>
#> Standardized regression slopes with MVN standard errors:
#>      est      se      t      p  0.05%  0.5%  2.5%  97.5%  99.5%  99.95%

```

```
#> NARTIC  0.4951 0.0759 6.5272 0.000  0.2268 0.2905 0.3421 0.6482 0.6998 0.7635
#> PCTGRT  0.3915 0.0770 5.0824 0.000  0.1190 0.1837 0.2360 0.5469 0.5993 0.6640
#> PCTSUPP 0.2632 0.0747 3.5224 0.001 -0.0011 0.0616 0.1124 0.4141 0.4649 0.5276
```

print

```
print(out)

#> Call:
#> BetaDelta(object = object, type = "mvn")
#>
#> Standardized regression slopes with MVN standard errors:
#>           est      se      t      p  0.05%  0.5%  2.5%  97.5%  99.5% 99.95%
#> NARTIC  0.4951 0.0759 6.5272 0.000  0.2268 0.2905 0.3421 0.6482 0.6998 0.7635
#> PCTGRT  0.3915 0.0770 5.0824 0.000  0.1190 0.1837 0.2360 0.5469 0.5993 0.6640
#> PCTSUPP 0.2632 0.0747 3.5224 0.001 -0.0011 0.0616 0.1124 0.4141 0.4649 0.5276
```

coef

```
coef(out)

#>      NARTIC      PCTGRT      PCTSUPP
#> 0.4951451 0.3914887 0.2632477
```

vcov

```
vcov(out)

#>           NARTIC           PCTGRT           PCTSUPP
#> NARTIC  0.005754524 -0.003360334 -0.002166127
#> PCTGRT -0.003360334  0.005933462 -0.001769723
#> PCTSUPP -0.002166127 -0.001769723  0.005585256
```

confint

```
confint(out, level = 0.95)

#>           2.5%           97.5%
#> NARTIC  0.3420563 0.6482339
#> PCTGRT  0.2360380 0.5469395
#> PCTSUPP 0.1124272 0.4140682
```

summary

```
summary(out)

#> Call:
#> BetaDelta(object = object, type = "mvn")
#>
#> Standardized regression slopes with MVN standard errors:
#>      est      se      t      p  0.05%  0.5%  2.5%  97.5%  99.5% 99.95%
#> NARTIC  0.4951 0.0759 6.5272 0.000  0.2268 0.2905 0.3421 0.6482 0.6998 0.7635
#> PCTGRT  0.3915 0.0770 5.0824 0.000  0.1190 0.1837 0.2360 0.5469 0.5993 0.6640
#> PCTSUPP 0.2632 0.0747 3.5224 0.001 -0.0011 0.0616 0.1124 0.4141 0.4649 0.5276
```

2 Asymptotic Distribution-Free Approach

```
object <- lm(QUALITY ~ NARTIC + PCTGRT + PCTSUPP, data = nas1982)
```

```
out <- BetaDelta(object, type = "adf")
str(out)

#> List of 8
#> $ call      : language BetaDelta(object = object, type = "adf")
#> $ lm        :List of 12
#> ..$ coefficients : Named num [1:4] 10.3592 0.0842 0.216 0.1126
#> .. ..- attr(*, "names")= chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ residuals    : Named num [1:46] -3.068 -0.688 2.675 2.052 4.039 ...
#> .. ..- attr(*, "names")= chr [1:46] "1" "2" "3" "4" ...
#> ..$ effects      : Named num [1:46] -187.4 51.49 27.59 -16.11 4.51 ...
#> .. ..- attr(*, "names")= chr [1:46] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP" ...
#> ..$ rank         : int 4
#> ..$ fitted.values: Named num [1:46] 15.1 23.7 26.3 33.9 40 ...
#> .. ..- attr(*, "names")= chr [1:46] "1" "2" "3" "4" ...
#> ..$ assign       : int [1:4] 0 1 2 3
#> ..$ qr           :List of 5
#> .. ..$ qr        : num [1:46, 1:4] -6.782 0.147 0.147 0.147 0.147 ...
#> .. .. ..- attr(*, "dimnames")=List of 2
#> .. .. ..$ : chr [1:46] "1" "2" "3" "4" ...
#> .. .. ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> .. .. ..- attr(*, "assign")= int [1:4] 0 1 2 3
#> .. ..$ qraux: num [1:4] 1.15 1.04 1.06 1.09
#> .. ..$ pivot: int [1:4] 1 2 3 4
#> .. ..$ tol   : num 1e-07
#> .. ..$ rank  : int 4
```

```

#> ..- attr(*, "class")= chr "qr"
#> ..$ df.residual : int 42
#> ..$ xlevels : Named list()
#> ..$ call : language lm(formula = QUALITY ~ NARTIC + PCTGRT + PCTSUPP, data = nas1982)
#> ..$ terms :Classes 'terms', 'formula' language QUALITY ~ NARTIC + PCTGRT + PCTSUPP
#> ..- attr(*, "variables")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
#> ..- attr(*, "factors")= int [1:4, 1:3] 0 1 0 0 0 0 1 0 0 0 ...
#> ..- attr(*, "dimnames")=List of 2
#> ..$ : chr [1:4] "QUALITY" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..- attr(*, "term.labels")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..- attr(*, "order")= int [1:3] 1 1 1
#> ..- attr(*, "intercept")= int 1
#> ..- attr(*, "response")= int 1
#> ..- attr(*, ".Environment")=<environment: 0x560bc2dae260>
#> ..- attr(*, "predvars")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
#> ..- attr(*, "dataClasses")= Named chr [1:4] "numeric" "numeric" "numeric" "numeric"
#> ..- attr(*, "names")= chr [1:4] "QUALITY" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ model :'data.frame': 46 obs. of 4 variables:
#> ..$ QUALITY: int [1:46] 12 23 29 36 44 21 40 42 24 30 ...
#> ..$ NARTIC : int [1:46] 14 61 68 49 130 65 79 187 32 50 ...
#> ..$ PCTGRT : int [1:46] 8 3 13 63 53 29 35 40 19 8 ...
#> ..$ PCTSUPP: int [1:46] 16 67 66 52 64 59 81 65 87 43 ...
#> ..- attr(*, "terms")=Classes 'terms', 'formula' language QUALITY ~ NARTIC + PCTGRT + PCTSUPP
#> ..- attr(*, "variables")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
#> ..- attr(*, "factors")= int [1:4, 1:3] 0 1 0 0 0 0 1 0 0 0 ...
#> ..- attr(*, "dimnames")=List of 2
#> ..$ : chr [1:4] "QUALITY" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..- attr(*, "term.labels")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..- attr(*, "order")= int [1:3] 1 1 1
#> ..- attr(*, "intercept")= int 1
#> ..- attr(*, "response")= int 1
#> ..- attr(*, ".Environment")=<environment: 0x560bc2dae260>
#> ..- attr(*, "predvars")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
#> ..- attr(*, "dataClasses")= Named chr [1:4] "numeric" "numeric" "numeric" "numeric"
#> ..- attr(*, "names")= chr [1:4] "QUALITY" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..- attr(*, "class")= chr "lm"
#> $ lm_process:List of 19
#> ..$ x : num [1:46, 1:4] 12 23 29 36 44 21 40 42 24 30 ...
#> ..- attr(*, "dimnames")=List of 2
#> ..$ : chr [1:46] "1" "2" "3" "4" ...
#> ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..- attr(*, "assign")= int [1:4] 0 1 2 3
#> ..$ dims : int [1:2] 46 4

```

```

#> ..$ n : int 46
#> ..$ k : int 4
#> ..$ p : num 3
#> ..$ q : num 10
#> ..$ df : int 42
#> ..$ pinv_of_dcap : num [1:10, 1:16] 1 0 0 0 0 0 0 0 0 0 ...
#> ..$ varnames : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ xnames : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ sigmacap : num [1:4, 1:4] 101 455 129 138 455 ...
#> ..- attr(*, "dimnames")=List of 2
#> .. ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ vechsigmacap : num [1:10] 101 455 129 138 3507 ...
#> ..$ sigma : Named num [1:4] 10.1 59.2 18.3 23.5
#> ..- attr(*, "names")= chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ sigmacap_consistent : num [1:4, 1:4] 99.2 444.7 125.9 135 444.7 ...
#> ..- attr(*, "dimnames")=List of 2
#> .. ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ vechsigmacap_consistent: num [1:10] 99.2 444.7 125.9 135 3430.9 ...
#> ..$ rhocap : num [1:4, 1:4] 1 0.762 0.7 0.582 0.762 ...
#> ..- attr(*, "dimnames")=List of 2
#> .. ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ betastar : Named num [1:3] 0.495 0.391 0.263
#> ..- attr(*, "names")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ beta : Named num [1:3] 0.0842 0.216 0.1126
#> ..- attr(*, "names")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> ..$ theta : Named num [1:10] 8.42e-02 2.16e-01 1.13e-01 2.12e+01 3.51e+03 ...
#> ..- attr(*, "names")= chr [1:10] "NARTIC" "PCTGRT" "PCTSUPP" "" ...
#> $ type : chr "adf"
#> $ gamma : num [1:10, 1:10] 13334 65359 17987 19780 336344 ...
#> $ est : Named num [1:3] 0.495 0.391 0.263
#> ..- attr(*, "names")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> $ vcov : num [1:3, 1:3] 0.00454 -0.00255 -0.00174 -0.00255 0.00504 ...
#> ..- attr(*, "dimnames")=List of 2
#> .. ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> $ acov : num [1:3, 1:3] 0.2088 -0.1174 -0.0802 -0.1174 0.2317 ...
#> ..- attr(*, "dimnames")=List of 2
#> .. ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> - attr(*, "class")= chr [1:2] "betadelta" "list"

BetaDelta(object, type = "adf")

#> Call:

```

```
#> BetaDelta(object = object, type = "adf")
#>
#> Standardized regression slopes with ADF standard errors:
#>      est      se      t      p  0.05%  0.5%  2.5%  97.5%  99.5% 99.95%
#> NARTIC  0.4951 0.0674 7.3490 0.0000  0.2568 0.3134 0.3592 0.6311 0.6769 0.7335
#> PCTGRT  0.3915 0.0710 5.5164 0.0000  0.1404 0.2000 0.2483 0.5347 0.5830 0.6426
#> PCTSUPP 0.2632 0.0769 3.4231 0.0014 -0.0088 0.0558 0.1081 0.4184 0.4707 0.5353
```

print

```
print(out)

#> Call:
#> BetaDelta(object = object, type = "adf")
#>
#> Standardized regression slopes with ADF standard errors:
#>      est      se      t      p  0.05%  0.5%  2.5%  97.5%  99.5% 99.95%
#> NARTIC  0.4951 0.0674 7.3490 0.0000  0.2568 0.3134 0.3592 0.6311 0.6769 0.7335
#> PCTGRT  0.3915 0.0710 5.5164 0.0000  0.1404 0.2000 0.2483 0.5347 0.5830 0.6426
#> PCTSUPP 0.2632 0.0769 3.4231 0.0014 -0.0088 0.0558 0.1081 0.4184 0.4707 0.5353
```

coef

```
coef(out)

#>      NARTIC      PCTGRT      PCTSUPP
#> 0.4951451 0.3914887 0.2632477
```

vcov

```
vcov(out)

#>      NARTIC      PCTGRT      PCTSUPP
#> NARTIC  0.004539472 -0.002552698 -0.001742698
#> PCTGRT -0.002552698  0.005036538 -0.001906216
#> PCTSUPP -0.001742698 -0.001906216  0.005914088
```

confint


```

confint(out, level = 0.95)

#>           2.5%      97.5%
#> NARTIC  0.3591757 0.6311146
#> PCTGRT  0.2482683 0.5347091
#> PCTSUPP 0.1080509 0.4184444

```

summary

```

summary(out)

#> Call:
#> BetaDelta(object = object, type = "adf")
#>
#> Standardized regression slopes with ADF standard errors:
#>      est      se      t      p  0.05%  0.5%  2.5%  97.5%  99.5% 99.95%
#> NARTIC  0.4951 0.0674 7.3490 0.0000  0.2568 0.3134 0.3592 0.6311 0.6769 0.7335
#> PCTGRT  0.3915 0.0710 5.5164 0.0000  0.1404 0.2000 0.2483 0.5347 0.5830 0.6426
#> PCTSUPP 0.2632 0.0769 3.4231 0.0014 -0.0088 0.0558 0.1081 0.4184 0.4707 0.5353

```

References

- Jones, J. A., & Waller, N. G. (2015). The normal-theory and asymptotic distribution-free (ADF) covariance matrix of standardized regression coefficients: Theoretical extensions and finite sample behavior. *Psychometrika*, 80(2), 365–378. <https://doi.org/10.1007/s11336-013-9380-y>
- R Core Team. (2022). *R: A language and environment for statistical computing*. R Foundation for Statistical Computing. Vienna, Austria. <https://www.R-project.org/>
- Yuan, K.-H., & Chan, W. (2011). Biases and standard errors of standardized regression coefficients. *Psychometrika*, 76(4), 670–690. <https://doi.org/10.1007/s11336-011-9224-6>