

Zero-Order Correlation

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Scalar Notation

The zero-order correlation between X and Y is given by Equation (1)

$$\rho_{X,Y} = \frac{\sigma_{X,Y}}{\sigma_X \sigma_Y} \quad (1)$$

where $\sigma_{X,Y}$ is the covariance between X and Y , σ_X is the standard deviation of X , and σ_Y is the standard deviation of Y .

Matrix Notation

The correlation matrix from the covariance matrix is given by Equation (2)

$$\mathbf{P} = \text{diag}(\mathbf{\Sigma})^{-\frac{1}{2}} \mathbf{\Sigma} \text{diag}(\mathbf{\Sigma})^{-\frac{1}{2}} \quad (2)$$

where \mathbf{P} is the correlation matrix, $\mathbf{\Sigma}$ is the covariance matrix, $\text{diag}(\cdot)$ is an operator that creates a diagonal matrix from the diagonal elements of the input matrix $\mathbf{\Sigma}$.

Table 1: Variables

Variable	Symbol	Description
sigmacap_i	Σ	covariance matrix
rhocap_i	P	correlation matrix

Examples

$$\Sigma = \begin{pmatrix} 0.6856935 & -0.042434 & 1.2743154 & 0.5162707 \\ -0.042434 & 0.1899794 & -0.3296564 & -0.1216394 \\ 1.2743154 & -0.3296564 & 3.1162779 & 1.2956094 \\ 0.5162707 & -0.1216394 & 1.2956094 & 0.5810063 \end{pmatrix} \quad (3)$$

$$P = \begin{pmatrix} 1 & -0.1175698 & 0.8717538 & 0.8179411 \\ -0.1175698 & 1 & -0.4284401 & -0.3661259 \\ 0.8717538 & -0.4284401 & 1 & 0.9628654 \\ 0.8179411 & -0.3661259 & 0.9628654 & 1 \end{pmatrix} \quad (4)$$

```
library(rhoMatrix)
```

```
sigmacap_i

##           Sepal.Length Sepal.Width Petal.Length Petal.Width
## Sepal.Length    0.6856935  -0.0424340    1.2743154    0.5162707
## Sepal.Width     -0.0424340   0.1899794   -0.3296564   -0.1216394
## Petal.Length     1.2743154  -0.3296564    3.1162779    1.2956094
## Petal.Width      0.5162707  -0.1216394    1.2956094    0.5810063

rhocap_i

##           Sepal.Length Sepal.Width Petal.Length Petal.Width
```

```
## Sepal.Length    1.0000000 -0.1175698    0.8717538    0.8179411
## Sepal.Width     -0.1175698    1.0000000   -0.4284401   -0.3661259
## Petal.Length     0.8717538   -0.4284401    1.0000000    0.9628654
## Petal.Width      0.8179411   -0.3661259    0.9628654    1.0000000
```

Correlation Matrix from Covariance Matrix

```
cor_of_cov(sigmacap_i)
```

```
##           Sepal.Length Sepal.Width Petal.Length Petal.Width
## Sepal.Length    1.0000000 -0.1175698    0.8717538    0.8179411
## Sepal.Width     -0.1175698    1.0000000   -0.4284401   -0.3661259
## Petal.Length     0.8717538   -0.4284401    1.0000000    0.9628654
## Petal.Width      0.8179411   -0.3661259    0.9628654    1.0000000
```

```
cov2cor(sigmacap_i)
```

```
##           Sepal.Length Sepal.Width Petal.Length Petal.Width
## Sepal.Length    1.0000000 -0.1175698    0.8717538    0.8179411
## Sepal.Width     -0.1175698    1.0000000   -0.4284401   -0.3661259
## Petal.Length     0.8717538   -0.4284401    1.0000000    0.9628654
## Petal.Width      0.8179411   -0.3661259    0.9628654    1.0000000
```