# Package 'bootStateSpace'

October 9, 2025

Title Bootstrap for State Space Models

Version 1.0.3

```
Description Provides a streamlined and user-friendly framework for
      bootstrapping in state space models, particularly when the number of
      subjects/units (n) exceeds one, a scenario commonly encountered in
      social and behavioral sciences. The parametric bootstrap implemented
      here was developed and applied in Pesigan, Russell, and Chow (2025)
      <doi:10.1037/met0000779>.
URL https://github.com/jeksterslab/bootStateSpace,
      https://jeksterslab.github.io/bootStateSpace/
BugReports https://github.com/jeksterslab/bootStateSpace/issues
License GPL (>= 3)
Encoding UTF-8
Roxygen list(markdown = TRUE)
Depends R (>= 3.5.0)
Imports stats, simStateSpace, dynr
Suggests knitr, rmarkdown, testthat
SystemRequirements GNU GSL (>= 2.5)
RoxygenNote 7.3.3.9000
NeedsCompilation no
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```

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coef.bootstatespace

Estimated Parameter Method for an Object of Class bootstatespace

## Description

Estimated Parameter Method for an Object of Class bootstatespace

## Usage

Index

```
## S3 method for class 'bootstatespace'
coef(object, ...)
```

## Arguments

object Object of Class bootstatespace.
... additional arguments.

#### Value

Returns a vector of estimated parameters.

# Author(s)

Ivan Jacob Agaloos Pesigan

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confint.bootstatespace

Confidence Intervals Method for an Object of Class bootstatespace

#### **Description**

Confidence Intervals Method for an Object of Class bootstatespace

#### Usage

```
## S3 method for class 'bootstatespace'
confint(object, parm = NULL, level = 0.95, type = "pc", ...)
```

## Arguments

object Object of Class bootstatespace.

parm a specification of which parameters are to be given confidence intervals, either

a vector of numbers or a vector of names. If missing, all parameters are consid-

ered.

level the confidence level required.

type Charater string. Confidence interval type, that is, type = "pc" for percentile;

type = "bc" for bias corrected.

... additional arguments.

#### Value

Returns a matrix of confidence intervals.

#### Author(s)

Ivan Jacob Agaloos Pesigan

extract

Extract Generic Function

## Description

A generic function for extracting elements from objects.

## Usage

```
extract(object, what)
```

#### **Arguments**

object An object.

what Character string.

#### Value

A value determined by the specific method for the object's class.

extract.bootstatespace

Extract Method for an Object of Class bootstatespace

## Description

Extract Method for an Object of Class bootstatespace

#### Usage

```
## S3 method for class 'bootstatespace'
extract(object, what = NULL)
```

# Arguments

object of Class bootstatespace.

what Character string. What specific matrix to extract. If what = NULL, extract all

available matrices.

#### Value

Returns a list. Each element of the list is a list of bootstrap estimates in matrix format.

## Author(s)

Ivan Jacob Agaloos Pesigan

**PBSSMFixed** 

Parametric Bootstrap for the State Space Model (Fixed Parameters)

#### **Description**

This function simulates data from a state-space model and fits the model using the dynr package. The process is repeated R times. It assumes that the parameters remain constant across individuals and over time. At the moment, the function only supports type =  $\emptyset$ .

#### Usage

```
PBSSMFixed(
 R,
 path,
 prefix,
 n,
  time,
  delta_t = 1,
 mu0,
  sigma0_1,
  alpha,
  beta,
  psi_l,
  nu,
  lambda,
  theta_1,
  type = 0,
  x = NULL
  gamma = NULL,
  kappa = NULL,
 mu0_fixed = FALSE,
  sigma0_fixed = FALSE,
  alpha_level = 0.05,
  optimization_flag = TRUE,
  hessian_flag = FALSE,
  verbose = FALSE,
  weight_flag = FALSE,
  debug_flag = FALSE,
  perturb_flag = FALSE,
  xtol_rel = 1e-07,
  stopval = -9999,
  ftol_rel = -1,
  ftol_abs = -1,
 maxeval = as.integer(-1),
 maxtime = -1,
  ncores = NULL,
  seed = NULL,
```

```
clean = TRUE
)
```

hessian\_flag

# **Arguments**

r	guments	
	R	Positive integer. Number of bootstrap samples.
	path	Path to a directory to store bootstrap samples and estimates.
	prefix	Character string. Prefix used for the file names for the bootstrap samples and estimates.
	n	Positive integer. Number of individuals.
	time	Positive integer. Number of time points.
	delta_t	Numeric. Time interval. The default value is 1.0 with an option to use a numeric value for the discretized state space model parameterization of the linear stochastic differential equation model.
	mu0	Numeric vector. Mean of initial latent variable values $(\mu_{\eta 0})$ .
	sigma0_l	Numeric matrix. Cholesky factorization (t(chol(sigma0))) of the covariance matrix of initial latent variable values ( $\Sigma_{\eta 0}$ ).
	alpha	Numeric vector. Vector of constant values for the dynamic model $(\alpha)$ .
	beta	Numeric matrix. Transition matrix relating the values of the latent variables at the previous to the current time point $(\beta)$ .
	psi_l	Numeric matrix. Cholesky factorization (t(chol(psi))) of the covariance matrix of the process noise ( $\Psi$ ).
	nu	Numeric vector. Vector of intercept values for the measurement model $(\nu)$ .
	lambda	Numeric matrix. Factor loading matrix linking the latent variables to the observed variables ( $\Lambda$ ).
	theta_l	Numeric matrix. Cholesky factorization (t(chol(theta))) of the covariance matrix of the measurement error $(\Theta)$ .
	type	Integer. State space model type. See Details for more information.
	x	List. Each element of the list is a matrix of covariates for each individual i in n. The number of columns in each matrix should be equal to time.
	gamma	Numeric matrix. Matrix linking the covariates to the latent variables at current time point $(\Gamma)$ .
	kappa	Numeric matrix. Matrix linking the covariates to the observed variables at current time point $(\kappa)$ .
	mu0_fixed	Logical. If mu0_fixed = TRUE, fix the initial mean vector to mu0. If mu0_fixed = FALSE, mu0 is estimated.
	sigma0_fixed	$\label{logical} Logical. If \verb sigma0_fixed  = TRUE , fix the initial covariance matrix to \verb tcrossprod(sigma0_1) . \\ If \verb sigma0_fixed  = FALSE , sigma0  is estimated .$
	alpha_level	Numeric vector. Significance level $\alpha$ .
	optimization_fl	~
		a flag (TRUE/FALSE) indicating whether optimization is to be done.

a flag (TRUE/FALSE) indicating whether the Hessian matrix is to be calculated.

verbose	a flag (TRUE/FALSE) indicating whether more detailed intermediate output during the estimation process should be printed
weight_flag	a flag (TRUE/FALSE) indicating whether the negative log likelihood function should be weighted by the length of the time series for each individual
debug_flag	a flag (TRUE/FALSE) indicating whether users want additional dynr output that can be used for diagnostic purposes
perturb_flag	a flag (TRUE/FLASE) indicating whether to perturb the latent states during estimation. Only useful for ensemble forecasting.
xtol_rel	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
stopval	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
ftol_rel	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
ftol_abs	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
maxeval	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
maxtime	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
ncores	Positive integer. Number of cores to use. If ncores = NULL, use a single core. Consider using multiple cores when number of bootstrap samples R is a large value.
seed	Random seed.
clean	Logical. If clean = TRUE, delete intermediate files generated by the function.

#### **Details**

#### Type 0

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad ext{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}
ight)$$

where  $\mathbf{y}_{i,t}$ ,  $\boldsymbol{\eta}_{i,t}$ , and  $\boldsymbol{\varepsilon}_{i,t}$  are random variables and  $\boldsymbol{\nu}$ ,  $\boldsymbol{\Lambda}$ , and  $\boldsymbol{\Theta}$  are model parameters.  $\mathbf{y}_{i,t}$  represents a vector of observed random variables,  $\boldsymbol{\eta}_{i,t}$  a vector of latent random variables, and  $\boldsymbol{\varepsilon}_{i,t}$  a vector of random measurement errors, at time t and individual i.  $\boldsymbol{\nu}$  denotes a vector of intercepts,  $\boldsymbol{\Lambda}$  a matrix of factor loadings, and  $\boldsymbol{\Theta}$  the covariance matrix of  $\boldsymbol{\varepsilon}$ .

An alternative representation of the measurement error is given by

$$oldsymbol{arepsilon}_{i,t} = oldsymbol{\Theta}^{rac{1}{2}} \mathbf{z}_{i,t}, \quad ext{with} \quad \mathbf{z}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \mathbf{I}
ight)$$

where  $\mathbf{z}_{i,t}$  is a vector of independent standard normal random variables and  $\left(\Theta^{\frac{1}{2}}\right)\left(\Theta^{\frac{1}{2}}\right)' = \Theta$ . The dynamic structure is given by

$$oldsymbol{\eta}_{i,t} = oldsymbol{lpha} + oldsymbol{eta} oldsymbol{\eta}_{i,t-1} + oldsymbol{\zeta}_{i,t}, \quad ext{with} \quad oldsymbol{\zeta}_{i,t} \sim \mathcal{N}\left(oldsymbol{0}, oldsymbol{\Psi}
ight)$$

where  $\eta_{i,t}$ ,  $\eta_{i,t-1}$ , and  $\zeta_{i,t}$  are random variables, and  $\alpha$ ,  $\beta$ , and  $\Psi$  are model parameters. Here,  $\eta_{i,t}$  is a vector of latent variables at time t and individual i,  $\eta_{i,t-1}$  represents a vector of latent variables at time t-1 and individual i, and  $\zeta_{i,t}$  represents a vector of dynamic noise at time t and individual i.  $\alpha$  denotes a vector of intercepts,  $\beta$  a matrix of autoregression and cross regression coefficients, and  $\Psi$  the covariance matrix of  $\zeta_{i,t}$ .

An alternative representation of the dynamic noise is given by

$$oldsymbol{\zeta}_{i,t} = oldsymbol{\Psi}^{rac{1}{2}} \mathbf{z}_{i,t}, \quad ext{with} \quad oldsymbol{z}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \mathbf{I}
ight)$$

where 
$$\left(\Psi^{rac{1}{2}}
ight)\left(\Psi^{rac{1}{2}}
ight)'=\Psi.$$

# Type 1:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right).$$

The dynamic structure is given by

$$\boldsymbol{\eta}_{i,t} = \boldsymbol{\alpha} + \boldsymbol{\beta} \boldsymbol{\eta}_{i,t-1} + \Gamma \mathbf{x}_{i,t} + \boldsymbol{\zeta}_{i,t}, \quad \text{with} \quad \boldsymbol{\zeta}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Psi}\right)$$

where  $\mathbf{x}_{i,t}$  represents a vector of covariates at time t and individual i, and  $\Gamma$  the coefficient matrix linking the covariates to the latent variables.

#### Type 2:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \kappa \mathbf{x}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right)$$

where  $\kappa$  represents the coefficient matrix linking the covariates to the observed variables.

The dynamic structure is given by

$$oldsymbol{\eta}_{i,t} = oldsymbol{lpha} + oldsymbol{eta} oldsymbol{\eta}_{i,t-1} + \Gamma \mathbf{x}_{i,t} + oldsymbol{\zeta}_{i,t}, \quad ext{with} \quad oldsymbol{\zeta}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, oldsymbol{\Psi}
ight).$$

#### Value

Returns an object of class bootstatespace which is a list with the following elements:

call Function call.

args Function arguments.

**thetahatstar** Sampling distribution of  $\hat{\theta}$ .

**vcov** Sampling variance-covariance matrix of  $\hat{\theta}$ .

**est** Vector of estimated  $\hat{\theta}$ .

fun Function used ("PBSSMFixed").

method Bootstrap method used ("parametric").

## Author(s)

Ivan Jacob Agaloos Pesigan

#### References

Chow, S.-M., Ho, M. R., Hamaker, E. L., & Dolan, C. V. (2010). Equivalence and differences between structural equation modeling and state-space modeling techniques. *Structural Equation Modeling: A Multidisciplinary Journal*, 17(2), 303–332. doi:10.1080/10705511003661553

#### See Also

Other Bootstrap for State Space Models Functions: PBSSMLinSDEFixed(), PBSSMOUFixed(), PBSSMVARFixed()

#### **Examples**

```
# prepare parameters
set.seed(42)
## number of individuals
n <- 5
## time points
time <- 50
delta_t <- 1
## dynamic structure
p <- 3
mu0 < -rep(x = 0, times = p)
sigma0 <- 0.001 * diag(p)
sigma0_l <- t(chol(sigma0))</pre>
alpha < - rep(x = 0, times = p)
beta \leftarrow 0.50 * diag(p)
psi <- 0.001 * diag(p)
psi_l <- t(chol(psi))</pre>
## measurement model
k <- 3
nu \leftarrow rep(x = 0, times = k)
lambda <- diag(k)</pre>
theta <- 0.001 * diag(k)
theta_l <- t(chol(theta))</pre>
path <- tempdir()</pre>
pb <- PBSSMFixed(</pre>
  R = 10L, # use at least 1000 in actual research
  path = path,
  prefix = "ssm",
  n = n,
  time = time,
  delta_t = delta_t,
  mu0 = mu0,
  sigma0_1 = sigma0_1,
  alpha = alpha,
  beta = beta,
  psi_l = psi_l,
  nu = nu,
  lambda = lambda,
  theta_l = theta_l,
  type = 0,
```

```
ncores = 1, # consider using multiple cores
seed = 42
)
print(pb)
summary(pb)
confint(pb)
vcov(pb)
coef(pb)
print(pb, type = "bc") # bias-corrected
summary(pb, type = "bc")
confint(pb, type = "bc")
```

**PBSSMLinSDEFixed** 

Parametric Bootstrap for the Linear Stochastic Differential Equation Model using a State Space Model Parameterization (Fixed Parameters)

#### **Description**

This function simulates data from a linear stochastic differential equation model using a state-space model parameterization and fits the model using the dynr package. The process is repeated R times. It assumes that the parameters remain constant across individuals and over time. At the moment, the function only supports type =  $\emptyset$ .

#### Usage

```
PBSSMLinSDEFixed(
  R,
  path,
  prefix,
  time,
  delta_t = 0.1,
 mu0,
  sigma0_1,
  iota,
  phi,
  sigma_1,
  nu,
  lambda,
  theta_1,
  type = 0,
  x = NULL
  gamma = NULL,
  kappa = NULL,
  mu0_fixed = FALSE,
```

```
sigma0_fixed = FALSE,
 alpha_level = 0.05,
 optimization_flag = TRUE,
 hessian_flag = FALSE,
 verbose = FALSE,
 weight_flag = FALSE,
 debug_flag = FALSE,
 perturb_flag = FALSE,
 xtol_rel = 1e-07,
 stopval = -9999,
 ftol_rel = -1,
 ftol_abs = -1,
 maxeval = as.integer(-1),
 maxtime = -1,
 ncores = NULL,
 seed = NULL,
 clean = TRUE
)
```

#### **Arguments**

R		Positive integer. Number of bootstrap samples.
р	ath	Path to a directory to store bootstrap samples and estimates.
р	refix	Character string. Prefix used for the file names for the bootstrap samples and estimates.
n		Positive integer. Number of individuals.
t	ime	Positive integer. Number of time points.
d	elta_t	Numeric. Time interval $(\Delta_t)$ .
m	u0	Numeric vector. Mean of initial latent variable values $(\mu_{\eta 0})$ .
S	igma0_l	Numeric matrix. Cholesky factorization (t(chol(sigma0))) of the covariance matrix of initial latent variable values $(\Sigma_{\eta 0})$ .
i	ota	Numeric vector. An unobserved term that is constant over time $(\iota)$ .
р	hi	Numeric matrix. The drift matrix which represents the rate of change of the solution in the absence of any random fluctuations $(\Phi)$ .
S	igma_l	Numeric matrix. Cholesky factorization (t(chol(sigma))) of the covariance matrix of volatility or randomness in the process $(\Sigma)$ .
n	u	Numeric vector. Vector of intercept values for the measurement model $(\nu)$ .
1	ambda	Numeric matrix. Factor loading matrix linking the latent variables to the observed variables ( $\Lambda$ ).
t	heta_l	Numeric matrix. Cholesky factorization (t(chol(theta))) of the covariance matrix of the measurement error $(\Theta)$ .
t	уре	Integer. State space model type. See Details for more information.
Х		List. Each element of the list is a matrix of covariates for each individual $i$ in $n$ . The number of columns in each matrix should be equal to time.

gamma	Numeric matrix. Matrix linking the covariates to the latent variables at current time point $(\Gamma)$ .
kappa	Numeric matrix. Matrix linking the covariates to the observed variables at current time point $(\kappa)$ .
mu0_fixed	Logical. If mu0_fixed = TRUE, fix the initial mean vector to mu0. If mu0_fixed = FALSE, mu0 is estimated.
sigma0_fixed	Logical. If sigma0_fixed = TRUE, fix the initial covariance matrix to tcrossprod(sigma0_1). If sigma0_fixed = FALSE, sigma0 is estimated.
alpha_level	Numeric vector. Significance level $\alpha$ .
optimization_f	
	a flag (TRUE/FALSE) indicating whether optimization is to be done.
hessian_flag	a flag (TRUE/FALSE) indicating whether the Hessian matrix is to be calculated.
verbose	a flag (TRUE/FALSE) indicating whether more detailed intermediate output during the estimation process should be printed
weight_flag	a flag (TRUE/FALSE) indicating whether the negative log likelihood function should be weighted by the length of the time series for each individual
debug_flag	a flag (TRUE/FALSE) indicating whether users want additional dynr output that can be used for diagnostic purposes
perturb_flag	a flag (TRUE/FLASE) indicating whether to perturb the latent states during estimation. Only useful for ensemble forecasting.
xtol_rel	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
stopval	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
ftol_rel	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
ftol_abs	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
maxeval	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
maxtime	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
ncores	Positive integer. Number of cores to use. If ncores = NULL, use a single core. Consider using multiple cores when number of bootstrap samples R is a large value.
seed	Random seed.
clean	Logical. If clean = TRUE, delete intermediate files generated by the function.

## **Details**

# Type 0:

The measurement model is given by

$$\mathbf{y}_{i,t} = oldsymbol{
u} + oldsymbol{\Lambda} oldsymbol{\eta}_{i,t} + oldsymbol{arepsilon}_{i,t}, \quad ext{with} \quad oldsymbol{arepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, oldsymbol{\Theta}
ight)$$

where  $\mathbf{y}_{i,t}$ ,  $\eta_{i,t}$ , and  $\varepsilon_{i,t}$  are random variables and  $\nu$ ,  $\Lambda$ , and  $\Theta$  are model parameters.  $\mathbf{y}_{i,t}$  represents a vector of observed random variables,  $\eta_{i,t}$  a vector of latent random variables, and  $\varepsilon_{i,t}$  a vector of random measurement errors, at time t and individual t.  $\nu$  denotes a vector of intercepts,  $\Lambda$  a matrix of factor loadings, and  $\Theta$  the covariance matrix of  $\varepsilon$ .

An alternative representation of the measurement error is given by

$$oldsymbol{arepsilon}_{i,t} = oldsymbol{\Theta}^{rac{1}{2}} \mathbf{z}_{i,t}, \quad ext{with} \quad \mathbf{z}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \mathbf{I}\right)$$

where  $\mathbf{z}_{i,t}$  is a vector of independent standard normal random variables and  $\left(\Theta^{\frac{1}{2}}\right)\left(\Theta^{\frac{1}{2}}\right)' = \Theta$ . The dynamic structure is given by

$$d\boldsymbol{\eta}_{i,t} = (\boldsymbol{\iota} + \boldsymbol{\Phi} \boldsymbol{\eta}_{i,t}) dt + \boldsymbol{\Sigma}^{\frac{1}{2}} d\mathbf{W}_{i,t}$$

where  $\iota$  is a term which is unobserved and constant over time,  $\Phi$  is the drift matrix which represents the rate of change of the solution in the absence of any random fluctuations,  $\Sigma$  is the matrix of volatility or randomness in the process, and  $\mathrm{d} W$  is a Wiener process or Brownian motion, which represents random fluctuations.

#### **Type 1:**

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{arepsilon}_{i,t}, \quad ext{with} \quad \boldsymbol{arepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, oldsymbol{\Theta}
ight).$$

The dynamic structure is given by

$$\mathrm{d} oldsymbol{\eta}_{i,t} = \left( oldsymbol{\iota} + oldsymbol{\Phi} oldsymbol{\eta}_{i,t} + oldsymbol{\Gamma} \mathbf{x}_{i,t} + oldsymbol{\Sigma}^{rac{1}{2}} \mathrm{d} \mathbf{W}_{i,t} 
ight.$$

where  $\mathbf{x}_{i,t}$  represents a vector of covariates at time t and individual i, and  $\Gamma$  the coefficient matrix linking the covariates to the latent variables.

#### **Type 2:**

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \kappa \mathbf{x}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right)$$

where  $\kappa$  represents the coefficient matrix linking the covariates to the observed variables.

The dynamic structure is given by

$$\mathrm{d} \boldsymbol{\eta}_{i,t} = \left( \boldsymbol{\iota} + \boldsymbol{\Phi} \boldsymbol{\eta}_{i,t} \right) \mathrm{d} t + \boldsymbol{\Gamma} \mathbf{x}_{i,t} + \boldsymbol{\Sigma}^{\frac{1}{2}} \mathrm{d} \mathbf{W}_{i,t}.$$

#### **State Space Parameterization:**

The state space parameters as a function of the linear stochastic differential equation model parameters are given by

$$\boldsymbol{\beta}_{\Delta t_{l_s}} = \exp\left(\Delta t \boldsymbol{\Phi}\right)$$

$$oldsymbol{lpha}_{\Delta t_{l_i}} = oldsymbol{\Phi}^{-1} \left( oldsymbol{eta} - \mathbf{I}_p 
ight) oldsymbol{\iota}$$

$$\operatorname{vec}\left(\mathbf{\Psi}_{\Delta t_{l_{i}}}\right) = \left[\left(\mathbf{\Phi} \otimes \mathbf{I}_{p}\right) + \left(\mathbf{I}_{p} \otimes \mathbf{\Phi}\right)\right] \left[\exp\left(\left[\left(\mathbf{\Phi} \otimes \mathbf{I}_{p}\right) + \left(\mathbf{I}_{p} \otimes \mathbf{\Phi}\right)\right] \Delta t\right) - \mathbf{I}_{p \times p}\right] \operatorname{vec}\left(\mathbf{\Sigma}\right)$$

where p is the number of latent variables and  $\Delta t$  is the time interval.

#### Value

Returns an object of class bootstatespace which is a list with the following elements:

```
call Function call.

args Function arguments.

thetahatstar Sampling distribution of \hat{\theta}.

vcov Sampling variance-covariance matrix of \hat{\theta}.

est Vector of estimated \hat{\theta}.

fun Function used ("PBSSMLinSDEFixed").
```

method Bootstrap method used ("parametric").

#### Author(s)

Ivan Jacob Agaloos Pesigan

#### References

Chow, S.-M., Ho, M. R., Hamaker, E. L., & Dolan, C. V. (2010). Equivalence and differences between structural equation modeling and state-space modeling techniques. *Structural Equation Modeling: A Multidisciplinary Journal*, 17(2), 303–332. doi:10.1080/10705511003661553

#### See Also

Other Bootstrap for State Space Models Functions: PBSSMFixed(), PBSSMOUFixed(), PBSSMVARFixed()

## **Examples**

```
# prepare parameters
## number of individuals
n <- 5
## time points
time <- 50
delta_t <- 0.10
## dynamic structure
p <- 2
mu0 < -c(-3.0, 1.5)
sigma0 <- 0.001 * diag(p)
sigma0_l <- t(chol(sigma0))</pre>
iota <- c(0.317, 0.230)
phi <- matrix(</pre>
  data = c(
    -0.10,
    0.05,
    0.05,
    -0.10
  ),
  nrow = p
sigma <- matrix(</pre>
```

```
data = c(
    2.79,
    0.06,
    0.06,
    3.27
  ),
  nrow = p
)
sigma_l <- t(chol(sigma))</pre>
## measurement model
k <- 2
nu \leftarrow rep(x = 0, times = k)
lambda <- diag(k)</pre>
theta <- 0.001 * diag(k)
theta_l \leftarrow t(chol(theta))
path <- tempdir()</pre>
pb <- PBSSMLinSDEFixed(</pre>
  R = 10L, # use at least 1000 in actual research
  path = path,
  prefix = "lse",
  n = n,
  time = time,
  delta_t = delta_t,
  mu0 = mu0,
  sigma0_1 = sigma0_1,
  iota = iota,
  phi = phi,
  sigma_l = sigma_l,
  nu = nu,
  lambda = lambda,
  theta_l = theta_l,
  type = 0,
  ncores = 1, # consider using multiple cores
  seed = 42
)
print(pb)
summary(pb)
confint(pb)
vcov(pb)
coef(pb)
print(pb, type = "bc") # bias-corrected
summary(pb, type = "bc")
confint(pb, type = "bc")
```

**PBSSMOUFixed** 

Parametric Bootstrap for the Ornstein-Uhlenbeck Model using a State Space Model Parameterization (Fixed Parameters)

#### **Description**

This function simulates data from a Ornstein-Uhlenbeck (OU) model using a state-space model parameterization and fits the model using the dynr package. The process is repeated R times. It assumes that the parameters remain constant across individuals and over time. At the moment, the function only supports type =  $\emptyset$ .

## Usage

```
PBSSMOUFixed(
  R,
  path,
  prefix,
  n,
  time,
  delta_t = 0.1,
 mu0,
  sigma0_1,
 mu,
  phi,
  sigma_1,
  nu,
  lambda,
  theta_1,
  type = 0,
  x = NULL
  gamma = NULL,
  kappa = NULL,
 mu0_fixed = FALSE,
  sigma0_fixed = FALSE,
  alpha_level = 0.05,
  optimization_flag = TRUE,
  hessian_flag = FALSE,
  verbose = FALSE,
  weight_flag = FALSE,
  debug_flag = FALSE,
  perturb_flag = FALSE,
  xtol_rel = 1e-07,
  stopval = -9999,
  ftol_rel = -1,
  ftol_abs = -1,
  maxeval = as.integer(-1),
 maxtime = -1,
  ncores = NULL,
  seed = NULL,
  clean = TRUE
)
```

# Arguments

١	•	
	R	Positive integer. Number of bootstrap samples.
	path	Path to a directory to store bootstrap samples and estimates.
	prefix	Character string. Prefix used for the file names for the bootstrap samples and estimates.
	n	Positive integer. Number of individuals.
	time	Positive integer. Number of time points.
	delta_t	Numeric. Time interval $(\Delta_t)$ .
	mu0	Numeric vector. Mean of initial latent variable values $(\mu_{\eta 0})$ .
	sigma0_l	Numeric matrix. Cholesky factorization (t(chol(sigma0))) of the covariance matrix of initial latent variable values $(\Sigma_{\eta 0})$ .
	mu	Numeric vector. The long-term mean or equilibrium level $(\mu)$ .
	phi	Numeric matrix. The drift matrix which represents the rate of change of the solution in the absence of any random fluctuations ( $\Phi$ ). It also represents the rate of mean reversion, determining how quickly the variable returns to its mean.
	sigma_l	Numeric matrix. Cholesky factorization ( $t(chol(sigma))$ ) of the covariance matrix of volatility or randomness in the process ( $\Sigma$ ).
	nu	Numeric vector. Vector of intercept values for the measurement model $(\nu)$ .
	lambda	Numeric matrix. Factor loading matrix linking the latent variables to the observed variables ( $\Lambda$ ).
	theta_l	Numeric matrix. Cholesky factorization $(t(chol(theta)))$ of the covariance matrix of the measurement error $(\Theta)$ .
	type	Integer. State space model type. See Details for more information.
	X	List. Each element of the list is a matrix of covariates for each individual i in n.  The number of columns in each matrix should be equal to time.
	gamma	Numeric matrix. Matrix linking the covariates to the latent variables at current time point $(\Gamma)$ .
	kappa	Numeric matrix. Matrix linking the covariates to the observed variables at current time point $(\kappa)$ .
	mu0_fixed	Logical. If mu0_fixed = TRUE, fix the initial mean vector to mu0. If mu0_fixed = FALSE, mu0 is estimated.
	sigma0_fixed	Logical. If sigma0_fixed = TRUE, fix the initial covariance matrix to tcrossprod(sigma0_1). If sigma0_fixed = FALSE, sigma0 is estimated.
	alpha_level	Numeric vector. Significance level $\alpha$ .
	optimization_fl	
		a flag (TRUE/FALSE) indicating whether optimization is to be done.
	hessian_flag	a flag (TRUE/FALSE) indicating whether the Hessian matrix is to be calculated.
	verbose	a flag (TRUE/FALSE) indicating whether more detailed intermediate output during the estimation process should be printed
	weight_flag	a flag (TRUE/FALSE) indicating whether the negative log likelihood function should be weighted by the length of the time series for each individual

debug_flag	a flag (TRUE/FALSE) indicating whether users want additional dynr output that can be used for diagnostic purposes
perturb_flag	a flag (TRUE/FLASE) indicating whether to perturb the latent states during estimation. Only useful for ensemble forecasting.
xtol_rel	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
stopval	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
ftol_rel	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
ftol_abs	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
maxeval	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
maxtime	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
ncores	Positive integer. Number of cores to use. If ncores = NULL, use a single core. Consider using multiple cores when number of bootstrap samples R is a large value.
seed	Random seed.
clean	Logical. If clean = TRUE, delete intermediate files generated by the function.

### **Details**

## Type 0:

The measurement model is given by

$$\mathbf{y}_{i,t} = oldsymbol{
u} + oldsymbol{\Lambda} oldsymbol{\eta}_{i,t} + oldsymbol{arepsilon}_{i,t}, \quad ext{with} \quad oldsymbol{arepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, oldsymbol{\Theta}
ight)$$

where  $\mathbf{y}_{i,t}$ ,  $\eta_{i,t}$ , and  $\varepsilon_{i,t}$  are random variables and  $\boldsymbol{\nu}$ ,  $\boldsymbol{\Lambda}$ , and  $\boldsymbol{\Theta}$  are model parameters.  $\mathbf{y}_{i,t}$  represents a vector of observed random variables,  $\eta_{i,t}$  a vector of latent random variables, and  $\varepsilon_{i,t}$  a vector of random measurement errors, at time t and individual i.  $\boldsymbol{\nu}$  denotes a vector of intercepts,  $\boldsymbol{\Lambda}$  a matrix of factor loadings, and  $\boldsymbol{\Theta}$  the covariance matrix of  $\varepsilon$ .

An alternative representation of the measurement error is given by

$$\boldsymbol{\varepsilon}_{i,t} = \boldsymbol{\Theta}^{\frac{1}{2}} \mathbf{z}_{i,t}, \quad \text{with} \quad \mathbf{z}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \mathbf{I}\right)$$

where  $\mathbf{z}_{i,t}$  is a vector of independent standard normal random variables and  $\left(\Theta^{\frac{1}{2}}\right)\left(\Theta^{\frac{1}{2}}\right)' = \Theta$ . The dynamic structure is given by

$$\mathrm{d}oldsymbol{\eta}_{i,t} = oldsymbol{\Phi} \left(oldsymbol{\eta}_{i,t} - oldsymbol{\mu} 
ight) \mathrm{d}t + oldsymbol{\Sigma}^{rac{1}{2}} \mathrm{d}\mathbf{W}_{i,t}$$

where  $\mu$  is the long-term mean or equilibrium level,  $\Phi$  is the rate of mean reversion, determining how quickly the variable returns to its mean,  $\Sigma$  is the matrix of volatility or randomness in the process, and dW is a Wiener process or Brownian motion, which represents random fluctuations.

#### Type 1:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad ext{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right).$$

The dynamic structure is given by

$$\mathrm{d} oldsymbol{\eta}_{i,t} = oldsymbol{\Phi} \left( oldsymbol{\eta}_{i,t} - oldsymbol{\mu} 
ight) \mathrm{d} t + oldsymbol{\Gamma} \mathbf{x}_{i,t} + oldsymbol{\Sigma}^{rac{1}{2}} \mathrm{d} \mathbf{W}_{i,t}$$

where  $\mathbf{x}_{i,t}$  represents a vector of covariates at time t and individual i, and  $\Gamma$  the coefficient matrix linking the covariates to the latent variables.

#### Type 2:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \kappa \mathbf{x}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right)$$

where  $\kappa$  represents the coefficient matrix linking the covariates to the observed variables. The dynamic structure is given by

$$\mathrm{d}\boldsymbol{\eta}_{i.t} = \boldsymbol{\Phi} \left( \boldsymbol{\eta}_{i.t} - \boldsymbol{\mu} \right) \mathrm{d}t + \boldsymbol{\Gamma} \mathbf{x}_{i.t} + \boldsymbol{\Sigma}^{\frac{1}{2}} \mathrm{d}\mathbf{W}_{i.t}.$$

#### The OU model as a linear stochastic differential equation model:

The OU model is a first-order linear stochastic differential equation model in the form of

$$\mathrm{d}\boldsymbol{\eta}_{i,t} = \left(\boldsymbol{\iota} + \boldsymbol{\Phi}\boldsymbol{\eta}_{i,t}\right) \mathrm{d}t + \boldsymbol{\Sigma}^{\frac{1}{2}} \mathrm{d}\mathbf{W}_{i,t}$$

where  $\mu = -\Phi^{-1}\iota$  and, equivalently  $\iota = -\Phi\mu$ .

## Value

Returns an object of class bootstatespace which is a list with the following elements:

call Function call.

args Function arguments.

**thetahatstar** Sampling distribution of  $\hat{\theta}$ .

**vcov** Sampling variance-covariance matrix of  $\hat{\theta}$ .

**est** Vector of estimated  $\hat{\theta}$ .

fun Function used ("PBSSMOUFixed").

method Bootstrap method used ("parametric").

## Author(s)

Ivan Jacob Agaloos Pesigan

#### References

Chow, S.-M., Ho, M. R., Hamaker, E. L., & Dolan, C. V. (2010). Equivalence and differences between structural equation modeling and state-space modeling techniques. *Structural Equation Modeling: A Multidisciplinary Journal*, 17(2), 303–332. doi:10.1080/10705511003661553

#### See Also

Other Bootstrap for State Space Models Functions: PBSSMFixed(), PBSSMLinSDEFixed(), PBSSMVARFixed()

## **Examples**

```
# prepare parameters
## number of individuals
n <- 5
## time points
time <- 50
delta_t <- 0.10
## dynamic structure
p <- 2
mu0 < -c(-3.0, 1.5)
sigma0 <- 0.001 * diag(p)
sigma0_l <- t(chol(sigma0))</pre>
mu < -c(5.76, 5.18)
phi <- matrix(</pre>
  data = c(
    -0.10,
    0.05,
    0.05,
    -0.10
  ),
  nrow = p
)
sigma <- matrix(</pre>
  data = c(
    2.79,
    0.06,
    0.06,
    3.27
  ),
  nrow = p
sigma_l <- t(chol(sigma))</pre>
## measurement model
k <- 2
nu \leftarrow rep(x = 0, times = k)
lambda <- diag(k)</pre>
theta <- 0.001 * diag(k)
theta_l <- t(chol(theta))</pre>
path <- tempdir()</pre>
pb <- PBSSMOUFixed(</pre>
  R = 10L, # use at least 1000 in actual research
  path = path,
  prefix = "ou",
  n = n,
  time = time,
  delta_t = delta_t,
```

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```
mu0 = mu0,
 sigma0_1 = sigma0_1,
 mu = mu,
 phi = phi,
 sigma_l = sigma_l,
 nu = nu,
 lambda = lambda,
 theta_l = theta_l,
 type = 0,
 ncores = 1, # consider using multiple cores
 seed = 42
)
print(pb)
summary(pb)
confint(pb)
vcov(pb)
coef(pb)
print(pb, type = "bc") # bias-corrected
summary(pb, type = "bc")
confint(pb, type = "bc")
```

**PBSSMVARFixed** 

Parametric Bootstrap for the Vector Autoregressive Model (Fixed Parameters)

## Description

This function simulates data from a vector autoregressive model using a state-space model parameterization and fits the model using the dynr package. The process is repeated R times. It assumes that the parameters remain constant across individuals and over time. At the moment, the function only supports type =  $\emptyset$ .

## Usage

```
PBSSMVARFixed(
    R,
    path,
    prefix,
    n,
    time,
    mu0,
    sigma0_l,
    alpha,
    beta,
    psi_l,
    type = 0,
    x = NULL,
```

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```
gamma = NULL,
mu0_fixed = FALSE,
sigma0_fixed = FALSE,
alpha_level = 0.05,
optimization_flag = TRUE,
hessian_flag = FALSE,
verbose = FALSE,
weight_flag = FALSE,
debug_flag = FALSE,
perturb_flag = FALSE,
xtol_rel = 1e-07,
stopval = -9999,
ftol_rel = -1,
ftol_abs = -1,
maxeval = as.integer(-1),
maxtime = -1,
ncores = NULL,
seed = NULL,
clean = TRUE
```

## **Arguments**

R	Positive integer. Number of bootstrap samples.
path	Path to a directory to store bootstrap samples and estimates.
prefix	Character string. Prefix used for the file names for the bootstrap samples and estimates.
n	Positive integer. Number of individuals.
time	Positive integer. Number of time points.
mu0	Numeric vector. Mean of initial latent variable values $(\mu_{\eta 0})$ .
sigma0_l	Numeric matrix. Cholesky factorization (t(chol(sigma0))) of the covariance matrix of initial latent variable values ( $\Sigma_{\eta 0}$ ).
alpha	Numeric vector. Vector of constant values for the dynamic model $(\alpha)$ .
beta	Numeric matrix. Transition matrix relating the values of the latent variables at the previous to the current time point $(\beta)$ .
psi_l	Numeric matrix. Cholesky factorization (t(chol(psi))) of the covariance matrix of the process noise $(\Psi)$ .
type	Integer. State space model type. See Details for more information.
х	List. Each element of the list is a matrix of covariates for each individual i in n. The number of columns in each matrix should be equal to time.
gamma	Numeric matrix. Matrix linking the covariates to the latent variables at current time point $(\Gamma)$ .
mu0_fixed	Logical. If mu0_fixed = TRUE, fix the initial mean vector to mu0. If mu0_fixed = FALSE, mu0 is estimated.

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sigma0_fixed	Logical. If sigma0_fixed = TRUE, fix the initial covariance matrix to tcrossprod(sigma0_1). If sigma0_fixed = FALSE, sigma0 is estimated.
alpha_level	Numeric vector. Significance level $\alpha$ .
optimization_f	
	a flag (TRUE/FALSE) indicating whether optimization is to be done.
hessian_flag	a flag (TRUE/FALSE) indicating whether the Hessian matrix is to be calculated.
verbose	a flag (TRUE/FALSE) indicating whether more detailed intermediate output during the estimation process should be printed
weight_flag	a flag (TRUE/FALSE) indicating whether the negative log likelihood function should be weighted by the length of the time series for each individual
debug_flag	a flag (TRUE/FALSE) indicating whether users want additional dynr output that can be used for diagnostic purposes
perturb_flag	a flag (TRUE/FLASE) indicating whether to perturb the latent states during estimation. Only useful for ensemble forecasting.
xtol_rel	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
stopval	Stopping criteria option for parameter optimization. See <a href="dynr.model">dynr.model</a> () for more details.
ftol_rel	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
ftol_abs	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
maxeval	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
maxtime	Stopping criteria option for parameter optimization. See dynr::dynr.model() for more details.
ncores	Positive integer. Number of cores to use. If ncores = NULL, use a single core. Consider using multiple cores when number of bootstrap samples R is a large value.
seed	Random seed.
clean	Logical. If clean = TRUE, delete intermediate files generated by the function.
	-

#### **Details**

## Type 0:

The measurement model is given by

$$\mathbf{y}_{i,t} = oldsymbol{\eta}_{i,t}$$

where  $\mathbf{y}_{i,t}$  represents a vector of observed variables and  $\boldsymbol{\eta}_{i,t}$  a vector of latent variables for individual i and time t. Since the observed and latent variables are equal, we only generate data from the dynamic structure.

The dynamic structure is given by

$$oldsymbol{\eta}_{i,t} = oldsymbol{lpha} + oldsymbol{eta} oldsymbol{\eta}_{i,t-1} + oldsymbol{\zeta}_{i,t}, \quad ext{with} \quad oldsymbol{\zeta}_{i,t} \sim \mathcal{N}\left(oldsymbol{0}, oldsymbol{\Psi}
ight)$$

where  $\eta_{i,t}$ ,  $\eta_{i,t-1}$ , and  $\zeta_{i,t}$  are random variables, and  $\alpha$ ,  $\beta$ , and  $\Psi$  are model parameters. Here,  $\eta_{i,t}$  is a vector of latent variables at time t and individual i,  $\eta_{i,t-1}$  represents a vector of latent variables at time t-1 and individual i, and  $\zeta_{i,t}$  represents a vector of dynamic noise at time t and individual i.  $\alpha$  denotes a vector of intercepts,  $\beta$  a matrix of autoregression and cross regression coefficients, and  $\Psi$  the covariance matrix of  $\zeta_{i,t}$ .

An alternative representation of the dynamic noise is given by

$$oldsymbol{\zeta}_{i,t} = oldsymbol{\Psi}^{rac{1}{2}} oldsymbol{\mathbf{z}}_{i,t}, \quad ext{with} \quad oldsymbol{\mathbf{z}}_{i,t} \sim \mathcal{N}\left(oldsymbol{0}, oldsymbol{\mathbf{I}}
ight)$$

where 
$$\left(\Psi^{rac{1}{2}}
ight)\left(\Psi^{rac{1}{2}}
ight)'=\Psi.$$

# Type 1:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\eta}_{i,t}.$$

The dynamic structure is given by

$$oldsymbol{\eta}_{i,t} = oldsymbol{lpha} + oldsymbol{eta} oldsymbol{\eta}_{i,t-1} + oldsymbol{\Gamma} \mathbf{x}_{i,t} + oldsymbol{\zeta}_{i,t}, \quad ext{with} \quad oldsymbol{\zeta}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, oldsymbol{\Psi}
ight)$$

where  $\mathbf{x}_{i,t}$  represents a vector of covariates at time t and individual i, and  $\Gamma$  the coefficient matrix linking the covariates to the latent variables.

#### Value

Returns an object of class bootstatespace which is a list with the following elements:

call Function call.

args Function arguments.

thetahatstar Sampling distribution of  $\hat{\theta}$ .

**vcov** Sampling variance-covariance matrix of  $\hat{\theta}$ .

**est** Vector of estimated  $\hat{\theta}$ .

fun Function used ("PBSSMVARFixed").

method Bootstrap method used ("parametric").

#### Author(s)

Ivan Jacob Agaloos Pesigan

### References

Chow, S.-M., Ho, M. R., Hamaker, E. L., & Dolan, C. V. (2010). Equivalence and differences between structural equation modeling and state-space modeling techniques. *Structural Equation Modeling: A Multidisciplinary Journal*, 17(2), 303–332. doi:10.1080/10705511003661553

#### See Also

Other Bootstrap for State Space Models Functions: PBSSMFixed(), PBSSMLinSDEFixed(), PBSSMOUFixed()

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#### **Examples**

```
# prepare parameters
## number of individuals
n <- 5
## time points
time <- 50
## dynamic structure
p <- 3
mu0 < -rep(x = 0, times = p)
sigma0 <- 0.001 * diag(p)
sigma0_l <- t(chol(sigma0))</pre>
alpha <- rep(x = 0, times = p)
beta <- 0.50 * diag(p)
psi <- 0.001 * diag(p)
psi_l <- t(chol(psi))</pre>
path <- tempdir()</pre>
pb <- PBSSMVARFixed(</pre>
  R = 10L, # use at least 1000 in actual research
  path = path,
  prefix = "var",
  n = n,
  time = time,
  mu0 = mu0,
  sigma0_1 = sigma0_1,
  alpha = alpha,
  beta = beta,
  psi_l = psi_l,
  type = 0,
  ncores = 1, # consider using multiple cores
  seed = 42
)
print(pb)
summary(pb)
confint(pb)
vcov(pb)
coef(pb)
print(pb, type = "bc") # bias-corrected
summary(pb, type = "bc")
confint(pb, type = "bc")
```

## **Description**

Print Method for an Object of Class bootstatespace

#### Usage

```
## S3 method for class 'bootstatespace'
print(x, alpha = NULL, type = "pc", digits = 4, ...)
```

## Arguments

X	Object of Class bootstatespace.
alpha	Numeric vector. Significance level $\alpha$ . If alpha = NULL, use the argument alpha used in x.
type	Charater string. Confidence interval type, that is, type = "pc" for percentile; type = "bc" for bias corrected.
digits	Digits to print.
	additional arguments.

#### Value

Prints a matrix of estimates, standard errors, number of bootstrap replications, and confidence intervals.

#### Author(s)

Ivan Jacob Agaloos Pesigan

```
summary.bootstatespace
```

Summary Method for an Object of Class bootstatespace

## **Description**

Summary Method for an Object of Class bootstatespace

## Usage

```
## S3 method for class 'bootstatespace'
summary(object, alpha = NULL, type = "pc", digits = 4, ...)
```

## **Arguments**

object	Object of Class bootstatespace.
alpha	Numeric vector. Significance level $\alpha.$ If alpha = NULL, use the argument alpha used in object.
type	Charater string. Confidence interval type, that is, type = "pc" for percentile; type = "bc" for bias corrected.
digits	Digits to print.
	additional arguments.

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#### Value

Returns a matrix of estimates, standard errors, number of bootstrap replications, and confidence intervals.

#### Author(s)

Ivan Jacob Agaloos Pesigan

vcov.bootstatespace

Sampling Variance-Covariance Matrix Method for an Object of Class bootstatespace

## Description

Sampling Variance-Covariance Matrix Method for an Object of Class bootstatespace

## Usage

```
## S3 method for class 'bootstatespace'
vcov(object, ...)
```

#### **Arguments**

object Object of Class bootstatespace.
... additional arguments.

## Value

Returns the variance-covariance matrix of estimates.

## Author(s)

Ivan Jacob Agaloos Pesigan

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