betaSandwich: Methods

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1 HC

```
object <- lm(QUALITY ~ NARTIC + PCTGRT + PCTSUPP, data = nas1982)
```

```
out <- BetaHC(object, type = "hc3")
str(out)
#> List of 8
#> $ call: language BetaHC(object = object, type = "hc3")
#> $ lm :List of 12
    ..$ coefficients : Named num [1:4] 10.3592 0.0842 0.216 0.1126
   ...- attr(*, "names")= chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
    ..$ residuals : Named num [1:46] -3.068 -0.688 2.675 2.052 4.039 ...
#>
    ....- attr(*, "names")= chr [1:46] "1" "2" "3" "4" ...
#>
    ..$ effects
                   : Named num [1:46] -187.4 51.49 27.59 -16.11 4.51 ...
    ... - attr(*, "names")= chr [1:46] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP" ...
#>
    ..$ rank
                   : int 4
    ..$ fitted.values: Named num [1:46] 15.1 23.7 26.3 33.9 40 ...
    ....- attr(*, "names")= chr [1:46] "1" "2" "3" "4" ...
                   : int [1:4] 0 1 2 3
    ..$ assign
#>
                    :List of 5
    ..$ qr
    ....$ qr : num [1:46, 1:4] -6.782 0.147 0.147 0.147 0.147 ...
    ..... attr(*, "dimnames")=List of 2
    .....$: chr [1:46] "1" "2" "3" "4" ...
    .....$ : chr [1:4] "(Intercept)" "NARTIC" "PCTGRT" "PCTSUPP"
#>
    ..... attr(*, "assign")= int [1:4] 0 1 2 3
    ....$ qraux: num [1:4] 1.15 1.04 1.06 1.09
#>
    ....$ pivot: int [1:4] 1 2 3 4
    ....$ tol : num 1e-07
#>
    .. ..$ rank : int 4
    .. ..- attr(*, "class")= chr "qr"
    ..$ df.residual : int 42
    ..$ xlevels : Named list()
#>
                   : language lm(formula = QUALITY ~ NARTIC + PCTGRT + PCTSUPP, data = nas1982)
#>
    ..$ call
                   :Classes 'terms', 'formula' language QUALITY ~ NARTIC + PCTGRT + PCTSUPP
    ..$ terms
```

```
....- attr(*, "variables")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
   .... attr(*, "factors")= int [1:4, 1:3] 0 1 0 0 0 0 1 0 0 0 ...
    ..... attr(*, "dimnames")=List of 2
    ..... s: chr [1:4] "QUALITY" "NARTIC" "PCTGRT" "PCTSUPP"
#>
#>
    ..... : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
    ..... attr(*, "term.labels")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
    ..... attr(*, "order")= int [1:3] 1 1 1
#>
    .. .. ..- attr(*, "intercept")= int 1
    .. .. - attr(*, "response")= int 1
    ..... attr(*, ".Environment")=<environment: 0x560054d50d70>
    .... attr(*, "predvars")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
#>
    ..... attr(*, "dataClasses")= Named chr [1:4] "numeric" "numeric" "numeric" "numeric"
    ..... attr(*, "names")= chr [1:4] "QUALITY" "NARTIC" "PCTGRT" "PCTSUPP"
    ..$ model
                   :'data.frame': 46 obs. of 4 variables:
#>
    ....$ QUALITY: int [1:46] 12 23 29 36 44 21 40 42 24 30 ...
    .. ..$ NARTIC : int [1:46] 14 61 68 49 130 65 79 187 32 50 ...
    ....$ PCTGRT : int [1:46] 8 3 13 63 53 29 35 40 19 8 ...
    ....$ PCTSUPP: int [1:46] 16 67 66 52 64 59 81 65 87 43 ...
    ...- attr(*, "terms")=Classes 'terms', 'formula' language QUALITY ~ NARTIC + PCTGRT + PCTSUI
#>
#>
    ..... attr(*, "variables")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
    ..... attr(*, "factors")= int [1:4, 1:3] 0 1 0 0 0 0 1 0 0 0 ...
#>
    ..... attr(*, "dimnames")=List of 2
#>
    ..... : chr [1:4] "QUALITY" "NARTIC" "PCTGRT" "PCTSUPP"
#>
    ..... : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
    ..... attr(*, "term.labels")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
    .. .. .. - attr(*, "order")= int [1:3] 1 1 1
#>
    ..... attr(*, "intercept")= int 1
#>
    .. .. .. - attr(*, "response")= int 1
#>
   ..... attr(*, ".Environment")=<environment: 0x560054d50d70>
    ..... attr(*, "predvars")= language list(QUALITY, NARTIC, PCTGRT, PCTSUPP)
#>
   ..... attr(*, "dataClasses")= Named chr [1:4] "numeric" "numeric" "numeric" "numeric"
   ..- attr(*, "class")= chr "lm"
#> $ type: chr "hc3"
#> $ beta: Named num [1:3] 0.495 0.391 0.263
#> ..- attr(*, "names")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> $ vcov: num [1:3, 1:3] 0.00617 -0.0036 -0.00194 -0.0036 0.0067 ...
#>
   ..- attr(*, "dimnames")=List of 2
   ....$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
   ....$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> $ n : int 46
#> $ p : num 3
#> $ df : int 42
#> - attr(*, "class")= chr [1:2] "betasandwich" "list"
BetaHC(object, type = "hc3")
```

```
#> Call:
#> BetaHC(object = object, type = "hc3")
#>

#> Standardized regression slopes with HC3 standard errors:
#> est se t p 0.05% 0.5% 2.5% 97.5% 99.5% 99.95%
#> NARTIC 0.4951 0.0786 6.3025 0.0000 0.2172 0.2832 0.3366 0.6537 0.7071 0.7731
#> PCTGRT 0.3915 0.0818 4.7831 0.0000 0.1019 0.1707 0.2263 0.5567 0.6123 0.6810
#> PCTSUPP 0.2632 0.0855 3.0786 0.0037 -0.0393 0.0325 0.0907 0.4358 0.4940 0.5658
```

print

```
print(out)

#> Call:
#> BetaHC(object = object, type = "hc3")
#>

#> Standardized regression slopes with HC3 standard errors:
#> est se t p 0.05% 0.5% 2.5% 97.5% 99.5% 99.95%
#> NARTIC 0.4951 0.0786 6.3025 0.0000 0.2172 0.2832 0.3366 0.6537 0.7071 0.7731
#> PCTGRT 0.3915 0.0818 4.7831 0.0000 0.1019 0.1707 0.2263 0.5567 0.6123 0.6810
#> PCTSUPP 0.2632 0.0855 3.0786 0.0037 -0.0393 0.0325 0.0907 0.4358 0.4940 0.5658
```

coef

```
coef(out)
#> NARTIC PCTGRT PCTSUPP
#> 0.4951451 0.3914887 0.2632477
```

vcov

```
vcov(out)

#> NARTIC PCTGRT PCTSUPP

#> NARTIC 0.006172168 -0.003602529 -0.001943469

#> PCTGRT -0.003602529 0.006699155 -0.002443584

#> PCTSUPP -0.001943469 -0.002443584 0.007311625
```

confint

summary

```
summary(out)

#> Call:
#> BetaHC(object = object, type = "hc3")

#>

#> Standardized regression slopes with HC3 standard errors:
#> est se t p 0.05% 0.5% 2.5% 97.5% 99.5% 99.95%

#> NARTIC 0.4951 0.0786 6.3025 0.0000 0.2172 0.2832 0.3366 0.6537 0.7071 0.7731

#> PCTGRT 0.3915 0.0818 4.7831 0.0000 0.1019 0.1707 0.2263 0.5567 0.6123 0.6810
#> PCTSUPP 0.2632 0.0855 3.0786 0.0037 -0.0393 0.0325 0.0907 0.4358 0.4940 0.5658
```

2 Multivariate Normal

```
object <- lm(rating ~ ., data = attitude)
```

```
out <- BetaN(object)</pre>
str(out)
#> List of 8
#> $ call: language BetaN(object = object)
#> $ lm :List of 12
   ..$ coefficients : Named num [1:7] 10.7871 0.6132 -0.0731 0.3203 0.0817 ...
   ...- attr(*, "names")= chr [1:7] "(Intercept)" "complaints" "privileges" "learning" ...
   ..$ residuals : Named num [1:30] -8.11 1.647 1.061 -0.227 6.546 ...
   ....- attr(*, "names")= chr [1:30] "1" "2" "3" "4" ...
                   : Named num [1:30] -354.011 54.107 2.742 11.715 -0.971 ...
#>
    ..$ effects
    ...- attr(*, "names")= chr [1:30] "(Intercept)" "complaints" "privileges" "learning" ...
   ..$ rank : int 7
    ..$ fitted.values: Named num [1:30] 51.1 61.4 69.9 61.2 74.5 ...
    ... - attr(*, "names")= chr [1:30] "1" "2" "3" "4" ...
   ..$ assign : int [1:7] 0 1 2 3 4 5 6
#>
                   :List of 5
   ..$ qr
```

```
....$ qr : num [1:30, 1:7] -5.477 0.183 0.183 0.183 0.183 ...
    ..... attr(*, "dimnames")=List of 2
    .....$: chr [1:30] "1" "2" "3" "4" ...
    .....$: chr [1:7] "(Intercept)" "complaints" "privileges" "learning" ...
#>
#>
    .. .. - attr(*, "assign")= int [1:7] 0 1 2 3 4 5 6
    ....$ qraux: num [1:7] 1.18 1 1.29 1.1 1.07 ...
    .. ..$ pivot: int [1:7] 1 2 3 4 5 6 7
    ...$ tol : num 1e-07
#>
#>
    ....$ rank : int 7
    ....- attr(*, "class")= chr "qr"
    ..$ df.residual : int 23
#>
#>
    ..$ xlevels : Named list()
                  : language lm(formula = rating ~ ., data = attitude)
#>
    ..$ call
                  :Classes 'terms', 'formula' language rating ~ complaints + privileges + learn
#>
    .... attr(*, "variables")= language list(rating, complaints, privileges, learning, raises
    ..... attr(*, "factors")= int [1:7, 1:6] 0 1 0 0 0 0 0 0 1 ...
    ..... attr(*, "dimnames")=List of 2
    ..... s: chr [1:7] "rating" "complaints" "privileges" "learning" ...
    ..... s: chr [1:6] "complaints" "privileges" "learning" "raises" ...
#>
#>
    ....- attr(*, "term.labels")= chr [1:6] "complaints" "privileges" "learning" "raises" ...
    ..... attr(*, "order")= int [1:6] 1 1 1 1 1 1
    .. .. ..- attr(*, "intercept")= int 1
#>
    .. .. - attr(*, "response")= int 1
#>
    ..... attr(*, ".Environment")=<environment: 0x560054d50d70>
    .... - attr(*, "predvars") = language list(rating, complaints, privileges, learning, raises,
    ....- attr(*, "dataClasses")= Named chr [1:7] "numeric" "numeric" "numeric" "numeric" ...
#>
    ..... attr(*, "names")= chr [1:7] "rating" "complaints" "privileges" "learning" ...
#>
                   :'data.frame': 30 obs. of 7 variables:
#>
    ..$ model
    .. ..$ rating
                  : num [1:30] 43 63 71 61 81 43 58 71 72 67 ...
    ....$ complaints: num [1:30] 51 64 70 63 78 55 67 75 82 61 ...
#>
    ....$ privileges: num [1:30] 30 51 68 45 56 49 42 50 72 45 ...
    ....$ learning : num [1:30] 39 54 69 47 66 44 56 55 67 47 ...
    ....$ raises : num [1:30] 61 63 76 54 71 54 66 70 71 62 ...
    ....$ critical : num [1:30] 92 73 86 84 83 49 68 66 83 80 ...
#>
    ....$ advance : num [1:30] 45 47 48 35 47 34 35 41 31 41 ...
#>
    ... - attr(*, "terms")=Classes 'terms', 'formula' language rating ~ complaints + privileges
    ..... attr(*, "variables")= language list(rating, complaints, privileges, learning, rais
    ..... attr(*, "factors")= int [1:7, 1:6] 0 1 0 0 0 0 0 0 1 ...
#>
    ..... attr(*, "dimnames")=List of 2
#>
    #>
    ..... attr(*, "term.labels")= chr [1:6] "complaints" "privileges" "learning" "raises" .
#>
    ..... attr(*, "order")= int [1:6] 1 1 1 1 1 1
#>
    .. .. .. - attr(*, "intercept")= int 1
    .. .. .. - attr(*, "response")= int 1
#>
```

```
#> ..... attr(*, ".Environment")=<environment: 0x560054d50d70>
#> ..... attr(*, "predvars")= language list(rating, complaints, privileges, learning, raise
#> ..... attr(*, "dataClasses")= Named chr [1:7] "numeric" "numeric" "numeric" ...
    ..... attr(*, "names")= chr [1:7] "rating" "complaints" "privileges" "learning" ...
#>
#>
   ..- attr(*, "class")= chr "lm"
#> $ type: chr "mvn"
#> $ beta: Named num [1:6] 0.6707 -0.0734 0.3089 0.0698 0.0312 ...
   ..- attr(*, "names")= chr [1:6] "complaints" "privileges" "learning" "raises" ...
#> $ vcov: num [1:6, 1:6] 0.020531 -0.006381 -0.009324 -0.013812 -0.000242 ...
#> ..- attr(*, "dimnames")=List of 2
#> ....$ : chr [1:6] "complaints" "privileges" "learning" "raises" ...
    ....$ : chr [1:6] "complaints" "privileges" "learning" "raises" ...
#> $ n : int 30
#> $ p : num 6
#> $ df : int 23
#> - attr(*, "class")= chr [1:2] "betasandwich" "list"
BetaN(object)
#> Call:
#> BetaN(object = object)
#>
#> Standardized regression slopes with MVN standard errors:
               est se t p 0.05% 0.5% 2.5% 97.5% 99.5%
#> complaints 0.6707 0.1433 4.6810 0.0001 0.1309 0.2685 0.3743 0.9671 1.0730
#> privileges -0.0734 0.1197 -0.6136 0.5455 -0.5243 -0.4094 -0.3210 0.1741 0.2625
#> learning 0.3089 0.1431 2.1580 0.0416 -0.2304 -0.0929 0.0128 0.6049 0.7107
#> raises
           0.0698 0.1657 0.4213 0.6774 -0.5545 -0.3954 -0.2730 0.4126 0.5350
#> critical 0.0312 0.1047 0.2980 0.7684 -0.3632 -0.2627 -0.1854 0.2478 0.3251
#> advance -0.1835 0.1338 -1.3717 0.1834 -0.6874 -0.5590 -0.4602 0.0932 0.1920
#>
            99.95%
#> complaints 1.2106
#> privileges 0.3774
#> learning 0.8481
#> raises 0.6941
#> critical 0.4256
#> advance 0.3205
```

print

```
print(out)

#> Call:
#> BetaN(object = object)
#>
```

```
#> Standardized regression slopes with MVN standard errors:
#> est se t p 0.05% 0.5%
                                                       2.5% 97.5% 99.5%
#> complaints 0.6707 0.1433 4.6810 0.0001 0.1309 0.2685 0.3743 0.9671 1.0730
#> privileges -0.0734 0.1197 -0.6136 0.5455 -0.5243 -0.4094 -0.3210 0.1741 0.2625
#> learning 0.3089 0.1431 2.1580 0.0416 -0.2304 -0.0929 0.0128 0.6049 0.7107
#> raises
           0.0698 0.1657 0.4213 0.6774 -0.5545 -0.3954 -0.2730 0.4126 0.5350
#> critical 0.0312 0.1047 0.2980 0.7684 -0.3632 -0.2627 -0.1854 0.2478 0.3251
#> advance -0.1835 0.1338 -1.3717 0.1834 -0.6874 -0.5590 -0.4602 0.0932 0.1920
            99.95%
#> complaints 1.2106
#> privileges 0.3774
#> learning 0.8481
#> raises 0.6941
#> critical 0.4256
#> advance 0.3205
```

coef

```
coef(out)

#> complaints privileges learning raises critical advance
#> 0.67072520 -0.07342743 0.30887024 0.06981172 0.03119975 -0.18346445
```

vcov

```
vcov(out)
                complaints privileges learning
                                                        raises
                                                                     critical
#> complaints 0.0205314876 -0.0063811296 -0.009324286 -0.013811718 -0.0002422133
#> privileges -0.0063811296  0.0143201460 -0.002170471  0.001552377 -0.0002768442
#> learning -0.0093242861 -0.0021704714 0.020484826 -0.004998152 0.0028372586
#> raises -0.0138117179 0.0015523774 -0.004998152 0.027456049 -0.0048713593
#> critical -0.0002422133 -0.0002768442 0.002837259 -0.004871359 0.0109607636
#> advance 0.0096650976 -0.0029432354 -0.006326814 -0.009305030 -0.0017608366
#>
                 advance
#> complaints 0.009665098
#> privileges -0.002943235
#> learning -0.006326814
#> raises -0.009305030
#> critical -0.001760837
#> advance 0.017890011
```

confint

summary

```
summary(out)
#> Call:
#> BetaN(object = object)
#> Standardized regression slopes with MVN standard errors:
#>
                est
                     se t p 0.05%
                                                 0.5%
                                                           2.5% 97.5% 99.5%
#> complaints 0.6707 0.1433 4.6810 0.0001 0.1309 0.2685 0.3743 0.9671 1.0730
#> privileges -0.0734 0.1197 -0.6136 0.5455 -0.5243 -0.4094 -0.3210 0.1741 0.2625
#> learning 0.3089 0.1431 2.1580 0.0416 -0.2304 -0.0929 0.0128 0.6049 0.7107
#> raises
            0.0698 0.1657 0.4213 0.6774 -0.5545 -0.3954 -0.2730 0.4126 0.5350
#> critical 0.0312 0.1047 0.2980 0.7684 -0.3632 -0.2627 -0.1854 0.2478 0.3251
#> advance
            -0.1835 0.1338 -1.3717 0.1834 -0.6874 -0.5590 -0.4602 0.0932 0.1920
#>
             99.95%
#> complaints 1.2106
#> privileges 0.3774
#> learning 0.8481
#> raises
             0.6941
#> critical
            0.4256
#> advance 0.3205
```

References

Dudgeon, P. (2017). Some improvements in confidence intervals for standardized regression coefficients. *Psychometrika*, 82(4), 928–951. https://doi.org/10.1007/s11336-017-9563-z

R Core Team. (2022). R: A language and environment for statistical computing. R Foundation for Statistical Computing. Vienna, Austria. https://www.R-project.org/