Package 'simStateSpace'

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OU2SSM Sim2Matrix SimSSM SimSSMFixed

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Description

This function converts parameters from the Ornstein–Uhlenbeck model to state space model parameterization. See details for more information.

Usage

```
OU2SSM(mu, phi, sigma_sqrt, delta_t)
```

Arguments

mu	Numeric vector. The long-term mean or equilibrium level (μ) .
phi	Numeric matrix. The rate of mean reversion, determining how quickly the variable returns to its mean (Φ) .
sigma_sqrt	Numeric matrix. Cholesky decomposition of the matrix of volatility or randomness in the process (Σ) .
delta_t	Numeric. Time interval (δ_t) .

Details

The state space parameters as a function of the Ornstein-Uhlenbeck model parameters are given by

$$\boldsymbol{\beta} = \exp\left(-\boldsymbol{\Phi}\Delta_t\right)$$

$$oldsymbol{lpha} = -oldsymbol{\Phi}^{-1} \left(oldsymbol{eta} - \mathbf{I}_p
ight)$$

$$\operatorname{vec}\left(\boldsymbol{\Psi}\right) = \left\{ \left[\left(-\boldsymbol{\Phi} \otimes \mathbf{I}_{p} \right) + \left(\mathbf{I}_{p} \otimes -\boldsymbol{\Phi} \right) \right] \left[\exp\left(\left[\left(-\boldsymbol{\Phi} \otimes \mathbf{I}_{p} \right) + \left(\mathbf{I}_{p} \otimes -\boldsymbol{\Phi} \right) \right] \Delta_{t} \right) - \mathbf{I}_{p \times p} \right] \operatorname{vec}\left(\boldsymbol{\Sigma}\right) \right\}$$

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Value

Returns a list of state space parameters:

- alpha: Numeric vector. Vector of intercepts for the dynamic model (α) .
- beta: Numeric matrix. Transition matrix relating the values of the latent variables at time t 1 to those at time t (β).
- psi: Numeric matrix. The process noise covariance matrix (Ψ) .

Author(s)

Ivan Jacob Agaloos Pesigan

See Also

Other Simulation of State Space Models Data Functions: Sim2Matrix(), SimSSMFixed(), SimSSMLinGrowth(), SimSSMOUFixed(), SimSSMOUVary(), SimSSMOU(), SimSSMVARFixed(), SimSSMVARVary(), SimSSMVAR(), SimSSMVary(), Si

Examples

```
p <- k <- 2
mu <- c(5.76, 5.18)
phi <- matrix(data = c(0.10, -0.05, -0.05, 0.10), nrow = p)
sigma_sqrt <- chol(
    matrix(data = c(2.79, 0.06, 0.06, 3.27), nrow = p)
)
delta_t <- 0.10

OU2SSM(
    mu = mu,
    phi = phi,
    sigma_sqrt = sigma_sqrt,
    delta_t = delta_t
)</pre>
```

Sim2Matrix

Simulation Output to Matrix

Description

This function converts the output of SimSSM(), SimSSMOU(), SimSSMVAR(), SimSSMFixed(), SimSSMOUFixed(), SimSSMVARFixed(), SimSSMVARY(), or SimSSMVARVary() to a matrix.

Usage

```
Sim2Matrix(x, eta = FALSE, long = TRUE)
```

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Arguments

X	R object. Output of SimSSM(), SimSSMOU(), SimSSMVAR(), SimSSMFixed(),
	<pre>SimSSMOUFixed(), SimSSMVARFixed(), SimSSMVary(), SimSSMOUVary(), or SimSSMVARVary().</pre>
eta	Logical. If eta = TRUE, include eta. If eta = FALSE, exclude eta.
long	Logical. If long = TRUE, use long format. If long = FALSE, use wide format.

Value

Returns a matrix of simulated data.

Author(s)

Ivan Jacob Agaloos Pesigan

See Also

Other Simulation of State Space Models Data Functions: OU2SSM(), SimSSMFixed(), SimSSMLinGrowth(), SimSSMOUFixed(), SimSSMOUVary(), SimSSMOU(), SimSSMVARFixed(), SimSSMVARVary(), SimSSMVAR(), SimSSMVary(), SimSSM

```
# prepare parameters
set.seed(42)
k < -p < -3
iden <- diag(k)</pre>
iden_sqrt <- chol(iden)</pre>
null_vec <- rep(x = 0, times = k)
n <- 5
mu0 <- null_vec
sigma0_sqrt <- iden_sqrt</pre>
alpha <- null_vec</pre>
beta \leftarrow diag(x = 0.50, nrow = k)
psi_sqrt <- iden_sqrt</pre>
nu <- null_vec
lambda <- iden
theta_sqrt <- chol(diag(x = 0.50, nrow = k))
time <- 50
burn_in <- 0
# generate data
ssm <- SimSSM(
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
  psi_sqrt = psi_sqrt,
  nu = nu,
  lambda = lambda,
  theta_sqrt = theta_sqrt,
```

```
type = 0,
  time = time,
  burn_in = burn_in
)
# list to matrix
mat <- Sim2Matrix(ssm, long = TRUE)</pre>
str(mat)
head(mat)
mat <- Sim2Matrix(ssm, long = FALSE)</pre>
str(mat)
head(mat)
# generate data
ssm <- SimSSMFixed(</pre>
  n = n,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
  psi_sqrt = psi_sqrt,
  nu = nu,
  lambda = lambda,
  theta_sqrt = theta_sqrt,
  type = 0,
  time = time,
  burn_in = burn_in
)
# list to matrix
mat <- Sim2Matrix(ssm, long = TRUE)</pre>
str(mat)
head(mat)
mat <- Sim2Matrix(ssm, long = FALSE)</pre>
str(mat)
head(mat)
```

SimSSM

Simulate Data from a State Space Model (n = 1)

Description

This function simulates data from a state space model. See details for more information.

Usage

```
SimSSM(
  mu0,
  sigma0_sqrt,
```

```
alpha,
beta,
psi_sqrt,
nu,
lambda,
theta_sqrt,
gamma_y = NULL,
gamma_eta = NULL,
type = 0,
time,
burn_in = 0
)
```

Arguments

mu0	Numeric vector. Mean of initial latent variable values $(\mu_{\eta 0})$.
sigma0_sqrt	Numeric matrix. Cholesky decomposition of the covariance matrix of initial latent variable values ($\Sigma_{\eta 0}$).
alpha	Numeric vector. Vector of intercepts for the dynamic model (α) .
beta	Numeric matrix. Transition matrix relating the values of the latent variables at time $t-1$ to those at time $t(\beta)$.
psi_sqrt	Numeric matrix. Cholesky decomposition of the process noise covariance matrix (Ψ) .
nu	Numeric vector. Vector of intercepts for the measurement model (ν) .
lambda	Numeric matrix. Factor loading matrix linking the latent variables to the observed variables (Λ) .
theta_sqrt	Numeric matrix. Cholesky decomposition of the measurement error covariance matrix (Θ) .
gamma_y	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the observed variables at time t (Γ_y) .
gamma_eta	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the latent variables at time t (Γ_{η}).
Х	Numeric matrix. The matrix of observed covariates in type = 1 or type = 2. The number of rows should be equal to time + burn_in.
type	Integer. State space model type.
time	Positive integer. Number of time points to simulate.
burn_in	Positive integer. Number of burn-in points to exclude before returning the results.

Details

Type 0:

The measurement model is given by

$$\mathbf{y}_{t} = oldsymbol{
u} + oldsymbol{\Lambda} oldsymbol{\eta}_{t} + oldsymbol{arepsilon}_{t} \quad ext{with} \quad oldsymbol{arepsilon}_{t} \sim \mathcal{N}\left(\mathbf{0}, oldsymbol{\Theta}
ight)$$

where \mathbf{y}_t , $\boldsymbol{\eta}_t$, and $\boldsymbol{\varepsilon}_t$ are random variables and $\boldsymbol{\nu}$, $\boldsymbol{\Lambda}$, and $\boldsymbol{\Theta}$ are model parameters. \mathbf{y}_t is a vector of observed random variables, $\boldsymbol{\eta}_t$ is a vector of latent random variables, and $\boldsymbol{\varepsilon}_t$ is a vector of random measurement errors, at time t. $\boldsymbol{\nu}$ is a vector of intercepts, $\boldsymbol{\Lambda}$ is a matrix of factor loadings, and $\boldsymbol{\Theta}$ is the covariance matrix of $\boldsymbol{\varepsilon}$.

The dynamic structure is given by

$$oldsymbol{\eta}_t = oldsymbol{lpha} + oldsymbol{eta} oldsymbol{\eta}_{t-1} + oldsymbol{\zeta}_t \quad ext{with} \quad oldsymbol{\zeta}_t \sim \mathcal{N}\left(oldsymbol{0}, oldsymbol{\Psi}
ight)$$

where η_t , η_{t-1} , and ζ_t are random variables, and α , β , and Ψ are model parameters. η_t is a vector of latent variables at time t, η_{t-1} is a vector of latent variables at time t-1, and ζ_t is a vector of dynamic noise at time t. α is a vector of intercepts, β is a matrix of autoregression and cross regression coefficients, and Ψ is the covariance matrix of ζ_t .

Type 1:

The measurement model is given by

$$\mathbf{y}_{t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{t} + \boldsymbol{\varepsilon}_{t} \quad \mathrm{with} \quad \boldsymbol{\varepsilon}_{t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right).$$

The dynamic structure is given by

$$oldsymbol{\eta}_t = oldsymbol{lpha} + oldsymbol{eta} oldsymbol{\eta}_{t-1} + oldsymbol{\Gamma}_{oldsymbol{\eta}} \mathbf{x}_t + oldsymbol{\zeta}_t \quad ext{with} \quad oldsymbol{\zeta}_t \sim \mathcal{N}\left(\mathbf{0}, oldsymbol{\Psi}
ight)$$

where \mathbf{x}_t is a vector of covariates at time t, and Γ_{η} is the coefficient matrix linking the covariates to the latent variables.

Type 2:

The measurement model is given by

$$\mathbf{y}_{t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{t} + \boldsymbol{\Gamma}_{\mathbf{v}} \mathbf{x}_{t} + \boldsymbol{\varepsilon}_{t} \quad \text{with} \quad \boldsymbol{\varepsilon}_{t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right)$$

where $\Gamma_{\mathbf{v}}$ is the coefficient matrix linking the covariates to the observed variables.

The dynamic structure is given by

$$\boldsymbol{\eta}_{t} = \boldsymbol{\alpha} + \boldsymbol{\beta} \boldsymbol{\eta}_{t-1} + \boldsymbol{\Gamma}_{\boldsymbol{\eta}} \mathbf{x}_{t} + \boldsymbol{\zeta}_{t} \quad \text{with} \quad \boldsymbol{\zeta}_{t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Psi}\right).$$

Value

Returns a list with the following elements:

- y: A t by k matrix of values for the manifest variables.
- eta: A t by p matrix of values for the latent variables.
- x: A t by j matrix of values for the covariates.
- time: A vector of discrete time points from 0 to t 1.
- id: A vector of ones.

References

Chow, S.-M., Ho, M. R., Hamaker, E. L., & Dolan, C. V. (2010). Equivalence and differences between structural equation modeling and state-space modeling techniques. *Structural Equation Modeling: A Multidisciplinary Journal*, 17(2), 303–332. doi:10.1080/10705511003661553

See Also

Other Simulation of State Space Models Data Functions: OU2SSM(), Sim2Matrix(), SimSSMFixed(), SimSSMLinGrowth(), SimSSMOUFixed(), SimSSMOUVary(), SimSSMVARFixed(), SimSSMVARVary(), SimSSMVAR(), SimSSMVAry()

```
# prepare parameters
set.seed(42)
k <- p <- 3
iden <- diag(k)</pre>
iden_sqrt <- chol(iden)</pre>
null\_vec \leftarrow rep(x = 0, times = k)
mu0 <- null_vec
sigma0_sqrt <- iden_sqrt</pre>
alpha <- null_vec</pre>
beta <- diag(x = 0.50, nrow = k)
psi_sqrt <- iden_sqrt</pre>
nu <- null_vec</pre>
lambda <- iden
theta_sqrt <- chol(diag(x = 0.50, nrow = k))
time <- 50
burn_in <- 0
gamma_y <- gamma_eta <- 0.10 * diag(k)</pre>
x <- matrix(</pre>
 data = rnorm(n = k * (time + burn_in)),
  ncol = k
)
# Type 0
ssm <- SimSSM(
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
  psi_sqrt = psi_sqrt,
  nu = nu,
  lambda = lambda,
  theta_sqrt = theta_sqrt,
  type = 0,
  time = time,
  burn_in = burn_in
)
str(ssm)
# Type 1
ssm <- SimSSM(
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
```

```
psi_sqrt = psi_sqrt,
 nu = nu,
 lambda = lambda,
 theta_sqrt = theta_sqrt,
 gamma_eta = gamma_eta,
 x = x,
 type = 1,
 time = time,
 burn_in = burn_in
)
str(ssm)
# Type 2
ssm <- SimSSM(
 mu0 = mu0,
 sigma0_sqrt = sigma0_sqrt,
 alpha = alpha,
 beta = beta,
 psi_sqrt = psi_sqrt,
 nu = nu,
 lambda = lambda,
 theta_sqrt = theta_sqrt,
 gamma_y = gamma_y,
 gamma_eta = gamma_eta,
 x = x,
 type = 2,
 time = time,
 burn_in = burn_in
)
str(ssm)
```

SimSSMFixed

Simulate Data using a State Space Model Parameterization for n > 1 Individuals (Fixed Parameters)

Description

This function simulates data using a state space model parameterization for n > 1 individuals. In this model, the parameters are invariant across individuals.

Usage

```
SimSSMFixed(
   n,
   mu0,
   sigma0_sqrt,
   alpha,
```

```
beta,
psi_sqrt,
nu,
lambda,
theta_sqrt,
gamma_y = NULL,
gamma_eta = NULL,
x = NULL,
type = 0,
time,
burn_in = 0
)
```

Arguments

n

mu0	Numeric vector. Mean of initial latent variable values $(\mu_{\eta 0})$.
sigma0_sqrt	Numeric matrix. Cholesky decomposition of the covariance matrix of initial latent variable values $(\Sigma_{\eta 0})$.
alpha	Numeric vector. Vector of intercepts for the dynamic model (α) .

Positive integer. Number of individuals.

beta Numeric matrix. Transition matrix relating the values of the latent variables at

time t - 1 to those at time t (β) .

psi_sqrt Numeric matrix. Cholesky decomposition of the process noise covariance ma-

trix (Ψ) .

nu Numeric vector. Vector of intercepts for the measurement model (ν) .

lambda Numeric matrix. Factor loading matrix linking the latent variables to the ob-

served variables (Λ) .

theta_sqrt Numeric matrix. Cholesky decomposition of the measurement error covariance

matrix (Θ) .

gamma_y Numeric matrix. Matrix relating the values of the covariate matrix at time t to

the observed variables at time t ($\Gamma_{\rm v}$).

gamma_eta Numeric matrix. Matrix relating the values of the covariate matrix at time t to

the latent variables at time t (Γ_n) .

x A list of length n of numeric matrices. Each element of the list is a matrix of

observed covariates in type = 1 or type = 2. The number of rows in each matrix

should be equal to time + burn_in.

type Integer. State space model type.

time Positive integer. Number of time points to simulate.

burn_in Positive integer. Number of burn-in points to exclude before returning the re-

sults.

Details

Type 0:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t} \quad ext{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right)$$

where $\mathbf{y}_{i,t}$, $\eta_{i,t}$, and $\varepsilon_{i,t}$ are random variables and ν , Λ , and Θ are model parameters. $\mathbf{y}_{i,t}$ is a vector of observed random variables, $\eta_{i,t}$ is a vector of latent random variables, and $\varepsilon_{i,t}$ is a vector of random measurement errors, at time t and individual i. ν is a vector of intercepts, Λ is a matrix of factor loadings, and Θ is the covariance matrix of ε .

The dynamic structure is given by

$$oldsymbol{\eta}_{i,t} = oldsymbol{lpha} + oldsymbol{eta} oldsymbol{\eta}_{i,t-1} + oldsymbol{\zeta}_{i,t} \quad ext{with} \quad oldsymbol{\zeta}_{i,t} \sim \mathcal{N}\left(oldsymbol{0}, oldsymbol{\Psi}
ight)$$

where $\eta_{i,t}$, $\eta_{i,t-1}$, and $\zeta_{i,t}$ are random variables, and α , β , and Ψ are model parameters. $\eta_{i,t}$ is a vector of latent variables at time t and individual i, $\eta_{i,t-1}$ is a vector of latent variables at time t-1 and individual i, and $\zeta_{i,t}$ is a vector of dynamic noise at time t and individual i. α is a vector of intercepts, β is a matrix of autoregression and cross regression coefficients, and Ψ is the covariance matrix of $\zeta_{i,t}$.

Type 1:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t} \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right).$$

The dynamic structure is given by

$$oldsymbol{\eta}_{i,t} = oldsymbol{lpha} + oldsymbol{eta} oldsymbol{\eta}_{i,t-1} + oldsymbol{\Gamma}_{oldsymbol{\eta}} \mathbf{x}_{i,t} + oldsymbol{\zeta}_{i,t} \quad ext{with} \quad oldsymbol{\zeta}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, oldsymbol{\Psi}
ight)$$

where $\mathbf{x}_{i,t}$ is a vector of covariates at time t and individual i, and Γ_{η} is the coefficient matrix linking the covariates to the latent variables.

Type 2:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\Gamma}_{\mathbf{v}} \mathbf{x}_{i,t} + \boldsymbol{\varepsilon}_{i,t} \quad ext{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right)$$

where $\Gamma_{\mathbf{y}}$ is the coefficient matrix linking the covariates to the observed variables.

The dynamic structure is given by

$$oldsymbol{\eta}_{i,t} = oldsymbol{lpha} + oldsymbol{eta} oldsymbol{\eta}_{i,t-1} + oldsymbol{\Gamma}_{oldsymbol{\eta}} \mathbf{x}_{i,t} + oldsymbol{\zeta}_{i,t} \quad ext{with} \quad oldsymbol{\zeta}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, oldsymbol{\Psi}
ight).$$

Value

Returns a list of length n. Each element is a list with the following elements:

- y: A t by k matrix of values for the manifest variables.
- eta: A t by p matrix of values for the latent variables.
- x: A t by j matrix of values for the covariates.
- time: A vector of discrete time points from 1 to t.
- id: A vector of ID numbers of length t.

Author(s)

Ivan Jacob Agaloos Pesigan

References

Chow, S.-M., Ho, M. R., Hamaker, E. L., & Dolan, C. V. (2010). Equivalence and differences between structural equation modeling and state-space modeling techniques. *Structural Equation Modeling: A Multidisciplinary Journal*, 17(2), 303–332. doi:10.1080/10705511003661553

See Also

Other Simulation of State Space Models Data Functions: OU2SSM(), Sim2Matrix(), SimSSMLinGrowth(), SimSSMOUFixed(), SimSSMOUVary(), SimSSMOU(), SimSSMVARFixed(), SimSSMVARVary(), SimSSMVAR(), SimSSMVary(), SimSSM()

```
# prepare parameters
set.seed(42)
k < -p < -3
iden <- diag(k)</pre>
iden_sqrt <- chol(iden)</pre>
null_vec <- rep(x = 0, times = k)
n <- 5
mu0 <- null_vec
sigma0_sqrt <- iden_sqrt</pre>
alpha <- null_vec</pre>
beta \leftarrow diag(x = 0.50, nrow = k)
psi_sqrt <- iden_sqrt</pre>
nu <- null_vec
lambda <- iden
theta_sqrt <- chol(diag(x = 0.50, nrow = k))
time <- 50
burn_in <- 0</pre>
gamma_y \leftarrow gamma_eta \leftarrow 0.10 * diag(k)
x <- lapply(
  X = seq_len(n),
  FUN = function(i) {
    return(
      matrix(
         data = rnorm(n = k * (time + burn_in)),
         ncol = k
  }
# Type 0
ssm <- SimSSMFixed(</pre>
  n = n,
  mu0 = mu0,
```

```
sigma0_sqrt = sigma0_sqrt,
 alpha = alpha,
 beta = beta,
 psi_sqrt = psi_sqrt,
 nu = nu,
 lambda = lambda,
 theta_sqrt = theta_sqrt,
 type = 0,
 time = time,
 burn_in = burn_in
)
str(ssm)
# Type 1
ssm <- SimSSMFixed(</pre>
 n = n,
 mu0 = mu0,
 sigma0_sqrt = sigma0_sqrt,
 alpha = alpha,
 beta = beta,
 psi_sqrt = psi_sqrt,
 nu = nu,
 lambda = lambda,
 theta_sqrt = theta_sqrt,
 gamma_eta = gamma_eta,
 x = x,
 type = 1,
 time = time,
 burn_in = burn_in
)
str(ssm)
# Type 2
ssm <- SimSSMFixed(</pre>
 n = n,
 mu0 = mu0,
 sigma0_sqrt = sigma0_sqrt,
 alpha = alpha,
 beta = beta,
 psi_sqrt = psi_sqrt,
 nu = nu,
 lambda = lambda,
 theta_sqrt = theta_sqrt,
 gamma_y = gamma_y,
 gamma_eta = gamma_eta,
 x = x,
 type = 2,
 time = time,
 burn_in = burn_in
)
```

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str(ssm)

 ${\tt SimSSMLinGrowth}$

Simulate Data from a Linear Growth Curve Model

Description

This function simulates data from a linear growth curve model.

Usage

```
SimSSMLinGrowth(
    n,
    mu0,
    sigma0_sqrt,
    theta_sqrt,
    gamma_y = NULL,
    gamma_eta = NULL,
    x = NULL,
    type = 0,
    time
)
```

Arguments

n	Positive integer. Number of individuals.
mu0	Numeric vector. A vector of length two. The first element is the mean of the intercept, and the second element is the mean of the slope.
sigma0_sqrt	Numeric matrix. Cholesky decomposition of the covariance matrix of the intercept and the slope.
theta_sqrt	Numeric. Square root of the common measurement error variance.
gamma_y	Numeric matrix. Matrix relating the values of the covariate matrix at time t to y at time t $(\Gamma_{\mathbf{y}}).$
gamma_eta	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the latent variables (intercept and slope) at time t (Γ_{η}) .
х	A list of length n of numeric matrices. Each element of the list is a matrix of observed covariates in type = 1 or type = 2. The number of rows in each matrix should be equal to time.
type	Integer. State space model type.
time	Positive integer. Number of time points to simulate.

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Details

Type 0:

The measurement model is given by

$$y_{i,t} = \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} \eta_{0_{i,t}} \\ \eta_{1_{i,t}} \end{pmatrix} + \boldsymbol{\varepsilon}_{i,t} \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(0, \theta^2\right)$$

where $y_{i,t}$, $\eta_{0_{i,t}}$, $\eta_{1_{i,t}}$, and $\varepsilon_{i,t}$ are random variables and and θ^2 is a model parameter. $y_{i,t}$ is a vector of observed random variables at time t and individual i, $\eta_{0_{i,t}}$, $\eta_{1_{i,t}}$ is forms a vector of latent random variables at time t and individual i, and $\varepsilon_{i,t}$ is a vector of random measurement errors at time t and individual i, and θ^2 is the variance of ε .

The dynamic structure is given by

$$\left(\begin{array}{c} \eta_{0_{i,t}} \\ \eta_{1_{i,t}} \end{array}\right) = \left(\begin{array}{cc} 1 & 1 \\ 0 & 1 \end{array}\right) \left(\begin{array}{c} \eta_{0_{i,t}} \\ \eta_{1_{i,t}} \end{array}\right).$$

The mean vector and covariance matrix of the intercept and slope are captured in the mean vector and covariance matrix of the initial condition given by

$$\mu_{\eta|0} = \begin{pmatrix} \mu_{\eta_0} \\ \mu_{\eta_1} \end{pmatrix}$$
 and,

$$\boldsymbol{\Sigma_{\eta|0}} = \left(\begin{array}{cc} \sigma_{\eta_0}^2 & \sigma_{\eta_0,\eta_1} \\ \sigma_{\eta_1,\eta_0} & \sigma_{\eta_1}^2 \end{array} \right).$$

Type 1:

The measurement model is given by

$$y_{i,t} = \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} \eta_{0_{i,t}} \\ \eta_{1_{i,t}} \end{pmatrix} + \boldsymbol{\varepsilon}_{i,t} \quad ext{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(0, \theta^2\right).$$

The dynamic structure is given by

$$\begin{pmatrix} \eta_{0_{i,t}} \\ \eta_{1_{i,t}} \end{pmatrix} = \begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \eta_{0_{i,t}} \\ \eta_{1_{i,t}} \end{pmatrix} + \mathbf{\Gamma}_{\boldsymbol{\eta}} \mathbf{x}_{i,t}$$

where $\mathbf{x}_{i,t}$ is a vector of covariates at time t and individual i, and Γ_{η} is the coefficient matrix linking the covariates to the latent variables.

Type 2:

The measurement model is given by

$$y_{i,t} = \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} \eta_{0_{i,t}} \\ \eta_{1_{i,t}} \end{pmatrix} + \mathbf{\Gamma}_{\mathbf{y}} \mathbf{x}_{i,t} + \boldsymbol{\varepsilon}_{i,t} \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(0, \theta^2\right)$$

where Γ_y is the coefficient matrix linking the covariates to the observed variables. The dynamic structure is given by

$$\begin{pmatrix} \eta_{0_{i,t}} \\ \eta_{1_{i,t}} \end{pmatrix} = \begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \eta_{0_{i,t}} \\ \eta_{1_{i,t}} \end{pmatrix} + \mathbf{\Gamma}_{\boldsymbol{\eta}} \mathbf{x}_{i,t}.$$

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Value

Returns a list of length n. Each element is a list with the following elements:

- y: A t by k matrix of values for the manifest variables.
- eta: A t by p matrix of values for the latent variables.
- x: A t by j matrix of values for the covariates.
- time: A vector of discrete time points from 1 to t.
- id: A vector of ID numbers of length t.

Author(s)

Ivan Jacob Agaloos Pesigan

References

Chow, S.-M., Ho, M. R., Hamaker, E. L., & Dolan, C. V. (2010). Equivalence and differences between structural equation modeling and state-space modeling techniques. *Structural Equation Modeling: A Multidisciplinary Journal*, 17(2), 303–332. doi:10.1080/10705511003661553

See Also

Other Simulation of State Space Models Data Functions: OU2SSM(), Sim2Matrix(), SimSSMFixed(), SimSSMOUFixed(), SimSSMOUVary(), SimSSMOU(), SimSSMVARFixed(), SimSSMVARVary(), SimSSMVARVary(), SimSSMVARVary(), SimSSMVary(), SimS

```
# prepare parameters
set.seed(42)
n <- 5
mu0 < -c(0.615, 1.006)
sigma0 <- matrix(</pre>
  data = c(
    1.932,
    0.618,
    0.618,
    0.587
  ),
  nrow = 2
sigma0_sqrt <- chol(sigma0)</pre>
theta <- 0.6
theta_sqrt <- sqrt(theta)</pre>
time <- 10
gamma_y \leftarrow matrix(data = 0.10, nrow = 1, ncol = 2)
gamma_eta <- matrix(data = 0.10, nrow = 2, ncol = 2)</pre>
x <- lapply(
  X = seq_len(n),
  FUN = function(i) {
    return(
```

```
matrix(
        data = rnorm(n = 2 * time),
        ncol = 2
     )
   )
}
)
# Type 0
ssm <- SimSSMLinGrowth(</pre>
 n = n,
 mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  theta_sqrt = theta_sqrt,
 type = 0,
 time = time
)
str(ssm)
# Type 1
ssm <- SimSSMLinGrowth(</pre>
 n = n,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  theta_sqrt = theta_sqrt,
  gamma_eta = gamma_eta,
  x = x,
  type = 1,
  time = time
)
str(ssm)
# Type 2
ssm <- SimSSMLinGrowth(</pre>
 n = n,
 mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  theta_sqrt = theta_sqrt,
  gamma_y = gamma_y,
  gamma_eta = gamma_eta,
  x = x,
  type = 2,
  time = time
)
str(ssm)
```

SimSSMOU

Simulate Data from the Ornstein-Uhlenbeck Model using a State Space Model Parameterization (n = 1)

Description

This function simulates data from the Ornstein–Uhlenbeck model using a state space model parameterization. See details for more information.

Usage

```
SimSSMOU(
 mu0,
  sigma0_sqrt,
 mu,
 phi,
  sigma_sqrt,
 nu,
 lambda,
  theta_sqrt,
  gamma_y = NULL,
  gamma_eta = NULL,
  x = NULL,
  type = 0,
  delta_t,
  time,
 burn_in = 0
```

Arguments

mu0	Numeric vector. Mean of initial latent variable values $(\mu_{\eta 0})$.
sigma0_sqrt	Numeric matrix. Cholesky decomposition of the covariance matrix of initial latent variable values ($\Sigma_{\eta 0}$).
mu	Numeric vector. The long-term mean or equilibrium level (μ) .
phi	Numeric matrix. The rate of mean reversion, determining how quickly the variable returns to its mean (Φ) .
sigma_sqrt	Numeric matrix. Cholesky decomposition of the matrix of volatility or randomness in the process (Σ) .
nu	Numeric vector. Vector of intercepts for the measurement model (ν) .
lambda	Numeric matrix. Factor loading matrix linking the latent variables to the observed variables (Λ) .
theta_sqrt	Numeric matrix. Cholesky decomposition of the measurement error covariance matrix (Θ) .
gamma_y	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the observed variables at time t (Γ_y).

gamma_eta	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the latent variables at time t (Γ_{η}) .
X	Numeric matrix. The matrix of observed covariates in type = 1 or type = 2. The number of rows should be equal to time + burn_in.
type	Integer. State space model type.
delta_t	Numeric. Time interval (δ_t) .
time	Positive integer. Number of time points to simulate.
burn_in	Positive integer. Number of burn-in points to exclude before returning the results.

Details

Type 0:

The measurement model is given by

$$\mathbf{y}_{t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{t} + \boldsymbol{\varepsilon}_{t} \quad ext{with} \quad \boldsymbol{\varepsilon}_{t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right)$$

where \mathbf{y}_t , $\boldsymbol{\eta}_t$, and $\boldsymbol{\varepsilon}_t$ are random variables and $\boldsymbol{\nu}$, $\boldsymbol{\Lambda}$, and $\boldsymbol{\Theta}$ are model parameters. \mathbf{y}_t is a vector of observed random variables, $\boldsymbol{\eta}_t$ is a vector of latent random variables, and $\boldsymbol{\varepsilon}_t$ is a vector of random measurement errors, at time t. $\boldsymbol{\nu}$ is a vector of intercepts, $\boldsymbol{\Lambda}$ is a matrix of factor loadings, and $\boldsymbol{\Theta}$ is the covariance matrix of $\boldsymbol{\varepsilon}$.

The dynamic structure is given by

$$\mathrm{d}\boldsymbol{\eta}_t = \boldsymbol{\Phi} \left(\boldsymbol{\mu} - \boldsymbol{\eta}_t \right) \mathrm{d}t + \boldsymbol{\Sigma}^{\frac{1}{2}} \mathrm{d}\mathbf{W}_t$$

where μ is the long-term mean or equilibrium level, Φ is the rate of mean reversion, determining how quickly the variable returns to its mean, Σ is the matrix of volatility or randomness in the process, and $\mathrm{d}W$ is a Wiener process or Brownian motion, which represents random fluctuations.

Type 1:

The measurement model is given by

$$\mathbf{y}_{t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{t} + \boldsymbol{\varepsilon}_{t} \quad ext{with} \quad \boldsymbol{\varepsilon}_{t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right).$$

The dynamic structure is given by

$$\mathrm{d} \boldsymbol{\eta}_t = \boldsymbol{\Phi} \left(\boldsymbol{\mu} - \boldsymbol{\eta}_t \right) \mathrm{d}t + \boldsymbol{\Gamma}_{\boldsymbol{\eta}} \mathbf{x}_t + \boldsymbol{\Sigma}^{\frac{1}{2}} \mathrm{d} \mathbf{W}_t$$

where \mathbf{x}_t is a vector of covariates at time t, and Γ_{η} is the coefficient matrix linking the covariates to the latent variables.

Type 2:

The measurement model is given by

$$\mathbf{y}_{t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{t} + \boldsymbol{\Gamma}_{\mathbf{y}} \mathbf{x}_{t} + \boldsymbol{\varepsilon}_{t} \quad ext{with} \quad \boldsymbol{\varepsilon}_{t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right)$$

where $\Gamma_{\mathbf{y}}$ is the coefficient matrix linking the covariates to the observed variables.

The dynamic structure is given by

$$d\boldsymbol{\eta}_t = \boldsymbol{\Phi} \left(\boldsymbol{\mu} - \boldsymbol{\eta}_t \right) dt + \boldsymbol{\Gamma}_n \mathbf{x}_t + \boldsymbol{\Sigma}^{\frac{1}{2}} d\mathbf{W}_t.$$

Value

Returns a list with the following elements:

- y: A t by k matrix of values for the manifest variables.
- eta: A t by p matrix of values for the latent variables.
- time: A vector of continuous time points of length t starting from 0 with delta_t increments.
- id: A vector of ones.

Author(s)

Ivan Jacob Agaloos Pesigan

References

Chow, S.-M., Losardo, D., Park, J., & Molenaar, P. C. M. (2023). Continuous-time dynamic models: Connections to structural equation models and other discrete-time models. In R. H. Hoyle (Ed.), Handbook of structural equation modeling (2nd ed.). The Guilford Press.

Uhlenbeck, G. E., & Ornstein, L. S. (1930). On the theory of the brownian motion. *Physical Review*, 36(5), 823–841. doi:10.1103/physrev.36.823

See Also

Other Simulation of State Space Models Data Functions: OU2SSM(), Sim2Matrix(), SimSSMFixed(), SimSSMLinGrowth(), SimSSMOUFixed(), SimSSMOUVary(), SimSSMVARFixed(), SimSSMVARVary(), SimSSMVAR(), SimSSMVAry(), SimS

```
# prepare parameters
set.seed(42)
p <- k <- 2
iden <- diag(p)</pre>
iden_sqrt <- chol(iden)</pre>
mu0 < -c(-3.0, 1.5)
sigma0_sqrt <- iden_sqrt</pre>
mu < -c(5.76, 5.18)
phi <- matrix(data = c(0.10, -0.05, -0.05, 0.10), nrow = p)
sigma_sqrt <- chol(</pre>
  matrix(data = c(2.79, 0.06, 0.06, 3.27), nrow = p)
)
nu \leftarrow rep(x = 0, times = k)
lambda <- diag(k)</pre>
theta_sqrt <- chol(diag(x = 0.50, nrow = k))
delta_t <- 0.10
time <- 50
burn_in <- 0
gamma_y <- gamma_eta <- 0.10 * diag(k)</pre>
x <- matrix(</pre>
  data = rnorm(n = k * (time + burn_in)),
  ncol = k
```

```
)
# Type 0
ssm <- SimSSMOU(
 mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  mu = mu,
  phi = phi,
  sigma_sqrt = sigma_sqrt,
  nu = nu,
  lambda = lambda,
  theta_sqrt = theta_sqrt,
  type = 0,
  delta_t = delta_t,
  time = time,
  burn_in = burn_in
)
str(ssm)
# Type 1
ssm <- SimSSMOU(
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  mu = mu,
  phi = phi,
  sigma_sqrt = sigma_sqrt,
  nu = nu,
  lambda = lambda,
  theta_sqrt = theta_sqrt,
  gamma_eta = gamma_eta,
  x = x,
  type = 1,
  delta_t = delta_t,
  time = time,
  burn_in = burn_in
)
str(ssm)
# Type 2
ssm <- SimSSMOU(
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  mu = mu,
  phi = phi,
  sigma_sqrt = sigma_sqrt,
  nu = nu,
  lambda = lambda,
  theta_sqrt = theta_sqrt,
  gamma_y = gamma_y,
  gamma_eta = gamma_eta,
  x = x,
```

```
type = 2,
  delta_t = delta_t,
  time = time,
  burn_in = burn_in
)
str(ssm)
```

SimSSMOUFixed

Simulate Data from an Ornstein-Uhlenbeck Model using a State Space Model Parameterization for n > 1 Individuals (Fixed Parameters)

Description

This function simulates data from an Ornstein–Uhlenbeck model using a state space model parameterization for n > 1 individuals. In this model, the parameters are invariant across individuals. See details for more information.

Usage

```
SimSSMOUFixed(
 n,
 mu0,
  sigma0_sqrt,
 mu,
 phi,
  sigma_sqrt,
  nu,
  lambda,
  theta_sqrt,
 gamma_y = NULL,
 gamma_eta = NULL,
 x = NULL
  type = 0,
  delta_t,
  time,
 burn_in = 0
)
```

Arguments

n Positive integer. Number of individuals. mu0 Numeric vector. Mean of initial latent variable values $(\mu_{\eta|0})$. sigma0_sqrt Numeric matrix. Cholesky decomposition of the covariance matrix of initial latent variable values $(\Sigma_{\eta|0})$. mu Numeric vector. The long-term mean or equilibrium level (μ) .

phi	Numeric matrix. The rate of mean reversion, determining how quickly the variable returns to its mean (Φ) .
sigma_sqrt	Numeric matrix. Cholesky decomposition of the matrix of volatility or randomness in the process (Σ) .
nu	Numeric vector. Vector of intercepts for the measurement model (ν) .
lambda	Numeric matrix. Factor loading matrix linking the latent variables to the observed variables (Λ) .
theta_sqrt	Numeric matrix. Cholesky decomposition of the measurement error covariance matrix (Θ) .
gamma_y	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the observed variables at time t (Γ_y) .
gamma_eta	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the latent variables at time t (Γ_{η}) .
X	Numeric matrix. The matrix of observed covariates in type = 1 or type = 2. The number of rows should be equal to time + burn_in.
type	Integer. State space model type.
delta_t	Numeric. Time interval (δ_t) .
time	Positive integer. Number of time points to simulate.
burn_in	Positive integer. Number of burn-in points to exclude before returning the results.

Details

Type 0:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t} \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right)$$

where $\mathbf{y}_{i,t}$, $\eta_{i,t}$, and $\varepsilon_{i,t}$ are random variables and $\boldsymbol{\nu}$, $\boldsymbol{\Lambda}$, and $\boldsymbol{\Theta}$ are model parameters. $\mathbf{y}_{i,t}$ is a vector of observed random variables, $\eta_{i,t}$ is a vector of latent random variables, and $\varepsilon_{i,t}$ is a vector of random measurement errors, at time t and individual i. $\boldsymbol{\nu}$ is a vector of intercepts, $\boldsymbol{\Lambda}$ is a matrix of factor loadings, and $\boldsymbol{\Theta}$ is the covariance matrix of ε .

The dynamic structure is given by

$$\mathrm{d} oldsymbol{\eta}_{i,t} = oldsymbol{\Phi} \left(oldsymbol{\mu} - oldsymbol{\eta}_{i,t}
ight) \mathrm{d} t + oldsymbol{\Sigma}^{rac{1}{2}} \mathrm{d} \mathbf{W}_{i,t}$$

where μ is the long-term mean or equilibrium level, Φ is the rate of mean reversion, determining how quickly the variable returns to its mean, Σ is the matrix of volatility or randomness in the process, and dW is a Wiener process or Brownian motion, which represents random fluctuations.

Type 1:

The measurement model is given by

$$\mathbf{y}_{i,t} = \mathbf{\nu} + \mathbf{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{arepsilon}_{i,t} \quad ext{with} \quad oldsymbol{arepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \mathbf{\Theta}
ight).$$

The dynamic structure is given by

$$\mathrm{d}\boldsymbol{\eta}_{i,t} = \boldsymbol{\Phi}\left(\boldsymbol{\mu} - \boldsymbol{\eta}_{i,t}\right)\mathrm{d}t + \boldsymbol{\Gamma}_{\boldsymbol{\eta}}\mathbf{x}_{i,t} + \boldsymbol{\Sigma}^{\frac{1}{2}}\mathrm{d}\mathbf{W}_{i,t}$$

where $\mathbf{x}_{i,t}$ is a vector of covariates at time t and individual i, and Γ_{η} is the coefficient matrix linking the covariates to the latent variables.

Type 2:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\Gamma}_{\mathbf{y}} \mathbf{x}_{i,t} + \boldsymbol{\varepsilon}_{i,t} \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right)$$

where $\Gamma_{\mathbf{y}}$ is the coefficient matrix linking the covariates to the observed variables.

The dynamic structure is given by

$$d\boldsymbol{\eta}_{i,t} = \boldsymbol{\Phi} \left(\boldsymbol{\mu} - \boldsymbol{\eta}_{i,t} \right) dt + \boldsymbol{\Gamma}_{\boldsymbol{\eta}} \mathbf{x}_{i,t} + \boldsymbol{\Sigma}^{\frac{1}{2}} d\mathbf{W}_{i,t}.$$

Value

Returns a list of length n. Each element is a list with the following elements:

- y: A t by k matrix of values for the manifest variables.
- eta: A t by p matrix of values for the latent variables.
- x: A t by j matrix of values for the covariates.
- time: A vector of continuous time points of length t starting from 0 with delta_t increments.
- id: A vector of ID numbers of length t.
- n: Number of individuals.

Author(s)

Ivan Jacob Agaloos Pesigan

References

Chow, S.-M., Losardo, D., Park, J., & Molenaar, P. C. M. (2023). Continuous-time dynamic models: Connections to structural equation models and other discrete-time models. In R. H. Hoyle (Ed.), Handbook of structural equation modeling (2nd ed.). The Guilford Press.

Uhlenbeck, G. E., & Ornstein, L. S. (1930). On the theory of the brownian motion. *Physical Review*, 36(5), 823–841. doi:10.1103/physrev.36.823

See Also

Other Simulation of State Space Models Data Functions: OU2SSM(), Sim2Matrix(), SimSSMFixed(), SimSSMLinGrowth(), SimSSMOUVary(), SimSSMOU(), SimSSMVARFixed(), SimSSMVARVary(), SimSSMVAR(), SimSSMVary(), SimSSM()

```
# prepare parameters
set.seed(42)
p <- k <- 2
iden <- diag(p)
iden_sqrt <- chol(iden)</pre>
```

```
n <- 5
mu0 < -c(-3.0, 1.5)
sigma0_sqrt <- iden_sqrt</pre>
mu < -c(5.76, 5.18)
phi <- matrix(data = c(0.10, -0.05, -0.05, 0.10), nrow = p)
sigma_sqrt <- chol(</pre>
  matrix(data = c(2.79, 0.06, 0.06, 3.27), nrow = p)
)
nu \leftarrow rep(x = 0, times = k)
lambda <- diag(k)</pre>
theta_sqrt <- chol(diag(x = 0.50, nrow = k))
delta_t <- 0.10
time <- 50
burn_in <- 0
gamma_y \leftarrow gamma_eta \leftarrow 0.10 * diag(k)
x \leftarrow lapply(
  X = seq_len(n),
  FUN = function(i) {
    return(
        data = rnorm(n = k * (time + burn_in)),
        ncol = k
      )
    )
  }
)
# Type 0
ssm <- SimSSMOUFixed(</pre>
  n = n,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  mu = mu,
  phi = phi,
  sigma_sqrt = sigma_sqrt,
  nu = nu,
  lambda = lambda,
  theta_sqrt = theta_sqrt,
  type = 0,
  delta_t = delta_t,
  time = time,
  burn_in = burn_in
)
str(ssm)
# Type 1
ssm <- SimSSMOUFixed(</pre>
  n = n,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  mu = mu,
  phi = phi,
```

```
sigma_sqrt = sigma_sqrt,
 nu = nu,
 lambda = lambda,
 theta_sqrt = theta_sqrt,
 gamma_eta = gamma_eta,
 x = x,
 type = 1,
 delta_t = delta_t,
 time = time,
 burn_in = burn_in
)
str(ssm)
# Type 2
ssm <- SimSSMOUFixed(</pre>
 n = n,
 mu0 = mu0,
 sigma0_sqrt = sigma0_sqrt,
 mu = mu,
 phi = phi,
 sigma_sqrt = sigma_sqrt,
 nu = nu,
 lambda = lambda,
 theta_sqrt = theta_sqrt,
 gamma_y = gamma_y,
 gamma_eta = gamma_eta,
 x = x,
 type = 2,
 delta_t = delta_t,
 time = time,
 burn_in = burn_in
)
str(ssm)
```

SimSSMOUVary

Simulate Data from an Ornstein-Uhlenbeck Model using a State Space Model Parameterization for n > 1 Individuals (Varying Parameters)

Description

This function simulates data from an Ornstein–Uhlenbeck model using a state space model parameterization for n > 1 individuals. In this model, the parameters can vary across individuals.

Usage

```
SimSSMOUVary(
   n,
```

```
mu0,
  sigma0_sqrt,
 mu,
  phi,
  sigma_sqrt,
  nu,
  lambda,
  theta_sqrt,
  gamma_y = NULL,
  gamma_eta = NULL,
  x = NULL
  type = 0,
  delta_t,
  time,
 burn_in = 0
)
```

Arguments

n Positive integer. Number of individuals.

mu0 Numeric vector. Mean of initial latent variable values $(\mu_{\eta|0})$.

sigma@_sqrt Numeric matrix. Cholesky decomposition of the covariance matrix of initial

latent variable values $(\Sigma_{\eta|0})$.

mu List of numeric vectors. The long-term mean or equilibrium level (μ) .

phi List of numeric matrices. The rate of mean reversion, determining how quickly

the variable returns to its mean (Φ) .

sigma_sqrt List of numeric matrices. Cholesky decomposition of the matrix of volatility or

randomness in the process (Σ) .

nu Numeric vector. Vector of intercepts for the measurement model (ν) .

lambda Numeric matrix. Factor loading matrix linking the latent variables to the ob-

served variables (Λ) .

theta_sqrt Numeric matrix. Cholesky decomposition of the measurement error covariance

matrix (Θ) .

gamma_y Numeric matrix. Matrix relating the values of the covariate matrix at time t to

the observed variables at time t $(\Gamma_{\mathbf{v}})$.

gamma_eta Numeric matrix. Matrix relating the values of the covariate matrix at time t to

the latent variables at time t (Γ_{η}) .

x Numeric matrix. The matrix of observed covariates in type = 1 or type = 2.

The number of rows should be equal to time + burn_in.

type Integer. State space model type.

delta_t Numeric. Time interval (δ_t) .

time Positive integer. Number of time points to simulate.

burn_in Positive integer. Number of burn-in points to exclude before returning the re-

sults.

Details

Parameters can vary across individuals by providing a list of parameter values. If the length of any of the parameters (mu0, sigma0_sqrt, mu, phi, sigma_sqrt, nu, lambda, theta_sqrt, gamma_y, or gamma_eta) is less the n, the function will cycle through the available values.

Value

Returns a list of length n. Each element is a list with the following elements:

- y: A t by k matrix of values for the manifest variables.
- eta: A t by p matrix of values for the latent variables.
- x: A t by j matrix of values for the covariates.
- time: A vector of discrete time points from 1 to t.
- id: A vector of ID numbers of length t.

Author(s)

Ivan Jacob Agaloos Pesigan

References

Chow, S.-M., Losardo, D., Park, J., & Molenaar, P. C. M. (2023). Continuous-time dynamic models: Connections to structural equation models and other discrete-time models. In R. H. Hoyle (Ed.), Handbook of structural equation modeling (2nd ed.). The Guilford Press.

Uhlenbeck, G. E., & Ornstein, L. S. (1930). On the theory of the brownian motion. *Physical Review*, *36*(5), 823–841. doi:10.1103/physrev.36.823

See Also

Other Simulation of State Space Models Data Functions: OU2SSM(), Sim2Matrix(), SimSSMFixed(), SimSSMLinGrowth(), SimSSMOUFixed(), SimSSMVARFixed(), SimSSMVARVary(), SimSSMVAR(), SimSSMVAry(), SimSSM

```
# prepare parameters
# In this example, phi varies across individuals
set.seed(42)
p <- k <- 2
iden <- diag(p)
iden_sqrt <- chol(iden)
n <- 5
mu0 <- list(c(-3.0, 1.5))
sigma0_sqrt <- list(iden_sqrt)
mu <- list(c(5.76, 5.18))
phi <- list(
    as.matrix(Matrix::expm(diag(x = -0.1, nrow = k))),
    as.matrix(Matrix::expm(diag(x = -0.2, nrow = k))),
    as.matrix(Matrix::expm(diag(x = -0.3, nrow = k))),</pre>
```

```
as.matrix(Matrix::expm(diag(x = -0.4, nrow = k))),
  as.matrix(Matrix::expm(diag(x = -0.5, nrow = k)))
)
sigma_sqrt <- list(</pre>
  chol(
    matrix(data = c(2.79, 0.06, 0.06, 3.27), nrow = p)
  )
)
nu \leftarrow list(rep(x = 0, times = k))
lambda <- list(diag(k))</pre>
theta_sqrt <- list(chol(diag(x = 0.50, nrow = k)))
delta_t <- 0.10
time <- 50
burn_in <- 0
gamma_y \leftarrow gamma_eta \leftarrow list(0.10 * diag(k))
x \leftarrow lapply(
  X = seq_len(n),
  FUN = function(i) {
    return(
        data = rnorm(n = k * (time + burn_in)),
        ncol = k
      )
    )
 }
)
# Type 0
ssm <- SimSSMOUVary(</pre>
  n = n,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  mu = mu,
  phi = phi,
  sigma_sqrt = sigma_sqrt,
  nu = nu,
  lambda = lambda,
  theta_sqrt = theta_sqrt,
  type = 0,
  delta_t = delta_t,
  time = time,
  burn_in = burn_in
)
str(ssm)
# Type 1
ssm <- SimSSMOUVary(</pre>
  n = n,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  mu = mu,
  phi = phi,
```

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```
sigma_sqrt = sigma_sqrt,
 nu = nu,
 lambda = lambda,
 theta_sqrt = theta_sqrt,
 gamma_eta = gamma_eta,
 x = x,
 type = 1,
 delta_t = delta_t,
 time = time,
 burn_in = burn_in
)
str(ssm)
# Type 2
ssm <- SimSSMOUVary(</pre>
 n = n,
 mu0 = mu0,
 sigma0_sqrt = sigma0_sqrt,
 mu = mu,
 phi = phi,
 sigma_sqrt = sigma_sqrt,
 nu = nu,
 lambda = lambda,
 theta_sqrt = theta_sqrt,
 gamma_y = gamma_y,
 gamma_eta = gamma_eta,
 x = x,
 type = 2,
 delta_t = delta_t,
 time = time,
 burn_in = burn_in
str(ssm)
```

SimSSMVAR

Simulate Data from the Vector Autoregressive Model using a State Space Model Parameterization (n = 1)

Description

This function simulates data from the vector autoregressive model using a state space model parameterization. See details for more information.

Usage

```
SimSSMVAR(
   mu0,
```

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```
sigma0_sqrt,
alpha,
beta,
psi_sqrt,
gamma_eta = NULL,
x = NULL,
time = 0,
burn_in = 0
)
```

Arguments

mu0	Numeric vector. Mean of initial latent variable values $(\mu_{\eta 0})$.
sigma0_sqrt	Numeric matrix. Cholesky decomposition of the covariance matrix of initial latent variable values $(\Sigma_{\eta 0})$.
alpha	Numeric vector. Vector of intercepts for the dynamic model (α) .
beta	Numeric matrix. Transition matrix relating the values of the latent variables at time $t-1$ to those at time $t(\beta)$.
psi_sqrt	Numeric matrix. Cholesky decomposition of the process noise covariance matrix (Ψ) .
gamma_eta	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the latent variables at time t (Γ_{η}).
X	Numeric matrix. The matrix of observed covariates in type = 1 or type = 2. The number of rows should be equal to time + burn_in.
time	Positive integer. Number of time points to simulate.
burn_in	Positive integer. Number of burn-in points to exclude before returning the results.

Details

The measurement model is given by

$$\mathbf{y}_t = \boldsymbol{\eta}_t$$
.

The dynamic structure is given by

$$oldsymbol{\eta}_t = oldsymbol{lpha} + oldsymbol{eta} oldsymbol{\eta}_{t-1} + oldsymbol{\zeta}_t \quad ext{with} \quad oldsymbol{\zeta}_t \sim \mathcal{N}\left(oldsymbol{0}, oldsymbol{\Psi}
ight)$$

where η_t , η_{t-1} , and ζ_t are random variables, and α , β , and Ψ are model parameters. η_t is a vector of latent variables at time t, η_{t-1} is a vector of latent variables at time t-1, and ζ_t is a vector of dynamic noise at time t. α is a vector of intercepts, β is a matrix of autoregression and cross regression coefficients, and Ψ is the covariance matrix of ζ_t .

Note that when gamma_eta and x are not NULL, the dynamic structure is given by

$$oldsymbol{\eta}_t = oldsymbol{lpha} + oldsymbol{eta} oldsymbol{\eta}_{t-1} + oldsymbol{\Gamma}_{oldsymbol{\eta}} \mathbf{x}_t + oldsymbol{\zeta}_t \quad ext{with} \quad oldsymbol{\zeta}_t \sim \mathcal{N}\left(\mathbf{0}, oldsymbol{\Psi}
ight)$$

where \mathbf{x}_t is a vector of covariates at time t, and Γ_{η} is the coefficient matrix linking the covariates to the latent variables.

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Value

Returns a list with the following elements:

- y: A t by k matrix of values for the manifest variables.
- eta: A t by p matrix of values for the latent variables.
- x: A t by j matrix of values for the covariates.
- time: A vector of discrete time points from 0 to t 1.
- id: A vector of ones.

References

Chow, S.-M., Ho, M. R., Hamaker, E. L., & Dolan, C. V. (2010). Equivalence and differences between structural equation modeling and state-space modeling techniques. *Structural Equation Modeling: A Multidisciplinary Journal*, 17(2), 303–332. doi:10.1080/10705511003661553

See Also

Other Simulation of State Space Models Data Functions: OU2SSM(), Sim2Matrix(), SimSSMFixed(), SimSSMLinGrowth(), SimSSMOUFixed(), SimSSMOUVary(), SimSSMOU(), SimSSMVARFixed(), SimSSMVARVary(), SimSSMVary(), SimSS

```
# prepare parameters
set.seed(42)
k <- 3
iden <- diag(k)</pre>
iden_sqrt <- chol(iden)</pre>
null_vec <- rep(x = 0, times = k)
mu0 <- null_vec
sigma0_sqrt <- iden_sqrt</pre>
alpha <- null_vec
beta \leftarrow diag(x = 0.5, nrow = k)
psi_sqrt <- iden_sqrt</pre>
time <- 50
burn_in <- 0
gamma_eta <- 0.10 * diag(k)
x <- matrix(
  data = rnorm(n = k * (time + burn_in)),
  ncol = k
)
# No covariates
ssm <- SimSSMVAR(</pre>
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
  psi_sqrt = psi_sqrt,
  time = time,
```

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```
burn_in = burn_in
)
str(ssm)

# With covariates
ssm <- SimSSMVAR(
   mu0 = mu0,
   sigma0_sqrt = sigma0_sqrt,
   alpha = alpha,
   beta = beta,
   psi_sqrt = psi_sqrt,
   gamma_eta = gamma_eta,
   x = x,
   time = time,
   burn_in = burn_in
)
str(ssm)</pre>
```

SimSSMVARFixed

Simulate Data from a Vector Autoregressive Model using a State Space Model Parameterization for n > 1 Individuals (Fixed Parameters)

Description

This function simulates data from a vector autoregressive model using a state space model parameterization for n > 1 individuals. In this model, the parameters are invariant across individuals.

Usage

```
SimSSMVARFixed(
    n,
    mu0,
    sigma0_sqrt,
    alpha,
    beta,
    psi_sqrt,
    gamma_eta = NULL,
    x = NULL,
    time = 0,
    burn_in = 0
)
```

Arguments

n Positive integer. Number of individuals. mu0 Numeric vector. Mean of initial latent variable values $(\mu_{\eta|0})$.

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sigma0_sqrt	Numeric matrix. Cholesky decomposition of the covariance matrix of initial latent variable values $(\Sigma_{\eta 0})$.
alpha	Numeric vector. Vector of intercepts for the dynamic model (α) .
beta	Numeric matrix. Transition matrix relating the values of the latent variables at time $t-1$ to those at time $t(\beta)$.
psi_sqrt	Numeric matrix. Cholesky decomposition of the process noise covariance matrix (Ψ) .
gamma_eta	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the latent variables at time t (Γ_{η}) .
x	A list of length n of numeric matrices. Each element of the list is a matrix of observed covariates in type = 1 or type = 2. The number of rows in each matrix should be equal to time + burn_in.
time	Positive integer. Number of time points to simulate.
burn_in	Positive integer. Number of burn-in points to exclude before returning the results.

Value

Returns a list of length n. Each element is a list with the following elements:

- y: A t by k matrix of values for the manifest variables.
- eta: A t by p matrix of values for the latent variables.
- x: A t by j matrix of values for the covariates.
- time: A vector of discrete time points from 1 to t.
- id: A vector of ID numbers of length t.

Author(s)

Ivan Jacob Agaloos Pesigan

References

Chow, S.-M., Ho, M. R., Hamaker, E. L., & Dolan, C. V. (2010). Equivalence and differences between structural equation modeling and state-space modeling techniques. *Structural Equation Modeling: A Multidisciplinary Journal*, 17(2), 303–332. doi:10.1080/10705511003661553

See Also

Other Simulation of State Space Models Data Functions: OU2SSM(), Sim2Matrix(), SimSSMFixed(), SimSSMLinGrowth(), SimSSMOUFixed(), SimSSMOUVary(), SimSSMVARVary(), SimSSMVARVary(), SimSSMVARVary(), SimSSMVARVary(), SimSSMVARVary(), SimSSMVARVary(), SimSSMVary(), SimSMVary(), SimS

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```
# prepare parameters
set.seed(42)
k <- 3
iden <- diag(k)</pre>
iden_sqrt <- chol(iden)</pre>
null_vec \leftarrow rep(x = 0, times = k)
n <- 5
mu0 <- null_vec
sigma0_sqrt <- iden_sqrt</pre>
alpha <- null_vec</pre>
beta <- diag(x = 0.5, nrow = k)
psi_sqrt <- iden_sqrt</pre>
time <- 50
burn_in <- 0</pre>
gamma_eta <- 0.10 * diag(k)
x <- lapply(
  X = seq_len(n),
  FUN = function(i) {
    return(
      matrix(
        data = rnorm(n = k * (time + burn_in)),
        ncol = k
      )
    )
 }
)
# No covariates
ssm <- SimSSMVARFixed(</pre>
 n = n,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
  psi_sqrt = psi_sqrt,
  time = time,
  burn_in = burn_in
)
str(ssm)
# With covariates
ssm <- SimSSMVARFixed(</pre>
  n = n,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
  psi_sqrt = psi_sqrt,
  gamma_eta = gamma_eta,
  x = x,
```

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```
time = time,
burn_in = burn_in
)
str(ssm)
```

SimSSMVARVary

Simulate Data from a Vector Autoregressive Model using a State Space Model Parameterization for n > 1 Individuals (Varying Parameters)

Description

This function simulates data from a vector autoregressive model using a state space model parameterization for n > 1 individuals. In this model, the parameters can vary across individuals.

Usage

```
SimSSMVARVary(
    n,
    mu0,
    sigma0_sqrt,
    alpha,
    beta,
    psi_sqrt,
    gamma_eta = NULL,
    x = NULL,
    time = 0,
    burn_in = 0
)
```

Arguments

n	Positive integer. Number of individuals.
mu0	List of numeric vectors. Mean of initial latent variable values $(\mu_{\eta 0})$.
sigma0_sqrt	List of numeric matrices. Cholesky decomposition of the covariance matrix of initial latent variable values $(\Sigma_{\eta 0})$.
alpha	List of numeric vectors. Vector of intercepts for the dynamic model (α) .
beta	List of numeric matrices. Transition matrix relating the values of the latent variables at time $t-1$ to those at time $t(\beta)$.
psi_sqrt	List of numeric matrices. Cholesky decomposition of the process noise covariance matrix (Ψ) .
gamma_eta	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the latent variables at time t (Γ_n) .

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x	A list of length n of numeric matrices. Each element of the list is a matrix of observed covariates in type = 1 or type = 2. The number of rows in each matrix should be equal to time + burn_in.
time	Positive integer. Number of time points to simulate.
burn_in	Positive integer. Number of burn-in points to exclude before returning the results.

Details

Parameters can vary across individuals by providing a list of parameter values. If the length of any of the parameters (mu0, sigma0_sqrt, alpha, beta, psi_sqrt, or gamma_eta) is less the n, the function will cycle through the available values.

Value

Returns a list of length n. Each element is a list with the following elements:

- y: A t by k matrix of values for the manifest variables.
- eta: A t by p matrix of values for the latent variables.
- x: A t by j matrix of values for the covariates.
- time: A vector of discrete time points from 1 to t.
- id: A vector of ID numbers of length t.

Author(s)

Ivan Jacob Agaloos Pesigan

References

Chow, S.-M., Ho, M. R., Hamaker, E. L., & Dolan, C. V. (2010). Equivalence and differences between structural equation modeling and state-space modeling techniques. *Structural Equation Modeling: A Multidisciplinary Journal*, 17(2), 303–332. doi:10.1080/10705511003661553

See Also

Other Simulation of State Space Models Data Functions: OU2SSM(), Sim2Matrix(), SimSSMFixed(), SimSSMLinGrowth(), SimSSMOUFixed(), SimSSMOUVary(), SimSSMOU(), SimSSMVARFixed(), SimSSMVAR(), SimSSMVary(), SimSSM()

```
# prepare parameters
# In this example, beta varies across individuals
set.seed(42)
k <- 3
iden <- diag(k)
iden_sqrt <- chol(iden)
null_vec <- rep(x = 0, times = k)
n <- 5</pre>
```

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```
mu0 <- list(null_vec)</pre>
sigma0_sqrt <- list(iden_sqrt)</pre>
alpha <- list(null_vec)</pre>
beta <- list(</pre>
  diag(x = 0.1, nrow = k),
  diag(x = 0.2, nrow = k),
  diag(x = 0.3, nrow = k),
  diag(x = 0.4, nrow = k),
  diag(x = 0.5, nrow = k)
)
psi_sqrt <- list(iden_sqrt)</pre>
time <- 50
burn_in <- 0</pre>
gamma_eta \leftarrow list(0.10 * diag(k))
x <- lapply(
  X = seq_len(n),
  FUN = function(i) {
    return(
      matrix(
        data = rnorm(n = k * (time + burn_in)),
        ncol = k
      )
    )
  }
)
# No covariates
ssm <- SimSSMVARVary(</pre>
  n = n,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
  psi_sqrt = psi_sqrt,
  time = time,
  burn_in = burn_in
)
str(ssm)
# With covariates
ssm <- SimSSMVARVary(</pre>
  n = n,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
  psi_sqrt = psi_sqrt,
  gamma_eta = gamma_eta,
  x = x,
  time = time,
  burn_in = burn_in
)
```

str(ssm)

SimSSMVary Simulate Data using a State Space Model Parameterization for n > 1Individuals (Varying Parameters)

Description

This function simulates data using a state space model parameterization for n > 1 individuals. In this model, the parameters can vary across individuals.

Usage

```
SimSSMVary(
  n,
  type,
 mu0,
  sigma0_sqrt,
  alpha,
 beta,
  psi_sqrt,
  nu,
  lambda,
  theta_sqrt,
  gamma_y = NULL,
  gamma_eta = NULL,
 x = NULL
  time = 0,
  burn_in = 0
)
```

Arguments n

type	Integer. State space model type.
mu0	List of numeric vectors. Mean of initial latent variable values $(\mu_{n 0})$.

Positive integer. Number of individuals.

sigma@_sqrt List of numeric matrices. Cholesky decomposition of the covariance matrix of

initial latent variable values $(\Sigma_{\eta|0})$.

alpha List of numeric vectors. Vector of intercepts for the dynamic model (α) .

beta List of numeric matrices. Transition matrix relating the values of the latent

variables at time t - 1 to those at time $t (\beta)$.

psi_sqrt List of numeric matrices. Cholesky decomposition of the process noise covari-

ance matrix (Ψ) .

nu	List of numeric vectors. Vector of intercepts for the measurement model (ν) .
lambda	List of numeric matrices. Factor loading matrix linking the latent variables to the observed variables (Λ) .
theta_sqrt	List of numeric matrices. Cholesky decomposition of the measurement error covariance matrix (Θ) .
gamma_y	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the observed variables at time t (Γ_y) .
gamma_eta	Numeric matrix. Matrix relating the values of the covariate matrix at time t to the latent variables at time t (Γ_{η}).
х	A list of length n of numeric matrices. Each element of the list is a matrix of observed covariates in type = 1 or type = 2. The number of rows in each matrix should be equal to time + burn_in.
time	Positive integer. Number of time points to simulate.
burn_in	Positive integer. Number of burn-in points to exclude before returning the results.

Details

Parameters can vary across individuals by providing a list of parameter values. If the length of any of the parameters (mu0, sigma0_sqrt, alpha, beta, psi_sqrt, nu, lambda, theta_sqrt, gamma_y, or gamma_eta) is less the n, the function will cycle through the available values.

Value

Returns a list of length n. Each element is a list with the following elements:

- y: A t by k matrix of values for the manifest variables.
- eta: A t by p matrix of values for the latent variables.
- x: A t by j matrix of values for the covariates.
- time: A vector of discrete time points from 1 to t.
- id: A vector of ID numbers of length t.

Author(s)

Ivan Jacob Agaloos Pesigan

References

Chow, S.-M., Ho, M. R., Hamaker, E. L., & Dolan, C. V. (2010). Equivalence and differences between structural equation modeling and state-space modeling techniques. *Structural Equation Modeling: A Multidisciplinary Journal*, 17(2), 303–332. doi:10.1080/10705511003661553

See Also

Other Simulation of State Space Models Data Functions: OU2SSM(), Sim2Matrix(), SimSSMFixed(), SimSSMLinGrowth(), SimSSMOUFixed(), SimSSMOUVary(), SimSSMOU(), SimSSMVARFixed(), SimSSMVARVary(), SimSSMVAR(), SimSSM()

```
# prepare parameters
# In this example, beta varies across individuals
set.seed(42)
k <- p <- 3
iden <- diag(k)</pre>
iden_sqrt <- chol(iden)</pre>
null\_vec \leftarrow rep(x = 0, times = k)
n <- 5
mu0 <- list(null_vec)</pre>
sigma0_sqrt <- list(iden_sqrt)</pre>
alpha <- list(null_vec)</pre>
beta <- list(</pre>
  diag(x = 0.1, nrow = k),
  diag(x = 0.2, nrow = k),
  diag(x = 0.3, nrow = k),
  diag(x = 0.4, nrow = k),
  diag(x = 0.5, nrow = k)
psi_sqrt <- list(iden_sqrt)</pre>
nu <- list(null_vec)</pre>
lambda <- list(iden)</pre>
theta_sqrt <- list(chol(diag(x = 0.50, nrow = k)))
time <- 50
burn_in <- 0
gamma_y <- gamma_eta <- list(0.10 * diag(k))</pre>
x \leftarrow lapply(
  X = seq_len(n),
  FUN = function(i) {
    return(
      matrix(
        data = rnorm(n = k * (time + burn_in)),
        ncol = k
    )
 }
)
# Type 0
ssm <- SimSSMVary(</pre>
  n = n,
  type = 0,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
  psi_sqrt = psi_sqrt,
  nu = nu,
  lambda = lambda,
  theta_sqrt = theta_sqrt,
  time = time,
  burn_in = burn_in
```

```
)
str(ssm)
# Type 1
ssm <- SimSSMVary(
 n = n,
  type = 1,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
  psi_sqrt = psi_sqrt,
  nu = nu,
  lambda = lambda,
  theta_sqrt = theta_sqrt,
  gamma_eta = gamma_eta,
 x = x,
 time = time,
  burn_in = burn_in
)
str(ssm)
# Type 2
ssm <- SimSSMVary(</pre>
 n = n,
  type = 2,
  mu0 = mu0,
  sigma0_sqrt = sigma0_sqrt,
  alpha = alpha,
  beta = beta,
  psi_sqrt = psi_sqrt,
  nu = nu,
  lambda = lambda,
  theta_sqrt = theta_sqrt,
  gamma_y = gamma_y,
  gamma_eta = gamma_eta,
  x = x,
  time = time,
  burn_in = burn_in
)
str(ssm)
```

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