

# betaSandwich: Methods

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## 1 HC

```
object <- lm(QUALITY ~ NARTIC + PCTGRT + PCTSUPP, data = nas1982)
```

```
out <- BetaHC(object, type = "hc3")
str(out)
```

```
#> List of 7
#> $ call: language BetaHC(object = object, type = "hc3")
#> $ type: chr "hc3"
#> $ beta: Named num [1:3] 0.495 0.391 0.263
#> ..- attr(*, "names")= chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> $ vcov: num [1:3, 1:3] 0.00617 -0.0036 -0.00194 -0.0036 0.0067 ...
#> ..- attr(*, "dimnames")=List of 2
#> .. ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> .. ..$ : chr [1:3] "NARTIC" "PCTGRT" "PCTSUPP"
#> $ n : int 46
#> $ p : num 3
#> $ df : int 42
#> - attr(*, "class")= chr [1:2] "betasandwich" "list"
```

```
BetaHC(object, type = "hc3")
```

```
#> Call:
#> BetaHC(object = object, type = "hc3")
#>
#> Standardized regression slopes with HC3 standard errors:
#>      est      se      t      p  0.05%  0.5%  2.5%  97.5%  99.5%  99.95%
#> NARTIC  0.4951 0.0786 6.3025 0.0000  0.2172 0.2832 0.3366 0.6537 0.7071 0.7731
#> PCTGRT  0.3915 0.0818 4.7831 0.0000  0.1019 0.1707 0.2263 0.5567 0.6123 0.6810
#> PCTSUPP 0.2632 0.0855 3.0786 0.0037 -0.0393 0.0325 0.0907 0.4358 0.4940 0.5658
```

**print**

```
print(out)

#> Call:
#> BetaHC(object = object, type = "hc3")
#>
#> Standardized regression slopes with HC3 standard errors:
#>      est      se      t      p  0.05%  0.5%  2.5% 97.5% 99.5% 99.95%
#> NARTIC  0.4951 0.0786 6.3025 0.0000  0.2172 0.2832 0.3366 0.6537 0.7071 0.7731
#> PCTGRT  0.3915 0.0818 4.7831 0.0000  0.1019 0.1707 0.2263 0.5567 0.6123 0.6810
#> PCTSUPP 0.2632 0.0855 3.0786 0.0037 -0.0393 0.0325 0.0907 0.4358 0.4940 0.5658
```

## coef

```
coef(out)

#>      NARTIC      PCTGRT      PCTSUPP
#> 0.4951451 0.3914887 0.2632477
```

## vcov

```
vcov(out)

#>      NARTIC      PCTGRT      PCTSUPP
#> NARTIC  0.006172168 -0.003602529 -0.001943469
#> PCTGRT -0.003602529  0.006699155 -0.002443584
#> PCTSUPP -0.001943469 -0.002443584  0.007311625
```

## confint

```
confint(out, level = 0.95)

#>      2.5%      97.5%
#> NARTIC  0.33659828 0.6536920
#> PCTGRT  0.22631203 0.5566654
#> PCTSUPP 0.09068548 0.4358099
```

## summary

```
summary(out)

#> Call:
#> BetaHC(object = object, type = "hc3")
#>
#> Standardized regression slopes with HC3 standard errors:
#>      est      se      t      p   0.05%   0.5%   2.5%  97.5%  99.5% 99.95%
#> NARTIC  0.4951 0.0786 6.3025 0.0000  0.2172 0.2832 0.3366 0.6537 0.7071 0.7731
#> PCTGRT  0.3915 0.0818 4.7831 0.0000  0.1019 0.1707 0.2263 0.5567 0.6123 0.6810
#> PCTSUPP 0.2632 0.0855 3.0786 0.0037 -0.0393 0.0325 0.0907 0.4358 0.4940 0.5658
```

## 2 Multivariate Normal

```
object <- lm(rating ~ ., data = attitude)
```

```
out <- BetaN(object)
str(out)

#> List of 7
#> $ call: language BetaN(object = object)
#> $ type: chr "mvn"
#> $ beta: Named num [1:6] 0.6707 -0.0734 0.3089 0.0698 0.0312 ...
#> ..- attr(*, "names")= chr [1:6] "complaints" "privileges" "learning" "raises" ...
#> $ vcov: num [1:6, 1:6] 0.020531 -0.006381 -0.009324 -0.013812 -0.000242 ...
#> ..- attr(*, "dimnames")=List of 2
#> .. ..$ : chr [1:6] "complaints" "privileges" "learning" "raises" ...
#> .. ..$ : chr [1:6] "complaints" "privileges" "learning" "raises" ...
#> $ n : int 30
#> $ p : num 6
#> $ df : int 23
#> - attr(*, "class")= chr [1:2] "betasandwich" "list"

BetaN(object)

#> Call:
#> BetaN(object = object)
#>
#> Standardized regression slopes with MVN standard errors:
#>      est      se      t      p   0.05%   0.5%   2.5%  97.5%  99.5%
#> complaints  0.6707 0.1433  4.6810 0.0001  0.1309  0.2685  0.3743 0.9671 1.0730
#> privileges -0.0734 0.1197 -0.6136 0.5455 -0.5243 -0.4094 -0.3210 0.1741 0.2625
#> learning   0.3089 0.1431  2.1580 0.0416 -0.2304 -0.0929  0.0128 0.6049 0.7107
#> raises     0.0698 0.1657  0.4213 0.6774 -0.5545 -0.3954 -0.2730 0.4126 0.5350
```

```
#> critical    0.0312 0.1047  0.2980 0.7684 -0.3632 -0.2627 -0.1854 0.2478 0.3251
#> advance    -0.1835 0.1338 -1.3717 0.1834 -0.6874 -0.5590 -0.4602 0.0932 0.1920
#>
#> 99.95%
#> complaints 1.2106
#> privileges 0.3774
#> learning   0.8481
#> raises     0.6941
#> critical   0.4256
#> advance    0.3205
```

## print

```
print(out)

#> Call:
#> BetaN(object = object)
#>
#> Standardized regression slopes with MVN standard errors:
#>      est      se      t      p  0.05%   0.5%   2.5%  97.5%  99.5%
#> complaints 0.6707 0.1433  4.6810 0.0001  0.1309  0.2685  0.3743 0.9671 1.0730
#> privileges -0.0734 0.1197 -0.6136 0.5455 -0.5243 -0.4094 -0.3210 0.1741 0.2625
#> learning   0.3089 0.1431  2.1580 0.0416 -0.2304 -0.0929  0.0128 0.6049 0.7107
#> raises     0.0698 0.1657  0.4213 0.6774 -0.5545 -0.3954 -0.2730 0.4126 0.5350
#> critical   0.0312 0.1047  0.2980 0.7684 -0.3632 -0.2627 -0.1854 0.2478 0.3251
#> advance    -0.1835 0.1338 -1.3717 0.1834 -0.6874 -0.5590 -0.4602 0.0932 0.1920
#>
#> 99.95%
#> complaints 1.2106
#> privileges 0.3774
#> learning   0.8481
#> raises     0.6941
#> critical   0.4256
#> advance    0.3205
```

## coef

```
coef(out)

#> complaints privileges learning raises critical advance
#> 0.67072520 -0.07342743 0.30887024 0.06981172 0.03119975 -0.18346445
```

## vcov

```
vcov(out)

#>
#>      complaints      privileges      learning      raises      critical
#> complaints  0.0205314876 -0.0063811296 -0.009324286 -0.013811718 -0.0002422133
#> privileges -0.0063811296  0.0143201460 -0.002170471  0.001552377 -0.0002768442
#> learning   -0.0093242861 -0.0021704714  0.020484826 -0.004998152  0.0028372586
#> raises     -0.0138117179  0.0015523774 -0.004998152  0.027456049 -0.0048713593
#> critical   -0.0002422133 -0.0002768442  0.002837259 -0.004871359  0.0109607636
#> advance    0.0096650976 -0.0029432354 -0.006326814 -0.009305030 -0.0017608366
#>
#>      advance
#> complaints  0.009665098
#> privileges -0.002943235
#> learning   -0.006326814
#> raises     -0.009305030
#> critical   -0.001760837
#> advance    0.017890011
```

## confint

```
confint(out, level = 0.95)

#>
#>      2.5%      97.5%
#> complaints  0.37431113 0.96713928
#> privileges -0.32097709 0.17412223
#> learning    0.01279319 0.60494730
#> raises     -0.27296210 0.41258553
#> critical   -0.18537560 0.24777510
#> advance    -0.46015474 0.09322584
```

## summary

```
summary(out)

#> Call:
#> BetaN(object = object)
#>
#> Standardized regression slopes with MVN standard errors:
#>      est      se      t      p    0.05%    0.5%    2.5%  97.5%  99.5%
#> complaints  0.6707 0.1433  4.6810 0.0001  0.1309  0.2685  0.3743 0.9671 1.0730
#> privileges -0.0734 0.1197 -0.6136 0.5455 -0.5243 -0.4094 -0.3210 0.1741 0.2625
#> learning    0.3089 0.1431  2.1580 0.0416 -0.2304 -0.0929  0.0128 0.6049 0.7107
#> raises      0.0698 0.1657  0.4213 0.6774 -0.5545 -0.3954 -0.2730 0.4126 0.5350
#> critical    0.0312 0.1047  0.2980 0.7684 -0.3632 -0.2627 -0.1854 0.2478 0.3251
```

```
#> advance      -0.1835  0.1338 -1.3717  0.1834 -0.6874 -0.5590 -0.4602  0.0932  0.1920
#>              99.95%
#> complaints  1.2106
#> privileges  0.3774
#> learning    0.8481
#> raises      0.6941
#> critical    0.4256
#> advance     0.3205
```

## References

- Dudgeon, P. (2017). Some improvements in confidence intervals for standardized regression coefficients. *Psychometrika*, 82(4), 928–951. <https://doi.org/10.1007/s11336-017-9563-z>
- R Core Team. (2022). *R: A language and environment for statistical computing*. R Foundation for Statistical Computing. Vienna, Austria. <https://www.R-project.org/>