## betaDelta: Staging

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## 1 Standardized Slopes

```
df <- nas1982
object <- lm(QUALITY ~ NARTIC + PCTGRT + PCTSUPP, data = df)
mvn <- BetaDelta(object, type = "mvn")</pre>
adf <- BetaDelta(object, type = "adf")</pre>
summary(mvn)
#>
                              t df
                                           0.05%
                                                    0.5%
                                                           2.5% 97.5% 99.5%
              est
                      se
                                       р
#> NARTIC 0.4951 0.0759 6.5272 42 0.000 0.2268 0.2905 0.3421 0.6482 0.6998
#> PCTGRT 0.3915 0.0770 5.0824 42 0.000 0.1190 0.1837 0.2360 0.5469 0.5993
#> PCTSUPP 0.2632 0.0747 3.5224 42 0.001 -0.0011 0.0616 0.1124 0.4141 0.4649
#>
           99.95%
#> NARTIC 0.7635
#> PCTGRT 0.6640
#> PCTSUPP 0.5276
summary(adf)
                              t df
                                            0.05%
                                                     0.5%
                                                            2.5% 97.5% 99.5%
              est
                      se
                                        р
#> NARTIC 0.4951 0.0674 7.3490 42 0.0000 0.2568 0.3134 0.3592 0.6311 0.6769
#> PCTGRT 0.3915 0.0710 5.5164 42 0.0000 0.1404 0.2000 0.2483 0.5347 0.5830
#> PCTSUPP 0.2632 0.0769 3.4231 42 0.0014 -0.0088 0.0558 0.1081 0.4184 0.4707
           99.95%
#> NARTIC 0.7335
#> PCTGRT 0.6426
#> PCTSUPP 0.5353
coef(mvn)
      NARTIC
                PCTGRT
                         PCTSUPP
#> 0.4951451 0.3914887 0.2632477
coef(adf)
      NARTIC
                PCTGRT
                         PCTSUPP
#> 0.4951451 0.3914887 0.2632477
```

```
vcov(mvn)
                NARTIC
                             PCTGRT
#>
                                         PCTSUPP
#> NARTIC 0.005754524 -0.003360334 -0.002166127
#> PCTGRT -0.003360334 0.005933462 -0.001769723
#> PCTSUPP -0.002166127 -0.001769723 0.005585256
vcov(adf)
#>
                NARTIC
                             PCTGRT
                                         PCTSUPP
#> NARTIC 0.004539472 -0.002552698 -0.001742698
#> PCTGRT -0.002552698 0.005036538 -0.001906216
#> PCTSUPP -0.001742698 -0.001906216 0.005914088
confint(mvn)
              2.5 % 97.5 %
#> NARTIC 0.3420563 0.6482339
#> PCTGRT 0.2360380 0.5469395
#> PCTSUPP 0.1124272 0.4140682
confint(adf)
              2.5 % 97.5 %
#> NARTIC 0.3591757 0.6311146
#> PCTGRT 0.2482683 0.5347091
#> PCTSUPP 0.1080509 0.4184444
```

## 2 Differences of Standardized Slopes

```
df <- nas1982
object <- lm(QUALITY ~ NARTIC + PCTGRT + PCTSUPP, data = df)
std_mvn <- BetaDelta(object, type = "mvn")</pre>
std_adf <- BetaDelta(object, type = "adf")</pre>
mvn <- DiffBetaDelta(std_mvn)</pre>
adf <- DiffBetaDelta(std_adf)</pre>
summary(mvn)
                                    z p 0.05% 0.5% 2.5% 97.5%
#>
                     est
                             se
#> NARTIC-PCTGRT 0.1037 0.1357 0.7640 0.4449 -0.3428 -0.2458 -0.1623 0.3696
#> NARTIC-PCTSUPP 0.2319 0.1252 1.8524 0.0640 -0.1800 -0.0906 -0.0135 0.4773
#> PCTGRT-PCTSUPP 0.1282 0.1227 1.0451 0.2960 -0.2755 -0.1878 -0.1123 0.3688
#>
                   99.5% 99.95%
#> NARTIC-PCTGRT 0.4531 0.5501
#> NARTIC-PCTSUPP 0.5544 0.6438
```

```
#> PCTGRT-PCTSUPP 0.4443 0.5320
summary(adf)
                         se z p 0.05% 0.5% 2.5% 97.5%
                   est
#> NARTIC-PCTGRT 0.1037 0.1212 0.8555 0.3923 -0.2950 -0.2084 -0.1338 0.3411
#> NARTIC-PCTSUPP 0.2319 0.1181 1.9642 0.0495 -0.1566 -0.0722 0.0005 0.4633
#> PCTGRT-PCTSUPP 0.1282 0.1215 1.0555 0.2912 -0.2716 -0.1847 -0.1099 0.3664
                99.5% 99.95%
#>
#> NARTIC-PCTGRT 0.4158 0.5024
#> NARTIC-PCTSUPP 0.5360 0.6204
#> PCTGRT-PCTSUPP 0.4412 0.5281
coef(mvn)
#> NARTIC-PCTGRT NARTIC-PCTSUPP PCTGRT-PCTSUPP
#> 0.1036564 0.2318974 0.1282410
coef(adf)
#> NARTIC-PCTGRT NARTIC-PCTSUPP PCTGRT-PCTSUPP
#> 0.1036564 0.2318974 0.1282410
vcov(mvn)
               NARTIC-PCTGRT NARTIC-PCTSUPP PCTGRT-PCTSUPP
#> NARTIC-PCTGRT 0.018408653 0.009511262 -0.008897391
#> NARTIC-PCTSUPP 0.009511262 0.015672035 0.006160773
#> PCTGRT-PCTSUPP -0.008897391 0.006160773 0.015058164
vcov(adf)
               NARTIC-PCTGRT NARTIC-PCTSUPP PCTGRT-PCTSUPP
#> NARTIC-PCTGRT 0.014681407 0.006928651 -0.007752755
#> NARTIC-PCTSUPP 0.006928651 0.013938955 0.007010303
#> PCTGRT-PCTSUPP -0.007752755 0.007010303 0.014763058
confint(mvn)
                     2.5 % 97.5 %
#> NARTIC-PCTGRT -0.16226855 0.3695814
#> NARTIC-PCTSUPP -0.01346652 0.4772614
#> PCTGRT-PCTSUPP -0.11226950 0.3687516
confint(adf)
                        2.5 % 97.5 %
#> NARTIC-PCTGRT -0.1338262589 0.3411391
#> NARTIC-PCTSUPP 0.0004975295 0.4632974
#> PCTGRT-PCTSUPP -0.1099011119 0.3663832
```