## Reticular Action Model (RAM) Notation Notes

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## Chapter 1

# Description

This is a collection of my personal notes on the Reticular Action Model (RAM) notation that accompanies the ramR package (Pesigan, 2021) in the R statistical environment (R Core Team, 2020). You can install the released version of ramR from GitHub with:

remotes::install\_github("jeksterslab/ramR")

These notes are based on the following resources:

- Boker and McArdle (2005)
- McArdle and McDonald (1984)
- McArdle (2005)

See GitHub Pages for the html deployment.

## Chapter 2

# Reticular Action Model (RAM) Matrix Notation

#### 2.1 Full Model

#### Definition 2.1.

$$\mathbf{v} = \mathbf{A}\mathbf{v} + \mathbf{u} \tag{2.1}$$

where

- $\mathbf{v}$  and  $\mathbf{u}$  are  $t \times 1$  vectors of random variables
- A is a  $t \times t$  matrix of directed or asymmetric relationship from column variable  $v_i$  to row variable  $v_i$ 
  - A represent the regression of each of the t variables  $\mathbf{v}$  on the other t-1 variables
  - diagonal  $a_{i,i}$  is zero
  - $u_i$  represent the residual of  $v_i$
  - if all regression coefficients on other variables are zero, then the variable  $v_i$  is considered the same as its own residual  $u_i$

#### Definition 2.2.

$$\mathbf{S} = \mathbb{E}\left\{\mathbf{u}\mathbf{u}'\right\},\tag{2.2}$$

where

- **S** is a  $t \times t$  matrix of undirected or symmetric relationship
  - the notation  $\Omega$  is used in other sources for **S**
- $\mathbb{E}$  is the expectation operator

#### Definition 2.3.

$$\mathbf{C} = \mathbb{E}\left\{\mathbf{v}\mathbf{v}'\right\},\tag{2.3}$$

where

- C is a  $t \times t$  variance-covariance matrix
  - the notation  $\Sigma$  is used in other sources for **C**

#### Definition 2.4.

$$v = Av + u$$

can be rewritten as

$$\mathbf{v} - \mathbf{A}\mathbf{v} = \mathbf{u}$$
  
 $\mathbf{u} = \mathbf{v} - \mathbf{A}\mathbf{v}$   
 $\mathbf{u} = (\mathbf{I} - \mathbf{A})\mathbf{v}$  (2.4)

assuming that  $(\mathbf{I} - \mathbf{A})$  is non-singular,

$$\mathbf{E} = (\mathbf{I} - \mathbf{A})^{-1} \tag{2.5}$$

then

$$\mathbf{v} = (\mathbf{I} - \mathbf{A})^{-1} \mathbf{u}$$

$$= \mathbf{E}\mathbf{u}.$$
(2.6)

Using the definitions above, S and C are given by

$$\mathbf{S} = (\mathbf{I} - \mathbf{A}) \mathbf{C} (\mathbf{I} - \mathbf{A})^{-1}$$

$$= \mathbf{E}^{-1} \mathbf{C} (\mathbf{E}^{-1})^{\mathsf{T}}$$
(2.7)

$$\mathbf{C} = (\mathbf{I} - \mathbf{A})^{-1} \mathbf{S} \left[ (\mathbf{I} - \mathbf{A})^{-1} \right]^{\mathsf{T}}$$

$$= \mathbf{E} \mathbf{S} \mathbf{E}^{\mathsf{T}}$$
(2.8)

# 2.2 Observed/Manifest/Given Variables vs. Unobserved/Latent/Hidden Variables

Definition 2.5.

$$\mathbf{v} = \begin{bmatrix} \mathbf{g}_{p \times 1} \\ \mathbf{h}_{q \times 1} \end{bmatrix} \tag{2.9}$$

$$t = p + q \tag{2.10}$$

- $\mathbf{g}$  may be considered observed, manifest or given variables
- h may be considered unobserved, latent, or hidden variables

#### Definition 2.6.

$$\mathbf{F} = \left[ \mathbf{I}_{p \times p} : \mathbf{0}_{p \times q} \right] \tag{2.11}$$

 $\bullet$  the **F** matrix acts as a *filter* to select the manifest variables out of the full set of manifest and latent variables

$$\mathbf{g} = \mathbf{F}\mathbf{v} \tag{2.12}$$

$$\mathbf{g} = \mathbf{F} \left( \mathbf{I} - \mathbf{A} \right)^{-1} \mathbf{u}$$

$$= \mathbf{FE} \mathbf{u}$$
(2.13)

Definition 2.7.

$$\mathbf{M} = \mathbb{E}\left\{\mathbf{g}\mathbf{g}^{\mathsf{T}}\right\} \tag{2.14}$$

$$\mathbf{M} = \mathbf{F} (\mathbf{I} - \mathbf{A})^{-1} \mathbf{S} \left[ (\mathbf{I} - \mathbf{A})^{-1} \right]^{\mathsf{T}} \mathbf{F}^{\mathsf{T}}$$

$$= \mathbf{F} \mathbf{E} \mathbf{S} \mathbf{E}^{\mathsf{T}} \mathbf{F}^{\mathsf{T}}$$

$$= \mathbf{F} \mathbf{C} \mathbf{F}^{\mathsf{T}}$$
(2.15)

- when components of  ${\bf v}$  are permuted, the columns of  ${\bf F}$  can be correspondingly permuted
- ullet the rows and columns of  ${f C}$  that are filtered out by  ${f F}$  contain useful information about the latent variable structure.

The equations above completely define RAM.

## Chapter 3

# Reticular Action Model (RAM) Path Diagram

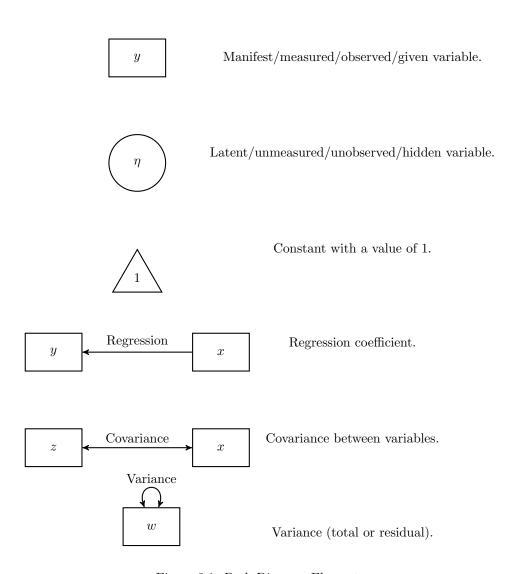
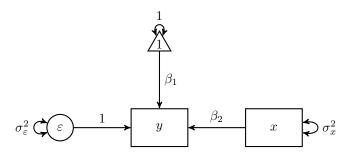


Figure 3.1: Path Diagram Elements



$$y = \alpha + \beta x + \varepsilon$$

Figure 3.2: Two-Variable Regression Model

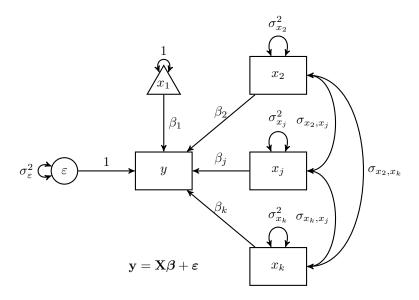


Figure 3.3: k-Variable Regression Model

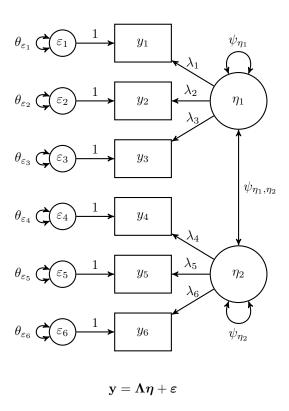


Figure 3.4: Two-Factor Confirmatory Factor Analysis Model

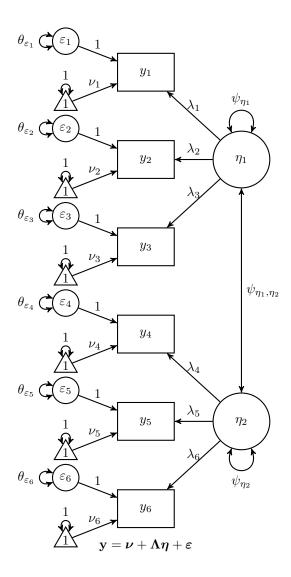
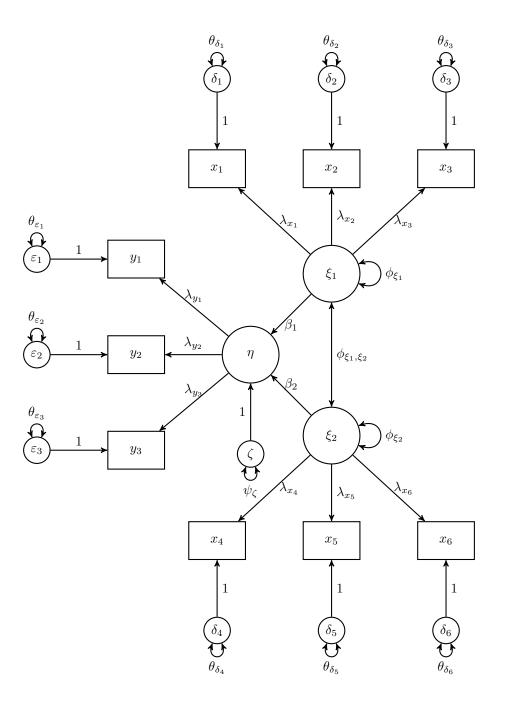


Figure 3.5: Two-Factor Confirmatory Factor Analysis Model with Mean Structure



$$oldsymbol{\eta} = \mathbf{B}oldsymbol{\eta} + \Gammaoldsymbol{\xi} + oldsymbol{\zeta}, \mathbf{y} = oldsymbol{\Lambda}_yoldsymbol{\eta} + oldsymbol{arepsilon}, \mathbf{x} = oldsymbol{\Lambda}_xoldsymbol{\xi} + oldsymbol{\delta}$$

Figure 3.6: Path Model with Latent Variables

## Chapter 4

## Student's t-test

In this section, the Student's t-test is presented as a structural equation model using the RAM notation. Let y be a continuous dependent variable, x be a dichotomous independent variable ( $x = \{0, 1\}$ ), and  $\varepsilon$  be the stochastic error term with mean 0 and constant variance of  $\sigma_{\varepsilon}^2$  across the values of x. The associations of the variables are given by

$$y = \alpha + \beta x + \varepsilon$$

where

- $\alpha$  is the expected value of y when x = 0
- $\beta$  is the unit change in y for unit change in x
- $\alpha + \beta$  is the expected value of y when x = 1

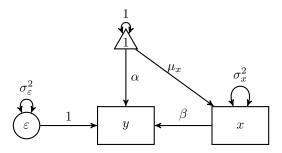


Figure 4.1: Student's t-test

### 4.1 Symbolic

Let  $\{y, x, \varepsilon\}$  be the variables of interest.

$$\mathbf{A} = \left( \begin{array}{ccc} 0 & \beta & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{array} \right)$$

$$\mathbf{S} = \left( \begin{array}{ccc} 0 & 0 & 0 \\ 0 & \sigma_x^2 & 0 \\ 0 & 0 & \sigma_\varepsilon^2 \end{array} \right)$$

$$\begin{split} \mathbf{C} &= \left(\mathbf{I} - \mathbf{A}\right)^{-1} \mathbf{S} \left[ \left(\mathbf{I} - \mathbf{A}\right)^{-1} \right]^\mathsf{T} \\ &= \mathbf{E} \mathbf{S} \mathbf{E}^\mathsf{T} \\ &= \begin{pmatrix} 1 & \beta & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 0 & 0 & 0 \\ 0 & \sigma_x^2 & 0 \\ 0 & 0 & \sigma_\varepsilon^2 \end{pmatrix} \begin{pmatrix} 1 & \beta & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}^\mathsf{T} \\ &= \begin{pmatrix} \sigma_x^2 \beta^2 + \sigma_\varepsilon^2 & \beta \sigma_x^2 & \sigma_\varepsilon^2 \\ \sigma_x^2 \beta & \sigma_x^2 & 0 \\ \sigma_\varepsilon^2 & 0 & \sigma_\varepsilon^2 \end{pmatrix} \end{split}$$

$$\mathbf{F} = \left( \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \end{array} \right)$$

$$\begin{split} \mathbf{M} &= \mathbf{F} \left( \mathbf{I} - \mathbf{A} \right)^{-1} \mathbf{S} \left[ \left( \mathbf{I} - \mathbf{A} \right)^{-1} \right]^{\mathsf{T}} \mathbf{F}^{\mathsf{T}} \\ &= \mathbf{F} \mathbf{E} \mathbf{S} \mathbf{E}^{\mathsf{T}} \mathbf{F}^{\mathsf{T}} \\ &= \mathbf{F} \mathbf{C} \mathbf{F}^{\mathsf{T}} \\ &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} \sigma_x^2 \beta^2 + \sigma_\varepsilon^2 & \beta \sigma_x^2 & \sigma_\varepsilon^2 \\ \sigma_x^2 \beta & \sigma_x^2 & 0 \\ \sigma_\varepsilon^2 & 0 & \sigma_\varepsilon^2 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}^{\mathsf{T}} \\ &= \begin{pmatrix} \sigma_x^2 \beta^2 + \sigma_\varepsilon^2 & \beta \sigma_x^2 \\ \sigma_x^2 \beta & \sigma_x^2 \end{pmatrix} \end{split}$$

$$\begin{split} \mathbf{v} &= \left(\mathbf{I} - \mathbf{A}\right)^{-1} \mathbf{u} \\ &= \left[ \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} - \begin{pmatrix} 0 & \beta & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \right]^{-1} \begin{pmatrix} \alpha \\ \mu_x \\ 0 \end{pmatrix} \\ &= \begin{pmatrix} \alpha + \beta \mu_x \\ \mu_x \\ 0 \end{pmatrix} \end{split}$$

4.1. SYMBOLIC 19

$$\begin{split} \mathbf{u} &= \left(\mathbf{I} - \mathbf{A}\right) \mathbf{v} \\ &= \left[ \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} - \begin{pmatrix} 0 & \beta & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \right] \begin{pmatrix} \alpha + \beta \mu_x \\ \mu_x \\ 0 \end{pmatrix} \\ &= \begin{pmatrix} \alpha \\ \mu_x \\ 0 \end{pmatrix} \end{split}$$

$$\begin{split} \mathbf{g} &= \mathbf{F} \left( \mathbf{I} - \mathbf{A} \right)^{-1} \mathbf{u} \\ &= \left[ \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} - \begin{pmatrix} 0 & \beta & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \right]^{-1} \begin{pmatrix} \alpha \\ \mu_x \\ 0 \end{pmatrix} \\ &= \begin{pmatrix} \alpha + \beta \mu_x \\ \mu_x \end{pmatrix} \end{split}$$

#### 4.1.1 Using the ramR Package

```
Α
```

```
## y x e
## y "0" "beta" "1"
## x "0" "0" "0"
## e "0" "0" "0"
```

S

u

```
## u
## y "alpha"
## x "mu[x]"
## e "0"
```

filter

```
## y x e
## y 1 0 0
## x 0 1 0
```

The covariance expectations can be symbolically derived using the  $\mathtt{ramR}::\mathtt{C\_sym}()$  function.

si

si

ramR::C\_sym(A, S)

$$\mathbf{C} = \left( \begin{array}{ccc} \sigma_x^2 \beta^2 + \sigma_\varepsilon^2 & \beta \sigma_x^2 & \sigma_\varepsilon^2 \\ \sigma_x^2 \beta & \sigma_x^2 & 0 \\ \sigma_\varepsilon^2 & 0 & \sigma_\varepsilon^2 \end{array} \right)$$

The covariance expectations for the observed variables can be symbolically derived using the ramR::M\_sym() function.

ramR::M\_sym(A, S, filter)

```
## {{sigma[x]^2*beta^2+sigma[varepsilon]^2, beta*sigma[x]^2},
## { sigma[x]^2*beta, sigma[x]^2}}
```

$$\mathbf{M} = \left( egin{array}{cc} \sigma_x^2 eta^2 + \sigma_arepsilon^2 & eta \sigma_x^2 \ \sigma_x^2 eta & \sigma_x^2 \end{array} 
ight)$$

The mean expectations can be symbolically derived using the ramR::v\_sym() function.

ramR::v\_sym(A, u)

$$\mathbf{v} = \left(\begin{array}{c} \alpha + \beta \mu_x \\ \mu_x \\ 0 \end{array}\right)$$

The mean expectations for the observed variables can be symbolically derived using the ramR::g\_sym() function.

ramR::g\_sym(A, u, filter)

$$\mathbf{g} = \left(\begin{array}{c} \alpha + \beta \mu_x \\ \mu_x \end{array}\right)$$

### 4.2 Numerical Example

Let df be a random sample with the following parameters

Parameter	\$x = 0\$	x = 1
Sample Size	500	500
\$\mu\$	0	1
\$\sigma^2\$	1	1

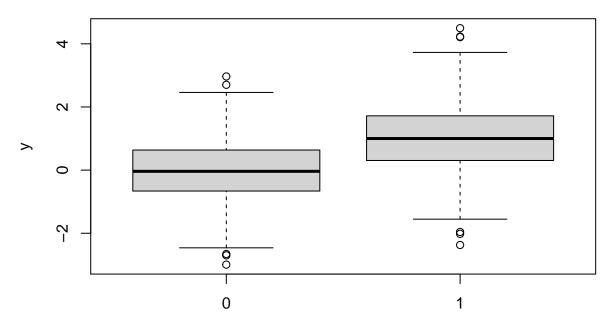
Parameter	Description	Estimate
\$\alpha\$	Mean of $x = 0$ .	0
\$\beta\$	Mean of $x = 1$ minus $x = 0$ .	1

#### head(df)

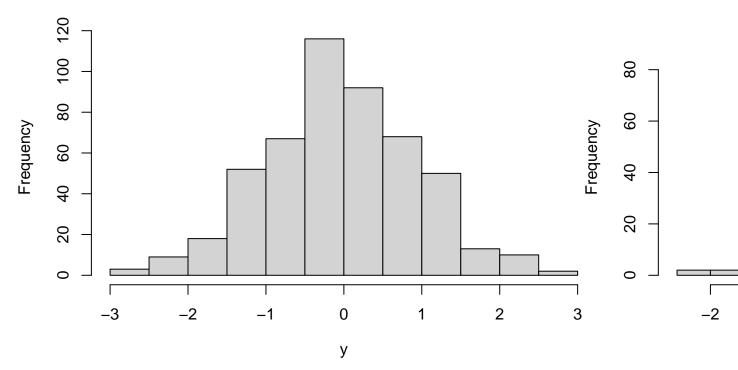
```
## y x
## 1 1.3709584 0
## 2 -0.5646982 0
## 3 0.3631284 0
## 4 0.6328626 0
## 5 0.4042683 0
## 6 -0.1061245 0
```

#### summary(df)

```
##
    {\tt Min.}
                        {\tt Min.}
##
            :-2.9931
                               :0.0
    1st Qu.:-0.2770
                        1st Qu.:0.0
##
##
    Median : 0.4503
                        Median:0.5
            : 0.4742
    Mean
                        Mean
                                :0.5
##
    3rd Qu.: 1.2492
                        3rd Qu.:1.0
    Max.
            : 4.4953
                        Max.
                                :1.0
```



### Histogram of y for x = 0



#### **4.2.1** *t*-test

```
t.test(y ~ x, data = df)

##

## Welch Two Sample t-test

##

## data: y by x

## t = -15.897, df = 994.36, p-value < 2.2e-16

## alternative hypothesis: true difference in means is not equal to 0

## 95 percent confidence interval:

## -1.1329278 -0.8839594

## sample estimates:

## mean in group 0 mean in group 1

## -0.03004622 0.97839737</pre>
```

#### 4.2.2 Linear Regression

```
summary(lm(y ~ x, data = df))

##
## Call:
## lm(formula = y ~ x, data = df)
##
```

```
## Residuals:
      Min 1Q Median
                            3Q
                                    Max
## -3.3501 -0.6517 0.0086 0.6858 3.5169
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.03005 0.04486 -0.67
                         0.06344 15.90 <2e-16 ***
## x
              1.00844
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.003 on 998 degrees of freedom
## Multiple R-squared: 0.2021, Adjusted R-squared: 0.2013
## F-statistic: 252.7 on 1 and 998 DF, p-value: < 2.2e-16
```

#### 4.2.3 Structural Equation Modeling

#### 4.2.3.1 lavaan (Rosseel, 2012)

```
model <- "
    y ~ x
"

fit <- lavaan::sem(
    model,
    data = df,
    meanstructure = TRUE,
    fixed.x = FALSE
)
lavaan::summary(fit)</pre>
```

```
## lavaan 0.6-7 ended normally after 12 iterations
##
##
    Estimator
                                                        ML
##
    Optimization method
                                                    NLMINB
    Number of free parameters
##
                                                         5
##
##
     Number of observations
                                                      1000
##
## Model Test User Model:
##
##
                                                     0.000
     Test statistic
##
     Degrees of freedom
##
## Parameter Estimates:
##
    Standard errors
                                                  Standard
##
##
     Information
                                                  Expected
##
     Information saturated (h1) model
                                                Structured
##
## Regressions:
##
                     Estimate Std.Err z-value P(>|z|)
##
    у ~
```

```
##
                         1.008
                                  0.063
                                         15.913
                                                    0.000
       Х
##
## Intercepts:
##
                      Estimate Std.Err z-value P(>|z|)
##
                        -0.030
                                  0.045
                                          -0.671
                                                    0.503
      .у
##
                         0.500
                                  0.016
                                          31.623
                                                    0.000
##
## Variances:
##
                      Estimate Std.Err z-value P(>|z|)
##
                        1.004
                                  0.045
      . у
                                         22.361
                                                    0.000
##
                         0.250
                                  0.011
                                          22.361
                                                    0.000
       х
```

#### 4.2.3.2 OpenMx (Boker et al., 2020)

RAM matrices can be used to specify models in OpenMx. Note, however, that the u vector in the RAM notation is M in the OpenMx notation.

```
mxData <- OpenMx::mxData(</pre>
  observed = df,
  type = "raw"
)
mxA <- OpenMx::mxMatrix(</pre>
  type = "Full",
  nrow = 3,
  ncol = 3,
  free = c(
    F, T, F,
    F, F, F,
    F, F, F
  ),
  values = c(
    0, 0.20, 1,
    0, 0, 0,
    0, 0, 0
  ),
  labels = c(
    NA, "beta", NA,
    NA, NA, NA,
    NA, NA, NA
  ),
  byrow = TRUE,
  name = "mxA"
)
mxS <- OpenMx::mxMatrix(</pre>
  type = "Symm",
  nrow = 3,
  ncol = 3,
  free = c(
   F, F, F,
   F, T, F,
   F, F, T
  ),
values = c(
```

```
0, 0, 0,
    0, 0.20, 0,
    0, 0, 0.20
  ),
 labels = c(
    NA, NA, NA,
    NA, "sigma2x", NA,
   NA, NA, "sigma2e"
  ),
  byrow = TRUE,
 name = "mxS"
mxM <- OpenMx::mxMatrix(</pre>
 type = "Full",
 nrow = 1,
 ncol = 3,
 free = c(
   T, T, F
  ),
  values = c(
   0.20,
    0.20,
    0
  ),
  labels = c(
   "alpha",
   "mux",
   NA
 byrow = TRUE,
  name = "mxM"
mxF <- OpenMx::mxMatrix(</pre>
 type = "Full",
 nrow = 2,
 ncol = 3,
 free = FALSE,
 values = c(
  1, 0, 0,
   0, 1, 0
  ),
  byrow = TRUE,
 name = "mxF"
expRAM <- OpenMx::mxExpectationRAM(</pre>
A = "mxA"
 S = "mxS",
 F = "mxF",
 M = "mxM"
  dimnames = c(
    "y",
    "x",
    "e"
```

```
)
)
objML <- OpenMx::mxFitFunctionML()
mxMod <- OpenMx::mxModel(
    name = "Model",
    data = mxData,
    matrices = list(
        mxA,
        mxS,
        mxF,
        mxM
),
    expectation = expRAM,
    fitfunction = objML
)
fit <- OpenMx::mxRun(mxMod)</pre>
```

## Running Model with 5 parameters

#### summary(fit)

```
## Summary of Model
##
## free parameters:
       name matrix row col Estimate Std.Error A
##
       beta mxA 1 2 1.00844356 0.06337369
## 1
## 2 sigma2x mxS 2 2 0.25000000 0.01118034
## 3 sigma2e mxS 3 1.00402596 0.04490152
## 4
     alpha mxM 1 y -0.03004621 0.04481202
## 5
        mux
             mxM
                   1 x 0.49999999 0.01581140
##
## Model Statistics:
               | Parameters | Degrees of Freedom | Fit (-2lnL units)
##
##
         Model:
                            5
                                               1995
                                                                4293.478
##
     Saturated:
                            5
                                               1995
                                                                      NA
## Independence:
                                               1996
                                                                      NA
## Number of observations/statistics: 1000/2000
## Information Criteria:
       | df Penalty | Parameters Penalty | Sample-Size Adjusted
## AIC:
           303.4776
                                  4303.478
                                                           4303.538
           -9487.4941
## BIC:
                                   4328.016
                                                           4312.136
## CFI: NA
## TLI: 1 (also known as NNFI)
## RMSEA: O [95% CI (NA, NA)]
## Prob(RMSEA <= 0.05): NA
## To get additional fit indices, see help(mxRefModels)
## timestamp: 2021-01-23 18:43:07
## Wall clock time: 0.04290342 secs
## optimizer: SLSQP
## OpenMx version number: 2.18.1
## Need help? See help(mxSummary)
```

#### 4.2.4 Using the ramR Package

```
## y 0 1.008444 1
## x 0 0.000000 0
## e 0 0.000000 0
## y 0 0.0000000 0.000000
## x 0 0.2502503 0.000000
## e 0 0.000000 1.006038
##
## y -0.03004622
## x 0.50000000
## e 0.00000000
filter
## y x e
## y 1 0 0
## x 0 1 0
The covariance expectations can be numerically derived using the ramR::C_num() function.
ramR::C_num(A, S)
             У
## y 1.2605321 0.2523633 1.006038
## x 0.2523633 0.2502503 0.000000
## e 1.0060380 0.0000000 1.006038
The covariance expectations for the observed variables can be numerically derived using the ramR::M_num()
function.
ramR::M_num(A, S, filter)
             У
## y 1.2605321 0.2523633
```

The mean expectations can be numerically derived using the ramR::v\_num() function.

## x 0.2523633 0.2502503

```
ramR::v_num(A, u)

## v
## y 0.4741756
## x 0.5000000
## e 0.0000000
```

The mean expectations for the observed variables can be numerically derived using the ramR::v\_num() function.

```
ramR::g_num(A, u, filter)

## g
## y 0.4741756
## x 0.5000000
```

### 4.3 Equations to RAM

The ramR package has a utility function to convert structural equations to RAM notation. The Student's t-test can be expressed in the following equations

```
eq <- "
 # VARIABLE1 OPERATION VARIABLE2 LABEL
                                   1
                        У
                                   beta
 у
              on
                        X
              with
                                   sigma[varepsilon]^2
  е
                         е
                                   sigma[x]^2
              with
 X
                        X
                                   alpha
              on
                         1
 У
                                   mu[x]
                         1
 X
              on
```

The error term is treated as a latent variable and defined with the operation by. It's value is constrained to 1. The regression of y on x is defined by operation on. It is labeled as beta. The variance of x and the error variance are defined using the operation with. These are labeled sigma[x]^2 and sigma[varepsilon]^2 respectively. The intercept and the mean of x are defined using the operation on 1. These are labeled alpha and mu[x] respectively.

The ramR::eq2ram converts the equations to RAM notation.

```
ramR::eq2ram(eq)
```

```
## $eq
##
                                     label
     var1
             op var2
## 1
             by
                   У
## 2
                                      beta
        У
             on
                   Х
                   e sigma[varepsilon]^2
## 3
        e with
## 4
                               sigma[x]^2
        x with
                   Х
## 5
                   1
                                     alpha
        у
             on
## 6
                                     mu[x]
             on
                   1
##
```

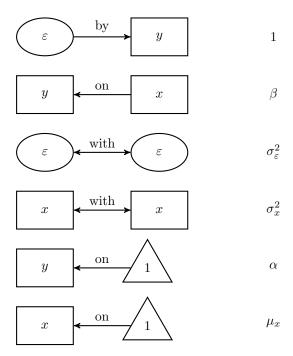


Figure 4.2: Student's t-test's Structural Equations

```
## $variables
## [1] "y" "x" "e"
## $A
     У
         Х
## y "0" "beta" "1"
## x "0" "0"
                "0"
## e "0" "0"
                "0"
##
## $S
##
    У
         Х
                      е
                       "0"
## y "0" "0"
## x "0" "sigma[x]^2" "0"
## e "0" "0"
                       "sigma[varepsilon]^2"
##
## $filter
    ухе
## y 1 0 0
## x 0 1 0
##
## $u
##
## y "alpha"
## x "mu[x]"
## e "0"
```

si

si

### 4.4 Equations to Expectations

The ramR package has a utility function to convert structural equations to expectations both symbolically and numerically.

```
eq <- "
 # VARIABLE1 OPERATION VARIABLE2 LABEL
                       У
                                 beta
 У
             on
                       X
                                sigma[varepsilon]^2
 е
             with
                       е
             with
                                 sigma[x]^2
                      X
                                 alpha
             on
                       1
 у
                       1
                                 mu[x]
             on
```

```
ramR::eq2exp_sym(eq)
```

```
## $variables
## [1] "y" "x" "e"
##
## $A
                     1},
## {{
        0, beta,
                     0},
##
        Ο,
              Ο,
##
                     0}}
        Ο,
##
## $S
## {{
                        0,
                                               0,
                                                                     0},
##
                        Ο,
                                     sigma[x]^2,
                                                                     0},
   {
                        0,
                                               0, sigma[varepsilon]^2}}
##
## $u
## {{alpha},
   {mu[x]},
    {
         0}}
##
##
## $filter
## {{1, 0, 0},
   {0, 1, 0}}
##
## $v
## {{alpha+beta*mu[x]},
   {
                mu[x]},
##
##
   {
                     0}}
##
## $g
## {{alpha+beta*mu[x]},
                mu[x]}}
##
   {
##
## $C
## {{sigma[x]^2*beta^2+sigma[varepsilon]^2,
                                                                      beta*sigma[x]^2,
                            sigma[x]^2*beta,
                                                                            sigma[x]^2,
##
   {
##
   {
                        sigma[varepsilon]^2,
                                                                                     0,
##
```

#### ramR::eq2exp\_num(eq)

```
## $variables
## [1] "y" "x" "e"
##
## $A
## y x e
## y 0 1 1
## x 0 0 0
## e 0 0 0
##
## $S
## y x e
## y 0 0.00 0
## x 0 0.25 0
## e 0 0.00 1
##
## $u
## u
## y 0.0
## x 0.5
## e 0.0
##
## $filter
## y x e
## y 1 0 0
## x 0 1 0
##
## $v
## v
## y 0.5
## x 0.5
## e 0.0
##
## $g
## g
## y 0.5
## x 0.5
```

##

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