Supplementary Material for Chapter 6

Table 1: Comparison of the methods in dataset emotions in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	$\overline{\mathrm{DGS}}$	-315.71	0.28	0.791	1.03	2	2
1	$\operatorname{DGS-clp}$	-300.3	0.28	0.78	1.03	2	2
1	GS-tw	-449.6	0.27	0.78	0.6	2	2
1	GS- clp	-317.61	0.294	0.79	0.6	2	2
1	GS-pruned	-361.94	0.27	0.78	0.65	4	2
2	DGS	-317.76	0.24	0.76	0.79	2	2
2	$\operatorname{DGS-clp}$	-309.24	0.24	0.76	0.79	2	2
2	GS-tw	-389.42	0.345	0.794	0.63	2	2
2	GS- clp	-301.9	0.32	0.79	0.63	2	2
2	GS-pruned	-336.51	0.28	0.76	0.6	3	2
3	DGS	-293.23	0.28	0.77	0.77	2	2
3	$\operatorname{DGS-clp}$	-285.3	0.319	0.78	0.77	2	2
3	GS-tw	-355.2	0.29	0.794	0.61	2	2
3	GS- clp	-313.23	0.23	0.76	0.61	2	2
3	GS-pruned	-298.79	0.23	0.78	0.6	3	2
4	DGS	-317.8	0.288	0.77	0.74	2	2
4	$\operatorname{DGS-clp}$	-309.2	0.288	0.77	0.74	2	2
4	GS-tw	-429.35	0.25	0.77	0.6	2	2
4	GS- clp	-349.22	0.27	0.777	0.6	2	2
4	GS-pruned	-352.53	0.28	0.76	0.65	3	2
5	DGS	-305.74	0.322	0.79	0.75	2	2
5	$\operatorname{DGS-clp}$	-298.4	0.322	0.78	0.75	2	2
5	GS-tw	-477.82	0.28	0.78	0.6	2	2
5	GS- clp	-343.7	0.25	0.76	0.6	2	2
5	GS-pruned	-338.7	0.322	0.797	0.93	4	2

Table 2: Comparison of the methods in dataset emotions in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-300.92	0.29	0.79	1.16	3	3
1	$\operatorname{DGS-clp}$	-279.3	0.311	0.78	1.16	3	3
1	GS-tw	-357.54	0.29	0.78	0.75	3	3
1	GS- clp	-295.83	0.29	0.789	0.75	3	3
1	GS-pruned	-348.87	0.28	0.78	0.6	4	3
2	DGS	-317.76	0.24	0.76	0.72	2	2
2	$\operatorname{DGS-clp}$	-309.24	0.24	0.76	0.72	2	2
2	GS-tw	-326.83	0.27	0.75	0.75	3	3
2	GS- clp	-299.5	0.277	0.768	0.75	3	3
2	GS-pruned	-322.52	0.2	0.76	0.6	4	3
3	DGS	-293.23	0.28	0.77	0.71	2	2
3	$\operatorname{DGS-clp}$	-285.34	0.319	0.78	0.71	2	2
3	GS-tw	-287.87	0.3	0.8	0.73	3	3
3	GS- clp	-273.5	0.3	0.79	0.73	3	3
3	GS-pruned	-292.9	0.28	0.8	0.6	4	3
4	DGS	-317.8	0.29	0.77	0.71	2	2
4	$\operatorname{DGS-clp}$	-309.2	0.29	0.77	0.71	2	2
4	GS-tw	-355.62	0.29	0.78	0.69	3	3
4	GS- clp	-313.92	0.314	0.798	0.69	3	3
4	GS-pruned	-347.44	0.3	0.79	0.6	4	3
5	DGS	-302.83	0.31	0.79	0.88	3	3
5	$\operatorname{DGS-clp}$	-295.5	0.322	0.78	0.88	3	3
5	GS-tw	-348.01	0.31	0.79	0.72	3	3
5	GS- clp	-311.3	0.28	0.77	0.72	3	3
5	GS-pruned	-333.77	0.31	0.802	0.7	4	3

Table 3: Comparison of the methods in dataset emotions in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	0.00	000	time	tw	tw-pr
			acc_G	acc_M			
1	DGS	-300.92	0.29	0.787	0.77	3	3
1	DGS-clp	-279.3	0.311	0.78	0.77	3	3
1	GS-tw	-348.87	0.28	0.78	0.74	3	3
1	GS- clp	-286.26	0.28	0.79	0.74	3	3
1	GS-pruned	-348.87	0.28	0.78	0.6	4	3
2	DGS	-317.76	0.244	0.76	0.76	2	2
2	$\operatorname{DGS-clp}$	-309.24	0.244	0.763	0.76	2	2
2	GS-tw	-322.52	0.2	0.76	0.78	4	3
2	GS- clp	-305.3	0.22	0.75	0.78	4	3
2	GS-pruned	-322.52	0.2	0.76	0.6	4	3
3	DGS	-293.23	0.28	0.77	0.81	2	2
3	$\operatorname{DGS-clp}$	-285.34	0.319	0.78	0.81	2	2
3	GS-tw	-286.04	0.29	0.801	0.8	4	3
3	GS- clp	-272.4	0.319	0.78	0.8	4	3
3	GS-pruned	-292.9	0.28	0.8	0.6	4	3
4	DGS	-317.8	0.29	0.77	0.75	2	2
4	$\operatorname{DGS-clp}$	-309.18	0.29	0.77	0.75	2	2
4	GS-tw	-348.21	0.314	0.78	0.75	3	3
4	GS- clp	-304.7	0.31	0.794	0.75	3	3
4	GS-pruned	-347.44	0.3	0.79	0.6	4	3
5	DGS	-302.83	0.31	0.79	0.78	3	3
5	$\operatorname{DGS-clp}$	-295.5	0.322	0.78	0.78	3	3
5	GS-tw	-334.73	0.31	0.79	0.77	4	3
5	GS- clp	-309.08	0.31	0.78	0.77	4	3
5	GS-pruned	-333.77	0.31	0.802	0.7	4	3

Table 4: Comparison of the methods in dataset emotions in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-300.92	0.29	0.787	0.76	3	3
1	DGS-clp	-279.3	0.311	0.78	0.76	3	3
1	GS-tw	-348.87	0.28	0.78	0.79	3	3
1	GS-clp	-286.26	0.28	0.79	0.79	3	3
1	GS-pruned	-348.87	0.28	0.78	0.7	4	3
2	DGS	-317.76	0.244	0.76	0.74	2	2
2	$\operatorname{DGS-clp}$	-309.24	0.244	0.763	0.74	2	2
2	GS-tw	-322.52	0.2	0.76	0.76	4	3
2	GS- clp	-305.3	0.22	0.75	0.76	4	3
2	GS-pruned	-322.52	0.2	0.76	0.7	4	3
3	DGS	-293.23	0.28	0.77	0.74	2	2
3	$\operatorname{DGS-clp}$	-285.34	0.319	0.78	0.74	2	2
3	GS-tw	-292.9	0.28	0.796	0.76	4	3
3	GS- clp	-274.1	0.29	0.77	0.76	4	3
3	GS-pruned	-292.9	0.28	0.796	0.7	4	3
4	DGS	-317.8	0.29	0.77	0.72	2	2
4	$\operatorname{DGS-clp}$	-309.18	0.29	0.77	0.72	2	2
4	GS-tw	-347.44	0.297	0.79	0.84	4	3
4	GS- clp	-302.8	0.297	0.794	0.84	4	3
4	GS-pruned	-347.44	0.297	0.79	0.6	4	3
5	DGS	-302.83	0.31	0.79	0.75	3	3
5	$\operatorname{DGS-clp}$	-295.5	0.322	0.78	0.75	3	3
5	GS-tw	-333.77	0.31	0.802	0.81	4	3
5	GS- clp	-309.21	0.29	0.79	0.81	4	3
5	GS-pruned	-333.77	0.31	0.802	0.7	4	3

Table 5: Comparison of the methods in dataset foodtruck in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	$\overline{\mathrm{DGS}}$	-342.28	0.317	0.852	0.23	2	2
1	$\operatorname{DGS-clp}$	-342.34	0.317	0.852	0.23	2	2
1	GS-tw	-341.1	0.29	0.85	0.06	2	2
1	$\operatorname{GS-clp}$	-339.6	0.317	0.84	0.06	2	2
1	GS-pruned	-341.1	0.29	0.85	0	2	2
2	DGS	-363.21	0.244	0.84	0.13	2	2
2	$\operatorname{DGS-clp}$	-364.11	0.244	0.84	0.13	2	2
2	GS-tw	-366.04	0.244	0.84	0.05	2	2
2	GS- clp	-360.3	0.23	0.845	0.05	2	2
2	GS-pruned	-366.04	0.244	0.84	0	2	2
3	DGS	-358	0.185	0.84	0.12	2	2
3	$\operatorname{DGS-clp}$	-358.5	0.185	0.84	0.12	2	2
3	GS-tw	-359.46	0.17	0.845	0	2	2
3	GS- clp	-361.47	0.185	0.84	0	2	2
3	GS-pruned	-359.46	0.17	0.845	0.07	2	2
4	DGS	-361.4	0.296	0.87	0.13	2	2
4	$\operatorname{DGS-clp}$	-362.6	0.296	0.866	0.13	2	2
4	GS-tw	-365.01	0.28	0.85	0.1	2	2
4	GS- clp	-363.35	0.28	0.85	0.1	2	2
4	GS-pruned	-365.01	0.28	0.85	0.06	2	2
5	DGS	-399.9	0.259	0.819	0.12	2	2
5	$\operatorname{DGS-clp}$	-400.81	0.259	0.819	0.12	2	2
5	GS-tw	-405.2	0.21	0.82	0.1	2	2
5	GS- clp	-400.49	0.25	0.819	0.1	2	2
5	GS-pruned	-405.2	0.21	0.82	0.06	2	2

Table 6: Comparison of the methods in dataset foodtruck in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	$\overline{\mathrm{DGS}}$	-342.28	0.317	0.852	0.12	2	2
1	$\operatorname{DGS-clp}$	-342.34	0.317	0.852	0.12	2	2
1	GS-tw	-341.1	0.29	0.85	0.06	2	2
1	GS- clp	-339.6	0.317	0.84	0.06	2	2
1	GS-pruned	-341.1	0.29	0.85	0	2	2
2	DGS	-363.21	0.244	0.84	0.12	2	2
2	$\operatorname{DGS-clp}$	-364.11	0.244	0.84	0.12	2	2
2	GS-tw	-366.04	0.244	0.84	0	2	2
2	GS- clp	-360.3	0.23	0.845	0	2	2
2	GS-pruned	-366.04	0.244	0.84	0.06	2	2
3	DGS	-358	0.185	0.84	0.12	2	2
3	$\operatorname{DGS-clp}$	-358.5	0.185	0.84	0.12	2	2
3	GS-tw	-359.46	0.17	0.845	0.05	2	2
3	GS- clp	-361.47	0.185	0.84	0.05	2	2
3	GS-pruned	-359.46	0.17	0.845	0.1	2	2
4	DGS	-360.4	0.296	0.87	0.13	3	3
4	$\operatorname{DGS-clp}$	-361.78	0.296	0.866	0.13	3	3
4	GS-tw	-364.03	0.28	0.85	0.06	3	3
4	GS- clp	-362.48	0.28	0.85	0.06	3	3
4	GS-pruned	-364.03	0.28	0.85	0.1	3	3
5	DGS	-399.9	0.259	0.819	0.12	2	2
5	$\operatorname{DGS-clp}$	-400.81	0.259	0.819	0.12	2	2
5	GS-tw	-405.2	0.21	0.82	0.1	2	2
5	GS- clp	-400.49	0.25	0.819	0.1	2	2
5	GS-pruned	-405.2	0.21	0.82	0.06	2	2

Table 7: Comparison of the methods in dataset foodtruck in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-342.28	0.317	0.852	0.12	2	2
1	$\operatorname{DGS-clp}$	-342.34	0.317	0.852	0.12	2	2
1	GS-tw	-341.1	0.29	0.85	0.05	2	2
1	GS- clp	-339.6	0.317	0.84	0.05	2	2
1	GS-pruned	-341.1	0.29	0.85	0	2	2
2	DGS	-363.21	0.244	0.84	0.11	2	2
2	$\operatorname{DGS-clp}$	-364.11	0.244	0.84	0.11	2	2
2	GS-tw	-366.04	0.244	0.84	0	2	2
2	GS- clp	-360.3	0.23	0.845	0	2	2
2	GS-pruned	-366.04	0.244	0.84	0.05	2	2
3	DGS	-358	0.185	0.84	0.13	2	2
3	$\operatorname{DGS-clp}$	-358.5	0.185	0.84	0.13	2	2
3	GS-tw	-359.46	0.17	0.845	0	2	2
3	GS- clp	-361.47	0.185	0.84	0	2	2
3	GS-pruned	-359.46	0.17	0.845	0.06	2	2
4	DGS	-360.4	0.296	0.87	0.13	3	3
4	$\operatorname{DGS-clp}$	-361.78	0.296	0.866	0.13	3	3
4	GS-tw	-364.03	0.28	0.85	0.1	3	3
4	GS- clp	-362.48	0.28	0.85	0.1	3	3
4	GS-pruned	-364.03	0.28	0.85	0.07	3	3
5	DGS	-399.9	0.259	0.819	0.12	2	2
5	$\operatorname{DGS-clp}$	-400.81	0.259	0.819	0.12	2	2
5	GS-tw	-405.2	0.21	0.82	0.07	2	2
5	GS- clp	-400.49	0.25	0.819	0.07	2	2
5	GS-pruned	-405.2	0.21	0.82	0.1	2	2

Table 8: Comparison of the methods in dataset foodtruck in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-342.28	0.317	0.852	0.13	2	2
1	$\operatorname{DGS-clp}$	-342.34	0.317	0.852	0.13	2	2
1	GS-tw	-341.1	0.29	0.85	0.06	2	2
1	GS- clp	-339.6	0.317	0.84	0.06	2	2
1	GS-pruned	-341.1	0.29	0.85	0	2	2
2	DGS	-363.21	0.244	0.84	0.12	2	2
2	$\operatorname{DGS-clp}$	-364.11	0.244	0.84	0.12	2	2
2	GS-tw	-366.04	0.244	0.84	0	2	2
2	GS- clp	-360.3	0.23	0.845	0	2	2
2	GS-pruned	-366.04	0.244	0.84	0.05	2	2
3	DGS	-358	0.185	0.84	0.16	2	2
3	$\operatorname{DGS-clp}$	-358.5	0.185	0.84	0.16	2	2
3	GS-tw	-359.46	0.17	0.845	0	2	2
3	GS- clp	-361.47	0.185	0.84	0	2	2
3	GS-pruned	-359.46	0.17	0.845	0.05	2	2
4	DGS	-360.4	0.296	0.87	0.12	3	3
4	$\operatorname{DGS-clp}$	-361.78	0.296	0.866	0.12	3	3
4	GS-tw	-364.03	0.28	0.85	0.1	3	3
4	GS- clp	-362.48	0.28	0.85	0.1	3	3
4	GS-pruned	-364.03	0.28	0.85	0.08	3	3
5	DGS	-399.9	0.259	0.819	0.13	2	2
5	$\operatorname{DGS-clp}$	-400.81	0.259	0.819	0.13	2	2
5	GS-tw	-405.2	0.21	0.82	0.06	2	2
5	GS- clp	-400.49	0.25	0.819	0.06	2	2
5	GS-pruned	-405.2	0.21	0.82	0.1	2	2

Table 9: Comparison of the methods in dataset birds in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-464.69	0.39	0.94	4.3	1	1
1	DGS-clp	-463.2	0.4	0.93	4.3	1	1
1	GS-tw	-764.85	0.39	0.93	8.02	2	2
1	GS- clp	-473.46	0.419	0.939	8.02	2	2
1	GS-pruned	-483.23	0.4	0.94	6.2	3	2
2	DGS	-432.34	0.47	0.95	4.8	1	1
2	$\operatorname{DGS-clp}$	-426.3	0.43	0.95	4.8	1	1
2	GS-tw	-683.37	0.46	0.94	7.23	2	2
2	GS- clp	-439.78	0.481	0.951	7.23	2	2
2	GS-pruned	-451.61	0.42	0.95	6.39	3	1
3	DGS	-414.8	0.45	0.944	4.9	1	1
3	$\operatorname{DGS-clp}$	-415.49	0.43	0.94	4.9	1	1
3	GS-tw	-629.66	0.44	0.93	7.12	2	2
3	GS- clp	-427.4	0.45	0.94	7.12	2	2
3	GS-pruned	-456.72	0.4	0.94	6.67	3	2
4	$\overline{\mathrm{DGS}}$	-364.14	0.55	0.959	4.4	2	1
4	$\operatorname{DGS-clp}$	-359.2	0.55	0.96	4.4	2	1
4	GS-tw	-657.38	0.51	0.94	6.64	2	2
4	GS- clp	-381.86	0.558	0.959	6.64	2	2
4	GS-pruned	-396.29	0.53	0.96	6.28	3	2
5	DGS	-371.8	0.52	0.95	4.4	1	1
5	$\operatorname{DGS-clp}$	-373.13	0.52	0.96	4.4	1	1
5	GS-tw	-615.19	0.45	0.93	6.8	2	2
5	GS- clp	-385.61	0.55	0.956	6.8	2	2
5	GS-pruned	-394.88	0.49	0.95	6.32	3	2

Table 10: Comparison of the methods in dataset birds in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-464.69	0.39	0.94	4.3	1	1
1	DGS-clp	-463.2	0.403	0.93	4.3	1	1
1	GS-tw	-493.39	0.36	0.94	7.81	3	3
1	GS- clp	-463.37	0.403	0.938	7.81	3	3
1	GS-pruned	-472.5	0.4	0.94	6.5	3	3
2	DGS	-432.34	0.47	0.95	4.9	1	1
2	$\operatorname{DGS-clp}$	-426.3	0.43	0.95	4.9	1	1
2	GS-tw	-473.13	0.481	0.94	7.82	3	2
2	$\operatorname{GS-clp}$	-440.55	0.44	0.948	7.82	3	2
2	GS-pruned	-447.78	0.44	0.95	8.09	3	3
3	DGS	-414.8	0.45	0.94	5.7	1	1
3	$\operatorname{DGS-clp}$	-415.49	0.43	0.94	5.7	1	1
3	GS-tw	-433.59	0.473	0.94	8.36	3	2
3	$\operatorname{GS-clp}$	-419.36	0.44	0.947	8.36	3	2
3	GS-pruned	-434.36	0.44	0.94	7.69	3	2
4	$\overline{\mathrm{DGS}}$	-364.14	0.55	0.959	5.6	2	1
4	$\operatorname{DGS-clp}$	-359.2	0.55	0.96	5.6	2	1
4	GS-tw	-422.26	0.52	0.95	9.38	3	2
4	$\operatorname{GS-clp}$	-377.26	0.558	0.96	9.38	3	2
4	GS-pruned	-393.49	0.52	0.96	6.83	4	2
5	DGS	-371.8	0.52	0.95	4.4	1	1
5	$\operatorname{DGS-clp}$	-373.13	0.52	0.955	4.4	1	1
5	GS-tw	-426.54	0.535	0.95	7.84	3	2
5	GS- clp	-395.78	0.53	0.95	7.84	3	2
5	GS-pruned	-400.2	0.52	0.95	6.49	4	2

Table 11: Comparison of the methods in dataset birds in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	$\overline{\mathrm{DGS}}$	-464.69	0.39	0.94	4.4	1	1
1	$\operatorname{DGS-clp}$	-463.2	0.403	0.93	4.4	1	1
1	GS-tw	-472.5	0.4	0.94	7.46	3	2
1	GS- clp	-468	0.403	0.94	7.46	3	2
1	GS-pruned	-472.5	0.4	0.94	7.11	3	3
2	DGS	-432.34	0.473	0.948	4.8	1	1
2	$\operatorname{DGS-clp}$	-426.3	0.43	0.948	4.8	1	1
2	GS-tw	-443.88	0.44	0.95	7.65	3	2
2	GS- clp	-440.34	0.43	0.95	7.65	3	2
2	GS-pruned	-447.78	0.44	0.95	7.04	3	3
3	DGS	-414.8	0.45	0.94	5.6	1	1
3	$\operatorname{DGS-clp}$	-415.49	0.43	0.94	5.6	1	1
3	GS-tw	-434.81	0.43	0.94	7.64	4	2
3	GS- clp	-432.79	0.43	0.94	7.64	4	2
3	GS-pruned	-434.36	0.44	0.945	6.36	3	2
4	DGS	-364.14	0.55	0.959	4.7	2	1
4	$\operatorname{DGS-clp}$	-359.2	0.55	0.96	4.7	2	1
4	GS-tw	-393.49	0.52	0.96	7.55	4	2
4	GS- clp	-371.88	0.566	0.96	7.55	4	2
4	GS-pruned	-393.49	0.52	0.96	7.18	4	2
5	DGS	-371.8	0.519	0.95	4.5	1	1
5	$\operatorname{DGS-clp}$	-373.13	0.519	0.955	4.5	1	1
5	GS-tw	-400.2	0.519	0.95	8.54	4	2
5	GS- clp	-396.89	0.51	0.95	8.54	4	2
5	GS-pruned	-400.2	0.519	0.95	6.5	4	2

Table 12: Comparison of the methods in dataset birds in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-464.69	0.39	0.94	4.3	1	1
1	$\operatorname{DGS-clp}$	-463.2	0.403	0.93	4.3	1	1
1	GS-tw	-472.5	0.4	0.94	7.47	3	2
1	GS- clp	-468	0.403	0.94	7.47	3	2
1	GS-pruned	-472.5	0.4	0.94	6.73	3	3
2	DGS	-432.34	0.473	0.948	4.7	1	1
2	$\operatorname{DGS-clp}$	-426.3	0.43	0.948	4.7	1	1
2	GS-tw	-447.78	0.44	0.95	7.78	3	2
2	GS- clp	-444.87	0.43	0.95	7.78	3	2
2	GS-pruned	-447.78	0.44	0.95	6.53	3	3
3	DGS	-414.8	0.45	0.94	5.5	1	1
3	$\operatorname{DGS-clp}$	-415.49	0.43	0.94	5.5	1	1
3	GS-tw	-434.36	0.44	0.945	7.89	4	2
3	GS- clp	-434.4	0.42	0.94	7.89	4	2
3	GS-pruned	-434.36	0.44	0.945	6.81	3	2
4	$\overline{\mathrm{DGS}}$	-364.14	0.55	0.959	4.5	2	1
4	$\operatorname{DGS-clp}$	-359.2	0.55	0.96	4.5	2	1
4	GS-tw	-393.49	0.52	0.96	7.7	4	2
4	$\operatorname{GS-clp}$	-371.88	0.566	0.96	7.7	4	2
4	GS-pruned	-393.49	0.52	0.96	6.26	4	2
5	DGS	-371.8	0.519	0.95	4.5	1	1
5	$\operatorname{DGS-clp}$	-373.13	0.519	0.955	4.5	1	1
5	GS-tw	-400.2	0.519	0.95	8.84	4	2
5	GS- clp	-396.89	0.51	0.95	8.84	4	2
5	GS-pruned	-400.2	0.519	0.95	6.58	4	2

Table 13: Comparison of the methods in dataset scene in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-674.62	0.6	0.897	16.15	2	2
1	DGS-clp	-643.3	0.59	0.9	16.15	2	2
1	GS-tw	-3190.74	0.51	0.86	11.8	2	2
1	GS-clp	-1326.52	0.53	0.88	11.8	2	2
1	GS-pruned	-799.89	0.43	0.88	24.99	20	2
2	DGS	-813.7	0.53	0.88	17.53	2	2
2	DGS-clp	-719.5	0.558	0.889	17.53	2	2
2	GS-tw	-2629.79	0.48	0.86	11.8	2	2
2	GS- clp	-1242.91	0.5	0.86	11.8	2	2
2	GS-pruned	-882.71	0.45	0.86	21.39	17	2
3	DGS	-643.25	0.613	0.9	20.16	2	2
3	DGS-clp	-615.2	0.6	0.899	20.16	2	2
3	GS-tw	-3140.02	0.42	0.85	12.2	2	2
3	GS- clp	-1328.36	0.48	0.87	12.2	2	2
3	GS-pruned	-866.79	0.45	0.86	25.96	13	2
4	DGS	-686.13	0.61	0.89	19.57	2	2
4	DGS-clp	-641.5	0.628	0.897	19.57	2	2
4	GS-tw	-4030.28	0.41	0.84	12.4	2	2
4	GS- clp	-1161.97	0.51	0.87	12.4	2	2
4	GS-pruned	-815.36	0.47	0.87	22.82	16	2
5	DGS	-660.32	0.57	0.89	19.08	2	2
5	DGS-clp	-634	0.599	0.897	19.08	2	2
5	GS-tw	-3049.73	0.48	0.86	12.4	2	2
5	GS- clp	-1075.31	0.56	0.88	12.4	2	2
5	GS-pruned	-800.85	0.41	0.87	27.73	20	2

Table 14: Comparison of the methods in dataset scene in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-618.2	0.61	0.899	17.7	3	3
1	$\operatorname{DGS-clp}$	-594	0.616	0.9	17.7	3	3
1	GS-tw	-1558.1	0.51	0.88	23.86	3	3
1	GS- clp	-737.24	0.55	0.88	23.86	3	3
1	GS-pruned	-733.82	0.49	0.88	22.92	21	3
2	DGS	-813.7	0.53	0.88	18.7	2	2
2	$\operatorname{DGS-clp}$	-719.5	0.558	0.889	18.7	2	2
2	GS-tw	-1356.8	0.51	0.87	24.01	3	3
2	GS- clp	-801.73	0.55	0.88	24.01	3	3
2	GS-pruned	-842.93	0.45	0.86	27.15	17	3
3	DGS	-631.4	0.626	0.901	18.1	3	3
3	$\operatorname{DGS-clp}$	-605.8	0.62	0.9	18.1	3	3
3	GS-tw	-1562.19	0.49	0.87	22.82	3	3
3	GS- clp	-758.8	0.52	0.88	22.82	3	3
3	GS-pruned	-773.21	0.49	0.87	25.7	22	3
4	DGS	-655.5	0.632	0.899	18.5	3	3
4	$\operatorname{DGS-clp}$	-623.5	0.62	0.9	18.5	3	3
4	GS-tw	-1395.93	0.5	0.87	24.01	3	3
4	GS- clp	-758.86	0.55	0.88	24.01	3	3
4	GS-pruned	-726.98	0.54	0.88	22.93	15	3
5	DGS	-648.42	0.599	0.894	17.4	3	3
5	$\operatorname{DGS-clp}$	-630.7	0.57	0.89	17.4	3	3
5	GS-tw	-1285.26	0.51	0.86	24.05	3	3
5	$\operatorname{GS-clp}$	-738.85	0.53	0.87	24.05	3	3
5	GS-pruned	-750.37	0.46	0.86	23.8	21	3

Table 15: Comparison of the methods in dataset scene in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-625.01	0.612	0.893	17.9	4	4
1	$\operatorname{DGS-clp}$	-590.7	0.612	0.89	17.9	4	4
1	GS-tw	-663.62	0.58	0.88	27.42	4	4
1	GS- clp	-656.09	0.55	0.88	27.42	4	4
1	GS-pruned	-678.54	0.53	0.88	24.42	20	4
2	DGS	-813.7	0.53	0.88	18.4	2	2
2	$\operatorname{DGS-clp}$	-719.45	0.558	0.889	18.4	2	2
2	GS-tw	-756.76	0.51	0.86	26.66	4	4
2	GS- clp	-699.3	0.54	0.87	26.66	4	4
2	GS-pruned	-762.25	0.46	0.85	29.05	18	4
3	DGS	-631.4	0.626	0.901	17.8	3	3
3	$\operatorname{DGS-clp}$	-605.8	0.62	0.9	17.8	3	3
3	GS-tw	-730.73	0.53	0.87	27.49	4	4
3	GS- clp	-678.2	0.55	0.88	27.49	4	4
3	GS-pruned	-703.37	0.55	0.87	24.96	17	4
4	DGS	-670.22	0.61	0.89	25.37	4	4
4	$\operatorname{DGS-clp}$	-604	0.626	0.896	25.37	4	4
4	GS-tw	-667.99	0.58	0.88	25.65	4	4
4	$\operatorname{GS-clp}$	-643.28	0.54	0.88	25.65	4	4
4	GS-pruned	-705.44	0.51	0.87	23.3	16	4
5	DGS	-574.27	0.653	0.9	18.3	4	4
5	$\operatorname{DGS-clp}$	-548	0.64	0.904	18.3	4	4
5	GS-tw	-690.44	0.56	0.87	26.56	4	4
5	$\operatorname{GS-clp}$	-669.79	0.54	0.87	26.56	4	4
5	GS-pruned	-708.94	0.57	0.87	26.72	22	4

Table 16: Comparison of the methods in dataset scene in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-625.01	0.61	0.893	18.6	4	4
1	DGS-clp	-590.68	0.61	0.89	18.6	4	4
1	GS-tw	-566.4	0.639	0.89	39.26	5	5
1	GS- clp	-581.01	0.61	0.88	39.26	5	5
1	GS-pruned	-590.17	0.62	0.88	25.07	20	5
2	DGS	-813.7	0.53	0.88	19.9	2	2
2	$\operatorname{DGS-clp}$	-719.45	0.56	0.889	19.9	2	2
2	GS-tw	-645.7	0.58	0.87	29.56	5	5
2	$\operatorname{GS-clp}$	-616.1	0.604	0.88	29.56	5	5
2	GS-pruned	-681.04	0.57	0.87	25.49	16	5
3	DGS	-631.4	0.626	0.901	20.1	3	3
3	$\operatorname{DGS-clp}$	-605.8	0.62	0.9	20.1	3	3
3	GS-tw	-659.28	0.6	0.88	28.57	5	5
3	$\operatorname{GS-clp}$	-665.85	0.58	0.87	28.57	5	5
3	GS-pruned	-670.17	0.58	0.87	25.43	18	5
4	DGS	-608.46	0.66	0.9	18.8	5	5
4	$\operatorname{DGS-clp}$	-527.1	0.672	0.898	18.8	5	5
4	GS-tw	-587.14	0.63	0.89	32.9	5	5
4	$\operatorname{GS-clp}$	-577.97	0.62	0.89	32.9	5	5
4	GS-pruned	-634.36	0.57	0.87	25.62	14	5
5	DGS	-574.27	0.653	0.9	18.8	4	4
5	$\operatorname{DGS-clp}$	-548	0.64	0.904	18.8	4	4
5	GS-tw	-602.4	0.58	0.88	29.17	5	5
5	$\operatorname{GS-clp}$	-591.39	0.58	0.88	29.17	5	5
5	GS-pruned	-623.14	0.58	0.87	27.33	22	5

Table 17: Comparison of the methods in dataset genbase in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-14.28	0.985	0.999	19.73	1	1
1	$\operatorname{DGS-clp}$	-3.8	0.985	0.999	19.73	1	1
1	GS-tw	-19.79	0.985	1	17.5	2	2
1	GS- clp	-8.36	0.985	1	17.5	2	2
1	GS-pruned	-20.18	0.985	1	17.8	4	2
2	DGS	-31.35	0.97	1	19.58	1	0
2	$\operatorname{DGS-clp}$	-42.69	0.97	1	19.58	1	0
2	GS-tw	-21.69	0.97	0.999	17.8	2	2
2	GS- clp	-35.97	0.97	1	17.8	2	2
2	GS-pruned	-21.7	0.97	0.999	18.28	4	2
3	DGS	-61.44	0.962	1	17.69	1	1
3	$\operatorname{DGS-clp}$	-90.64	0.962	1	17.69	1	1
3	GS-tw	-49.9	0.95	1	17.1	2	2
3	$\operatorname{GS-clp}$	-80.94	0.962	0.998	17.1	2	2
3	GS-pruned	-50.25	0.95	1	17.43	5	2
4	DGS	-24.61	0.962	0.999	18.6	2	1
4	$\operatorname{DGS-clp}$	-25.92	0.962	0.999	18.6	2	1
4	GS-tw	-19.5	0.962	0.999	16.7	2	2
4	$\operatorname{GS-clp}$	-31.44	0.962	0.999	16.7	2	2
4	GS-pruned	-20.1	0.962	0.999	17.05	5	2
5	DGS	-17.49	0.985	1	19.6	1	1
5	$\operatorname{DGS-clp}$	-21.59	0.985	1	19.6	1	1
5	GS-tw	-12.11	0.985	1	17.2	2	2
5	GS- clp	-12.1	0.985	1	17.2	2	2
5	GS-pruned	-12.15	0.985	1	18.04	4	2

Table 18: Comparison of the methods in dataset genbase in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-14.28	0.985	0.999	19.76	1	1
1	$\operatorname{DGS-clp}$	-3.8	0.985	0.999	19.76	1	1
1	GS-tw	-19.79	0.985	1	18.87	3	3
1	GS- clp	-9.88	0.985	1	18.87	3	3
1	GS-pruned	-19.79	0.985	1	18.4	3	3
2	DGS	-31.35	0.97	1	19.66	1	0
2	$\operatorname{DGS-clp}$	-42.69	0.97	1	19.66	1	0
2	GS-tw	-23.2	0.97	0.999	20.86	3	3
2	GS- clp	-31.62	0.97	1	20.86	3	3
2	GS-pruned	-23.25	0.97	0.999	18.6	4	3
3	DGS	-61.44	0.962	1	18.25	1	1
3	$\operatorname{DGS-clp}$	-90.64	0.962	1	18.25	1	1
3	GS-tw	-50.2	0.95	1	18.3	3	3
3	$\operatorname{GS-clp}$	-71.64	0.962	0.998	18.3	3	3
3	GS-pruned	-50.21	0.95	1	18.1	5	3
4	DGS	-24.61	0.962	0.999	18.74	2	1
4	$\operatorname{DGS-clp}$	-25.92	0.962	0.999	18.74	2	1
4	GS-tw	-20.04	0.962	0.999	17.5	3	3
4	$\operatorname{GS-clp}$	-33.68	0.962	0.999	17.5	3	3
4	GS-pruned	-20	0.962	0.999	17.59	4	3
5	DGS	-17.49	0.985	1	19.98	1	1
5	$\operatorname{DGS-clp}$	-21.59	0.985	1	19.98	1	1
5	GS-tw	-12	0.985	1	18.14	3	3
5	GS- clp	-14.28	0.985	1	18.14	3	3
5	GS-pruned	-12.09	0.985	1	18.1	4	3

Table 19: Comparison of the methods in dataset genbase in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-14.28	0.985	0.999	19.77	1	1
1	$\operatorname{DGS-clp}$	-3.8	0.985	0.999	19.77	1	1
1	GS-tw	-19.86	0.985	1	18.87	4	4
1	GS- clp	-10.32	0.985	1	18.87	4	4
1	GS-pruned	-19.86	0.985	1	18.8	4	4
2	DGS	-31.35	0.97	1	19.45	1	0
2	$\operatorname{DGS-clp}$	-42.69	0.97	1	19.45	1	0
2	GS-tw	-23.3	0.97	0.999	19.09	4	3
2	GS- clp	-41.76	0.97	1	19.09	4	3
2	GS-pruned	-23.3	0.97	0.999	18.7	4	3
3	DGS	-61.44	0.962	1	18	1	1
3	$\operatorname{DGS-clp}$	-90.64	0.962	1	18	1	1
3	GS-tw	-49.29	0.95	1	18.24	4	3
3	GS- clp	-87.86	0.962	0.998	18.24	4	3
3	GS-pruned	-49.3	0.95	1	18.44	5	3
4	DGS	-24.61	0.962	0.999	18.75	2	1
4	$\operatorname{DGS-clp}$	-25.92	0.962	0.999	18.75	2	1
4	GS-tw	-20.02	0.962	0.999	17.5	4	4
4	GS- clp	-49.4	0.962	0.999	17.5	4	4
4	GS-pruned	-20	0.962	0.999	18.02	5	4
5	DGS	-17.49	0.985	1	19.88	1	1
5	$\operatorname{DGS-clp}$	-21.59	0.985	1	19.88	1	1
5	GS-tw	-12.1	0.985	1	18.53	4	3
5	GS- clp	-16.38	0.985	1	18.53	4	3
5	GS-pruned	-12.1	0.985	1	18.4	4	3

Table 20: Comparison of the methods in dataset genbase in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-14.28	0.985	0.999	19.57	1	1
1	$\operatorname{DGS-clp}$	-3.8	0.985	0.999	19.57	1	1
1	GS-tw	-19.86	0.985	1	18.6	4	4
1	GS- clp	-10.32	0.985	1	18.6	4	4
1	GS-pruned	-19.86	0.985	1	18.71	4	4
2	DGS	-31.35	0.97	1	19.67	1	0
2	$\operatorname{DGS-clp}$	-42.69	0.97	1	19.67	1	0
2	GS-tw	-23.3	0.97	0.999	18.83	4	3
2	GS- clp	-41.76	0.97	1	18.83	4	3
2	GS-pruned	-23.3	0.97	0.999	18.7	4	3
3	DGS	-61.44	0.962	1	18	1	1
3	$\operatorname{DGS-clp}$	-90.64	0.962	1	18	1	1
3	GS-tw	-49.3	0.95	1	18.46	5	3
3	GS- clp	-87.07	0.962	0.998	18.46	5	3
3	GS-pruned	-49.3	0.95	1	18.48	5	3
4	DGS	-24.61	0.962	0.999	18.63	2	1
4	$\operatorname{DGS-clp}$	-25.92	0.962	0.999	18.63	2	1
4	GS-tw	-20	0.962	0.999	17.95	5	4
4	GS- clp	-41.39	0.962	0.999	17.95	5	4
4	GS-pruned	-20	0.962	0.999	17.9	5	4
5	DGS	-17.49	0.985	1	19.79	1	1
5	$\operatorname{DGS-clp}$	-21.59	0.985	1	19.79	1	1
5	GS-tw	-12.1	0.985	1	18.2	4	3
5	GS- clp	-16.38	0.985	1	18.2	4	3
5	GS-pruned	-12.1	0.985	1	18.2	4	3

Table 21: Comparison of the methods in dataset yeast in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold Method CLL acc_G acc_M time tw tw-pr 1 DGS -2192.33 0.14 0.78 2.84 2 2 1 DGS-clp -2173.3 0.13 0.784 2.84 2 2 1 GS-tw -2660.47 0.143 0.77 1.9 2 2 1 GS-clp -2611.93 0.08 0.75 1.9 2 2 1 GS-pruned -2260.46 0.12 0.78 2.4 5 2 2 DGS -2098.62 0.17 0.79 2.59 2 2 2 DGS-clp -2089.3 0.16 0.79 1.7 2 2 2 DGS-clp -2209.91 0.16 0.79 1.7 2 2 2 GS-pruned -2185.57 0.17 0.79 2.7 2 2 3 DGS-clp -2117.1 0.16 0.79 </th <th></th> <th></th> <th></th> <th></th> <th></th> <th></th> <th></th> <th></th>								
1 DGS-clp -2173.3 0.13 0.784 2.84 2 2 1 GS-tw -2660.47 0.143 0.77 1.9 2 2 1 GS-clp -2611.93 0.08 0.75 1.9 2 2 1 GS-pruned -2260.46 0.12 0.78 2.4 5 2 2 DGS -2098.62 0.17 0.79 2.59 2 2 2 DGS-clp -2089.3 0.178 0.791 2.59 2 2 2 DGS-clp -2089.3 0.178 0.791 2.59 2 2 2 GS-tw -2642.62 0.16 0.79 1.7 2 2 2 GS-clp -2200.91 0.16 0.78 1.7 2 2 3 DGS -2137.6 0.16 0.79 2.7 2 2 3 DGS-clp -2111.1 0.16 0.79 2.7 2 2 3 GS-pruned -2182.17 0.12	Fold	Method	CLL	acc_G	acc_M	$_{ m time}$	tw	tw-pr
1 GS-tw -2660.47 0.143 0.77 1.9 2 2 1 GS-clp -2611.93 0.08 0.75 1.9 2 2 1 GS-pruned -2260.46 0.12 0.78 2.4 5 2 2 DGS -2098.62 0.17 0.79 2.59 2 2 2 DGS-clp -2089.3 0.178 0.791 2.59 2 2 2 DGS-clp -2089.3 0.178 0.791 2.59 2 2 2 DGS-clp -2209.91 0.16 0.791 1.7 2 2 2 GS-pruned -2185.57 0.17 0.79 2.43 6 2 3 DGS -2137.6 0.16 0.79 2.7 2 2 3 DGS-clp -2111.1 0.16 0.79 2.7 2 2 3 GS-pruned -2279.63 0.18 0.798 1.7 2 2 3 GS-pruned -2182.17 0.12	1	DGS	-2192.33	0.14	0.78	2.84	2	2
1 GS-clp -2611.93 0.08 0.75 1.9 2 2 1 GS-pruned -2260.46 0.12 0.78 2.4 5 2 2 DGS -2098.62 0.17 0.79 2.59 2 2 2 DGS-clp -2089.3 0.178 0.791 2.59 2 2 2 DGS-clp -2089.3 0.16 0.791 2.59 2 2 2 DGS-clp -2089.3 0.16 0.791 1.7 2 2 2 DGS-clp -2200.91 0.16 0.79 1.7 2 2 2 DGS-pruned -2185.57 0.17 0.79 2.43 6 2 3 DGS -2137.6 0.16 0.79 2.7 2 2 3 DGS-clp -2111.1 0.16 0.79 1.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-pruned -2182.17 0.12	1	$\operatorname{DGS-clp}$	-2173.3	0.13	0.784	2.84	2	2
1 GS-pruned -2260.46 0.12 0.78 2.4 5 2 2 DGS -2098.62 0.17 0.79 2.59 2 2 2 DGS-clp -2089.3 0.178 0.791 2.59 2 2 2 GS-tw -2642.62 0.16 0.79 1.7 2 2 2 GS-clp -2200.91 0.16 0.78 1.7 2 2 2 GS-pruned -2185.57 0.17 0.79 2.43 6 2 3 DGS -2137.6 0.16 0.79 2.7 2 2 3 DGS-clp -2111.1 0.16 0.79 2.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-pruned -2279.63 0.18 0.798 1.7 2 2 4 DGS -2194.79 0.12 0.78 <	1	GS-tw	-2660.47	0.143	0.77	1.9	2	2
2 DGS -2098.62 0.17 0.79 2.59 2 2 2 DGS-clp -2089.3 0.178 0.791 2.59 2 2 2 GS-tw -2642.62 0.16 0.79 1.7 2 2 2 GS-clp -2200.91 0.16 0.78 1.7 2 2 2 GS-pruned -2185.57 0.17 0.79 2.43 6 2 3 DGS -2137.6 0.16 0.79 2.7 2 2 3 DGS-clp -2111.1 0.16 0.79 2.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-clp -2279.63 0.18 0.798 1.7 2 2 3 GS-pruned -2194.79 0.12 0.78 2.5 2 2 4 DGS -2194.79 0.12 0.78 <td>1</td> <td>GS-clp</td> <td>-2611.93</td> <td>0.08</td> <td>0.75</td> <td>1.9</td> <td>2</td> <td>2</td>	1	GS- clp	-2611.93	0.08	0.75	1.9	2	2
2 DGS-clp -2089.3 0.178 0.791 2.59 2 2 2 GS-tw -2642.62 0.16 0.79 1.7 2 2 2 GS-clp -2200.91 0.16 0.79 1.7 2 2 2 GS-pruned -2185.57 0.17 0.79 2.43 6 2 3 DGS -2137.6 0.16 0.79 2.7 2 2 3 DGS-clp -2111.1 0.16 0.79 2.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-tw -2279.63 0.18 0.798 1.7 2 2 3 GS-pruned -2182.17 0.12 0.78 2.3 4 2 4 DGS -2194.79 0.12 0.78 2.5 2 2 4 GS-tw -240.16 0.11 0.77	1	GS-pruned	-2260.46	0.12	0.78	2.4	5	2
2 GS-tw -2642.62 0.16 0.79 1.7 2 2 2 GS-clp -2200.91 0.16 0.78 1.7 2 2 2 GS-pruned -2185.57 0.17 0.79 2.43 6 2 3 DGS -2137.6 0.16 0.79 2.7 2 2 3 DGS-clp -2111.1 0.16 0.79 2.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-tpuned -2279.63 0.18 0.798 1.7 2 2 3 GS-pruned -2182.17 0.12 0.78 2.3 4 2 4 DGS -2194.79 0.12 0.78 2.5 2 2 4 GS-clp -2182.1 0.12 0.79 2.5 2 2 4 GS-tw -2740.16 0.11 0.77 2 2 2 4 GS-pruned -2270.94 0.09 0.77 </td <td>2</td> <td>DGS</td> <td>-2098.62</td> <td>0.17</td> <td>0.79</td> <td>2.59</td> <td>2</td> <td>2</td>	2	DGS	-2098.62	0.17	0.79	2.59	2	2
2 GS-clp -2200.91 0.16 0.78 1.7 2 2 2 GS-pruned -2185.57 0.17 0.79 2.43 6 2 3 DGS -2137.6 0.16 0.79 2.7 2 2 3 DGS-clp -2111.1 0.16 0.79 1.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-clp -2279.63 0.18 0.798 1.7 2 2 3 GS-pruned -2182.17 0.12 0.78 2.3 4 2 4 DGS -2194.79 0.12 0.78 2.5 2 2 4 GS-clp -2182.1 0.12 0.79 2.5 2 2 4 GS-tw -2740.16 0.11 0.77 2 2 2 4 GS-pruned -2270.94 0.09 0.77	2	$\operatorname{DGS-clp}$	-2089.3	0.178	0.791	2.59	2	2
2 GS-pruned -2185.57 0.17 0.79 2.43 6 2 3 DGS -2137.6 0.16 0.79 2.7 2 2 3 DGS-clp -2111.1 0.16 0.79 2.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-clp -2279.63 0.18 0.798 1.7 2 2 3 GS-pruned -2182.17 0.12 0.78 2.3 4 2 4 DGS -2194.79 0.12 0.78 2.5 2 2 4 DGS-clp -2182.1 0.12 0.79 2.5 2 2 4 GS-tw -2740.16 0.11 0.77 2 2 2 4 GS-pruned -2226.07 0.128 0.788 2 2 2 4 GS-pruned -2270.94 0.09 0.77 2.36 5 2 5 DGS-clp -2078.1 0.17 0.7	2	GS-tw	-2642.62	0.16	0.79	1.7	2	2
3 DGS -2137.6 0.16 0.79 2.7 2 2 3 DGS-clp -2111.1 0.16 0.79 2.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-clp -2279.63 0.18 0.798 1.7 2 2 3 GS-pruned -2182.17 0.12 0.78 2.3 4 2 4 DGS -2194.79 0.12 0.78 2.5 2 2 4 DGS-clp -2182.1 0.12 0.79 2.5 2 2 4 GS-tw -2740.16 0.11 0.77 2 2 2 4 GS-clp -2226.07 0.128 0.788 2 2 2 4 GS-pruned -2270.94 0.09 0.77 2.36 5 2 5 DGS -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.78	2	$\operatorname{GS-clp}$	-2200.91	0.16	0.78	1.7	2	2
3 DGS-clp -2111.1 0.16 0.79 2.7 2 2 3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-clp -2279.63 0.18 0.798 1.7 2 2 3 GS-pruned -2182.17 0.12 0.78 2.3 4 2 4 DGS -2194.79 0.12 0.78 2.5 2 2 4 DGS-clp -2182.1 0.12 0.79 2.5 2 2 4 GS-tw -2740.16 0.11 0.77 2 2 2 4 GS-clp -2226.07 0.128 0.788 2 2 2 4 GS-pruned -2270.94 0.09 0.77 2.36 5 2 5 DGS -2089.25 0.18 0.79 2.45 2 2 5 DGS-clp -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.79 <td>2</td> <td>GS-pruned</td> <td>-2185.57</td> <td>0.17</td> <td>0.79</td> <td>2.43</td> <td>6</td> <td>2</td>	2	GS-pruned	-2185.57	0.17	0.79	2.43	6	2
3 GS-tw -2816.39 0.16 0.79 1.7 2 2 3 GS-clp -2279.63 0.18 0.798 1.7 2 2 3 GS-pruned -2182.17 0.12 0.78 2.3 4 2 4 DGS -2194.79 0.12 0.78 2.5 2 2 4 DGS-clp -2182.1 0.12 0.79 2.5 2 2 4 GS-tw -2740.16 0.11 0.77 2 2 2 4 GS-clp -2226.07 0.128 0.788 2 2 2 4 GS-pruned -2270.94 0.09 0.77 2.36 5 2 5 DGS -2089.25 0.18 0.79 2.45 2 2 5 DGS-clp -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.79 1.6 2 2 5 GS-clp -2139.19 0.18 0.79 <td>3</td> <td>DGS</td> <td>-2137.6</td> <td>0.16</td> <td>0.79</td> <td>2.7</td> <td>2</td> <td>2</td>	3	DGS	-2137.6	0.16	0.79	2.7	2	2
3 GS-clp -2279.63 0.18 0.798 1.7 2 2 3 GS-pruned -2182.17 0.12 0.78 2.3 4 2 4 DGS -2194.79 0.12 0.78 2.5 2 2 4 DGS-clp -2182.1 0.12 0.79 2.5 2 2 4 GS-tw -2740.16 0.11 0.77 2 2 2 4 GS-clp -2226.07 0.128 0.788 2 2 2 4 GS-pruned -2270.94 0.09 0.77 2.36 5 2 5 DGS -2089.25 0.18 0.79 2.45 2 2 5 DGS-clp -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.78 1.6 2 2 5 GS-clp -2139.19 0.18 0.79 1.6 2 2	3	$\operatorname{DGS-clp}$	-2111.1	0.16	0.79	2.7	2	2
3 GS-pruned -2182.17 0.12 0.78 2.3 4 2 4 DGS -2194.79 0.12 0.78 2.5 2 2 4 DGS-clp -2182.1 0.12 0.79 2.5 2 2 4 GS-tw -2740.16 0.11 0.77 2 2 2 4 GS-clp -2226.07 0.128 0.788 2 2 2 4 GS-pruned -2270.94 0.09 0.77 2.36 5 2 5 DGS -2089.25 0.18 0.79 2.45 2 2 5 DGS-clp -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.78 1.6 2 2 5 GS-clp -2139.19 0.18 0.79 1.6 2 2	3	GS-tw	-2816.39	0.16	0.79	1.7	2	2
4 DGS -2194.79 0.12 0.78 2.5 2 2 4 DGS-clp -2182.1 0.12 0.79 2.5 2 2 4 GS-tw -2740.16 0.11 0.77 2 2 2 4 GS-pruned -2226.07 0.128 0.788 2 2 2 4 GS-pruned -2270.94 0.09 0.77 2.36 5 2 5 DGS -2089.25 0.18 0.79 2.45 2 2 5 DGS-clp -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.78 1.6 2 2 5 GS-clp -2139.19 0.18 0.79 1.6 2 2	3	$\operatorname{GS-clp}$	-2279.63	0.18	0.798	1.7	2	2
4 DGS-clp -2182.1 0.12 0.79 2.5 2 2 4 GS-tw -2740.16 0.11 0.77 2 2 2 4 GS-clp -2226.07 0.128 0.788 2 2 2 4 GS-pruned -2270.94 0.09 0.77 2.36 5 2 5 DGS -2089.25 0.18 0.79 2.45 2 2 5 DGS-clp -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.78 1.6 2 2 5 GS-clp -2139.19 0.18 0.79 1.6 2 2	3	GS-pruned	-2182.17	0.12	0.78	2.3	4	2
4 GS-tw -2740.16 0.11 0.77 2 2 2 4 GS-clp -2226.07 0.128 0.788 2 2 2 4 GS-pruned -2270.94 0.09 0.77 2.36 5 2 5 DGS -2089.25 0.18 0.79 2.45 2 2 5 DGS-clp -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.78 1.6 2 2 5 GS-clp -2139.19 0.18 0.79 1.6 2 2	4	DGS	-2194.79	0.12	0.78	2.5	2	2
4 GS-clp -2226.07 0.128 0.788 2 2 2 4 GS-pruned -2270.94 0.09 0.77 2.36 5 2 5 DGS -2089.25 0.18 0.79 2.45 2 2 5 DGS-clp -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.78 1.6 2 2 5 GS-clp -2139.19 0.18 0.79 1.6 2 2	4	$\operatorname{DGS-clp}$	-2182.1	0.12	0.79	2.5	2	2
4 GS-pruned -2270.94 0.09 0.77 2.36 5 2 5 DGS -2089.25 0.18 0.79 2.45 2 2 5 DGS-clp -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.78 1.6 2 2 5 GS-clp -2139.19 0.18 0.79 1.6 2 2	4	GS-tw	-2740.16	0.11	0.77	2	2	2
5 DGS -2089.25 0.18 0.79 2.45 2 2 5 DGS-clp -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.78 1.6 2 2 5 GS-clp -2139.19 0.18 0.79 1.6 2 2	4	$\operatorname{GS-clp}$	-2226.07	0.128	0.788	2	2	2
5 DGS-clp -2078.1 0.17 0.79 2.45 2 2 5 GS-tw -2489.37 0.18 0.78 1.6 2 2 5 GS-clp -2139.19 0.18 0.79 1.6 2 2	4	GS-pruned	-2270.94	0.09	0.77	2.36	5	2
5 GS-tw -2489.37 0.18 0.78 1.6 2 2 5 GS-clp -2139.19 0.18 0.79 1.6 2 2	5	DGS	-2089.25	0.18	0.79	2.45	2	2
5 GS-clp -2139.19 0.18 0.79 1.6 2 2	5	$\operatorname{DGS-clp}$	-2078.1	0.17	0.79	2.45	2	2
	5	GS-tw	-2489.37	0.18	0.78	1.6	2	2
5 GS-pruned -2115.9 0.18 0.79 2.5 6 2	5	$\operatorname{GS-clp}$	-2139.19	0.18	0.79	1.6	2	2
3 ds praned 2110.0 0.10 0.10 2.0 0 2	5	GS-pruned	-2115.9	0.18	0.79	2.5	6	2

Table 22: Comparison of the methods in dataset yeast in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

	ethod DGS	CLL	acc_G	acc_M	$_{ m time}$	tw	tw-pr
1	DGS						ow-br
	Dab	-2045.9	0.19	0.78	2.83	3	3
1 D	GS-clp	-2018	0.194	0.78	2.83	3	3
1 ($\mathrm{GS-tw}$	-2116.96	0.18	0.78	2.81	3	3
1 6	S-clp	-2055.3	0.19	0.78	2.81	3	3
1 GS-	-pruned	-2109.76	0.17	0.77	2.3	6	3
2	DGS	-1984.15	0.186	0.79	2.78	3	3
2 D	GS-clp	-1969.7	0.18	0.795	2.78	3	3
2 (S-tw	-2039.12	0.18	0.79	2.6	3	3
2 6	S-clp	-1990.05	0.18	0.79	2.6	3	3
2 GS-	-pruned	-2036.01	0.18	0.78	2.5	5	3
3	DGS	-2017.79	0.18	0.792	2.95	3	3
3 De	GS-clp	-1988.3	0.18	0.79	2.95	3	3
3	GS-tw	-2120.75	0.19	0.79	2.3	3	3
3 G	S-clp	-1998.96	0.19	0.79	2.3	3	3
3 GS-	pruned	-2058.6	0.17	0.78	2.38	5	3
4	DGS	-2008.69	0.168	0.78	2.77	3	3
4 De	GS-clp	-2002.13	0.16	0.784	2.77	3	3
4 (GS-tw	-2031.25	0.16	0.78	2.3	3	3
4 G	S-clp	-1997.6	0.16	0.78	2.3	3	3
4 GS-	-pruned	-2066.41	0.15	0.78	2.55	6	3
5	DGS	-1979.35	0.2	0.79	2.64	3	3
5 De	GS-clp	-1966.5	0.19	0.79	2.64	3	3
5 (GS-tw	-1982.61	0.21	0.795	2.55	3	3
5 G	S-clp	-1947.1	0.217	0.79	2.55	3	3
5 GS-	-pruned	-1964.74	0.2	0.79	2.4	6	3

Table 23: Comparison of the methods in dataset yeast in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-1998.73	0.19	0.78	3.2	4	4
1	$\operatorname{DGS-clp}$	-1973.6	0.205	0.783	3.2	4	4
1	GS-tw	-2038.22	0.19	0.78	2.87	4	4
1	GS- clp	-2000.96	0.19	0.77	2.87	4	4
1	GS-pruned	-2030.35	0.19	0.78	2.6	6	4
2	DGS	-1962.04	0.188	0.79	2.97	4	4
2	$\operatorname{DGS-clp}$	-1947.8	0.18	0.794	2.97	4	4
2	GS-tw	-2012.18	0.17	0.79	2.66	4	4
2	$\operatorname{GS-clp}$	-1996.68	0.17	0.78	2.66	4	4
2	GS-pruned	-2015.46	0.18	0.78	2.5	5	4
3	DGS	-1980	0.197	0.79	3.04	4	4
3	$\operatorname{DGS-clp}$	-1955.5	0.19	0.794	3.04	4	4
3	GS-tw	-2017.83	0.18	0.79	2.94	4	4
3	GS- clp	-1968.22	0.19	0.79	2.94	4	4
3	GS-pruned	-2023.37	0.18	0.78	2.6	5	4
4	DGS	-1973.53	0.18	0.79	2.85	4	4
4	$\operatorname{DGS-clp}$	-1966.7	0.16	0.786	2.85	4	4
4	GS-tw	-2002.32	0.15	0.78	2.86	4	4
4	GS- clp	-1987.94	0.16	0.78	2.86	4	4
4	GS-pruned	-2038.18	0.15	0.77	2.4	5	4
5	DGS	-1927.96	0.19	0.791	3.13	4	4
5	$\operatorname{DGS-clp}$	-1910.8	0.2	0.79	3.13	4	4
5	GS-tw	-1933.26	0.209	0.79	3.06	4	4
5	GS- clp	-1927.73	0.2	0.79	3.06	4	4
5	GS-pruned	-1934.79	0.2	0.79	2.6	6	4

Table 24: Comparison of the methods in dataset yeast in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-1979.19	0.2	0.78	3.52	5	5
1	$\operatorname{DGS-clp}$	-1955.7	0.213	0.783	3.52	5	5
1	GS-tw	-2007.4	0.17	0.77	3.07	5	5
1	GS- clp	-1993.13	0.18	0.77	3.07	5	5
1	GS-pruned	-2023.76	0.18	0.77	2.5	6	5
2	DGS	-1962.04	0.188	0.79	3.2	4	4
2	$\operatorname{DGS-clp}$	-1947.8	0.18	0.794	3.2	4	4
2	GS-tw	-2023.42	0.18	0.78	2.79	5	5
2	$\operatorname{GS-clp}$	-2010.23	0.18	0.78	2.79	5	5
2	GS-pruned	-2023.37	0.18	0.78	2.3	5	5
3	DGS	-1976.93	0.199	0.79	3.54	5	5
3	$\operatorname{DGS-clp}$	-1952	0.19	0.795	3.54	5	5
3	GS-tw	-2034.29	0.19	0.79	2.82	5	5
3	GS- clp	-1987.55	0.18	0.79	2.82	5	5
3	GS-pruned	-2031.61	0.18	0.78	2.7	5	5
4	DGS	-1955.15	0.174	0.786	3.04	5	5
4	$\operatorname{DGS-clp}$	-1948.8	0.16	0.786	3.04	5	5
4	GS-tw	-1991.59	0.15	0.78	2.89	5	5
4	GS- clp	-1986.86	0.15	0.78	2.89	5	5
4	GS-pruned	-2018.41	0.15	0.77	2.5	6	5
5	DGS	-1922.15	0.19	0.79	2.89	5	5
5	$\operatorname{DGS-clp}$	-1903.6	0.203	0.79	2.89	5	5
5	GS-tw	-1924.62	0.2	0.79	2.9	5	5
5	GS- clp	-1914.44	0.2	0.79	2.9	5	5
5	GS-pruned	-1930.62	0.203	0.79	2.3	6	5

Table 25: Comparison of the methods in dataset medical in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-297.1	0.62	0.99	88.5	2	1
1	$\operatorname{DGS-clp}$	-317.2	0.663	0.989	88.5	2	1
1	GS-tw	-459.99	0.55	0.99	182.41	2	2
1	GS- clp	-339.2	0.62	0.99	182.41	2	2
1	GS-pruned	-365.45	0.63	0.99	221.29	20	2
2	DGS	-325.3	0.67	0.99	92.6	2	1
2	$\operatorname{DGS-clp}$	-327.56	0.679	0.989	92.6	2	1
2	GS-tw	-478.11	0.6	0.99	170.01	2	2
2	GS- clp	-368.45	0.62	0.99	170.01	2	2
2	GS-pruned	-343.09	0.61	0.99	203.29	18	2
3	DGS	-249	0.69	0.991	97.1	2	1
3	$\operatorname{DGS-clp}$	-251.1	0.704	0.99	97.1	2	1
3	GS-tw	-376.55	0.6	0.99	188.42	2	2
3	GS- clp	-298.22	0.65	0.99	188.42	2	2
3	GS-pruned	-295.64	0.62	0.99	224.87	20	2
4	DGS	-341.9	0.59	0.99	90.1	2	2
4	$\operatorname{DGS-clp}$	-376.74	0.59	0.99	90.1	2	2
4	GS-tw	-452.76	0.58	0.99	185.87	2	2
4	GS- clp	-382.54	0.58	0.99	185.87	2	2
4	GS-pruned	-377.71	0.621	0.988	237.23	19	2
5	DGS	-277.7	0.64	0.99	89.9	2	1
5	$\operatorname{DGS-clp}$	-287.12	0.682	0.99	89.9	2	1
5	GS-tw	-378.15	0.62	0.99	181.93	2	2
5	GS- clp	-327.35	0.68	0.99	181.93	2	2
5	GS-pruned	-322.51	0.66	0.99	231.24	16	2

Table 26: Comparison of the methods in dataset medical in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-283.5	0.65	0.99	91.3	3	2
1	$\operatorname{DGS-clp}$	-291.64	0.658	0.99	91.3	3	2
1	GS-tw	-396.33	0.57	0.99	223.35	3	3
1	GS- clp	-368.83	0.64	0.989	223.35	3	3
1	GS-pruned	-361.57	0.61	0.99	241.87	20	3
2	DGS	-308	0.663	0.99	91.9	3	2
2	$\operatorname{DGS-clp}$	-323.19	0.65	0.99	91.9	3	2
2	GS-tw	-384	0.62	0.99	212	3	3
2	GS- clp	-338.26	0.64	0.99	212	3	3
2	GS-pruned	-341.38	0.63	0.988	221.57	20	3
3	DGS	-248.3	0.69	0.991	96.6	3	1
3	$\operatorname{DGS-clp}$	-251.98	0.704	0.99	96.6	3	1
3	GS-tw	-300.24	0.64	0.99	232.62	3	3
3	$\operatorname{GS-clp}$	-319.13	0.62	0.99	232.62	3	3
3	GS-pruned	-298.75	0.65	0.99	245.04	22	3
4	DGS	-331.2	0.605	0.988	92.3	3	2
4	$\operatorname{DGS-clp}$	-357.54	0.6	0.99	92.3	3	2
4	GS-tw	-432.17	0.57	0.99	231.52	3	3
4	GS- clp	-400.04	0.57	0.99	231.52	3	3
4	GS-pruned	-390.18	0.6	0.99	235.87	19	3
5	DGS	-273.9	0.64	0.99	96.4	3	1
5	$\operatorname{DGS-clp}$	-289.16	0.677	0.99	96.4	3	1
5	GS-tw	-331.65	0.64	0.99	218.36	3	3
5	GS- clp	-333.48	0.65	0.99	218.36	3	3
5	GS-pruned	-329.74	0.63	0.99	231.44	16	3

Table 27: Comparison of the methods in dataset medical in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

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Fold	Method	CLL	acc_G	acc_M	$_{ m time}$	tw	tw-pr
1	DGS	-283.5	0.65	0.99	93.7	3	2
1	$\operatorname{DGS-clp}$	-291.64	0.66	0.99	93.7	3	2
1	GS-tw	-386.58	0.58	0.99	220.73	4	3
1	GS- clp	-362.49	0.658	0.989	220.73	4	3
1	GS-pruned	-361.57	0.61	0.99	227.32	20	3
2	DGS	-308	0.663	0.99	95.8	3	2
2	$\operatorname{DGS-clp}$	-323.19	0.65	0.99	95.8	3	2
2	GS-tw	-359.65	0.63	0.99	214.23	4	4
2	GS- clp	-375.46	0.63	0.99	214.23	4	4
2	GS-pruned	-342.07	0.63	0.988	209.79	20	4
3	DGS	-248.3	0.69	0.991	99.1	3	1
3	$\operatorname{DGS-clp}$	-251.98	0.704	0.99	99.1	3	1
3	GS-tw	-302.69	0.65	0.99	226.99	4	3
3	GS- clp	-305.31	0.67	0.99	226.99	4	3
3	GS-pruned	-298.75	0.65	0.99	229.07	22	3
4	DGS	-331.2	0.605	0.988	94.6	3	2
4	$\operatorname{DGS-clp}$	-357.54	0.6	0.99	94.6	3	2
4	GS-tw	-408.62	0.59	0.99	218.29	4	4
4	GS- clp	-398.08	0.6	0.99	218.29	4	4
4	GS-pruned	-394.87	0.6	0.99	227.9	19	4
5	DGS	-273.9	0.64	0.99	95.5	3	1
5	$\operatorname{DGS-clp}$	-289.16	0.677	0.99	95.5	3	1
5	GS-tw	-324.49	0.63	0.99	213.73	4	3
5	GS- clp	-300.53	0.65	0.99	213.73	4	3
5	GS-pruned	-329.74	0.63	0.99	219.21	16	3

Table 28: Comparison of the methods in dataset medical in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	$\overline{\mathrm{DGS}}$	-283.5	0.65	0.99	93.5	3	2
1	$\operatorname{DGS-clp}$	-291.64	0.658	0.989	93.5	3	2
1	GS-tw	-380.44	0.58	0.99	221.47	5	3
1	GS- clp	-356.73	0.65	0.99	221.47	5	3
1	GS-pruned	-361.57	0.61	0.99	230.65	20	3
2	DGS	-308	0.66	0.99	91	3	2
2	$\operatorname{DGS-clp}$	-323.19	0.65	0.99	91	3	2
2	GS-tw	-352.29	0.63	0.99	216.3	5	4
2	GS- clp	-325.75	0.668	0.989	216.3	5	4
2	GS-pruned	-342.07	0.63	0.99	211.38	20	4
3	DGS	-248.3	0.69	0.991	99.2	3	1
3	$\operatorname{DGS-clp}$	-251.98	0.704	0.99	99.2	3	1
3	GS-tw	-294.97	0.64	0.99	234.83	5	3
3	GS- clp	-313.04	0.68	0.99	234.83	5	3
3	GS-pruned	-298.75	0.65	0.99	230.21	22	3
4	DGS	-331.2	0.605	0.988	93.9	3	2
4	$\operatorname{DGS-clp}$	-357.54	0.6	0.99	93.9	3	2
4	GS-tw	-405.3	0.59	0.99	223.41	5	3
4	GS- clp	-385.28	0.59	0.99	223.41	5	3
4	GS-pruned	-394.87	0.6	0.99	226.14	19	4
5	DGS	-273.9	0.64	0.99	93.3	3	1
5	$\operatorname{DGS-clp}$	-289.16	0.677	0.99	93.3	3	1
5	GS-tw	-318.9	0.63	0.99	230.34	5	3
5	GS- clp	-302.74	0.67	0.99	230.34	5	3
5	GS-pruned	-329.74	0.63	0.99	217.13	16	3

Table 29: Comparison of the methods in dataset enron in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	$_{ m time}$	\mathbf{tw}	tw-pr
1	DGS	-2230	0.18	0.95	516.89	2	2
1	$\operatorname{DGS-clp}$	-2208.9	0.208	0.954	516.89	2	2
1	GS-tw	-4945.07	0.16	0.95	$\boldsymbol{465.2}$	2	2
1	GS- clp	-2509.63	0.15	0.95	$\boldsymbol{465.2}$	2	2
1	GS-pruned	-2540.47	0.18	0.95	879.31	301	2
2	DGS	-2343.35	0.13	0.95	502.19	2	2
2	$\operatorname{DGS-clp}$	-2328.4	0.12	0.95	502.19	2	2
2	GS-tw	-6225.88	0.12	0.95	499.8	2	2
2	GS- clp	-3354.15	0.12	0.95	499.8	2	2
2	GS-pruned	-2601.76	0.138	0.95	865.86	290	2
3	DGS	-2598.96	0.12	0.95	525.1	2	2
3	$\operatorname{DGS-clp}$	-2585	0.13	0.948	525.1	2	2
3	GS-tw	-6974.26	0.12	0.95	466.3	2	2
3	GS- clp	-2786.05	0.13	0.94	466.3	2	2
3	GS-pruned	-2955.42	0.147	0.95	832.53	285	2
4	DGS	-2369	0.13	0.951	527.42	2	2
4	$\operatorname{DGS-clp}$	-2362.3	0.13	0.95	527.42	2	2
4	GS-tw	-5536.03	0.13	0.95	502.1	2	2
4	GS- clp	-3175.06	0.11	0.94	502.1	2	2
4	GS-pruned	-2640.17	0.138	0.95	852.39	321	2
5	DGS	-2481.97	0.14	0.95	511.71	2	2
5	$\operatorname{DGS-clp}$	-2468.7	0.153	0.951	511.71	2	2
5	GS-tw	-6744.56	0.12	0.95	470.6	2	2
5	GS- clp	-3092.26	0.12	0.95	470.6	2	2
5	GS-pruned	-3112.37	0.14	0.95	817.18	280	2

Table 30: Comparison of the methods in dataset enron in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

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Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-2228.26	0.18	0.95	566	3	3
1	$\operatorname{DGS-clp}$	-2206.5	0.208	0.954	566	3	3
1	GS-tw	-3546.09	0.18	0.95	737.09	3	3
1	$\operatorname{GS-clp}$	-2506.06	0.17	0.95	737.09	3	3
1	GS-pruned	-2487.65	0.19	0.95	861.36	278	3
2	DGS	-2320.67	0.12	0.95	589.1	3	3
2	$\operatorname{DGS-clp}$	-2300.6	0.12	0.951	589.1	3	3
2	GS-tw	-3954.07	0.138	0.95	694.1	3	3
2	GS- clp	-2972.07	0.12	0.95	694.1	3	3
2	GS-pruned	-2668.47	0.13	0.95	892.97	306	3
3	DGS	-2581.5	0.14	0.95	565	3	3
3	$\operatorname{DGS-clp}$	-2571.4	0.13	0.948	565	3	3
3	GS-tw	-4502.73	0.13	0.95	649.7	3	3
3	GS- clp	-3464.55	0.13	0.94	649.7	3	3
3	GS-pruned	-2976.54	0.147	0.95	858.14	295	3
4	DGS	-2334.63	0.14	0.95	578	3	3
4	$\operatorname{DGS-clp}$	-2325.6	0.14	0.95	578	3	3
4	GS-tw	-3371.59	0.162	0.95	687.44	3	3
4	GS- clp	-2875.02	0.12	0.95	687.44	3	3
4	GS-pruned	-2669.71	0.15	0.95	868.05	302	3
5	DGS	-2450.76	0.15	0.95	555.8	3	3
5	$\operatorname{DGS-clp}$	-2436.6	0.153	0.952	555.8	3	3
5	GS-tw	-5049.49	0.12	0.95	629.29	3	3
5	GS- clp	-2770.65	0.12	0.95	629.29	3	3
5	GS-pruned	-3085.85	0.13	0.95	830.34	286	3

Table 31: Comparison of the methods in dataset enron in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	\mathbf{tw}	tw-pr
1	$\overline{\mathrm{DGS}}$	-2185.81	0.2	0.95	643.1	4	4
1	$\operatorname{DGS-clp}$	-2163.9	0.226	0.954	643.1	4	4
1	GS-tw	-3171.39	0.19	0.95	680.08	4	4
1	GS- clp	-2527.01	0.17	0.95	680.08	4	4
1	GS-pruned	-2436.24	0.2	0.95	889.45	287	4
2	DGS	-2320.25	0.12	0.95	635	4	4
2	$\operatorname{DGS-clp}$	-2299.1	0.13	0.951	635	4	4
2	GS-tw	-3709.44	0.141	0.95	680.87	4	4
2	GS- clp	-2808.06	0.1	0.95	680.87	4	4
2	GS-pruned	-2660.41	0.13	0.95	888.34	312	4
3	DGS	-2578.17	0.14	0.95	644.82	4	4
3	$\operatorname{DGS-clp}$	-2569.6	0.14	0.948	644.82	4	4
3	GS-tw	-4157.39	0.13	0.95	631.3	4	4
3	GS- clp	-2993.42	0.14	0.948	631.3	4	4
3	GS-pruned	-2941.35	0.147	0.95	867.92	288	4
4	DGS	-2335.72	0.14	0.95	633	4	4
4	$\operatorname{DGS-clp}$	-2326.1	0.15	0.95	633	4	4
4	GS-tw	-3008.88	0.14	0.95	687.45	4	4
4	GS- clp	-2483.79	0.13	0.951	687.45	4	4
4	GS-pruned	-2646.01	0.15	0.95	903.22	299	4
5	DGS	-2416.73	0.14	0.95	625.3	4	4
5	$\operatorname{DGS-clp}$	-2405	0.153	0.95	625.3	4	4
5	GS-tw	-4523.7	0.13	0.95	627.91	4	4
5	GS- clp	-3014.18	0.11	0.95	627.91	4	4
5	GS-pruned	-3075.93	0.14	0.95	849.94	272	4

Table 32: Comparison of the methods in dataset enron in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

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Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-2182.96	0.2	0.95	685.1	5	4
1	$\operatorname{DGS-clp}$	-2161.1	0.223	0.954	685.1	5	4
1	GS-tw	-3075.4	0.19	0.95	729.43	5	5
1	GS- clp	-2485.14	0.2	0.95	729.43	5	5
1	GS-pruned	-2472.03	0.18	0.95	914.53	298	5
2	DGS	-2320.25	0.12	0.95	686.1	4	4
2	$\operatorname{DGS-clp}$	-2299.1	0.13	0.951	686.1	4	4
2	GS-tw	-3450.06	0.129	0.95	693.06	5	5
2	GS- clp	-2784.21	0.12	0.95	693.06	5	5
2	GS-pruned	-2655.29	0.129	0.95	888.46	303	4
3	DGS	-2582.09	0.14	0.95	769.64	5	4
3	$\operatorname{DGS-clp}$	-2573.8	0.14	0.95	769.64	5	4
3	GS-tw	-3944.27	0.14	0.94	669	5	5
3	GS- clp	-2943.77	0.14	0.949	669	5	5
3	GS-pruned	-2970.11	0.147	0.95	898.75	286	4
4	DGS	-2338.75	0.15	0.95	728.8	5	4
4	$\operatorname{DGS-clp}$	-2330.1	0.15	0.95	728.8	5	4
4	GS-tw	-3002.33	0.156	0.95	759.91	5	5
4	GS- clp	-2686.29	0.12	0.95	759.91	5	5
4	GS-pruned	-2642.63	0.15	0.95	931.31	310	4
5	DGS	-2417.49	0.14	0.95	671.63	5	4
5	$\operatorname{DGS-clp}$	-2405.2	0.153	0.95	671.63	5	4
5	GS-tw	-4351.29	0.13	0.95	655.9	5	5
5	GS- clp	-2888.93	0.13	0.95	655.9	5	5
5	GS-pruned	-3072.84	0.12	0.95	872.62	282	5

Table 33: Comparison of the methods in dataset obsumed in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	$_{ m time}$	\mathbf{tw}	tw-pr
1	DGS	-10585.72	0.239	0.94	513.48	2	2
1	$\operatorname{DGS-clp}$	-10516.5	0.23	0.94	513.48	2	2
1	GS-tw	-13210.81	0.2	0.94	233.5	2	2
1	GS- clp	-10683.48	0.23	0.94	233.5	2	2
1	GS-pruned	-10745.48	0.23	0.945	473.26	177	2
2	DGS	-10511	0.239	0.944	515.66	2	2
2	$\operatorname{DGS-clp}$	-10456.9	0.24	0.94	515.66	2	2
2	GS-tw	-13114.68	0.2	0.94	239.6	2	2
2	GS- clp	-10613.86	0.23	0.94	239.6	2	2
2	GS-pruned	-10738.35	0.24	0.94	482.9	172	2
3	DGS	-10703.43	0.24	0.944	527.64	2	2
3	$\operatorname{DGS-clp}$	-10659.4	0.246	0.94	527.64	2	2
3	GS-tw	-13287.28	0.21	0.94	234.1	2	2
3	GS- clp	-10801.13	0.23	0.94	234.1	2	2
3	GS-pruned	-10794.84	0.24	0.94	468.76	171	2
4	DGS	-10697.67	0.24	0.94	544.44	2	2
4	$\operatorname{DGS-clp}$	-10640.4	0.24	0.943	544.44	2	2
4	GS-tw	-13091.09	0.21	0.94	239.9	2	2
4	GS- clp	-11199.58	0.23	0.94	239.9	2	2
4	GS-pruned	-10879.39	0.239	0.94	487.51	173	2
5	DGS	-10695.9	0.23	0.94	531.76	2	2
5	$\operatorname{DGS-clp}$	-10629	0.23	0.944	531.76	2	2
5	GS-tw	-13430.92	0.21	0.94	238	2	2
5	GS- clp	-11380.13	0.22	0.94	238	2	2
5	GS-pruned	-10925.12	0.239	0.94	467.16	170	2

Table 34: Comparison of the methods in dataset obsumed in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	$_{ m time}$	$\mathbf{t}\mathbf{w}$	tw-pr
1	DGS	-10470.96	0.24	0.95	596.33	3	3
1	$\operatorname{DGS-clp}$	-10416.1	0.24	0.95	596.33	3	3
1	GS-tw	-11908.4	0.22	0.94	314.7	3	3
1	GS- clp	-10789.73	0.244	0.94	314.7	3	3
1	GS-pruned	-10663.21	0.24	0.945	499.53	175	3
2	DGS	-10506.17	0.24	0.944	604.36	3	3
2	$\operatorname{DGS-clp}$	-10452.1	0.24	0.94	604.36	3	3
2	GS-tw	-11638.21	0.23	0.94	320.4	3	3
2	GS- clp	-10525.21	0.24	0.94	320.4	3	3
2	GS-pruned	-10663.87	0.246	0.94	491.28	169	3
3	DGS	-10600.59	0.251	0.945	639.68	3	3
3	$\operatorname{DGS-clp}$	-10571.8	0.251	0.94	639.68	3	3
3	GS-tw	-11994.52	0.22	0.94	323.4	3	3
3	GS- clp	-10879.78	0.23	0.94	323.4	3	3
3	GS-pruned	-10779.47	0.25	0.945	488.49	175	3
4	DGS	-10686.93	0.23	0.94	602.6	3	3
4	DGS-clp	-10633.9	0.23	0.94	602.6	3	3
4	GS-tw	-11902.49	0.23	0.94	326.2	3	3
4	GS- clp	-10876.01	0.24	0.944	326.2	3	3
4	GS-pruned	-10846.24	0.242	0.94	496.2	167	3
5	DGS	-10703.08	0.23	0.94	609.17	3	3
5	DGS-clp	-10638.5	0.23	0.944	609.17	3	3
5	GS-tw	-12153.04	0.22	0.94	319.2	3	3
5	GS-clp	-11089.49	0.23	0.94	319.2	3	3
5	GS-pruned	-10896.06	0.244	0.94	469.98	180	3

Table 35: Comparison of the methods in dataset obsumed in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	$_{ m time}$	$\mathbf{t}\mathbf{w}$	tw-pr
1	DGS	-10379.37	0.24	0.95	638.99	4	4
1	$\operatorname{DGS-clp}$	-10325.3	0.24	0.95	638.99	4	4
1	GS-tw	-11508.74	0.23	0.94	356.6	4	4
1	GS- clp	-10663.18	0.244	0.94	356.6	4	4
1	GS-pruned	-10645.1	0.24	0.945	525.42	176	4
2	DGS	-10457.92	0.248	0.944	761.95	4	4
2	$\operatorname{DGS-clp}$	-10403	0.24	0.94	761.95	4	4
2	GS-tw	-11495.26	0.24	0.94	353.7	4	4
2	GS- clp	-10736.82	0.24	0.94	353.7	4	4
2	GS-pruned	-10681.22	0.25	0.94	504.34	175	4
3	DGS	-10539.04	0.25	0.945	779.53	4	4
3	$\operatorname{DGS-clp}$	-10508.9	0.253	0.94	779.53	4	4
3	GS-tw	-11634.14	0.23	0.94	364.4	4	4
3	GS- clp	-10691.9	0.24	0.94	364.4	4	4
3	GS-pruned	-10737.43	0.25	0.94	520.56	173	4
4	DGS	-10636.07	0.24	0.94	715.77	4	4
4	$\operatorname{DGS-clp}$	-10587.5	0.23	0.94	715.77	4	4
4	GS-tw	-11554.26	0.24	0.94	363.3	4	4
4	GS- clp	-10654.76	0.24	0.944	363.3	4	4
4	GS-pruned	-10786.37	0.254	0.94	510.39	176	4
5	DGS	-10626.17	0.24	0.94	729.99	4	4
5	$\operatorname{DGS-clp}$	-10562.7	0.24	0.94	729.99	4	4
5	GS-tw	-11673.81	0.24	0.94	384.3	4	4
5	GS- clp	-10846.8	0.25	0.94	384.3	4	4
5	GS-pruned	-10835.45	0.252	0.944	496.44	170	4

Table 36: Comparison of the methods in dataset obsumed in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Floid Method CLL acc _G acc _M time tw tw-pr 1 DGS -10384.76 0.24 0.95 771.87 5 5 1 DGS-clp -10326.2 0.24 0.95 771.87 5 5 1 GS-tw -11287.85 0.23 0.94 400.5 5 5 1 GS-clp -10443.61 0.247 0.95 400.5 5 5 1 GS-pruned -10558.59 0.24 0.946 533.56 163 5 2 DGS -10465.5 0.25 0.944 896.56 5 5 2 DGS-tw -11265.4 0.24 0.94 386.1 5 5 2 GS-pruned -10560.3 0.25 0.94 386.1 5 5 3 DGS -10505.3 0.25 0.94 894.1 5 5 3 DGS-clp -10505.3 0.25 </th <th></th> <th></th> <th></th> <th></th> <th></th> <th></th> <th></th> <th></th>								
1 DGS-clp -10326.2 0.24 0.95 771.87 5 5 1 GS-tw -11287.85 0.23 0.94 400.5 5 5 1 GS-clp -10443.61 0.247 0.95 400.5 5 5 1 GS-pruned -10558.59 0.24 0.946 533.56 163 5 2 DGS -10465.5 0.253 0.944 896.56 5 5 2 DGS-clp -10410.9 0.25 0.94 896.56 5 5 2 GS-tw -11265.4 0.24 0.94 386.1 5 5 2 GS-clp -10560.3 0.25 0.94 386.1 5 5 2 GS-pruned -10652.25 0.25 0.94 386.1 5 5 3 DGS -10534.18 0.25 0.94 384.1 5 5 3 GS-clp -10505.3 0.25 0.94 894.1 5 5 3 GS-tw -11471.09	Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1 GS-tw -11287.85 0.23 0.94 400.5 5 5 1 GS-clp -10443.61 0.247 0.95 400.5 5 5 1 GS-pruned -10558.59 0.24 0.946 533.56 163 5 2 DGS -10465.5 0.253 0.944 896.56 5 5 2 DGS-clp -10410.9 0.25 0.94 386.1 5 5 2 GS-tw -11265.4 0.24 0.94 386.1 5 5 2 GS-clp -10560.3 0.25 0.94 386.1 5 5 2 GS-pruned -10652.25 0.25 0.94 386.1 5 5 3 DGS -10563.3 0.25 0.94 384.1 5 5 3 DGS-clp -10505.3 0.25 0.94 894.1 5 5 3 GS-tw -11471.09 0.23	1	DGS	-10384.76	0.24	0.95	771.87	5	5
1 GS-clp -10443.61 0.247 0.95 400.5 5 5 1 GS-pruned -10558.59 0.24 0.946 533.56 163 5 2 DGS -10465.5 0.253 0.944 896.56 5 5 2 DGS-clp -10410.9 0.25 0.94 386.1 5 5 2 GS-tw -11265.4 0.24 0.94 386.1 5 5 2 GS-clp -10560.3 0.25 0.94 386.1 5 5 2 GS-pruned -10652.25 0.25 0.94 386.1 5 5 3 DGS -10534.18 0.251 0.94 386.1 5 5 3 DGS -10534.18 0.251 0.94 894.1 5 5 3 DGS-clp -10505.3 0.25 0.94 894.1 5 5 3 GS-tw -11471.09 0.23 0.94 421.6 5 5 3 GS-pruned -10683.44 <td>1</td> <td>$\operatorname{DGS-clp}$</td> <td>-10326.2</td> <td>0.24</td> <td>0.95</td> <td>771.87</td> <td>5</td> <td>5</td>	1	$\operatorname{DGS-clp}$	-10326.2	0.24	0.95	771.87	5	5
1 GS-pruned -10558.59 0.24 0.946 533.56 163 5 2 DGS -10465.5 0.253 0.944 896.56 5 5 2 DGS-clp -10410.9 0.25 0.94 896.56 5 5 2 GS-tw -11265.4 0.24 0.94 386.1 5 5 2 GS-clp -10560.3 0.25 0.94 386.1 5 5 2 GS-pruned -10652.25 0.25 0.94 386.1 5 5 3 DGS -10552.25 0.25 0.94 384.1 5 5 3 DGS -10534.18 0.251 0.945 894.1 5 5 3 DGS-clp -10505.3 0.25 0.94 894.1 5 5 3 GS-tw -11471.09 0.23 0.94 421.6 5 5 3 GS-pruned -10683.44 0.25 <td>1</td> <td>GS-tw</td> <td>-11287.85</td> <td>0.23</td> <td>0.94</td> <td>400.5</td> <td>5</td> <td>5</td>	1	GS-tw	-11287.85	0.23	0.94	400.5	5	5
2 DGS -10465.5 0.253 0.944 896.56 5 5 2 DGS-clp -10410.9 0.25 0.94 896.56 5 5 2 GS-tw -11265.4 0.24 0.94 386.1 5 5 2 GS-clp -10560.3 0.25 0.94 386.1 5 5 2 GS-pruned -10652.25 0.25 0.94 508 175 5 3 DGS -10534.18 0.251 0.945 894.1 5 5 3 DGS-clp -10505.3 0.25 0.94 894.1 5 5 3 DGS-clp -10505.3 0.25 0.94 894.1 5 5 3 GS-tw -11471.09 0.23 0.94 421.6 5 5 3 GS-pruned -10605.64 0.24 0.94 421.6 5 5 4 DGS -10619.17 0.24 0.94 877.31 5 5 4 DGS-clp -10566.8	1	GS- clp	-10443.61	0.247	0.95	400.5	5	5
2 DGS-clp -10410.9 0.25 0.94 896.56 5 5 2 GS-tw -11265.4 0.24 0.94 386.1 5 5 2 GS-clp -10560.3 0.25 0.94 386.1 5 5 2 GS-pruned -10652.25 0.25 0.94 508 175 5 3 DGS -10534.18 0.251 0.945 894.1 5 5 3 DGS-clp -10505.3 0.25 0.94 894.1 5 5 3 GS-tw -11471.09 0.23 0.94 421.6 5 5 3 GS-tw -10605.64 0.24 0.94 421.6 5 5 3 GS-pruned -10683.44 0.25 0.94 514.42 175 5 4 DGS -10619.17 0.24 0.94 877.31 5 5 4 GS-tp -10566.8 0.24 0.94 877.31 5 5 4 GS-tp -10642.31	1	GS-pruned	-10558.59	0.24	0.946	533.56	163	5
2 GS-tw -11265.4 0.24 0.94 386.1 5 5 2 GS-clp -10560.3 0.25 0.94 386.1 5 5 2 GS-pruned -10652.25 0.25 0.94 508 175 5 3 DGS -10534.18 0.251 0.945 894.1 5 5 3 DGS-clp -10505.3 0.25 0.94 894.1 5 5 3 GS-tw -11471.09 0.23 0.94 421.6 5 5 3 GS-clp -10605.64 0.24 0.94 421.6 5 5 3 GS-pruned -10605.64 0.24 0.94 421.6 5 5 4 DGS -10619.17 0.24 0.94 877.31 5 5 4 DGS-clp -10566.8 0.24 0.94 877.31 5 5 4 GS-tw -11437.73 0.24 0.94 398.5 5 5 4 GS-pruned -10715.44	2	DGS	-10465.5	0.253	0.944	896.56	5	5
2 GS-clp -10560.3 0.25 0.94 386.1 5 5 2 GS-pruned -10652.25 0.25 0.94 508 175 5 3 DGS -10534.18 0.251 0.945 894.1 5 5 3 DGS-clp -10505.3 0.25 0.94 894.1 5 5 3 GS-tw -11471.09 0.23 0.94 421.6 5 5 3 GS-clp -10605.64 0.24 0.94 421.6 5 5 3 GS-pruned -10605.64 0.24 0.94 421.6 5 5 4 DGS -10619.17 0.24 0.94 877.31 5 5 4 DGS-clp -10566.8 0.24 0.94 877.31 5 5 4 GS-tw -11437.73 0.24 0.94 398.5 5 5 4 GS-pruned -10715.44 0.25 0.94 516.16 169 5 5 DGS -10494.9	2	$\operatorname{DGS-clp}$	-10410.9	0.25	0.94	896.56	5	5
2 GS-pruned -10652.25 0.25 0.94 508 175 5 3 DGS -10534.18 0.251 0.945 894.1 5 5 3 DGS-clp -10505.3 0.25 0.94 894.1 5 5 3 GS-tw -11471.09 0.23 0.94 421.6 5 5 3 GS-clp -10605.64 0.24 0.94 421.6 5 5 3 GS-pruned -10683.44 0.25 0.94 514.42 175 5 4 DGS -10619.17 0.24 0.94 877.31 5 5 4 DGS-clp -10566.8 0.24 0.94 877.31 5 5 4 GS-tw -11437.73 0.24 0.94 398.5 5 5 4 GS-pruned -10715.44 0.25 0.944 398.5 5 5 5 DGS -10552.22 0.25 0.944 920.54 5 5 5 DGS-clp -10494.9<	2	GS-tw	-11265.4	0.24	0.94	386.1	5	5
3 DGS -10534.18 0.251 0.945 894.1 5 3 DGS-clp -10505.3 0.25 0.94 894.1 5 5 3 GS-tw -11471.09 0.23 0.94 421.6 5 5 3 GS-clp -10605.64 0.24 0.94 421.6 5 5 3 GS-pruned -10605.64 0.24 0.94 421.6 5 5 4 DGS -10605.64 0.24 0.94 514.42 175 5 4 DGS -10619.17 0.24 0.94 877.31 5 5 4 DGS-clp -10566.8 0.24 0.94 877.31 5 5 4 GS-tw -11437.73 0.24 0.94 398.5 5 5 4 GS-pruned -10715.44 0.25 0.94 516.16 169 5 5 DGS -10494.9 0.24 0.944 920.54 5 5 5 GS-tw -11597.13	2	GS- clp	-10560.3	0.25	0.94	386.1	5	5
3 DGS-clp -10505.3 0.25 0.94 894.1 5 5 3 GS-tw -11471.09 0.23 0.94 421.6 5 5 3 GS-clp -10605.64 0.24 0.94 421.6 5 5 3 GS-pruned -10683.44 0.25 0.94 514.42 175 5 4 DGS -10619.17 0.24 0.94 877.31 5 5 4 DGS-clp -10566.8 0.24 0.94 877.31 5 5 4 GS-tw -11437.73 0.24 0.94 398.5 5 5 4 GS-clp -10642.31 0.256 0.944 398.5 5 5 4 GS-pruned -10715.44 0.25 0.94 516.16 169 5 5 DGS -10552.22 0.25 0.944 920.54 5 5 5 DGS-clp -10494.9 0.24 0.94 406.8 5 5 5 GS-tw -11597.13	2	GS-pruned	-10652.25	0.25	0.94	508	175	5
3 GS-tw -11471.09 0.23 0.94 421.6 5 5 3 GS-clp -10605.64 0.24 0.94 421.6 5 5 3 GS-pruned -10683.44 0.25 0.94 514.42 175 5 4 DGS -10619.17 0.24 0.94 877.31 5 5 4 DGS-clp -10566.8 0.24 0.94 877.31 5 5 4 GS-tw -11437.73 0.24 0.94 398.5 5 5 4 GS-clp -10642.31 0.256 0.944 398.5 5 5 4 GS-pruned -10715.44 0.25 0.94 516.16 169 5 5 DGS -10552.22 0.25 0.944 920.54 5 5 5 DGS-clp -10494.9 0.24 0.944 920.54 5 5 5 GS-tw -11597.13 0.24 0.94 406.8 5 5 5 GS-clp -10788.	3	DGS	-10534.18	0.251	0.945	894.1	5	5
3 GS-clp -10605.64 0.24 0.94 421.6 5 5 3 GS-pruned -10683.44 0.25 0.94 514.42 175 5 4 DGS -10619.17 0.24 0.94 877.31 5 5 4 DGS-clp -10566.8 0.24 0.94 877.31 5 5 4 GS-tw -11437.73 0.24 0.94 398.5 5 5 4 GS-clp -10642.31 0.256 0.944 398.5 5 5 4 GS-pruned -10715.44 0.25 0.94 516.16 169 5 5 DGS -10552.22 0.25 0.944 920.54 5 5 5 DGS-clp -10494.9 0.24 0.944 920.54 5 5 5 GS-tw -11597.13 0.24 0.94 406.8 5 5 5 GS-clp -10788.52 0.24 0.94 406.8 5 5	3	$\operatorname{DGS-clp}$	-10505.3	0.25	0.94	894.1	5	5
3 GS-pruned -10683.44 0.25 0.94 514.42 175 5 4 DGS -10619.17 0.24 0.94 877.31 5 5 4 DGS-clp -10566.8 0.24 0.94 877.31 5 5 4 GS-tw -11437.73 0.24 0.94 398.5 5 5 4 GS-clp -10642.31 0.256 0.944 398.5 5 5 4 GS-pruned -10715.44 0.25 0.94 516.16 169 5 5 DGS -10552.22 0.25 0.944 920.54 5 5 5 DGS-clp -10494.9 0.24 0.944 920.54 5 5 5 GS-tw -11597.13 0.24 0.94 406.8 5 5 5 GS-clp -10788.52 0.24 0.94 406.8 5 5	3	GS-tw	-11471.09	0.23	0.94	421.6	5	5
4 DGS -10619.17 0.24 0.94 877.31 5 5 4 DGS-clp -10566.8 0.24 0.94 877.31 5 5 4 GS-tw -11437.73 0.24 0.94 398.5 5 5 4 GS-clp -10642.31 0.256 0.944 398.5 5 5 4 GS-pruned -10715.44 0.25 0.94 516.16 169 5 5 DGS -10552.22 0.25 0.944 920.54 5 5 5 DGS-clp -10494.9 0.24 0.944 920.54 5 5 5 GS-tw -11597.13 0.24 0.94 406.8 5 5 5 GS-clp -10788.52 0.24 0.94 406.8 5 5	3	GS- clp	-10605.64	0.24	0.94	421.6	5	5
4 DGS-clp -10566.8 0.24 0.94 877.31 5 4 GS-tw -11437.73 0.24 0.94 398.5 5 5 4 GS-clp -10642.31 0.256 0.944 398.5 5 5 4 GS-pruned -10715.44 0.25 0.94 516.16 169 5 5 DGS -10552.22 0.25 0.944 920.54 5 5 5 DGS-clp -10494.9 0.24 0.944 920.54 5 5 5 GS-tw -11597.13 0.24 0.94 406.8 5 5 5 GS-clp -10788.52 0.24 0.94 406.8 5 5	3	GS-pruned	-10683.44	0.25	0.94	514.42	175	5
4 GS-tw -11437.73 0.24 0.94 398.5 5 5 4 GS-clp -10642.31 0.256 0.944 398.5 5 5 4 GS-pruned -10715.44 0.25 0.94 516.16 169 5 5 DGS -10552.22 0.25 0.94 920.54 5 5 5 DGS-clp -10494.9 0.24 0.944 920.54 5 5 5 GS-tw -11597.13 0.24 0.94 406.8 5 5 5 GS-clp -10788.52 0.24 0.94 406.8 5 5	4	DGS	-10619.17	0.24	0.94	877.31	5	5
4 GS-clp -10642.31 0.256 0.944 398.5 5 5 4 GS-pruned -10715.44 0.25 0.94 516.16 169 5 5 DGS -10552.22 0.25 0.944 920.54 5 5 5 DGS-clp -10494.9 0.24 0.944 920.54 5 5 5 GS-tw -11597.13 0.24 0.94 406.8 5 5 5 GS-clp -10788.52 0.24 0.94 406.8 5 5	4	$\operatorname{DGS-clp}$	-10566.8	0.24	0.94	877.31	5	5
4 GS-pruned -10715.44 0.25 0.94 516.16 169 5 5 DGS -10552.22 0.25 0.944 920.54 5 5 5 DGS-clp -10494.9 0.24 0.944 920.54 5 5 5 GS-tw -11597.13 0.24 0.94 406.8 5 5 5 GS-clp -10788.52 0.24 0.94 406.8 5 5	4	GS-tw	-11437.73	0.24	0.94	398.5	5	5
5 DGS -10552.22 0.25 0.944 920.54 5 5 5 DGS-clp -10494.9 0.24 0.944 920.54 5 5 5 GS-tw -11597.13 0.24 0.94 406.8 5 5 5 GS-clp -10788.52 0.24 0.94 406.8 5 5	4	GS- clp	-10642.31	0.256	0.944	398.5	5	5
5 DGS-clp -10494.9 0.24 0.944 920.54 5 5 5 GS-tw -11597.13 0.24 0.94 406.8 5 5 5 GS-clp -10788.52 0.24 0.94 406.8 5 5	4	GS-pruned	-10715.44	0.25	0.94	516.16	169	5
5 GS-tw -11597.13 0.24 0.94 406.8 5 5 5 5 GS-clp -10788.52 0.24 0.94 406.8 5 5	5	DGS	-10552.22	0.25	0.944	920.54	5	5
5 GS-clp -10788.52 0.24 0.94 406.8 5 5	5	$\operatorname{DGS-clp}$	-10494.9	0.24	0.944	920.54	5	5
	5	GS-tw	-11597.13	0.24	0.94	406.8	5	5
5 GS-pruned -10806.91 0.25 0.94 491.91 174 5	5	GS- clp	-10788.52	0.24	0.94	406.8	5	5
	5	GS-pruned	-10806.91	0.25	0.94	491.91	174	5

Table 37: Comparison of the methods in dataset reutersk500 in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-7006.06	0.03	0.99	14.96	2	2
1	$\operatorname{DGS-clp}$	-7005.76	0.03	0.99	14.96	2	2
1	GS-tw	-7011.71	0.03	0.99	8.1	2	2
1	$\operatorname{GS-clp}$	-7011.37	0.03	0.99	8.1	2	2
1	GS-pruned	-7003.8	0.061	0.986	8.05	3	2
2	DGS	-6863.31	0.03	0.99	15.1	2	2
2	$\operatorname{DGS-clp}$	-6862.38	0.03	0.99	15.1	2	2
2	GS-tw	-6857.9	0.03	0.99	8	2	2
2	GS- clp	-6856.9	0.03	0.99	8	2	2
2	GS-pruned	-6862.44	0.044	0.986	8.07	4	2
3	DGS	-6934.8	0.022	0.986	15.39	2	2
3	$\operatorname{DGS-clp}$	-6935.61	0.022	0.986	15.39	2	2
3	GS-tw	-6946.74	0.022	0.986	8	2	2
3	GS- clp	-6947.38	0.022	0.986	8	2	2
3	GS-pruned	-6947.91	0.01	0.99	8.09	3	2
4	DGS	-6988.74	0.03	0.99	14.96	2	2
4	$\operatorname{DGS-clp}$	-6988.6	0.03	0.99	14.96	2	2
4	GS-tw	-6989.59	0.03	0.99	7.8	2	2
4	GS- clp	-6989.34	0.03	0.99	7.8	2	2
4	GS-pruned	-6990.22	0.047	0.986	7.84	4	2
5	DGS	-7068.12	0.02	0.986	16.13	2	2
5	$\operatorname{DGS-clp}$	-7067.88	0.02	0.986	16.13	2	2
5	GS-tw	-7064.29	0.02	0.986	8.5	2	2
5	GS- clp	-7064	0.02	0.986	8.5	2	2
5	GS-pruned	-7054.9	0.02	0.99	8.71	4	2

Table 38: Comparison of the methods in dataset reutersk500 in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold Method CLL acc_G acc_M time tw tw-pr 1 DGS -6905.89 0.05 0.986 16.04 3 3 1 DGS-clp -6902.71 0.05 0.986 16.04 3 3 1 GS-tw -6898.37 0.05 0.986 8.5 3 3 1 GS-clp -6894.58 0.05 0.986 8.5 3 3 1 GS-pruned -6876.6 0.06 0.99 8.62 4 3 2 DGS -6775.64 0.04 0.986 16.93 3 3 2 DGS-clp -6769.72 0.04 0.986 8.6 3 3 2 GS-tw -6769.78 0.04 0.986 8.6 3 3 3 DGS -6845.91 0.03 0.99 16.61 3 3 3 GS-tw <			ı					
1 DGS-clp -6902.71 0.05 0.986 16.04 3 3 1 GS-tw -6898.37 0.05 0.986 8.5 3 3 1 GS-clp -6894.58 0.05 0.986 8.5 3 3 1 GS-pruned -6876.6 0.066 0.99 8.62 4 3 2 DGS -6775.64 0.04 0.986 16.93 3 3 2 DGS-clp -6769.52 0.04 0.986 8.6 3 3 2 GS-tw -6769.78 0.04 0.986 8.6 3 3 2 GS-pruned -6769.78 0.04 0.986 8.6 3 3 2 GS-pruned -6769.78 0.04 0.986 8.6 3 3 3 DGS -6845.91 0.03 0.99 16.61 3 3 3 DGS-clp -6840.59 0.03 0.99 8.7 3 3 3 GS-pruned -6840.91 0.03<	Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1 GS-tw -6898.37 0.05 0.986 8.5 3 1 GS-clp -6894.58 0.05 0.986 8.5 3 1 GS-pruned -6876.6 0.066 0.99 8.62 4 3 2 DGS -6775.64 0.04 0.986 16.93 3 3 2 DGS-clp -6769.52 0.04 0.986 8.6 3 3 2 GS-tw -6769.78 0.04 0.986 8.6 3 3 2 GS-pruned -6769.78 0.04 0.986 8.6 3 3 2 GS-pruned -6769.74 0.062 0.99 8.78 4 3 3 DGS -6845.91 0.03 0.99 16.61 3 3 3 DGS-clp -6840.59 0.03 0.99 8.7 3 3 3 GS-tw -6852.63 0.04 0.99 8.71 4 3 4 DGS -6933.33 0.04 0.99 16.12 <td>1</td> <td>$\overline{\mathrm{DGS}}$</td> <td>-6905.89</td> <td>0.05</td> <td>0.986</td> <td>16.04</td> <td>3</td> <td>3</td>	1	$\overline{\mathrm{DGS}}$	-6905.89	0.05	0.986	16.04	3	3
1 GS-clp -6894.58 0.05 0.986 8.5 3 3 1 GS-pruned -6876.6 0.066 0.99 8.62 4 3 2 DGS -6775.64 0.04 0.986 16.93 3 3 2 DGS-clp -6769.52 0.04 0.986 16.93 3 3 2 GS-tw -6762.3 0.05 0.986 8.6 3 3 2 GS-clp -6769.78 0.04 0.986 8.6 3 3 2 GS-pruned -6767.4 0.062 0.99 8.78 4 3 3 DGS -6845.91 0.03 0.99 16.61 3 3 3 DGS-clp -6840.59 0.03 0.99 8.7 3 3 3 GS-tw -6852.63 0.04 0.99 8.7 3 3 4 DGS -6933.33 0.04 0.99	1	$\operatorname{DGS-clp}$	-6902.71	0.05	0.986	16.04	3	3
1 GS-pruned -6876.6 0.066 0.99 8.62 4 3 2 DGS -6775.64 0.04 0.986 16.93 3 3 2 DGS-clp -6769.52 0.04 0.986 16.93 3 3 2 GS-tw -6769.78 0.04 0.986 8.6 3 3 2 GS-pruned -6767.4 0.062 0.99 8.78 4 3 3 DGS -6845.91 0.03 0.99 16.61 3 3 3 DGS-clp -6840.59 0.03 0.99 16.61 3 3 3 GS-tw -6852.63 0.04 0.99 8.7 3 3 3 GS-pruned -6846.91 0.03 0.986 8.7 3 3 4 DGS -6933.33 0.04 0.99 8.71 4 3 4 DGS-clp -6930.54 0.04 0.99 </td <td>1</td> <td>GS-tw</td> <td>-6898.37</td> <td>0.05</td> <td>0.986</td> <td>8.5</td> <td>3</td> <td>3</td>	1	GS-tw	-6898.37	0.05	0.986	8.5	3	3
2 DGS -6775.64 0.04 0.986 16.93 3 3 2 DGS-clp -6769.52 0.04 0.986 16.93 3 3 2 GS-tw -6769.52 0.04 0.986 8.6 3 3 2 GS-clp -6769.78 0.04 0.986 8.6 3 3 2 GS-pruned -6767.4 0.062 0.99 8.78 4 3 3 DGS -6845.91 0.03 0.99 16.61 3 3 3 DGS-clp -6840.59 0.03 0.99 16.61 3 3 3 GS-tw -6852.63 0.04 0.99 8.7 3 3 3 GS-pruned -6846.91 0.03 0.986 8.7 3 3 4 DGS -6933.33 0.04 0.99 8.71 4 3 4 GS-tw -6928.91 0.057 0.99	1	GS- clp	-6894.58	0.05	0.986	8.5	3	3
2 DGS-clp -6769.52 0.04 0.986 16.93 3 3 2 GS-tw -6769.78 0.05 0.986 8.6 3 3 2 GS-clp -6769.78 0.04 0.986 8.6 3 3 2 GS-pruned -6767.4 0.062 0.99 8.78 4 3 3 DGS -6845.91 0.03 0.99 16.61 3 3 3 DGS-clp -6840.59 0.03 0.99 16.61 3 3 3 GS-tw -6852.63 0.04 0.99 8.7 3 3 3 GS-tw -6846.91 0.03 0.986 8.7 3 3 3 GS-pruned -6840.5 0.054 0.99 8.71 4 3 4 DGS -6933.33 0.04 0.99 16.12 3 3 4 DGS-clp -6928.91 0.057 0.99 8 3 3 4 GS-pruned -6925.9 0.04	1	GS-pruned	-6876.6	0.066	0.99	8.62	4	3
2 GS-tw -6776.23 0.05 0.986 8.6 3 3 2 GS-clp -6769.78 0.04 0.986 8.6 3 3 2 GS-pruned -6767.4 0.062 0.99 8.78 4 3 3 DGS -6845.91 0.03 0.99 16.61 3 3 3 DGS-clp -6840.59 0.03 0.99 16.61 3 3 3 GS-tw -6852.63 0.04 0.99 8.7 3 3 3 GS-clp -6846.91 0.03 0.986 8.7 3 3 3 GS-pruned -6840.5 0.054 0.99 8.71 4 3 4 DGS -6933.33 0.04 0.99 16.12 3 3 4 DGS-clp -6930.54 0.04 0.99 16.12 3 3 4 GS-tw -6928.91 0.057 0.99 8 3 3 4 GS-pruned -6927.49 0.05	2	DGS	-6775.64	0.04	0.986	16.93	3	3
2 GS-clp -6769.78 0.04 0.986 8.6 3 3 2 GS-pruned -6767.4 0.062 0.99 8.78 4 3 3 DGS -6845.91 0.03 0.99 16.61 3 3 3 DGS-clp -6840.59 0.03 0.99 16.61 3 3 3 GS-tw -6852.63 0.04 0.99 8.7 3 3 3 GS-clp -6846.91 0.03 0.986 8.7 3 3 3 GS-pruned -6840.5 0.054 0.99 8.71 4 3 4 DGS -6933.33 0.04 0.99 16.12 3 3 4 DGS-clp -6930.54 0.04 0.99 16.12 3 3 4 GS-tw -6928.91 0.057 0.99 8 3 3 4 GS-clp -6925.9 0.04 0.99 17.41 3 3 5 DGS -6956.92 0.03 <t< td=""><td>2</td><td>$\operatorname{DGS-clp}$</td><td>-6769.52</td><td>0.04</td><td>0.986</td><td>16.93</td><td>3</td><td>3</td></t<>	2	$\operatorname{DGS-clp}$	-6769.52	0.04	0.986	16.93	3	3
2 GS-pruned -6767.4 0.062 0.99 8.78 4 3 3 DGS -6845.91 0.03 0.99 16.61 3 3 3 DGS-clp -6840.59 0.03 0.99 16.61 3 3 3 GS-tw -6852.63 0.04 0.99 8.7 3 3 3 GS-clp -6846.91 0.03 0.986 8.7 3 3 3 GS-pruned -6840.5 0.054 0.99 8.71 4 3 4 DGS -6933.33 0.04 0.99 16.12 3 3 4 DGS-clp -6930.54 0.04 0.99 16.12 3 3 4 GS-tw -6928.91 0.057 0.99 8 3 3 4 GS-pruned -6927.49 0.05 0.986 8.19 5 3 5 DGS -6956.92 0.03 0.99 17.41 3 3 5 GS-tw -6959.44 0.03	2	GS-tw	-6776.23	0.05	0.986	8.6	3	3
3 DGS -6845.91 0.03 0.99 16.61 3 3 3 DGS-clp -6840.59 0.03 0.99 16.61 3 3 3 GS-tw -6852.63 0.04 0.99 8.7 3 3 3 GS-clp -6846.91 0.03 0.986 8.7 3 3 3 GS-pruned -6840.5 0.054 0.99 8.71 4 3 4 DGS -6933.33 0.04 0.99 16.12 3 3 4 DGS-clp -6930.54 0.04 0.99 16.12 3 3 4 GS-tw -6928.91 0.057 0.99 8 3 3 4 GS-pruned -6927.49 0.05 0.986 8.19 5 3 5 DGS -6956.92 0.03 0.99 17.41 3 3 5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 0.986 8.94 3 3	2	GS- clp	-6769.78	0.04	0.986	8.6	3	3
3 DGS-clp -6840.59 0.03 0.99 16.61 3 3 3 GS-tw -6852.63 0.04 0.99 8.7 3 3 3 GS-clp -6846.91 0.03 0.986 8.7 3 3 3 GS-pruned -6840.5 0.054 0.99 8.71 4 3 4 DGS -6933.33 0.04 0.99 16.12 3 3 4 DGS-clp -6930.54 0.04 0.99 16.12 3 3 4 GS-tw -6928.91 0.057 0.99 8 3 3 4 GS-clp -6925.9 0.04 0.99 8 3 3 4 GS-pruned -6927.49 0.05 0.986 8.19 5 3 5 DGS -6956.92 0.03 0.99 17.41 3 3 5 DGS-clp -6958.15 0.03 0.986 8.94 3 3 5 GS-tw -6959.69 0.03 <	2	GS-pruned	-6767.4	0.062	0.99	8.78	4	3
3 GS-tw -6852.63 0.04 0.99 8.7 3 3 3 GS-clp -6846.91 0.03 0.986 8.7 3 3 3 GS-pruned -6840.5 0.054 0.99 8.71 4 3 4 DGS -6933.33 0.04 0.99 16.12 3 3 4 DGS-clp -6930.54 0.04 0.99 16.12 3 3 4 GS-tw -6928.91 0.057 0.99 8 3 3 4 GS-clp -6925.9 0.04 0.99 8 3 3 4 GS-pruned -6927.49 0.05 0.986 8.19 5 3 5 DGS -6956.92 0.03 0.99 17.41 3 3 5 DGS-clp -6958.15 0.03 0.986 8.94 3 3 5 GS-tw -6959.69 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 <t< td=""><td>3</td><td>DGS</td><td>-6845.91</td><td>0.03</td><td>0.99</td><td>16.61</td><td>3</td><td>3</td></t<>	3	DGS	-6845.91	0.03	0.99	16.61	3	3
3 GS-clp -6846.91 0.03 0.986 8.7 3 3 3 GS-pruned -6840.5 0.054 0.99 8.71 4 3 4 DGS -6933.33 0.04 0.99 16.12 3 3 4 DGS-clp -6930.54 0.04 0.99 16.12 3 3 4 GS-tw -6928.91 0.057 0.99 8 3 3 4 GS-clp -6925.9 0.04 0.99 8 3 3 4 GS-pruned -6927.49 0.05 0.986 8.19 5 3 5 DGS -6956.92 0.03 0.99 17.41 3 3 5 DGS-clp -6958.15 0.03 0.99 17.41 3 3 5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 0.986 8.94 3 3	3	$\operatorname{DGS-clp}$	-6840.59	0.03	0.99	16.61	3	3
3 GS-pruned -6840.5 0.054 0.99 8.71 4 3 4 DGS -6933.33 0.04 0.99 16.12 3 3 4 DGS-clp -6930.54 0.04 0.99 16.12 3 3 4 GS-tw -6928.91 0.057 0.99 8 3 3 4 GS-clp -6925.9 0.04 0.99 8 3 3 4 GS-pruned -6927.49 0.05 0.986 8.19 5 3 5 DGS -6956.92 0.03 0.99 17.41 3 3 5 DGS-clp -6958.15 0.03 0.99 17.41 3 3 5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 0.986 8.94 3 3	3	GS-tw	-6852.63	0.04	0.99	8.7	3	3
4 DGS -6933.33 0.04 0.99 16.12 3 3 4 DGS-clp -6930.54 0.04 0.99 16.12 3 3 4 GS-tw -6928.91 0.057 0.99 8 3 3 4 GS-clp - 6925.9 0.04 0.99 8 3 3 4 GS-pruned -6927.49 0.05 0.986 8.19 5 3 5 DGS -6956.92 0.03 0.99 17.41 3 3 5 DGS-clp -6958.15 0.03 0.99 17.41 3 3 5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 0.986 8.94 3 3	3	GS- clp	-6846.91	0.03	0.986	8.7	3	3
4 DGS-clp -6930.54 0.04 0.99 16.12 3 3 4 GS-tw -6928.91 0.057 0.99 8 3 3 4 GS-clp -6925.9 0.04 0.99 8 3 3 4 GS-pruned -6927.49 0.05 0.986 8.19 5 3 5 DGS -6956.92 0.03 0.99 17.41 3 3 5 DGS-clp -6958.15 0.03 0.99 17.41 3 3 5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 0.986 8.94 3 3	3	GS-pruned	-6840.5	0.054	0.99	8.71	4	3
4 GS-tw -6928.91 0.057 0.99 8 3 3 4 GS-clp -6925.9 0.04 0.99 8 3 3 4 GS-pruned -6927.49 0.05 0.986 8.19 5 3 5 DGS -6956.92 0.03 0.99 17.41 3 3 5 DGS-clp -6958.15 0.03 0.99 17.41 3 3 5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 0.986 8.94 3 3	4	DGS	-6933.33	0.04	0.99	16.12	3	3
4 GS-clp -6925.9 0.04 0.99 8 3 3 4 GS-pruned -6927.49 0.05 0.986 8.19 5 3 5 DGS -6956.92 0.03 0.99 17.41 3 3 5 DGS-clp -6958.15 0.03 0.99 17.41 3 3 5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 0.986 8.94 3 3	4	$\operatorname{DGS-clp}$	-6930.54	0.04	0.99	16.12	3	3
4 GS-pruned -6927.49 0.05 0.986 8.19 5 3 5 DGS -6956.92 0.03 0.99 17.41 3 3 5 DGS-clp -6958.15 0.03 0.99 17.41 3 3 5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 0.986 8.94 3 3	4	GS-tw	-6928.91	0.057	0.99	8	3	3
5 DGS -6956.92 0.03 0.99 17.41 3 3 5 DGS-clp -6958.15 0.03 0.99 17.41 3 3 5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 0.986 8.94 3 3	4	GS- clp	-6925.9	0.04	0.99	8	3	3
5 DGS-clp -6958.15 0.03 0.99 17.41 3 3 5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 0.986 8.94 3 3	4	GS-pruned	-6927.49	0.05	0.986	8.19	5	3
5 GS-tw -6959.44 0.03 0.986 8.94 3 3 5 GS-clp -6959.69 0.03 0.986 8.94 3 3	5	DGS	-6956.92	0.03	0.99	17.41	3	3
5 GS-clp -6959.69 0.03 0.986 8.94 3 3	5	$\operatorname{DGS-clp}$	-6958.15	0.03	0.99	17.41	3	3
	5	GS-tw	-6959.44	0.03	0.986	8.94	3	3
5 GS-pruned -6936.3 0.045 0.99 8.9 5 3	5	GS- clp	-6959.69	0.03	0.986	8.94	3	3
	5	GS-pruned	-6936.3	0.045	0.99	8.9	5	3

Table 39: Comparison of the methods in dataset reutersk500 in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-6829.29	0.06	0.99	16.7	4	4
1	$\operatorname{DGS-clp}$	-6827.11	0.07	0.99	16.7	4	4
1	GS-tw	-6829.82	0.05	0.99	8.8	4	4
1	GS- clp	-6826.43	0.05	0.986	8.8	4	4
1	GS-pruned	-6818.5	0.072	0.99	8.88	5	4
2	DGS	-6720.48	0.08	0.99	17.38	4	4
2	$\operatorname{DGS-clp}$	-6719.38	0.06	0.99	17.38	4	4
2	GS-tw	-6708.65	0.084	0.986	8.7	4	4
2	GS- clp	-6703.2	0.07	0.986	8.7	4	4
2	GS-pruned	-6703.77	0.06	0.986	8.96	5	4
3	DGS	-6766.23	0.08	0.99	17.27	4	4
3	$\operatorname{DGS-clp}$	-6767.42	0.06	0.99	17.27	4	4
3	GS-tw	-6780.41	0.081	0.986	8.8	4	4
3	GS- clp	-6777.84	0.05	0.986	8.8	4	4
3	GS-pruned	-6757.3	0.06	0.99	9.01	5	4
4	DGS	-6889.86	0.07	0.99	16.67	4	4
4	$\operatorname{DGS-clp}$	-6887.8	0.06	0.99	16.67	4	4
4	GS-tw	-6845.49	0.07	0.986	8.5	4	4
4	GS- clp	-6841.5	0.074	0.986	8.5	4	4
4	GS-pruned	-6844.63	0.06	0.99	8.63	5	4
5	DGS	-6875.33	0.065	0.99	18.19	4	4
5	$\operatorname{DGS-clp}$	-6874.72	0.05	0.99	18.19	4	4
5	GS-tw	-6864.08	0.06	0.99	9.2	4	4
5	GS- clp	-6865.68	0.02	0.986	9.2	4	4
5	GS-pruned	-6854.4	0.06	0.99	9.37	5	4

Table 40: Comparison of the methods in dataset reutersk500 in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	$_{ m time}$	tw	tw-pr
1	DGS	-6794.44	0.08	0.99	17.98	5	5
1	$\operatorname{DGS-clp}$	-6792.1	0.08	0.986	17.98	5	5
1	GS-tw	-6801.82	0.08	0.986	9.1	5	5
1	GS- clp	-6801.04	0.087	0.986	9.1	5	5
1	GS-pruned	-6801.82	0.08	0.986	9.13	5	5
2	DGS	-6660.87	0.076	0.99	18.34	5	5
2	$\operatorname{DGS-clp}$	-6659.51	0.06	0.99	18.34	5	5
2	GS-tw	-6649.62	0.07	0.986	8.9	5	5
2	GS- clp	-6644.4	0.07	0.986	8.9	5	5
2	GS-pruned	-6655.26	0.07	0.99	8.94	6	5
3	DGS	-6719.4	0.075	0.986	18.24	5	5
3	$\operatorname{DGS-clp}$	-6720.43	0.04	0.986	18.24	5	5
3	GS-tw	-6739.97	0.06	0.99	9.21	5	5
3	GS- clp	-6738.14	0.06	0.99	9.21	5	5
3	GS-pruned	-6739.97	0.06	0.99	9.2	5	5
4	DGS	-6833.36	0.07	0.99	17.5	5	5
4	$\operatorname{DGS-clp}$	-6831.15	0.06	0.99	17.5	5	5
4	GS-tw	-6806.98	0.074	0.986	8.7	5	5
4	GS- clp	-6803	0.074	0.99	8.7	5	5
4	GS-pruned	-6812.67	0.06	0.986	8.85	6	5
5	DGS	-6834.56	0.065	0.99	19.16	5	5
5	$\operatorname{DGS-clp}$	-6833.87	0.05	0.986	19.16	5	5
5	GS-tw	-6827.5	0.05	0.986	9.7	5	5
5	GS- clp	-6828.42	0.05	0.986	9.7	5	5
5	GS-pruned	-6827.5	0.05	0.986	9.72	5	5

Table 41: Comparison of the methods in dataset mediamill in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

		1					
Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	$\overline{\mathrm{DGS}}$	-63335.47	0.091	0.97	661.77	2	2
1	$\operatorname{DGS-clp}$	-63004.6	0.09	0.967	661.77	2	2
1	GS-tw	-230702.76	0.04	0.96	13.5	2	2
1	GS- clp	-66996.52	0.08	0.97	13.5	2	2
1	GS-pruned	-65127.5	0.07	0.97	23.72	35	2
2	DGS	-62152.82	0.09	0.97	619.41	2	2
2	$\operatorname{DGS-clp}$	-61765.1	0.091	0.968	619.41	2	2
2	GS-tw	-225868.26	0.04	0.96	13.7	2	2
2	GS- clp	-70425.73	0.07	0.97	13.7	2	2
2	GS-pruned	-64141.2	0.08	0.97	23.48	42	2
3	DGS	-63169.85	0.084	0.97	606.22	2	2
3	$\operatorname{DGS-clp}$	-62675.5	0.08	0.968	606.22	2	2
3	GS-tw	-230041.11	0.04	0.96	13.6	2	2
3	GS- clp	-70842.95	0.07	0.97	13.6	2	2
3	GS-pruned	-64703.39	0.07	0.97	23.59	45	2
4	DGS	-63369.16	0.074	0.97	630.16	2	2
4	$\operatorname{DGS-clp}$	-63015.2	0.07	0.968	630.16	2	2
4	GS-tw	-230803.25	0.03	0.96	13.8	2	2
4	GS- clp	-66036.85	0.07	0.97	13.8	2	2
4	GS-pruned	-65069.46	0.07	0.97	23.54	42	2
5	DGS	-63703.38	0.084	0.97	652.26	2	2
5	$\operatorname{DGS-clp}$	-63230	0.08	0.968	652.26	2	2
5	GS-tw	-230562.66	0.04	0.96	14.2	2	2
5	GS- clp	-65908.34	0.08	0.97	14.2	2	2
5	GS-pruned	-65745.22	0.07	0.97	23.69	37	2

Table 42: Comparison of the methods in dataset mediamill in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold Method CLL acc_G acc_M time tw tw-pr 1 DGS -61521.56 0.095 0.97 986.28 3 3 1 DGS-clp -61239.4 0.09 0.968 986.28 3 3 1 GS-tw -260184.35 0.03 0.96 17.7 3 3 1 GS-clp -70348.16 0.08 0.97 17.7 3 3 1 GS-pruned -62980.4 0.08 0.97 28.95 38 3 2 DGS -61091.35 0.095 0.97 893.15 3 3 2 DGS-clp -60783 0.09 0.968 893.15 3 3 3 2 GS-tw -260044.28 0.04 0.96 17.4 3 3 3 2 GS-pruned -62803.99 0.07 0.97 852.45 3 3 <t< th=""><th></th><th></th><th></th><th></th><th></th><th></th><th></th><th></th></t<>								
1 DGS-clp -61239.4 0.09 0.968 986.28 3 3 1 GS-tw -260184.35 0.03 0.96 17.7 3 3 1 GS-clp -70348.16 0.08 0.97 17.7 3 3 1 GS-pruned -62980.4 0.08 0.97 28.95 38 3 2 DGS -61091.35 0.095 0.97 893.15 3 3 2 DGS-clp -60783 0.09 0.968 893.15 3 3 2 GS-tw -260044.28 0.04 0.96 17.4 3 3 2 GS-tw -260044.28 0.04 0.96 17.4 3 3 2 GS-pruned -62803.99 0.07 0.97 29.8 37 3 3 DGS -61447.42 0.09 0.97 852.45 3 3 3 GS-tw -268497.53 0.03 0.96 17.3 3 3 3 GS-pruned -62681.33	Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1 GS-tw -260184.35 0.03 0.96 17.7 3 3 1 GS-clp -70348.16 0.08 0.97 17.7 3 3 1 GS-pruned -62980.4 0.08 0.97 28.95 38 3 2 DGS -61091.35 0.095 0.97 893.15 3 3 2 DGS-clp -60783 0.09 0.968 893.15 3 3 2 GS-tw -260044.28 0.04 0.96 17.4 3 3 2 GS-clp -137287.94 0.03 0.96 17.4 3 3 2 GS-pruned -62803.99 0.07 0.97 29.8 37 3 3 DGS -61447.42 0.09 0.97 852.45 3 3 3 DGS-clp -60943.1 0.092 0.968 852.45 3 3 3 GS-tw -268497.53 0.03 0.96 17.3 3 3 3 GS-pruned -62681.33 <td>1</td> <td>$\overline{\mathrm{DGS}}$</td> <td>-61521.56</td> <td>0.095</td> <td>0.97</td> <td>986.28</td> <td>3</td> <td>3</td>	1	$\overline{\mathrm{DGS}}$	-61521.56	0.095	0.97	986.28	3	3
1 GS-clp -70348.16 0.08 0.97 17.7 3 3 1 GS-pruned -62980.4 0.08 0.97 28.95 38 3 2 DGS -61091.35 0.095 0.97 893.15 3 3 2 DGS-clp -60783 0.09 0.968 893.15 3 3 2 GS-tw -260044.28 0.04 0.96 17.4 3 3 2 GS-clp -137287.94 0.03 0.96 17.4 3 3 2 GS-pruned -62803.99 0.07 0.97 29.8 37 3 3 DGS -61447.42 0.09 0.97 852.45 3 3 3 DGS-clp -60943.1 0.092 0.968 852.45 3 3 3 GS-tw -268497.53 0.03 0.96 17.3 3 3 3 GS-pruned -62681.33 0.07 0.97 29.62 40 3 4 DGS -61759.03	1	$\operatorname{DGS-clp}$	-61239.4	0.09	0.968	986.28	3	3
1 GS-pruned -62980.4 0.08 0.97 28.95 38 3 2 DGS -61091.35 0.095 0.97 893.15 3 3 2 DGS-clp -60783 0.09 0.968 893.15 3 3 2 GS-tw -260044.28 0.04 0.96 17.4 3 3 2 GS-clp -137287.94 0.03 0.96 17.4 3 3 2 GS-pruned -62803.99 0.07 0.97 29.8 37 3 3 DGS -61447.42 0.09 0.97 852.45 3 3 3 DGS-clp -60943.1 0.092 0.968 852.45 3 3 3 GS-tw -268497.53 0.03 0.96 17.3 3 3 3 GS-pruned -62681.33 0.07 0.97 29.62 40 3 4 DGS-clp -61428.1 0.084	1	GS-tw	-260184.35	0.03	0.96	17.7	3	3
2 DGS -61091.35 0.095 0.97 893.15 3 2 DGS-clp -60783 0.09 0.968 893.15 3 2 GS-tw -260044.28 0.04 0.96 17.4 3 3 2 GS-clp -137287.94 0.03 0.96 17.4 3 3 2 GS-pruned -62803.99 0.07 0.97 29.8 37 3 3 DGS -61447.42 0.09 0.97 852.45 3 3 3 DGS-clp -60943.1 0.092 0.968 852.45 3 3 3 GS-tw -268497.53 0.03 0.96 17.3 3 3 3 GS-pruned -62681.33 0.07 0.97 29.62 40 3 4 DGS -61759.03 0.08 0.97 842.94 3 3 4 GS-tw -262699.9 0.04 0.968 842.94 3 3 4 GS-pruned -62464.53 0.08	1	GS- clp	-70348.16	0.08	0.97	17.7	3	3
2 DGS-clp -60783 0.09 0.968 893.15 3 2 GS-tw -260044.28 0.04 0.96 17.4 3 3 2 GS-clp -137287.94 0.03 0.96 17.4 3 3 2 GS-pruned -62803.99 0.07 0.97 29.8 37 3 3 DGS -61447.42 0.09 0.97 852.45 3 3 3 DGS-clp -60943.1 0.092 0.968 852.45 3 3 3 GS-tw -268497.53 0.03 0.96 17.3 3 3 3 GS-pruned -62681.33 0.07 0.97 29.62 40 3 4 DGS -61759.03 0.08 0.97 17.3 3 3 4 DGS-clp -61428.1 0.084 0.968 842.94 3 3 4 GS-tw -262699.9 0.04 0.96 16.9 3 3 4 GS-pruned -62464.53 0.08	1	GS-pruned	-62980.4	0.08	0.97	28.95	38	3
2 GS-tw -260044.28 0.04 0.96 17.4 3 3 3 2 GS-clp -137287.94 0.03 0.96 17.4 3 3 3 2 GS-pruned -62803.99 0.07 0.97 29.8 37 3 3 3 DGS -61447.42 0.09 0.97 852.45 3 3 3 3 DGS-clp -60943.1 0.092 0.968 852.45 3 3 3 3 GS-tw -268497.53 0.03 0.96 17.3 3 3 3 GS-pruned -62681.33 0.07 0.97 29.62 40 3 4 DGS -61759.03 0.08 0.97 842.94 3 3 4 DGS-clp -61428.1 0.084 0.968 842.94 3 3 4 GS-tw -262699.9 0.04 0.96 16.9 3 3 4 GS-pruned -62464.53 0.08 0.97 28.71 42 3 5 DGS -62317.84 0.086 0.97 976.3 3 3 5 DGS-clp -61971.7 0.08 0.968 976.3 3 3 5 GS-tw -262344.27 0.04 0.96 17.4 3 3	2	DGS	-61091.35	0.095	0.97	893.15	3	3
2 GS-clp -137287.94 0.03 0.96 17.4 3 3 2 GS-pruned -62803.99 0.07 0.97 29.8 37 3 3 DGS -61447.42 0.09 0.97 852.45 3 3 3 DGS-clp -60943.1 0.092 0.968 852.45 3 3 3 GS-tw -268497.53 0.03 0.96 17.3 3 3 3 GS-clp -69728.8 0.08 0.97 17.3 3 3 3 GS-pruned -62681.33 0.07 0.97 29.62 40 3 4 DGS -61759.03 0.08 0.97 842.94 3 3 4 DGS-clp -61428.1 0.084 0.968 842.94 3 3 4 GS-tw -262699.9 0.04 0.96 16.9 3 3 4 GS-pruned -62464.53 0.08 0.97 28.71 42 3 5 DGS -61971.7	2	$\operatorname{DGS-clp}$	-60783	0.09	0.968	893.15	3	3
2 GS-pruned -62803.99 0.07 0.97 29.8 37 3 3 DGS -61447.42 0.09 0.97 852.45 3 3 3 DGS-clp -60943.1 0.092 0.968 852.45 3 3 3 GS-tw -268497.53 0.03 0.96 17.3 3 3 3 GS-clp -69728.8 0.08 0.97 17.3 3 3 3 GS-pruned -62681.33 0.07 0.97 29.62 40 3 4 DGS -61759.03 0.08 0.97 842.94 3 3 4 DGS-clp -61428.1 0.084 0.968 842.94 3 3 4 GS-tw -262699.9 0.04 0.96 16.9 3 3 4 GS-pruned -62464.53 0.08 0.97 28.71 42 3 5 DGS -62317.84 0.086 0.97 976.3 3 3 5 DGS-clp -61971.7 <td>2</td> <td>GS-tw</td> <td>-260044.28</td> <td>0.04</td> <td>0.96</td> <td>17.4</td> <td>3</td> <td>3</td>	2	GS-tw	-260044.28	0.04	0.96	17.4	3	3
3 DGS	2	GS- clp	-137287.94	0.03	0.96	17.4	3	3
3 DGS-clp -60943.1 0.092 0.968 852.45 3 3 3 GS-tw -268497.53 0.03 0.96 17.3 3 3 3 GS-clp -69728.8 0.08 0.97 17.3 3 3 3 GS-pruned -62681.33 0.07 0.97 29.62 40 3 4 DGS -61759.03 0.08 0.97 842.94 3 3 4 DGS-clp -61428.1 0.084 0.968 842.94 3 3 4 GS-tw -262699.9 0.04 0.96 16.9 3 3 4 GS-clp -72954.53 0.07 0.97 16.9 3 3 4 GS-pruned -62464.53 0.08 0.97 28.71 42 3 5 DGS -62317.84 0.086 0.97 976.3 3 3 5 DGS-clp -61971.7 0.08 0.968 976.3 3 3 5 GS-tw -262344.27 <td>2</td> <td>GS-pruned</td> <td>-62803.99</td> <td>0.07</td> <td>0.97</td> <td>29.8</td> <td>37</td> <td>3</td>	2	GS-pruned	-62803.99	0.07	0.97	29.8	37	3
3 GS-tw -268497.53 0.03 0.96 17.3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	3	DGS	-61447.42	0.09	0.97	852.45	3	3
3 GS-clp -69728.8 0.08 0.97 17.3 3 3 3 GS-pruned -62681.33 0.07 0.97 29.62 40 3 4 DGS -61759.03 0.08 0.97 842.94 3 3 4 DGS-clp -61428.1 0.084 0.968 842.94 3 3 4 GS-tw -262699.9 0.04 0.96 16.9 3 3 4 GS-clp -72954.53 0.07 0.97 16.9 3 3 4 GS-pruned -62464.53 0.08 0.97 28.71 42 3 5 DGS -62317.84 0.086 0.97 976.3 3 3 5 DGS-clp -61971.7 0.08 0.968 976.3 3 3 5 GS-tw -262344.27 0.04 0.96 17.4 3 3	3	$\operatorname{DGS-clp}$	-60943.1	0.092	0.968	852.45	3	3
3 GS-pruned -62681.33 0.07 0.97 29.62 40 3 4 DGS -61759.03 0.08 0.97 842.94 3 3 4 DGS-clp -61428.1 0.084 0.968 842.94 3 3 4 GS-tw -262699.9 0.04 0.96 16.9 3 3 4 GS-clp -72954.53 0.07 0.97 16.9 3 3 4 GS-pruned -62464.53 0.08 0.97 28.71 42 3 5 DGS -62317.84 0.086 0.97 976.3 3 3 5 DGS-clp -61971.7 0.08 0.968 976.3 3 3 5 GS-tw -262344.27 0.04 0.96 17.4 3 3	3	GS-tw	-268497.53	0.03	0.96	17.3	3	3
4 DGS -61759.03 0.08 0.97 842.94 3 3 4 DGS-clp -61428.1 0.084 0.968 842.94 3 3 4 GS-tw -262699.9 0.04 0.96 16.9 3 3 4 GS-clp -72954.53 0.07 0.97 16.9 3 3 4 GS-pruned -62464.53 0.08 0.97 28.71 42 3 5 DGS -62317.84 0.086 0.97 976.3 3 3 5 DGS-clp -61971.7 0.08 0.968 976.3 3 3 5 GS-tw -262344.27 0.04 0.96 17.4 3 3	3	GS- clp	-69728.8	0.08	0.97	17.3	3	3
4 DGS-clp -61428.1 0.084 0.968 842.94 3 3 4 GS-tw -262699.9 0.04 0.96 16.9 3 3 4 GS-clp -72954.53 0.07 0.97 16.9 3 3 4 GS-pruned -62464.53 0.08 0.97 28.71 42 3 5 DGS -62317.84 0.086 0.97 976.3 3 3 5 DGS-clp -61971.7 0.08 0.968 976.3 3 3 5 GS-tw -262344.27 0.04 0.96 17.4 3 3	3	GS-pruned	-62681.33	0.07	0.97	29.62	40	3
4 GS-tw -262699.9 0.04 0.96 16.9 3 3 4 GS-clp -72954.53 0.07 0.97 16.9 3 3 4 GS-pruned -62464.53 0.08 0.97 28.71 42 3 5 DGS -62317.84 0.086 0.97 976.3 3 3 5 DGS-clp -61971.7 0.08 0.968 976.3 3 3 5 GS-tw -262344.27 0.04 0.96 17.4 3 3	4	DGS	-61759.03	0.08	0.97	842.94	3	3
4 GS-clp -72954.53 0.07 0.97 16.9 3 3 4 GS-pruned -62464.53 0.08 0.97 28.71 42 3 5 DGS -62317.84 0.086 0.97 976.3 3 3 5 DGS-clp -61971.7 0.08 0.968 976.3 3 3 5 GS-tw -262344.27 0.04 0.96 17.4 3 3	4	$\operatorname{DGS-clp}$	-61428.1	0.084	0.968	842.94	3	3
4 GS-pruned -62464.53 0.08 0.97 28.71 42 3 5 DGS -62317.84 0.086 0.97 976.3 3 3 5 DGS-clp -61971.7 0.08 0.968 976.3 3 3 5 GS-tw -262344.27 0.04 0.96 17.4 3 3	4	GS-tw	-262699.9	0.04	0.96	16.9	3	3
5 DGS -62317.84 0.086 0.97 976.3 3 3 5 5 DGS-clp -61971.7 0.08 0.968 976.3 3 3 5 GS-tw -262344.27 0.04 0.96 17.4 3 3	4	GS- clp	-72954.53	0.07	0.97	16.9	3	3
5 DGS-clp -61971.7 0.08 0.968 976.3 3 3 5 5 GS-tw -262344.27 0.04 0.96 17.4 3 3	4	GS-pruned	-62464.53	0.08	0.97	28.71	42	3
5 GS-tw -262344.27 0.04 0.96 17.4 3 3	5	DGS	-62317.84	0.086	0.97	976.3	3	3
	5	$\operatorname{DGS-clp}$	-61971.7	0.08	0.968	976.3	3	3
5 GS-clp -71138.28 0.07 0.97 17.4 3 3	5	GS-tw	-262344.27	0.04	0.96	17.4	3	3
	5	GS- clp	-71138.28	0.07	0.97	17.4	3	3
5 GS-pruned -62650.41 0.08 0.97 28.88 34 3	5	GS-pruned	-62650.41	0.08	0.97	28.88	34	3

Table 43: Comparison of the methods in dataset mediamill in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold Method CLL acc $_G$ acc $_M$ time tw twpr 1 DGS -60934.34 0.093 0.97 1673.88 4 4 1 DGS-clp -60641.9 0.09 0.968 1673.88 4 4 1 GS-tw -261727.4 0.04 0.96 20.9 4 4 1 GS-pruned -61661.65 0.08 0.97 33.84 40 4 2 DGS -59978.94 0.09 0.97 1145.26 4 4 2 DGS-clp -59649.4 0.09 0.968 1145.26 4 4 2 DGS-clp -59978.94 0.09 0.97 1145.26 4 4 2 DGS -59978.94 0.09 0.97 1145.26 4 4 2 DGS-clp -165912.91 0.03 0.96 21.3 4 4 3 DGS -60492.21 <td< th=""><th></th><th></th><th></th><th></th><th></th><th></th><th></th><th></th></td<>								
1 DGS-clp -60641.9 0.09 0.968 1673.88 4 4 1 GS-tw -261727.4 0.04 0.96 20.9 4 4 1 GS-clp -144692.3 0.03 0.96 20.9 4 4 1 GS-pruned -61661.65 0.08 0.97 33.84 40 4 2 DGS -59978.94 0.09 0.97 1145.26 4 4 2 DGS-clp -59649.4 0.09 0.968 1145.26 4 4 2 GS-tw -258541.44 0.04 0.96 21.3 4 4 2 GS-clp -165912.91 0.03 0.96 21.3 4 4 2 GS-pruned -61737.62 0.08 0.97 33.92 36 4 3 DGS-clp -60469.24 0.09 0.97 1193.82 4 4 3 GS-tw -264572.27 0.04 0.96 21 4 4 3 GS-pruned -61631	Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1 GS-tw -261727.4 0.04 0.96 20.9 4 4 1 GS-clp -144692.3 0.03 0.96 20.9 4 4 1 GS-pruned -61661.65 0.08 0.97 33.84 40 4 2 DGS -59978.94 0.09 0.97 1145.26 4 4 2 DGS-clp -59649.4 0.09 0.968 1145.26 4 4 2 GS-tw -258541.44 0.04 0.96 21.3 4 4 2 GS-clp -165912.91 0.03 0.96 21.3 4 4 2 GS-pruned -61737.62 0.08 0.97 33.92 36 4 3 DGS -60469.24 0.09 0.97 1193.82 4 4 3 GS-clp -60029.9 0.09 0.97 1193.82 4 4 3 GS-tw -264572.27 0.04 0.96 21 4 4 3 GS-pruned -61631.92 <td>1</td> <td>$\overline{\mathrm{DGS}}$</td> <td>-60934.34</td> <td>0.093</td> <td>0.97</td> <td>1673.88</td> <td>4</td> <td>4</td>	1	$\overline{\mathrm{DGS}}$	-60934.34	0.093	0.97	1673.88	4	4
1 GS-clp -144692.3 0.03 0.96 20.9 4 4 1 GS-pruned -61661.65 0.08 0.97 33.84 40 4 2 DGS -59978.94 0.09 0.97 1145.26 4 4 2 DGS-clp -59649.4 0.09 0.968 1145.26 4 4 2 GS-tw -258541.44 0.04 0.96 21.3 4 4 2 GS-clp -165912.91 0.03 0.96 21.3 4 4 2 GS-pruned -61737.62 0.08 0.97 33.92 36 4 3 DGS -60469.24 0.09 0.97 1193.82 4 4 3 DGS-clp -6029.9 0.09 0.97 1193.82 4 4 3 GS-tw -264572.27 0.04 0.96 21 4 4 3 GS-clp -64719.1 0.093 0.968 21 4 4 4 DGS -60310.1	1	$\operatorname{DGS-clp}$	-60641.9	0.09	0.968	1673.88	4	4
1 GS-pruned -61661.65 0.08 0.97 33.84 40 4 2 DGS -59978.94 0.09 0.97 1145.26 4 4 2 DGS-clp -59649.4 0.09 0.968 1145.26 4 4 2 GS-tw -258541.44 0.04 0.96 21.3 4 4 2 GS-clp -165912.91 0.03 0.96 21.3 4 4 2 GS-pruned -61737.62 0.08 0.97 33.92 36 4 3 DGS -60469.24 0.09 0.97 1193.82 4 4 3 DGS-clp -6029.9 0.09 0.97 1193.82 4 4 3 GS-tw -264572.27 0.04 0.96 21 4 4 3 GS-pruned -61631.92 0.09 0.97 33.8 40 4 4 DGS -60310.1 0.085 <td>1</td> <td>GS-tw</td> <td>-261727.4</td> <td>0.04</td> <td>0.96</td> <td>20.9</td> <td>4</td> <td>4</td>	1	GS-tw	-261727.4	0.04	0.96	20.9	4	4
2 DGS -59978.94 0.09 0.97 1145.26 4 4 2 DGS-clp -59649.4 0.09 0.968 1145.26 4 4 2 GS-tw -258541.44 0.04 0.96 21.3 4 4 2 GS-clp -165912.91 0.03 0.96 21.3 4 4 2 GS-pruned -61737.62 0.08 0.97 33.92 36 4 3 DGS -60469.24 0.09 0.97 1193.82 4 4 3 DGS-clp -60029.9 0.09 0.97 1193.82 4 4 3 GS-tw -264572.27 0.04 0.96 21 4 4 3 GS-clp -64719.1 0.093 0.968 21 4 4 4 DGS -60310.1 0.085 0.97 1274.16 4 4 4 DGS-clp -59959.1 0.08 0.968 1274.16 4 4 4 GS-tw -272078.14	1	GS- clp	-144692.3	0.03	0.96	20.9	4	4
2 DGS-clp -59649.4 0.09 0.968 1145.26 4 4 2 GS-tw -258541.44 0.04 0.96 21.3 4 4 2 GS-clp -165912.91 0.03 0.96 21.3 4 4 2 GS-pruned -61737.62 0.08 0.97 33.92 36 4 3 DGS -60469.24 0.09 0.97 1193.82 4 4 3 DGS-clp -60029.9 0.09 0.97 1193.82 4 4 3 GS-tw -264572.27 0.04 0.96 21 4 4 3 GS-pruned -61631.92 0.09 0.97 33.8 40 4 4 DGS -60310.1 0.085 0.97 1274.16 4 4 4 DGS-clp -59959.1 0.08 0.968 1274.16 4 4 4 GS-tw -272078.14 0.04 0.96 20.8 4 4 4 GS-pruned -61270.	1	GS-pruned	-61661.65	0.08	0.97	33.84	40	4
2 GS-tw -258541.44 0.04 0.96 21.3 4 4 2 GS-clp -165912.91 0.03 0.96 21.3 4 4 2 GS-pruned -61737.62 0.08 0.97 33.92 36 4 3 DGS -60469.24 0.09 0.97 1193.82 4 4 3 DGS-clp -60029.9 0.09 0.97 1193.82 4 4 3 GS-tw -264572.27 0.04 0.96 21 4 4 3 GS-clp -64719.1 0.093 0.968 21 4 4 3 GS-pruned -61631.92 0.09 0.97 33.8 40 4 4 DGS -60310.1 0.085 0.97 1274.16 4 4 4 GS-tw -272078.14 0.04 0.96 20.8 4 4 4 GS-pruned -61270.81 0.08 0.97 33.8 37 4 5 DGS -60978.42	2	DGS	-59978.94	0.09	0.97	1145.26	4	4
2 GS-clp -165912.91 0.03 0.96 21.3 4 4 2 GS-pruned -61737.62 0.08 0.97 33.92 36 4 3 DGS -60469.24 0.09 0.97 1193.82 4 4 3 DGS-clp -60029.9 0.09 0.97 1193.82 4 4 3 GS-tw -264572.27 0.04 0.96 21 4 4 3 GS-clp -64719.1 0.093 0.968 21 4 4 3 GS-pruned -61631.92 0.09 0.97 33.8 40 4 4 DGS -60310.1 0.085 0.97 1274.16 4 4 4 DGS-clp -59959.1 0.08 0.968 1274.16 4 4 4 GS-tw -272078.14 0.04 0.96 20.8 4 4 4 GS-pruned -61270.81 0.08 0.97 33.8 37 4 5 DGS -60532.4	2	$\operatorname{DGS-clp}$	-59649.4	0.09	0.968	1145.26	4	4
2 GS-pruned -61737.62 0.08 0.97 33.92 36 4 3 DGS -60469.24 0.09 0.97 1193.82 4 4 3 DGS-clp -60029.9 0.09 0.97 1193.82 4 4 3 GS-tw -264572.27 0.04 0.96 21 4 4 3 GS-clp -64719.1 0.093 0.968 21 4 4 3 GS-pruned -61631.92 0.09 0.97 33.8 40 4 4 DGS -60310.1 0.085 0.97 1274.16 4 4 4 DGS-clp -59959.1 0.08 0.968 1274.16 4 4 4 GS-tw -272078.14 0.04 0.96 20.8 4 4 4 GS-pruned -61270.81 0.08 0.97 33.8 37 4 5 DGS -60978.42 0.088 0.97 1407.1 4 4 5 GS-tw -262981.07 <td>2</td> <td>GS-tw</td> <td>-258541.44</td> <td>0.04</td> <td>0.96</td> <td>21.3</td> <td>4</td> <td>4</td>	2	GS-tw	-258541.44	0.04	0.96	21.3	4	4
3 DGS	2	GS- clp	-165912.91	0.03	0.96	21.3	4	4
3 DGS-clp -60029.9 0.09 0.97 1193.82 4 4 3 GS-tw -264572.27 0.04 0.96 21 4 4 3 GS-clp -64719.1 0.093 0.968 21 4 4 3 GS-pruned -61631.92 0.09 0.97 33.8 40 4 4 DGS -60310.1 0.085 0.97 1274.16 4 4 4 DGS-clp -59959.1 0.08 0.968 1274.16 4 4 4 GS-tw -272078.14 0.04 0.96 20.8 4 4 4 GS-clp -155287.25 0.03 0.96 20.8 4 4 4 GS-pruned -61270.81 0.08 0.97 33.8 37 4 5 DGS -60532.4 0.08 0.97 1407.1 4 4 5 GS-tw -262981.07 0.04 0.96 20.7 4 4 5 GS-clp -67988.49	2	GS-pruned	-61737.62	0.08	0.97	33.92	36	4
3 GS-tw -264572.27 0.04 0.96 21 4 4 4 3 GS-clp -64719.1 0.093 0.968 21 4 4 4 4 3 GS-clp -60532.4 0.08 0.968 21 4 4 4 4 4 4 4 4 5 5 GS-clp -60532.4 0.08 0.968 0.968 0.968 1274.1 4 4 4 5 GS-clp -67988.49 0.088 0.968 0.968 0.968 0.968 1274.1 4 4 4 4 5 GS-clp -60532.4 0.08 0.968 0.97 0.97 0.97 0.97 0.97 0.97 0.97 0.97	3	DGS	-60469.24	0.09	0.97	1193.82	4	4
3 GS-clp -64719.1 0.093 0.968 21 4 4 3 GS-pruned -61631.92 0.09 0.97 33.8 40 4 4 DGS -60310.1 0.085 0.97 1274.16 4 4 4 DGS-clp -59959.1 0.08 0.968 1274.16 4 4 4 GS-tw -272078.14 0.04 0.96 20.8 4 4 4 GS-clp -155287.25 0.03 0.96 20.8 4 4 4 GS-pruned -61270.81 0.08 0.97 33.8 37 4 5 DGS -60978.42 0.088 0.97 1407.1 4 4 5 DGS-clp -60532.4 0.08 0.97 1407.1 4 4 5 GS-tw -262981.07 0.04 0.96 20.7 4 4 5 GS-clp -67988.49 0.088 0.968 20.7 4 4	3	$\operatorname{DGS-clp}$	-60029.9	0.09	0.97	1193.82	4	4
3 GS-pruned -61631.92 0.09 0.97 33.8 40 4 4 DGS -60310.1 0.085 0.97 1274.16 4 4 4 DGS-clp -59959.1 0.08 0.968 1274.16 4 4 4 GS-tw -272078.14 0.04 0.96 20.8 4 4 4 GS-clp -155287.25 0.03 0.96 20.8 4 4 4 GS-pruned -61270.81 0.08 0.97 33.8 37 4 5 DGS -60978.42 0.088 0.97 1407.1 4 4 5 DGS-clp -60532.4 0.08 0.97 1407.1 4 4 5 GS-tw -262981.07 0.04 0.96 20.7 4 4 5 GS-clp -67988.49 0.088 0.968 20.7 4 4	3	GS-tw	-264572.27	0.04	0.96	21	4	4
4 DGS -60310.1 0.085 0.97 1274.16 4 4 4 DGS-clp -59959.1 0.08 0.968 1274.16 4 4 4 GS-tw -272078.14 0.04 0.96 20.8 4 4 4 GS-clp -155287.25 0.03 0.96 20.8 4 4 4 GS-pruned -61270.81 0.08 0.97 33.8 37 4 5 DGS -60978.42 0.088 0.97 1407.1 4 4 5 DGS-clp -60532.4 0.08 0.97 1407.1 4 4 5 GS-tw -262981.07 0.04 0.96 20.7 4 4 5 GS-clp -67988.49 0.088 0.968 20.7 4 4	3	GS- clp	-64719.1	0.093	0.968	21	4	4
4 DGS-clp -59959.1 0.08 0.968 1274.16 4 4 4 GS-tw -272078.14 0.04 0.96 20.8 4 4 4 GS-clp -155287.25 0.03 0.96 20.8 4 4 4 GS-pruned -61270.81 0.08 0.97 33.8 37 4 5 DGS -60978.42 0.088 0.97 1407.1 4 4 5 DGS-clp -60532.4 0.08 0.97 1407.1 4 4 5 GS-tw -262981.07 0.04 0.96 20.7 4 4 5 GS-clp -67988.49 0.088 0.968 20.7 4 4	3	GS-pruned	-61631.92	0.09	0.97	33.8	40	4
4 GS-tw -272078.14 0.04 0.96 20.8 4 4 4 GS-clp -155287.25 0.03 0.96 20.8 4 4 4 GS-pruned -61270.81 0.08 0.97 33.8 37 4 5 DGS -60978.42 0.088 0.97 1407.1 4 4 5 DGS-clp -60532.4 0.08 0.97 1407.1 4 4 5 GS-tw -262981.07 0.04 0.96 20.7 4 4 5 GS-clp -67988.49 0.088 0.968 20.7 4 4	4	DGS	-60310.1	0.085	0.97	1274.16	4	4
4 GS-clp -155287.25 0.03 0.96 20.8 4 4 4 GS-pruned -61270.81 0.08 0.97 33.8 37 4 5 DGS -60978.42 0.088 0.97 1407.1 4 4 5 DGS-clp -60532.4 0.08 0.97 1407.1 4 4 5 GS-tw -262981.07 0.04 0.96 20.7 4 4 5 GS-clp -67988.49 0.088 0.968 20.7 4 4	4	$\operatorname{DGS-clp}$	-59959.1	0.08	0.968	1274.16	4	4
4 GS-pruned -61270.81 0.08 0.97 33.8 37 4 5 DGS -60978.42 0.088 0.97 1407.1 4 4 5 DGS-clp -60532.4 0.08 0.97 1407.1 4 4 5 GS-tw -262981.07 0.04 0.96 20.7 4 4 5 GS-clp -67988.49 0.088 0.968 20.7 4 4	4	GS-tw	-272078.14	0.04	0.96	20.8	4	4
5 DGS -60978.42 0.088 0.97 1407.1 4 4 5 DGS-clp -60532.4 0.08 0.97 1407.1 4 4 5 GS-tw -262981.07 0.04 0.96 20.7 4 4 5 GS-clp -67988.49 0.088 0.968 20.7 4 4	4	GS- clp	-155287.25	0.03	0.96	20.8	4	4
5 DGS-clp -60532.4 0.08 0.97 1407.1 4 4 5 GS-tw -262981.07 0.04 0.96 20.7 4 4 5 GS-clp -67988.49 0.088 0.968 20.7 4 4	4	GS-pruned	-61270.81	0.08	0.97	33.8	37	4
5 GS-tw -262981.07 0.04 0.96 20.7 4 4 5 GS-clp -67988.49 0.088 0.968 20.7 4 4	5	DGS	-60978.42	0.088	0.97	1407.1	4	4
5 GS-clp -67988.49 0.088 0.968 20.7 4 4	5	$\operatorname{DGS-clp}$	-60532.4	0.08	0.97	1407.1	4	4
•	5	GS-tw	-262981.07	0.04	0.96	20.7	4	4
5 GS-pruned -61992.07 0.08 0.97 33.41 42 4	5	GS- clp	-67988.49	0.088	0.968	20.7	4	4
1	5	GS-pruned	-61992.07	0.08	0.97	33.41	42	4

Table 44: Comparison of the methods in dataset mediamill in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold Method CLL acc _G acc _M time tw tw-pr 1 DGS -60371.47 0.09 0.97 2502.95 5 5 1 DGS-clp -60028.3 0.091 0.97 2502.95 5 5 1 GS-tw -90368.71 0.06 0.96 30 5 5 1 GS-clp -60294.09 0.08 0.968 30 5 5 2 DGS -59653.79 0.09 0.97 1918.17 5 5 2 DGS-clp -5963.79 0.09 0.97 1918.17 5 5 2 DGS-tw -102520.34 0.09 0.97 1918.17 5 5 2 DGS-th -65278.33 0.09 0.97 1918.17 5 5 3 DGS-clp -65278.33 0.09 0.97 2302.43 5 5 3 DGS-clp -59558.9 0.0								
1 DGS-clp -60028.3 0.091 0.97 2502.95 5 5 1 GS-tw -90368.71 0.06 0.96 30 5 5 1 GS-clp -60294.09 0.08 0.968 30 5 5 1 GS-pruned -61429.4 0.07 0.97 34.45 44 5 2 DGS -59653.79 0.09 0.97 1918.17 5 5 2 DGS-clp -59340.9 0.09 0.97 1918.17 5 5 2 DGS-clp -59340.9 0.09 0.97 1918.17 5 5 2 GS-tw -102520.34 0.06 0.96 29.3 5 5 2 GS-clp -65278.33 0.093 0.968 29.3 5 5 2 GS-pruned -61258.64 0.08 0.97 333.61 41 5 3 DGS-clp -59558.9 0.09 0.97 2302.43 5 5 3 GS-tup -60433.8	Fold	Method	CLL	acc_G	acc_M	$_{ m time}$	tw	tw-pr
1 GS-tw -90368.71 0.06 0.96 30 5 5 1 GS-clp -60294.09 0.08 0.968 30 5 5 1 GS-pruned -61429.4 0.07 0.97 34.45 44 5 2 DGS -59653.79 0.09 0.97 1918.17 5 5 2 DGS-clp -59340.9 0.09 0.97 1918.17 5 5 2 GS-tw -102520.34 0.06 0.96 29.3 5 5 2 GS-clp -65278.33 0.093 0.968 29.3 5 5 2 GS-pruned -61258.64 0.08 0.97 33.61 41 5 3 DGS -6021.5 0.09 0.97 2302.43 5 5 3 DGS-clp -59558.9 0.09 0.97 2302.43 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-pruned -60433.8	1	DGS	-60371.47	0.09	0.97	2502.95	5	5
1 GS-clp -60294.09 0.08 0.968 30 5 5 1 GS-pruned -61429.4 0.07 0.97 34.45 44 5 2 DGS -59653.79 0.09 0.97 1918.17 5 5 2 DGS-clp -59340.9 0.09 0.97 1918.17 5 5 2 DGS-clp -59340.9 0.09 0.97 1918.17 5 5 2 DGS-clp -65278.33 0.06 0.96 29.3 5 5 2 GS-pruned -61258.64 0.08 0.97 33.61 41 5 3 DGS -6021.5 0.09 0.97 2302.43 5 5 3 DGS-clp -59558.9 0.09 0.97 2302.43 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-pruned -60433.8 0.095<	1	$\operatorname{DGS-clp}$	-60028.3	0.091	0.97	2502.95	5	5
1 GS-pruned -61429.4 0.07 0.97 34.45 44 5 2 DGS -59653.79 0.09 0.97 1918.17 5 5 2 DGS-clp -59340.9 0.09 0.97 1918.17 5 5 2 GS-tw -102520.34 0.06 0.96 29.3 5 5 2 GS-clp -65278.33 0.093 0.968 29.3 5 5 2 GS-pruned -61258.64 0.08 0.97 33.61 41 5 3 DGS -6021.5 0.09 0.97 2302.43 5 5 3 DGS-clp -59558.9 0.09 0.97 2302.43 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-tw -95421.69 0.07	1	GS-tw	-90368.71	0.06	0.96	30	5	5
2 DGS -59653.79 0.09 0.97 1918.17 5 5 2 DGS-clp -59340.9 0.09 0.97 1918.17 5 5 2 GS-tw -102520.34 0.06 0.96 29.3 5 5 2 GS-clp -65278.33 0.093 0.968 29.3 5 5 2 GS-pruned -61258.64 0.08 0.97 33.61 41 5 3 DGS -60021.5 0.09 0.97 2302.43 5 5 3 DGS-clp -59558.9 0.09 0.97 2302.43 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-pruned -61086.39 0.07 0.97 35.33 41 5 4 DGS -59788.2	1	GS- clp	-60294.09	0.08	0.968	30	5	5
2 DGS-clp -59340.9 0.09 0.97 1918.17 5 5 2 GS-tw -102520.34 0.06 0.96 29.3 5 5 2 GS-clp -65278.33 0.093 0.968 29.3 5 5 2 GS-pruned -61258.64 0.08 0.97 33.61 41 5 3 DGS -60021.5 0.09 0.97 2302.43 5 5 3 DGS-clp -59558.9 0.09 0.97 2302.43 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-tp -60433.8 0.095 0.968 30.2 5 5 4 DGS -60096.82 0.09 0.97 1970.78 5 5 4 GS-tw -93889.54 0.06	1	GS-pruned	-61429.4	0.07	0.97	34.45	44	5
2 GS-tw -102520.34 0.06 0.96 29.3 5 5 2 GS-clp -65278.33 0.093 0.968 29.3 5 5 2 GS-pruned -61258.64 0.08 0.97 33.61 41 5 3 DGS -60021.5 0.09 0.97 2302.43 5 5 3 DGS-clp -59558.9 0.09 0.97 2302.43 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 4 DGS -60433.8 0.095 0.97 35.33 41 5 4 DGS-clp -59788.2 0	2	DGS	-59653.79	0.09	0.97	1918.17	5	5
2 GS-clp -65278.33 0.093 0.968 29.3 5 5 2 GS-pruned -61258.64 0.08 0.97 33.61 41 5 3 DGS -60021.5 0.09 0.97 2302.43 5 5 3 DGS-clp - 59558.9 0.09 0.97 2302.43 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-clp -60433.8 0.095 0.968 30.2 5 5 3 GS-pruned -61086.39 0.07 0.97 35.33 41 5 4 DGS -6096.82 0.09 0.97 1970.78 5 5 4 DGS-clp - 59788.2 0.08 0.97 1970.78 5 5 4 GS-tw -93889.54 0.06 0.96 29.3 5 5 4 GS-pruned -61700.14 0.08 0.97 33.92 43 5 5 DGS	2	$\operatorname{DGS-clp}$	-59340.9	0.09	0.97	1918.17	5	5
2 GS-pruned -61258.64 0.08 0.97 33.61 41 5 3 DGS -60021.5 0.09 0.97 2302.43 5 5 3 DGS-clp -59558.9 0.09 0.97 2302.43 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-clp -60433.8 0.095 0.968 30.2 5 5 3 GS-pruned -61086.39 0.07 0.97 35.33 41 5 4 DGS -60096.82 0.09 0.97 1970.78 5 5 4 DGS-clp -59788.2 0.08 0.97 1970.78 5 5 4 GS-tw -93889.54 0.06 0.96 29.3 5 5 4 GS-clp -60794.68 0.095 0.968 29.3 5 5 4 GS-pruned -61700.14 0.08 0.97 33.92 43 5 5 DGS-clp -59976.	2	GS-tw	-102520.34	0.06	0.96	29.3	5	5
3 DGS -60021.5 0.09 0.97 2302.43 5 5 3 DGS-clp -59558.9 0.09 0.97 2302.43 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-clp -60433.8 0.095 0.968 30.2 5 5 3 GS-pruned -61086.39 0.07 0.97 35.33 41 5 4 DGS -60096.82 0.09 0.97 1970.78 5 5 4 DGS-clp -59788.2 0.08 0.97 1970.78 5 5 4 GS-tw -93889.54 0.06 0.96 29.3 5 5 4 GS-clp -60794.68 0.095 0.968 29.3 5 5 5 DGS -60381.59 0.09 0.97 2380.98 5 5 5 DGS-clp -59976.4 0.095	2	GS- clp	-65278.33	0.093	0.968	29.3	5	5
3 DGS-clp -59558.9 0.09 0.97 2302.43 5 5 3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-clp -60433.8 0.095 0.968 30.2 5 5 3 GS-pruned -61086.39 0.07 0.97 35.33 41 5 4 DGS -60096.82 0.09 0.97 1970.78 5 5 4 DGS-clp -59788.2 0.08 0.97 1970.78 5 5 4 GS-tw -93889.54 0.06 0.96 29.3 5 5 4 GS-clp -60794.68 0.095 0.968 29.3 5 5 4 GS-pruned -61700.14 0.08 0.97 33.92 43 5 5 DGS -60381.59 0.09 0.97 2380.98 5 5 5 DGS-clp -59976.4 0.095 0.96 29.7 5 5 5 GS-tw -92636.48 <td>2</td> <td>GS-pruned</td> <td>-61258.64</td> <td>0.08</td> <td>0.97</td> <td>33.61</td> <td>41</td> <td>5</td>	2	GS-pruned	-61258.64	0.08	0.97	33.61	41	5
3 GS-tw -95421.69 0.07 0.96 30.2 5 5 3 GS-clp -60433.8 0.095 0.968 30.2 5 5 3 GS-pruned -61086.39 0.07 0.97 35.33 41 5 4 DGS -60096.82 0.09 0.97 1970.78 5 5 4 DGS-clp -59788.2 0.08 0.97 1970.78 5 5 4 GS-tw -93889.54 0.06 0.96 29.3 5 5 4 GS-clp -60794.68 0.095 0.968 29.3 5 5 4 GS-pruned -61700.14 0.08 0.97 33.92 43 5 5 DGS -60381.59 0.09 0.97 2380.98 5 5 5 DGS-clp -59976.4 0.095 0.96 29.7 5 5 5 GS-tw -92636.48 0.07 0.96 29.7 5 5 5 GS-clp -61024.52	3	DGS	-60021.5	0.09	0.97	2302.43	5	5
3 GS-clp -60433.8 0.095 0.968 30.2 5 5 3 GS-pruned -61086.39 0.07 0.97 35.33 41 5 4 DGS -60096.82 0.09 0.97 1970.78 5 5 4 DGS-clp -59788.2 0.08 0.97 1970.78 5 5 4 GS-tw -93889.54 0.06 0.96 29.3 5 5 4 GS-clp -60794.68 0.095 0.968 29.3 5 5 4 GS-pruned -61700.14 0.08 0.97 33.92 43 5 5 DGS -60381.59 0.09 0.97 2380.98 5 5 5 DGS-clp -59976.4 0.095 0.97 2380.98 5 5 5 GS-tw -92636.48 0.07 0.96 29.7 5 5 5 GS-clp -61024.52 0.09 0.968 29.7 5 5	3	$\operatorname{DGS-clp}$	-59558.9	0.09	0.97	2302.43	5	5
3 GS-pruned -61086.39 0.07 0.97 35.33 41 5 4 DGS -60096.82 0.09 0.97 1970.78 5 5 4 DGS-clp -59788.2 0.08 0.97 1970.78 5 5 4 GS-tw -93889.54 0.06 0.96 29.3 5 5 4 GS-pruned -61700.14 0.08 0.97 33.92 43 5 5 DGS -60381.59 0.09 0.97 2380.98 5 5 5 DGS-clp -59976.4 0.095 0.97 2380.98 5 5 5 GS-tw -92636.48 0.07 0.96 29.7 5 5 5 GS-clp -61024.52 0.09 0.968 29.7 5 5	3	GS-tw	-95421.69	0.07	0.96	30.2	5	5
4 DGS -60096.82 0.09 0.97 1970.78 5 5 4 DGS-clp -59788.2 0.08 0.97 1970.78 5 5 4 GS-tw -93889.54 0.06 0.96 29.3 5 5 4 GS-clp -60794.68 0.095 0.968 29.3 5 5 4 GS-pruned -61700.14 0.08 0.97 33.92 43 5 5 DGS -60381.59 0.09 0.97 2380.98 5 5 5 DGS-clp -59976.4 0.095 0.97 2380.98 5 5 5 GS-tw -92636.48 0.07 0.96 29.7 5 5 5 GS-clp -61024.52 0.09 0.968 29.7 5 5	3	GS- clp	-60433.8	0.095	0.968	30.2	5	5
4 DGS-clp -59788.2 0.08 0.97 1970.78 5 5 4 GS-tw -93889.54 0.06 0.96 29.3 5 5 4 GS-clp -60794.68 0.095 0.968 29.3 5 5 4 GS-pruned -61700.14 0.08 0.97 33.92 43 5 5 DGS -60381.59 0.09 0.97 2380.98 5 5 5 DGS-clp -59976.4 0.095 0.97 2380.98 5 5 5 GS-tw -92636.48 0.07 0.96 29.7 5 5 5 GS-clp -61024.52 0.09 0.968 29.7 5 5	3	GS-pruned	-61086.39	0.07	0.97	35.33	41	5
4 GS-tw -93889.54 0.06 0.96 29.3 5 5 4 GS-clp -60794.68 0.095 0.968 29.3 5 5 4 GS-pruned -61700.14 0.08 0.97 33.92 43 5 5 DGS -60381.59 0.09 0.97 2380.98 5 5 5 DGS-clp -59976.4 0.095 0.97 2380.98 5 5 5 GS-tw -92636.48 0.07 0.96 29.7 5 5 5 GS-clp -61024.52 0.09 0.968 29.7 5 5	4	DGS	-60096.82	0.09	0.97	1970.78	5	5
4 GS-clp -60794.68 0.095 0.968 29.3 5 5 4 GS-pruned -61700.14 0.08 0.97 33.92 43 5 5 DGS -60381.59 0.09 0.97 2380.98 5 5 5 DGS-clp -59976.4 0.095 0.97 2380.98 5 5 5 GS-tw -92636.48 0.07 0.96 29.7 5 5 5 GS-clp -61024.52 0.09 0.968 29.7 5 5	4	$\operatorname{DGS-clp}$	-59788.2	0.08	0.97	1970.78	5	5
4 GS-pruned -61700.14 0.08 0.97 33.92 43 5 5 DGS -60381.59 0.09 0.97 2380.98 5 5 5 DGS-clp -59976.4 0.095 0.97 2380.98 5 5 5 GS-tw -92636.48 0.07 0.96 29.7 5 5 5 GS-clp -61024.52 0.09 0.968 29.7 5 5	4	GS-tw	-93889.54	0.06	0.96	29.3	5	5
5 DGS -60381.59 0.09 0.97 2380.98 5 5 5 DGS-clp -59976.4 0.095 0.97 2380.98 5 5 5 GS-tw -92636.48 0.07 0.96 29.7 5 5 5 GS-clp -61024.52 0.09 0.968 29.7 5 5	4	GS- clp	-60794.68	0.095	0.968	29.3	5	5
5 DGS-clp -59976.4 0.095 0.97 2380.98 5 5 5 GS-tw -92636.48 0.07 0.96 29.7 5 5 5 GS-clp -61024.52 0.09 0.968 29.7 5 5	4	GS-pruned	-61700.14	0.08	0.97	33.92	43	5
5 GS-tw -92636.48 0.07 0.96 29.7 5 5 5 5 GS-clp -61024.52 0.09 0.968 29.7 5 5	5	DGS	-60381.59	0.09	0.97	2380.98	5	5
5 GS-clp -61024.52 0.09 0.968 29.7 5 5	5	$\operatorname{DGS-clp}$	-59976.4	0.095	0.97	2380.98	5	5
	5	GS-tw	-92636.48	0.07	0.96	29.7	5	5
5 GS-pruned -61922.54 0.08 0.97 33.61 40 5	5	GS- clp	-61024.52	0.09	0.968	29.7	5	5
	5	GS-pruned	-61922.54	0.08	0.97	33.61	40	5

Table 45: Comparison of the methods in dataset corel5k in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

D.11	Nf 41 1	CLI					
Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-12888.47	0	0.99	254.62	2	2
1	DGS- clp	-12862	0	0.99	254.62	2	2
1	GS-tw	-12982.03	0.007	0.99	98.5	2	2
1	GS- clp	-12937.48	0.007	0.99	98.5	2	2
1	GS-pruned	-12970.06	0	0.99	119.03	42	2
2	DGS	-12738.84	0.01	0.99	260.18	2	2
2	$\operatorname{DGS-clp}$	-12716.7	0.01	0.99	260.18	2	2
2	GS-tw	-12961.6	0.009	0.99	97.7	2	2
2	GS- clp	-12924.43	0.009	0.99	97.7	2	2
2	GS-pruned	-12934.12	0.01	0.99	119.27	58	2
3	DGS	-12852.12	0.01	0.99	241.69	2	2
3	$\operatorname{DGS-clp}$	-12834.5	0.01	0.99	241.69	2	2
3	GS-tw	-12899.4	0.014	0.99	100.1	2	2
3	GS- clp	-12869.72	0.014	0.99	100.1	2	2
3	GS-pruned	-12890.29	0.01	0.99	119.93	45	2
4	DGS	-13033.48	0	0.99	241.61	2	2
4	$\operatorname{DGS-clp}$	-13008.65	0	0.99	241.61	2	2
4	GS-tw	-13030.36	0.012	0.99	97.3	2	2
4	GS- clp	-12994	0.01	0.99	97.3	2	2
4	GS-pruned	-13014.81	0.01	0.99	120.77	40	2
5	DGS	-12910.67	0.02	0.99	253.19	2	2
5	$\operatorname{DGS-clp}$	-12882.5	0.02	0.991	253.19	2	2
5	GS-tw	-12972.62	0.02	0.99	98.7	2	2
5	GS- clp	-12936.61	0.02	0.99	98.7	2	2
5	GS-pruned	-12950.17	0.02	0.99	127.47	51	2

Table 46: Comparison of the methods in dataset corel5k in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	OT T					
	monioa	CLL	acc_G	acc_M	$_{ m time}$	tw	tw-pr
1	DGS	-12767.68	0	0.99	248.38	3	3
1	$\operatorname{DGS-clp}$	-12740.9	0	0.99	248.38	3	3
1	GS-tw	-12831.43	0.006	0.99	113.4	3	3
1	GS- clp	-12792.95	0.006	0.99	113.4	3	3
1	GS-pruned	-12837.21	0.006	0.99	124.83	44	3
2	DGS	-12697.59	0.01	0.99	262.58	3	3
2	DGS-clp	-12674.1	0.008	0.99	262.58	3	3
2	GS-tw	-12827.13	0.01	0.99	111.1	3	3
2	GS- clp	-12791.64	0.01	0.99	111.1	3	3
2	GS-pruned	-12832.62	0.008	0.99	133.28	52	3
3	DGS	-12738.77	0.01	0.99	249.18	3	3
3	DGS-clp	-12719.4	0.01	0.99	249.18	3	3
3	GS-tw	-12760.2	0.016	0.99	111.2	3	3
3	GS- clp	-12731.13	0.02	0.99	111.2	3	3
3	GS-pruned	-12795.29	0.01	0.99	128.75	51	3
4	DGS	-12979.8	0	0.99	254.93	3	3
4	DGS-clp	-12955.87	0	0.99	254.93	3	3
4	GS-tw	-12904.04	0.011	0.99	107.7	3	3
4	GS- clp	-12870.2	0.011	0.99	107.7	3	3
4	GS-pruned	-12934.33	0.011	0.99	127.05	48	3
5	DGS	-12803.18	0.021	0.99	263.84	3	3
5	DGS-clp	-12775.1	0.02	0.991	263.84	3	3
5	GS-tw	-12832.31	0.021	0.99	108.6	3	3
5	GS- clp	-12797.31	0.02	0.99	108.6	3	3
5	GS-pruned	-12817.6	0.02	0.99	124.77	55	3

Table 47: Comparison of the methods in dataset corel5k in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	$\overline{\mathrm{DGS}}$	-12721.19	0	0.99	271.93	4	4
1	$\operatorname{DGS-clp}$	-12693.1	0	0.99	271.93	4	4
1	GS-tw	-12800.96	0.01	0.99	113.8	4	4
1	GS- clp	-12760.81	0.01	0.99	113.8	4	4
1	GS-pruned	-12830.52	0.008	0.99	131.04	46	4
2	DGS	-12651.61	0.01	0.99	271.98	4	4
2	$\operatorname{DGS-clp}$	-12628.4	0.01	0.99	271.98	4	4
2	GS-tw	-12779.1	0.01	0.99	112.2	4	4
2	GS- clp	-12743.09	0.01	0.99	112.2	4	4
2	GS-pruned	-12778.24	0.01	0.99	130.39	56	4
3	DGS	-12652.39	0.01	0.99	275.77	4	4
3	$\operatorname{DGS-clp}$	-12635.2	0.01	0.99	275.77	4	4
3	GS-tw	-12674.03	0.016	0.99	113.3	4	4
3	GS- clp	-12646.15	0.02	0.99	113.3	4	4
3	GS-pruned	-12706.9	0.01	0.99	130.27	53	4
4	DGS	-12912.24	0	0.99	305.56	4	4
4	$\operatorname{DGS-clp}$	-12889.31	0	0.99	305.56	4	4
4	GS-tw	-12809.5	0.01	0.99	110.4	4	4
4	GS- clp	-12779.5	0.01	0.99	110.4	4	4
4	GS-pruned	-12836.54	0.011	0.99	128.42	47	4
5	DGS	-12750.36	0.02	0.99	304.35	4	4
5	$\operatorname{DGS-clp}$	-12721.7	0.02	0.99	304.35	4	4
5	GS-tw	-12793.31	0.022	0.99	109.5	4	4
5	GS-clp	-12759.07	0.02	0.99	109.5	4	4
5	GS-pruned	-12785.62	0.02	0.99	129	56	4

Table 48: Comparison of the methods in dataset corel5k in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-12728.1	0	0.99	305.44	5	5
1	DGS-clp	-12699.6	0	0.99	305.44	5	5
1	GS-tw	-12824.47	0.01	0.99	115.2	5	5
1	GS- clp	-12787.43	0.01	0.99	115.2	5	5
1	GS-pruned	-12832.04	0.008	0.99	139.98	51	5
2	DGS	-12635.71	0.01	0.99	322.18	5	5
2	$\operatorname{DGS-clp}$	-12613.1	0.01	0.99	322.18	5	5
2	GS-tw	-12774.04	0.01	0.99	114.4	5	5
2	GS- clp	-12737.61	0.01	0.99	114.4	5	5
2	GS-pruned	-12783.79	0.012	0.99	143.67	52	5
3	DGS	-12641.14	0.01	0.99	315.76	5	5
3	$\operatorname{DGS-clp}$	-12623.01	0.01	0.991	315.76	5	5
3	GS-tw	-12649.94	0.019	0.99	121	5	5
3	GS- clp	-12620.7	0.02	0.99	121	5	5
3	GS-pruned	-12685.71	0.01	0.99	145.14	47	5
4	DGS	-12875.75	0.01	0.99	304.58	5	5
4	$\operatorname{DGS-clp}$	-12852.74	0.01	0.99	304.58	5	5
4	GS-tw	-12806.13	0.01	0.99	123	5	5
4	$\operatorname{GS-clp}$	-12777.3	0.01	0.99	123	5	5
4	GS-pruned	-12835.98	0.011	0.99	143.36	44	5
5	DGS	-12706.61	0.02	0.99	292.79	5	5
5	$\operatorname{DGS-clp}$	-12677.9	0.02	0.991	292.79	5	5
5	GS-tw	-12803.46	0.02	0.99	121.2	5	5
5	GS- clp	-12765.85	0.02	0.99	121.2	5	5
5	GS-pruned	-12776.74	0.021	0.99	159.4	54	5

Table 49: Comparison of the methods in dataset $tmc2007_{-}500$ in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

		1					
Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-20250.13	0.26	0.93	612.09	2	2
1	$\operatorname{DGS-clp}$	-20063.4	0.265	0.93	612.09	2	2
1	GS-tw	-28030.39	0.24	0.93	55.7	2	2
1	GS- clp	-20628.18	0.25	0.935	55.7	2	2
1	GS-pruned	-21116.28	0.26	0.93	102.67	74	2
2	DGS	-20244.04	0.26	0.93	546.33	2	2
2	$\operatorname{DGS-clp}$	-20055.8	0.26	0.93	546.33	2	2
2	GS-tw	-27084.77	0.24	0.93	54	2	2
2	GS- clp	-21603.03	0.26	0.93	54	2	2
2	GS-pruned	-20496.28	0.266	0.935	101.32	62	2
3	DGS	-19863.35	0.26	0.94	591.37	2	2
3	$\operatorname{DGS-clp}$	-19587.1	0.26	0.94	591.37	2	2
3	GS-tw	-26223.62	0.25	0.93	54.5	2	2
3	GS- clp	-19811.79	0.271	0.94	54.5	2	2
3	GS-pruned	-20218.88	0.27	0.936	103.64	66	2
4	DGS	-20191.89	0.279	0.94	605.42	2	2
4	$\operatorname{DGS-clp}$	-19797.8	0.28	0.94	605.42	2	2
4	GS-tw	-28104.55	0.24	0.93	54.4	2	2
4	GS- clp	-20240.57	0.27	0.935	54.4	2	2
4	GS-pruned	-21134.37	0.26	0.93	101.45	62	2
5	DGS	-20167.57	0.26	0.93	593.13	2	2
5	$\operatorname{DGS-clp}$	-19950	0.266	0.934	593.13	2	2
5	GS-tw	-27389.33	0.22	0.93	54.5	2	2
5	GS- clp	-21832.16	0.22	0.93	54.5	2	2
5	GS-pruned	-20851.24	0.24	0.93	106.29	64	2

Table 50: Comparison of the methods in dataset tmc2007_500 in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G), the mean accuracy (acc_M), the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold Method CLL acc_G acc_M time tw tw- 1 DGS -19944.63 0.27 0.94 881.13 3 3 1 DGS-clp -19771 0.27 0.93 881.13 3 3 1 GS-tw -26100.14 0.24 0.93 75.1 3 3 1 GS-clp -20302.07 0.27 0.93 75.1 3 3 1 GS-pruned -20768.92 0.272 0.936 110.03 59 3 2 DGS -19857.24 0.28 0.93 840.87 3 3 2 DGS-clp -19683.9 0.28 0.94 840.87 3 3
1 DGS-clp -19771 0.27 0.93 881.13 3 1 GS-tw -26100.14 0.24 0.93 75.1 3 1 GS-clp -20302.07 0.27 0.93 75.1 3 1 GS-pruned -20768.92 0.272 0.936 110.03 59 3 2 DGS -19857.24 0.28 0.93 840.87 3 3
1 GS-tw -26100.14 0.24 0.93 75.1 3 3 1 GS-clp -20302.07 0.27 0.93 75.1 3 3 1 GS-pruned -20768.92 0.272 0.936 110.03 59 3 2 DGS -19857.24 0.28 0.93 840.87 3 3
1 GS-clp -20302.07 0.27 0.93 75.1 3 3 1 GS-pruned -20768.92 0.272 0.936 110.03 59 3 2 DGS -19857.24 0.28 0.93 840.87 3 3
1 GS-pruned -20768.92 0.272 0.936 110.03 59 3 2 DGS -19857.24 0.28 0.93 840.87 3
2 DGS -19857.24 0.28 0.93 840.87 3 3
2 DGS-clp -19683 9 0.28 0.94 840.87 3 3
2 Das ap 1900.9 0.20 0.91 010.01 0
2 GS-tw -25537.51 0.27 0.93 74.1 3 3
2 GS-clp -20127.96 0.29 0.94 74.1 3 3
2 GS-pruned -20455.26 0.293 0.938 112.16 54 3
3 DGS -19555.06 0.28 0.94 816.24 3 3
3 DGS-clp -19320.8 0.28 0.94 816.24 3 3
3 GS-tw -24578.89 0.26 0.93 74.3 3 3
3 GS-clp -21347.79 0.22 0.93 74.3 3
3 GS-pruned -20002.24 0.284 0.938 112.05 59 3
4 DGS -19865.92 0.286 0.94 838.1 3 3
4 DGS-clp -19471.1 0.29 0.94 838.1 3 3
4 GS-tw -26518.1 0.26 0.93 74.2 3 3
4 GS-clp -19626.01 0.286 0.937 74.2 3 3
4 GS-pruned -21013.55 0.27 0.94 109.68 56 3
5 DGS -19806.17 0.28 0.93 860.03 3 3
5 DGS-clp -19609.32 0.28 0.94 860.03 3 3
5 GS-tw -25099.09 0.25 0.93 76 3 3
5 GS-clp -19451.6 0.282 0.937 76 3 3
5 GS-pruned -20521.63 0.27 0.94 110.38 61 3

Table 51: Comparison of the methods in dataset $tmc2007_{-}500$ in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold Method CLL 1 DGS -19785.1	$ \begin{array}{cc} acc_G \\ 9 & 0.27 \end{array} $	$\frac{\mathrm{acc}_{M}}{0.93}$	time	tw	tw-pr
1 DGS -19785.1	9 0.27	0.03			
		0.95	1104.03	4	4
1 DGS-clp -19580 .	8 0.26	0.94	1104.03	4	4
1 GS-tw -24785.	8 0.25	0.93	87.9	4	4
1 GS-clp -20132.6	7 0.285	0.937	87.9	4	4
1 GS-pruned -21042.0	0.27	0.94	112.29	63	4
2 DGS -19804.4	4 0.28	0.94	1120.51	4	4
2 DGS-clp -19626	6 0.29	0.94	1120.51	4	4
2 GS-tw -24063.9	0.27	0.93	88.2	4	4
2 GS-clp -19979.2	22 0.295	0.938	88.2	4	4
2 GS-pruned -20619.8	36 0.29	0.94	112.54	51	4
3 DGS -19304.4	8 0.28	0.94	1080.47	4	4
3 DGS-clp -1904 5	0.28	0.94	1080.47	4	4
3 GS-tw -23033.7	78 0.28	0.94	89.1	4	4
3 GS-clp -19063.5	55 0.297	0.939	89.1	4	4
3 GS-pruned -20042.3	36 0.29	0.94	114.89	60	4
4 DGS -19613.7	78 0.286	0.94	1197.77	4	4
4 DGS-clp -19422	6 0.28	0.936	1197.77	4	4
4 GS-tw -24891.7	1 0.26	0.93	87.3	4	4
4 GS-clp -20134.3	32 0.28	0.94	87.3	4	4
4 GS-pruned -21046.3	0.28	0.94	111.19	62	4
5 DGS -19580.9	0.28	0.93	1156.26	4	4
5 DGS-clp -19388 .	2 0.28	0.94	1156.26	4	4
5 GS-tw -23842.4	9 0.26	0.93	88.7	4	4
5 GS-clp -20077.9	9 0.284	0.936	88.7	4	4
5 GS-pruned -20602.6	0.28	0.94	112.8	60	4

Table 52: Comparison of the methods in dataset tmc2007_500 in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G), the mean accuracy (acc_M), the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	$_{ m time}$	tw	tw-pr
1	DGS	-19691.57	0.27	0.93	1611.95	5	5
1	$\operatorname{DGS-clp}$	-19498.3	0.26	0.94	1611.95	5	5
1	GS-tw	-23431.19	0.27	0.93	95	5	5
1	GS- clp	-19586.56	0.282	0.937	95	5	5
1	GS-pruned	-20993.18	0.27	0.94	113.26	62	5
2	DGS	-19725.29	0.29	0.94	1488.23	5	5
2	$\operatorname{DGS-clp}$	-19549.15	0.29	0.94	1488.23	5	5
2	GS-tw	-23068.58	0.27	0.94	93.9	5	5
2	GS- clp	-19142.3	0.301	0.938	93.9	5	5
2	GS-pruned	-20984.62	0.27	0.94	111.53	50	5
3	DGS	-19323.68	0.28	0.94	1380.7	5	5
3	$\operatorname{DGS-clp}$	-19054.92	0.28	0.94	1380.7	5	5
3	GS-tw	-22342.69	0.28	0.94	95.8	5	5
3	GS- clp	-19052.7	0.293	0.94	95.8	5	5
3	GS-pruned	-20419.94	0.29	0.94	114.15	61	5
4	DGS	-19467.8	0.29	0.94	1699.84	5	5
4	$\operatorname{DGS-clp}$	-19140.63	0.29	0.94	1699.84	5	5
4	GS-tw	-23616.57	0.28	0.93	94.2	5	5
4	GS- clp	-19068.1	0.307	0.939	94.2	5	5
4	GS-pruned	-21111.88	0.29	0.94	112	53	5
5	DGS	-19647.84	0.28	0.93	1584.57	5	5
5	$\operatorname{DGS-clp}$	-19448.1	0.28	0.94	1584.57	5	5
5	GS-tw	-22894.14	0.27	0.93	96.9	5	5
5	GS- clp	-19252.1	0.288	0.938	96.9	5	5
5	GS-pruned	-20876.97	0.27	0.94	114.3	58	5

Table 53: Comparison of the methods in dataset bibtex in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	$\overline{\mathrm{DGS}}$	-10668.67	0.17	0.99	3195.46	2	2
1	$\operatorname{DGS-clp}$	-10622.9	0.166	0.99	3195.46	2	2
1	GS-tw	-13425.81	0.15	0.98	1298.6	2	2
1	$\operatorname{GS-clp}$	-10845.99	0.16	0.987	1298.6	2	2
1	GS-pruned	-11299.4	0.16	0.99	2227.37	157	2
2	DGS	-10821.1	0.16	0.99	3222.08	2	2
2	$\operatorname{DGS-clp}$	-10761.2	0.16	0.99	3222.08	2	2
2	GS-tw	-12858.09	0.16	0.99	1413.9	2	2
2	GS- clp	-10772.04	0.17	0.987	1413.9	2	2
2	GS-pruned	-11240.62	0.176	0.99	2222.64	157	2
3	DGS	-10702.02	0.16	0.99	3074.02	2	2
3	$\operatorname{DGS-clp}$	-10642.5	0.16	0.99	3074.02	2	2
3	GS-tw	-13169.12	0.15	0.99	1401.5	2	2
3	GS- clp	-10738.04	0.17	0.988	1401.5	2	2
3	GS-pruned	-11108.49	0.17	0.99	2112.64	168	2
4	DGS	-10542.38	0.16	0.99	3008.42	2	2
4	$\operatorname{DGS-clp}$	-10485.6	0.16	0.99	3008.42	2	2
4	GS-tw	-12769.65	0.17	0.99	1437.6	2	2
4	GS- clp	-10674.65	0.18	0.987	1437.6	2	2
4	GS-pruned	-10871.39	0.183	0.99	2108.82	170	2
5	DGS	-10668.06	0.15	0.99	2999.46	2	2
5	$\operatorname{DGS-clp}$	-10609.3	0.15	0.99	2999.46	2	2
5	GS-tw	-13374.59	0.14	0.98	1454	2	2
5	GS- clp	-10689.19	0.159	0.987	1454	2	2
5	GS-pruned	-11352.09	0.15	0.99	2165.53	173	2

Table 54: Comparison of the methods in dataset bibtex in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

		1					
Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	$\overline{\mathrm{DGS}}$	-10659.93	0.17	0.99	3603.34	3	3
1	$\operatorname{DGS-clp}$	-10610.8	0.16	0.99	3603.34	3	3
1	GS-tw	-13031.31	0.15	0.98	1659.8	3	3
1	GS- clp	-10691.18	0.16	0.987	1659.8	3	3
1	GS-pruned	-11090.35	0.17	0.99	2252.57	161	3
2	DGS	-10793.71	0.16	0.99	3558.33	3	3
2	$\operatorname{DGS-clp}$	-10738.01	0.16	0.99	3558.33	3	3
2	GS-tw	-12384.95	0.16	0.99	1695.3	3	3
2	GS- clp	-10524.3	0.17	0.987	1695.3	3	3
2	GS-pruned	-11093.07	0.181	0.99	2209.16	168	3
3	DGS	-10591.06	0.16	0.99	3458.82	3	3
3	$\operatorname{DGS-clp}$	-10534.01	0.16	0.99	3458.82	3	3
3	GS-tw	-12785.68	0.16	0.99	1612.8	3	3
3	GS- clp	-10455.9	0.17	0.988	1612.8	3	3
3	GS-pruned	-11098.76	0.169	0.99	2166	161	3
4	DGS	-10467.39	0.16	0.99	3404.01	3	3
4	$\operatorname{DGS-clp}$	-10407	0.16	0.99	3404.01	3	3
4	GS-tw	-12406.06	0.16	0.99	1730.5	3	3
4	GS- clp	-10573.98	0.18	0.987	1730.5	3	3
4	GS-pruned	-10869.41	0.184	0.99	2264.55	153	3
5	DGS	-10631.63	0.15	0.99	3331.59	3	3
5	$\operatorname{DGS-clp}$	-10568.99	0.15	0.99	3331.59	3	3
5	GS-tw	-12640.94	0.16	0.99	1724.1	3	3
5	GS- clp	-10345.3	0.169	0.987	1724.1	3	3
5	GS-pruned	-11343.91	0.16	0.99	2241.75	163	3

Table 55: Comparison of the methods in dataset bibtex in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	\mathbf{tw}	tw-pr
1	DGS	-10625.38	0.17	0.99	3984.99	4	4
1	$\operatorname{DGS-clp}$	-10576.58	0.16	0.99	3984.99	4	4
1	GS-tw	-12030.82	0.17	0.99	1795.5	4	4
1	GS- clp	-10475.5	0.17	0.987	1795.5	4	4
1	GS-pruned	-11163.7	0.17	0.99	2344.13	154	4
2	DGS	-10752.18	0.16	0.99	4087.34	4	4
2	$\operatorname{DGS-clp}$	-10696.34	0.16	0.99	4087.34	4	4
2	GS-tw	-11615.69	0.17	0.99	1913.5	4	4
2	GS- clp	-10466.4	0.18	0.987	1913.5	4	4
2	GS-pruned	-11044.28	0.185	0.99	2403.38	158	4
3	DGS	-10570.34	0.17	0.99	3782.72	4	4
3	$\operatorname{DGS-clp}$	-10511.02	0.17	0.99	3782.72	4	4
3	GS-tw	-11871.06	0.17	0.99	1873	4	4
3	GS- clp	-10475.6	0.17	0.988	1873	4	4
3	GS-pruned	-11112.76	0.17	0.99	2351.94	183	4
4	DGS	-10434.02	0.16	0.99	4062.21	4	4
4	$\operatorname{DGS-clp}$	-10374.54	0.16	0.99	4062.21	4	4
4	GS-tw	-11594.91	0.185	0.99	1863.2	4	4
4	$\operatorname{GS-clp}$	-10294.9	0.18	0.987	1863.2	4	4
4	GS-pruned	-10837.86	0.18	0.99	2199.8	153	4
5	DGS	-10567.59	0.16	0.99	3686.44	4	4
5	$\operatorname{DGS-clp}$	-10508.51	0.16	0.99	3686.44	4	4
5	GS-tw	-12038.81	0.171	0.99	1868.8	4	4
5	GS- clp	-10340.3	0.17	0.987	1868.8	4	4
5	GS-pruned	-11335.94	0.16	0.99	2360.88	171	4

Table 56: Comparison of the methods in dataset bibtex in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	DGS	-10599.53	0.17	0.99	4141.01	5	5
1	$\operatorname{DGS-clp}$	-10550.3	0.17	0.987	4141.01	5	5
1	GS-tw	-11909.28	0.17	0.99	1886.9	5	5
1	$\operatorname{GS-clp}$	-11807.36	0.172	0.99	1886.9	5	5
1	GS-pruned	-11179.94	0.17	0.99	2349.92	167	5
2	DGS	-10723.1	0.16	0.99	4085.36	5	4
2	$\operatorname{DGS-clp}$	-10667.7	0.16	0.99	4085.36	5	4
2	GS-tw	-11584.34	0.18	0.99	1910.9	5	5
2	GS- clp	-11503.89	0.17	0.99	1910.9	5	5
2	GS-pruned	-11029.72	0.182	0.987	2359.26	172	5
3	DGS	-10550.99	0.16	0.99	4087.37	5	5
3	$\operatorname{DGS-clp}$	-10491.7	0.16	0.987	4087.37	5	5
3	GS-tw	-11680.54	0.17	0.99	1979.9	5	5
3	GS- clp	-11589.85	0.168	0.99	1979.9	5	5
3	GS-pruned	-11107.63	0.17	0.99	2376.38	184	5
4	DGS	-10424.31	0.16	0.99	4211.13	5	5
4	$\operatorname{DGS-clp}$	-10364.3	0.16	0.987	4211.13	5	5
4	GS-tw	-11392.62	0.17	0.99	1936.3	5	5
4	GS- clp	-11299.44	0.17	0.99	1936.3	5	5
4	GS-pruned	-10837.48	0.185	0.99	2319.04	172	5
5	DGS	-10532.02	0.16	0.99	4130.05	5	4
5	$\operatorname{DGS-clp}$	-10473.5	0.16	0.987	4130.05	5	4
5	GS-tw	-11974.16	0.169	0.99	1995.7	5	5
5	GS- clp	-11868.68	0.17	0.99	1995.7	5	5
5	GS-pruned	-11437.38	0.16	0.99	2284.55	172	5

Table 57: Comparison of the methods in dataset imdb in 5-fold cross-validation, using a treewidth bound of 2. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

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Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1	$\overline{\mathrm{DGS}}$	-130004.63	0.11	0.93	1689.36	2	2
1	$\operatorname{DGS-clp}$	-129932.2	0.11	0.929	1689.36	2	2
1	GS-tw	-131700.79	0.09	0.93	383.9	2	2
1	$\operatorname{GS-clp}$	-131045.72	0.11	0.93	383.9	2	2
1	GS-pruned	-130185.53	0.118	0.93	824.91	147	2
2	DGS	-130559.47	0.11	0.93	1735.31	2	2
2	$\operatorname{DGS-clp}$	-130489.6	0.11	0.93	1735.31	2	2
2	GS-tw	-132110.88	0.11	0.93	394.8	2	2
2	$\operatorname{GS-clp}$	-131494.44	0.11	0.93	394.8	2	2
2	GS-pruned	-130732.96	0.118	0.928	803.65	133	2
3	DGS	-129531.21	0.06	0.93	1873.71	2	2
3	$\operatorname{DGS-clp}$	-129467.9	0.11	0.93	1873.71	2	2
3	GS-tw	-131500.83	0.08	0.93	390.9	2	2
3	GS- clp	-130803.19	0.11	0.93	390.9	2	2
3	GS-pruned	-129653.49	0.118	0.929	820.19	144	2
4	DGS	-130982.75	0.11	0.93	1841.36	2	2
4	DGS-clp	-130907.2	0.11	0.928	1841.36	2	2
4	GS-tw	-133351.94	0.09	0.93	399	2	2
4	GS- clp	-132525.99	0.11	0.93	399	2	2
4	GS-pruned	-131302.48	0.109	0.93	846.24	152	2
5	DGS	-130113.36	0.11	0.93	1703.97	2	2
5	DGS-clp	-130063.6	0.1	0.929	1703.97	2	2
5	GS-tw	-132272.68	0.08	0.93	396.3	2	2
5	GS- clp	-131524.7	0.11	0.93	396.3	2	2
5	GS-pruned	-130542.74	0.114	0.93	833.14	141	2

Table 58: Comparison of the methods in dataset imdb in 5-fold cross-validation, using a treewidth bound of 3. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Folid Method CLL acc _G acc _M time tw tw-pr 1 DGS -127954.11 0.11 0.93 2434.01 3 3 1 DGS-clp -128290.35 0.12 0.93 535.4 3 3 1 GS-clp -127971.75 0.117 0.93 535.4 3 3 1 GS-pruned -128035.66 0.12 0.929 848.91 160 3 2 DGS -128517.17 0.12 0.93 2101.35 3 3 2 DGS-clp -128444.5 0.12 0.93 2101.35 3 3 2 DGS-clp -128444.5 0.12 0.93 252.8 3 3 2 GS-tw -128794.85 0.12 0.93 552.8 3 3 3 DGS -128475.51 0.12 0.93 552.8 3 3 3 DGS -126861.1			ı					
1 DGS-clp -127868.8 0.11 0.93 2434.01 3 3 1 GS-tw -128290.35 0.12 0.93 535.4 3 3 1 GS-clp -127971.75 0.117 0.93 535.4 3 3 1 GS-pruned -128035.66 0.12 0.929 848.91 160 3 2 DGS -128517.17 0.12 0.93 2101.35 3 3 2 DGS-clp -128444.5 0.12 0.93 2101.35 3 3 2 GS-tw -128794.85 0.12 0.93 552.8 3 3 2 GS-clp -128477.51 0.12 0.93 552.8 3 3 2 GS-pruned -128606.61 0.12 0.93 552.8 3 3 3 DGS -126950.48 0.12 0.93 564.8 3 3 3 GS-clp -126871.1 0.12 0.93 564.8 3 3 3 GS-tw	Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1 GS-tw -128290.35 0.12 0.93 535.4 3 3 1 GS-clp -127971.75 0.117 0.93 535.4 3 3 1 GS-pruned -128035.66 0.12 0.929 848.91 160 3 2 DGS -128517.17 0.12 0.93 2101.35 3 3 2 DGS-clp -128444.5 0.12 0.93 2101.35 3 3 2 GS-tw -128794.85 0.12 0.93 552.8 3 3 2 GS-clp -128477.51 0.12 0.93 552.8 3 3 2 GS-pruned -128606.61 0.12 0.93 552.8 3 3 3 DGS -128606.61 0.12 0.93 552.8 3 3 3 DGS-clp -126871.1 0.12 0.93 2435.7 3 3 3 GS-clp -127113.91 0.12 0.93 564.8 3 3 3 GS-pruned	1	DGS	-127954.11	0.11	0.93	2434.01	3	3
1 GS-clp -127971.75 0.117 0.93 535.4 3 3 1 GS-pruned -128035.66 0.12 0.929 848.91 160 3 2 DGS -128517.17 0.12 0.93 2101.35 3 3 2 DGS-clp -128444.5 0.12 0.93 552.8 3 3 2 GS-tw -128794.85 0.12 0.93 552.8 3 3 2 GS-pruned -128606.61 0.12 0.93 552.8 3 3 2 GS-pruned -128606.61 0.12 0.93 552.8 3 3 3 DGS -128606.61 0.12 0.93 552.8 3 3 3 DGS -126950.48 0.12 0.93 52435.7 3 3 3 DGS-clp -126871.1 0.12 0.93 564.8 3 3 3 GS-pruned -127113.91	1	$\operatorname{DGS-clp}$	-127868.8	0.11	0.93	2434.01	3	3
1 GS-pruned -128035.66 0.12 0.929 848.91 160 3 2 DGS -128517.17 0.12 0.93 2101.35 3 3 2 DGS-clp -128444.5 0.12 0.928 2101.35 3 3 2 GS-tw -128794.85 0.12 0.93 552.8 3 3 2 GS-pruned -128477.51 0.12 0.93 552.8 3 3 2 GS-pruned -128606.61 0.123 0.93 552.8 3 3 3 DGS -126950.48 0.12 0.93 552.8 3 3 3 DGS -126950.48 0.12 0.93 552.8 3 3 3 DGS-clp -126950.48 0.12 0.93 564.8 3 3 3 GS-tw -127440.46 0.12 0.93 564.8 3 3 3 GS-pruned -128693.12	1	GS-tw	-128290.35	0.12	0.93	535.4	3	3
2 DGS -128517.17 0.12 0.93 2101.35 3 3 2 DGS-clp -128444.5 0.12 0.928 2101.35 3 3 2 GS-tw -128794.85 0.12 0.93 552.8 3 3 2 GS-clp -128477.51 0.12 0.93 552.8 3 3 2 GS-pruned -128606.61 0.123 0.93 552.8 3 3 3 DGS -126950.48 0.12 0.93 552.8 3 3 3 DGS -126950.48 0.12 0.93 552.8 3 3 3 DGS-clp -126950.48 0.12 0.93 2435.7 3 3 3 DGS-clp -127440.46 0.12 0.93 564.8 3 3 3 GS-pruned -127059.64 0.126 0.93 832.76 134 3 4 DGS-clp -128623.5	1	GS- clp	-127971.75	0.117	0.93	535.4	3	3
2 DGS-clp -128444.5 0.12 0.928 2101.35 3 2 GS-tw -128794.85 0.12 0.93 552.8 3 3 2 GS-clp -128477.51 0.12 0.93 552.8 3 3 2 GS-pruned -128606.61 0.123 0.93 812.61 128 3 3 DGS -126950.48 0.12 0.93 2435.7 3 3 3 DGS-clp -126871.1 0.12 0.929 2435.7 3 3 3 GS-tw -127440.46 0.12 0.93 564.8 3 3 3 GS-pruned -127113.91 0.12 0.93 564.8 3 3 3 GS-pruned -127059.64 0.126 0.93 832.76 134 3 4 DGS -128693.12 0.11 0.93 2312.82 3 3 4 GS-clp -128623.5 0.11 0.928 2312.82 3 3 4 GS-pruned -1	1	GS-pruned	-128035.66	0.12	0.929	848.91	160	3
2 GS-tw -128794.85 0.12 0.93 552.8 3 3 2 GS-clp -128477.51 0.12 0.93 552.8 3 3 2 GS-pruned -128606.61 0.123 0.93 812.61 128 3 3 DGS -126950.48 0.12 0.93 2435.7 3 3 3 DGS-clp -126871.1 0.12 0.929 2435.7 3 3 3 GS-tw -127440.46 0.12 0.93 564.8 3 3 3 GS-pruned -127113.91 0.12 0.93 564.8 3 3 3 GS-pruned -127059.64 0.126 0.93 832.76 134 3 4 DGS -128693.12 0.11 0.93 2312.82 3 3 4 DGS-clp -128623.5 0.11 0.928 2312.82 3 3 4 GS-tw -128915.3 0.111 0.93 531.4 3 3 4 GS-pruned <td>2</td> <td>DGS</td> <td>-128517.17</td> <td>0.12</td> <td>0.93</td> <td>2101.35</td> <td>3</td> <td>3</td>	2	DGS	-128517.17	0.12	0.93	2101.35	3	3
2 GS-clp -128477.51 0.12 0.93 552.8 3 3 2 GS-pruned -128606.61 0.123 0.93 812.61 128 3 3 DGS -126950.48 0.12 0.93 2435.7 3 3 3 DGS-clp -126871.1 0.12 0.929 2435.7 3 3 3 GS-tw -127440.46 0.12 0.93 564.8 3 3 3 GS-clp -127113.91 0.12 0.93 564.8 3 3 3 GS-pruned -127059.64 0.126 0.93 832.76 134 3 4 DGS -128693.12 0.11 0.93 2312.82 3 3 4 DGS-clp -128623.5 0.11 0.928 2312.82 3 3 4 GS-tw -129254.32 0.11 0.93 531.4 3 3 4 GS-pruned -128915.3 0.111 0.93 531.4 3 3 5 DGS	2	$\operatorname{DGS-clp}$	-128444.5	0.12	0.928	2101.35	3	3
2 GS-pruned -128606.61 0.123 0.93 812.61 128 3 3 DGS -126950.48 0.12 0.93 2435.7 3 3 3 DGS-clp -126871.1 0.12 0.929 2435.7 3 3 3 GS-tw -127440.46 0.12 0.93 564.8 3 3 3 GS-clp -127113.91 0.12 0.93 564.8 3 3 3 GS-pruned -127059.64 0.126 0.93 832.76 134 3 4 DGS -128693.12 0.11 0.93 2312.82 3 3 4 GS-clp -128623.5 0.11 0.928 2312.82 3 3 4 GS-tw -128954.32 0.11 0.93 531.4 3 3 4 GS-clp -128915.3 0.111 0.93 531.4 3 3 4 GS-pruned -128954.35 0.11 0.93 860.87 154 3 <td< td=""><td>2</td><td>GS-tw</td><td>-128794.85</td><td>0.12</td><td>0.93</td><td>552.8</td><td>3</td><td>3</td></td<>	2	GS-tw	-128794.85	0.12	0.93	552.8	3	3
3 DGS -126950.48 0.12 0.93 2435.7 3 3 3 DGS-clp -126871.1 0.12 0.929 2435.7 3 3 3 GS-tw -127440.46 0.12 0.93 564.8 3 3 3 GS-clp -127113.91 0.12 0.93 564.8 3 3 3 GS-pruned -127059.64 0.126 0.93 832.76 134 3 4 DGS -128693.12 0.11 0.93 2312.82 3 3 4 DGS-clp -128623.5 0.11 0.928 2312.82 3 3 4 GS-tw -128623.5 0.11 0.93 531.4 3 3 4 GS-tw -128915.3 0.11 0.93 531.4 3 3 4 GS-pruned -128954.35 0.11 0.93 860.87 154 3 5 DGS -128273.41	2	$\operatorname{GS-clp}$	-128477.51	0.12	0.93	552.8	3	3
3 DGS-clp -126871.1 0.12 0.929 2435.7 3 3 3 GS-tw -127440.46 0.12 0.93 564.8 3 3 3 GS-clp -127113.91 0.12 0.93 564.8 3 3 3 GS-pruned -127059.64 0.126 0.93 832.76 134 3 4 DGS -128693.12 0.11 0.93 2312.82 3 3 4 DGS-clp -128623.5 0.11 0.928 2312.82 3 3 4 GS-tw -129254.32 0.11 0.93 531.4 3 3 4 GS-clp -128915.3 0.111 0.93 531.4 3 3 4 GS-pruned -128954.35 0.11 0.93 860.87 154 3 5 DGS -128273.41 0.11 0.93 2177.14 3 3 5 DGS-clp -128661.81 0.11 0.93 534.7 3 3 5 GS-clp	2	GS-pruned	-128606.61	0.123	0.93	812.61	128	3
3 GS-tw -127440.46 0.12 0.93 564.8 3 3 3 GS-clp -127113.91 0.12 0.93 564.8 3 3 3 GS-pruned -127059.64 0.126 0.93 832.76 134 3 4 DGS -128693.12 0.11 0.93 2312.82 3 3 4 DGS-clp -128623.5 0.11 0.928 2312.82 3 3 4 GS-tw -129254.32 0.11 0.93 531.4 3 3 4 GS-clp -128915.3 0.111 0.93 531.4 3 3 4 GS-pruned -128954.35 0.11 0.93 531.4 3 3 5 DGS -128273.41 0.11 0.93 2177.14 3 3 5 DGS-clp -128205.7 0.11 0.929 2177.14 3 3 5 GS-tw -128661.81 0.11 0.93 534.7 3 3 5 GS-clp	3	DGS	-126950.48	0.12	0.93	2435.7	3	3
3 GS-clp -127113.91 0.12 0.93 564.8 3 3 3 GS-pruned -127059.64 0.126 0.93 832.76 134 3 4 DGS -128693.12 0.11 0.93 2312.82 3 3 4 DGS-clp -128623.5 0.11 0.928 2312.82 3 3 4 GS-tw -129254.32 0.11 0.93 531.4 3 3 4 GS-clp -128915.3 0.111 0.93 531.4 3 3 4 GS-pruned -128954.35 0.11 0.93 860.87 154 3 5 DGS -128273.41 0.11 0.93 2177.14 3 3 5 DGS-clp -128205.7 0.11 0.929 2177.14 3 3 5 GS-tw -128661.81 0.11 0.93 534.7 3 3 5 GS-clp -128353.72 0.11 0.93 534.7 3 3	3	$\operatorname{DGS-clp}$	-126871.1	0.12	0.929	2435.7	3	3
3 GS-pruned -127059.64 0.126 0.93 832.76 134 3 4 DGS -128693.12 0.11 0.93 2312.82 3 3 4 DGS-clp -128623.5 0.11 0.928 2312.82 3 3 4 GS-tw -129254.32 0.11 0.93 531.4 3 3 4 GS-clp -128915.3 0.111 0.93 531.4 3 3 4 GS-pruned -128954.35 0.11 0.93 860.87 154 3 5 DGS -128273.41 0.11 0.93 2177.14 3 3 5 DGS-clp -128205.7 0.11 0.929 2177.14 3 3 5 GS-tw -128661.81 0.11 0.93 534.7 3 3 5 GS-clp -128353.72 0.11 0.93 534.7 3 3	3	GS-tw	-127440.46	0.12	0.93	564.8	3	3
4 DGS -128693.12 0.11 0.93 2312.82 3 3 4 DGS-clp -128623.5 0.11 0.928 2312.82 3 3 4 GS-tw -129254.32 0.11 0.93 531.4 3 3 4 GS-clp -128915.3 0.11 0.93 531.4 3 3 4 GS-pruned -128954.35 0.11 0.93 860.87 154 3 5 DGS -128273.41 0.11 0.93 2177.14 3 3 5 DGS-clp -128205.7 0.11 0.929 2177.14 3 3 5 GS-tw -128661.81 0.11 0.93 534.7 3 3 5 GS-clp -128353.72 0.11 0.93 534.7 3 3	3	GS- clp	-127113.91	0.12	0.93	564.8	3	3
4 DGS-clp -128623.5 0.11 0.928 2312.82 3 3 4 GS-tw -129254.32 0.11 0.93 531.4 3 3 4 GS-clp -128915.3 0.111 0.93 531.4 3 3 4 GS-pruned -128954.35 0.11 0.93 860.87 154 3 5 DGS -128273.41 0.11 0.93 2177.14 3 3 5 DGS-clp -128205.7 0.11 0.929 2177.14 3 3 5 GS-tw -128661.81 0.11 0.93 534.7 3 3 5 GS-clp -128353.72 0.11 0.93 534.7 3 3	3	GS-pruned	-127059.64	0.126	0.93	832.76	134	3
4 GS-tw -129254.32 0.11 0.93 531.4 3 3 4 GS-clp -128915.3 0.111 0.93 531.4 3 3 4 GS-pruned -128954.35 0.11 0.93 860.87 154 3 5 DGS -128273.41 0.11 0.93 2177.14 3 3 5 DGS-clp -128205.7 0.11 0.929 2177.14 3 3 5 GS-tw -128661.81 0.11 0.93 534.7 3 3 5 GS-clp -128353.72 0.11 0.93 534.7 3 3	4	DGS	-128693.12	0.11	0.93	2312.82	3	3
4 GS-clp -128915.3 0.111 0.93 531.4 3 4 GS-pruned -128954.35 0.11 0.93 860.87 154 3 5 DGS -128273.41 0.11 0.93 2177.14 3 3 5 DGS-clp - 128205.7 0.11 0.929 2177.14 3 3 5 GS-tw -128661.81 0.11 0.93 534.7 3 3 5 GS-clp -128353.72 0.11 0.93 534.7 3 3	4	$\operatorname{DGS-clp}$	-128623.5	0.11	0.928	2312.82	3	3
4 GS-pruned -128954.35 0.11 0.93 860.87 154 3 5 DGS -128273.41 0.11 0.93 2177.14 3 3 5 DGS-clp -128205.7 0.11 0.929 2177.14 3 3 5 GS-tw -128661.81 0.11 0.93 534.7 3 3 5 GS-clp -128353.72 0.11 0.93 534.7 3 3	4	GS-tw	-129254.32	0.11	0.93	531.4	3	3
5 DGS -128273.41 0.11 0.93 2177.14 3 3 5 DGS-clp -128205.7 0.11 0.929 2177.14 3 3 5 GS-tw -128661.81 0.11 0.93 534.7 3 3 5 GS-clp -128353.72 0.11 0.93 534.7 3 3	4	GS- clp	-128915.3	0.111	0.93	531.4	3	3
5 DGS-clp -128205.7 0.11 0.929 2177.14 3 3 5 GS-tw -128661.81 0.11 0.93 534.7 3 3 5 GS-clp -128353.72 0.11 0.93 534.7 3 3	4	GS-pruned	-128954.35	0.11	0.93	860.87	154	3
5 GS-tw -128661.81 0.11 0.93 534.7 3 3 5 GS-clp -128353.72 0.11 0.93 534.7 3 3	5	DGS	-128273.41	0.11	0.93	2177.14	3	3
5 GS-clp -128353.72 0.11 0.93 534.7 3 3	5	$\operatorname{DGS-clp}$	-128205.7	0.11	0.929	2177.14	3	3
	5	GS-tw	-128661.81	0.11	0.93	534.7	3	3
5 GS-pruned -128508.74 0.117 0.93 840.93 137 3	5	GS- clp	-128353.72	0.11	0.93	534.7	3	3
	5	GS-pruned	-128508.74	0.117	0.93	840.93	137	3

Table 59: Comparison of the methods in dataset imdb in 5-fold cross-validation, using a treewidth bound of 4. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Folid Method CLL acc _G acc _M time tw tw-pr 1 DGS -126593.67 0.12 0.93 2971.53 4 4 1 DGS-clp -126695.81 0.12 0.93 2971.53 4 4 1 GS-tw -126695.81 0.12 0.93 591.2 4 4 1 GS-clp -126443.4 0.12 0.929 846.6 139 4 2 DGS -127786.02 0.12 0.93 2741.12 4 4 2 DGS-clp -127781.78 0.12 0.93 591.4 4 4 2 DGS-clp -127781.78 0.12 0.93 591.4 4 4 2 GS-tw -127781.78 0.12 0.93 591.4 4 4 2 GS-ptuned -127786.67 0.12 0.93 591.4 4 4 3 DGS -127585.5								
1 DGS-clp -126478.99 0.125 0.93 2971.53 4 4 1 GS-tw -126695.81 0.12 0.93 591.2 4 4 1 GS-clp -126443.4 0.12 0.93 591.2 4 4 1 GS-pruned -126716.17 0.12 0.929 846.6 139 4 2 DGS -127786.02 0.12 0.93 2741.12 4 4 2 DGS-clp -127719.93 0.12 0.93 2741.12 4 4 2 GS-tw -127781.78 0.12 0.93 591.4 4 4 2 GS-clp -127566.5 0.122 0.93 591.4 4 4 2 GS-pruned -127660.67 0.12 0.93 816.94 142 4 3 DGS -125785.55 0.12 0.93 2822.44 4 4 3 GS-clp -125698 0.12 0.93 605.3 4 4 3 GS-tw <	Fold	Method	CLL	acc_G	acc_M	time	tw	tw-pr
1 GS-tw -126695.81 0.12 0.93 591.2 4 4 1 GS-clp -126443.4 0.12 0.93 591.2 4 4 1 GS-pruned -126716.17 0.12 0.929 846.6 139 4 2 DGS -127786.02 0.12 0.93 2741.12 4 4 2 DGS-clp -127719.93 0.12 0.928 2741.12 4 4 2 GS-tw -127781.78 0.12 0.93 591.4 4 4 2 GS-clp -127566.5 0.122 0.93 591.4 4 4 2 GS-pruned -127860.67 0.12 0.93 591.4 4 4 3 DGS -127860.67 0.12 0.93 591.4 4 4 3 DGS-clp -125698 0.12 0.93 816.94 142 4 3 DGS-clp -126046.37 0.12 0.93 605.3 4 4 3 GS-pruned	1	$\overline{\mathrm{DGS}}$	-126593.67	0.12	0.93	2971.53	4	4
1 GS-clp -126443.4 0.12 0.93 591.2 4 4 1 GS-pruned -126716.17 0.12 0.929 846.6 139 4 2 DGS -127786.02 0.12 0.93 2741.12 4 4 2 DGS-clp -127719.93 0.12 0.928 2741.12 4 4 2 GS-tw -127781.78 0.12 0.93 591.4 4 4 2 GS-clp -127566.5 0.122 0.93 591.4 4 4 2 GS-pruned -127860.67 0.12 0.93 591.4 4 4 3 DGS -125785.55 0.12 0.93 591.4 4 4 3 DGS-clp -125698 0.12 0.93 582.44 4 4 3 GS-clp -126046.37 0.12 0.93 605.3 4 4 3 GS-clp -125840.88 0.12 0.93 848.1 147 4 4 DGS -1	1	$\operatorname{DGS-clp}$	-126478.99	0.125	0.93	2971.53	4	4
1 GS-pruned -126716.17 0.12 0.929 846.6 139 4 2 DGS -127786.02 0.12 0.93 2741.12 4 4 2 DGS-clp -127719.93 0.12 0.938 2741.12 4 4 2 GS-tw -127781.78 0.12 0.93 591.4 4 4 2 GS-clp -127566.5 0.122 0.93 591.4 4 4 2 GS-pruned -127860.67 0.12 0.93 591.4 4 4 3 DGS -125785.55 0.12 0.93 816.94 142 4 3 DGS-clp -125698 0.12 0.93 2822.44 4 4 3 GS-tw -126046.37 0.12 0.93 605.3 4 4 3 GS-pruned -125959.52 0.12 0.93 848.1 147 4 4 DGS -127045.18	1	GS-tw	-126695.81	0.12	0.93	591.2	4	4
DGS	1	GS- clp	-126443.4	0.12	0.93	591.2	4	4
2 DGS-clp -127719.93 0.12 0.928 2741.12 4 4 2 GS-tw -127781.78 0.12 0.93 591.4 4 4 2 GS-clp -127566.5 0.122 0.93 591.4 4 4 2 GS-pruned -127860.67 0.12 0.93 816.94 142 4 3 DGS -125785.55 0.12 0.93 2822.44 4 4 3 DGS-clp -125698 0.123 0.929 2822.44 4 4 3 GS-tw -126046.37 0.12 0.93 605.3 4 4 3 GS-clp -125840.88 0.12 0.93 605.3 4 4 3 GS-pruned -125959.52 0.12 0.93 848.1 147 4 4 DGS -127045.18 0.11 0.93 3059.47 4 4 4 DGS-clp -126950.3 0.12 0.93 606.5 4 4 4 GS-tw	1	GS-pruned	-126716.17	0.12	0.929	846.6	139	4
2 GS-tw -127781.78 0.12 0.93 591.4 4 4 2 GS-clp -127566.5 0.122 0.93 591.4 4 4 2 GS-pruned -127860.67 0.12 0.93 816.94 142 4 3 DGS -125785.55 0.12 0.93 2822.44 4 4 3 DGS-clp -125698 0.123 0.929 2822.44 4 4 3 GS-tw -126046.37 0.12 0.93 605.3 4 4 3 GS-clp -125840.88 0.12 0.93 605.3 4 4 3 GS-pruned -125959.52 0.12 0.93 848.1 147 4 4 DGS -127045.18 0.11 0.93 3059.47 4 4 4 GS-tw -126950.3 0.12 0.928 3059.47 4 4 4 GS-tw -127299.75 0.118 0.93 606.5 4 4 4 GS-pruned	2	DGS	-127786.02	0.12	0.93	2741.12	4	4
2 GS-clp -127566.5 0.122 0.93 591.4 4 4 2 GS-pruned -127860.67 0.12 0.93 816.94 142 4 3 DGS -125785.55 0.12 0.93 2822.44 4 4 3 DGS-clp -125698 0.123 0.929 2822.44 4 4 3 GS-tw -126046.37 0.12 0.93 605.3 4 4 3 GS-clp -125840.88 0.12 0.93 605.3 4 4 3 GS-pruned -125959.52 0.12 0.93 848.1 147 4 4 DGS -127045.18 0.11 0.93 3059.47 4 4 4 DGS-clp -126950.3 0.12 0.928 3059.47 4 4 4 GS-tw -127299.75 0.118 0.93 606.5 4 4 4 GS-pruned -127236.8 0.12 0.93 859.36 137 4 5 DGS	2	$\operatorname{DGS-clp}$	-127719.93	0.12	0.928	2741.12	4	4
2 GS-pruned -127860.67 0.12 0.93 816.94 142 4 3 DGS -125785.55 0.12 0.93 2822.44 4 4 3 DGS-clp -125698 0.123 0.929 2822.44 4 4 3 GS-tw -126046.37 0.12 0.93 605.3 4 4 3 GS-clp -125840.88 0.12 0.93 605.3 4 4 3 GS-pruned -125959.52 0.12 0.93 605.3 4 4 4 DGS -127045.18 0.11 0.93 848.1 147 4 4 DGS-clp -126950.3 0.12 0.93 3059.47 4 4 4 GS-tw -127299.75 0.118 0.93 606.5 4 4 4 GS-clp -126987.52 0.12 0.93 859.36 137 4 5 DGS -127021.17 0.12 0.93 2857.09 4 4 5 GS-tw	2	GS-tw	-127781.78	0.12	0.93	591.4	4	4
3 DGS -125785.55 0.12 0.93 2822.44 4 4 3 DGS-clp -125698 0.123 0.929 2822.44 4 4 3 GS-tw -126046.37 0.12 0.93 605.3 4 4 3 GS-clp -125840.88 0.12 0.93 605.3 4 4 3 GS-pruned -125959.52 0.12 0.93 848.1 147 4 4 DGS -127045.18 0.11 0.93 3059.47 4 4 4 DGS-clp -126950.3 0.12 0.928 3059.47 4 4 4 GS-tw -127299.75 0.118 0.93 606.5 4 4 4 GS-clp -126987.52 0.12 0.93 606.5 4 4 5 DGS -127021.17 0.12 0.93 859.36 137 4 5 DGS-clp -126944.3	2	$\operatorname{GS-clp}$	-127566.5	0.122	0.93	591.4	4	4
3 DGS-clp -125698 0.123 0.929 2822.44 4 4 3 GS-tw -126046.37 0.12 0.93 605.3 4 4 3 GS-clp -125840.88 0.12 0.93 605.3 4 4 3 GS-pruned -125959.52 0.12 0.93 848.1 147 4 4 DGS -127045.18 0.11 0.93 3059.47 4 4 4 DGS-clp -126950.3 0.12 0.928 3059.47 4 4 4 GS-tw -127299.75 0.118 0.93 606.5 4 4 4 GS-clp -126987.52 0.12 0.93 859.36 137 4 5 DGS -127021.17 0.12 0.93 2857.09 4 4 5 DGS-clp -126944.3 0.118 0.929 2857.09 4 4 5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp	2	GS-pruned	-127860.67	0.12	0.93	816.94	142	4
3 GS-tw -126046.37 0.12 0.93 605.3 4 4 3 GS-clp -125840.88 0.12 0.93 605.3 4 4 3 GS-pruned -125959.52 0.12 0.93 848.1 147 4 4 DGS -127045.18 0.11 0.93 3059.47 4 4 4 DGS-clp -126950.3 0.12 0.928 3059.47 4 4 4 GS-tw -127299.75 0.118 0.93 606.5 4 4 4 GS-clp -126987.52 0.12 0.93 606.5 4 4 4 GS-pruned -127236.8 0.12 0.93 859.36 137 4 5 DGS -127021.17 0.12 0.93 2857.09 4 4 5 GS-clp -126944.3 0.118 0.929 2857.09 4 4 5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp	3	DGS	-125785.55	0.12	0.93	2822.44	4	4
3 GS-clp -125840.88 0.12 0.93 605.3 4 4 3 GS-pruned -125959.52 0.12 0.93 848.1 147 4 4 DGS -127045.18 0.11 0.93 3059.47 4 4 4 DGS-clp -126950.3 0.12 0.928 3059.47 4 4 4 GS-tw -127299.75 0.118 0.93 606.5 4 4 4 GS-clp -126987.52 0.12 0.93 606.5 4 4 4 GS-pruned -127236.8 0.12 0.93 859.36 137 4 5 DGS -127021.17 0.12 0.93 2857.09 4 4 5 DGS-clp -126944.3 0.118 0.929 2857.09 4 4 5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp -127125.43 0.12 0.93 598.7 4 4	3	$\operatorname{DGS-clp}$	-125698	0.123	0.929	2822.44	4	4
3 GS-pruned -125959.52 0.12 0.93 848.1 147 4 4 DGS -127045.18 0.11 0.93 3059.47 4 4 4 DGS-clp -126950.3 0.12 0.928 3059.47 4 4 4 GS-tw -127299.75 0.118 0.93 606.5 4 4 4 GS-clp -126987.52 0.12 0.93 606.5 4 4 4 GS-pruned -127236.8 0.12 0.93 859.36 137 4 5 DGS -127021.17 0.12 0.93 2857.09 4 4 5 DGS-clp -126944.3 0.118 0.929 2857.09 4 4 5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp -127125.43 0.12 0.93 598.7 4 4	3	GS-tw	-126046.37	0.12	0.93	605.3	4	4
4 DGS -127045.18 0.11 0.93 3059.47 4 4 4 DGS-clp -126950.3 0.12 0.928 3059.47 4 4 4 GS-tw -127299.75 0.118 0.93 606.5 4 4 4 GS-clp -126987.52 0.12 0.93 606.5 4 4 4 GS-pruned -127236.8 0.12 0.93 859.36 137 4 5 DGS -127021.17 0.12 0.93 2857.09 4 4 5 DGS-clp -126944.3 0.118 0.929 2857.09 4 4 5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp -127125.43 0.12 0.93 598.7 4 4	3	GS- clp	-125840.88	0.12	0.93	605.3	4	4
4 DGS-clp -126950.3 0.12 0.928 3059.47 4 4 4 GS-tw -127299.75 0.118 0.93 606.5 4 4 4 GS-clp -126987.52 0.12 0.93 606.5 4 4 4 GS-pruned -127236.8 0.12 0.93 859.36 137 4 5 DGS -127021.17 0.12 0.93 2857.09 4 4 5 DGS-clp -126944.3 0.118 0.929 2857.09 4 4 5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp -127125.43 0.12 0.93 598.7 4 4	3	GS-pruned	-125959.52	0.12	0.93	848.1	147	4
4 GS-tw -127299.75 0.118 0.93 606.5 4 4 4 GS-clp -126987.52 0.12 0.93 606.5 4 4 4 GS-pruned -127236.8 0.12 0.93 859.36 137 4 5 DGS -127021.17 0.12 0.93 2857.09 4 4 5 DGS-clp -126944.3 0.118 0.929 2857.09 4 4 5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp -127125.43 0.12 0.93 598.7 4 4	4	DGS	-127045.18	0.11	0.93	3059.47	4	4
4 GS-clp -126987.52 0.12 0.93 606.5 4 4 4 GS-pruned -127236.8 0.12 0.93 859.36 137 4 5 DGS -127021.17 0.12 0.93 2857.09 4 4 5 DGS-clp -126944.3 0.118 0.929 2857.09 4 4 5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp -127125.43 0.12 0.93 598.7 4 4	4	$\operatorname{DGS-clp}$	-126950.3	0.12	0.928	3059.47	4	4
4 GS-pruned -127236.8 0.12 0.93 859.36 137 4 5 DGS -127021.17 0.12 0.93 2857.09 4 4 5 DGS-clp -126944.3 0.118 0.929 2857.09 4 4 5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp -127125.43 0.12 0.93 598.7 4 4	4	GS-tw	-127299.75	0.118	0.93	606.5	4	4
5 DGS -127021.17 0.12 0.93 2857.09 4 4 5 DGS-clp -126944.3 0.118 0.929 2857.09 4 4 5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp -127125.43 0.12 0.93 598.7 4 4	4	GS- clp	-126987.52	0.12	0.93	606.5	4	4
5 DGS-clp -126944.3 0.118 0.929 2857.09 4 4 5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp -127125.43 0.12 0.93 598.7 4 4	4	GS-pruned	-127236.8	0.12	0.93	859.36	137	4
5 GS-tw -127398.88 0.12 0.93 598.7 4 4 5 GS-clp -127125.43 0.12 0.93 598.7 4 4	5	DGS	-127021.17	0.12	0.93	2857.09	4	4
5 GS-clp -127125.43 0.12 0.93 598.7 4 4	5	$\operatorname{DGS-clp}$	-126944.3	0.118	0.929	2857.09	4	4
	5	GS-tw	-127398.88	0.12	0.93	598.7	4	4
5 GS-pruned -127246.2 0.12 0.93 857.86 153 4	5	$\operatorname{GS-clp}$	-127125.43	0.12	0.93	598.7	4	4
	5	GS-pruned	-127246.2	0.12	0.93	857.86	153	4

Table 60: Comparison of the methods in dataset imdb in 5-fold cross-validation, using a treewidth bound of 5. For each fold and method, the conditional log-likelihood in the test dataset (CLL), the global accuracy (acc_G) , the mean accuracy (acc_M) , the learning time (time), the treewidth (tw) and the treewidth of the pruned graph (tw-pr) are shown. The optimal results are denoted in boldface.

Fold	Method	CLL	0.00 -	0.00-	time	trr	tur no
			acc_G	acc_M		tw	tw-pr
1	DGS	-126123.47	0.12	0.93	3677.5	5	5
1	DGS- clp	-126031.13	0.125	0.929	3677.5	5	5
1	GS-tw	-126132.06	0.12	0.93	$\boldsymbol{658.5}$	5	5
1	$\operatorname{GS-clp}$	-125895.8	0.12	0.93	$\boldsymbol{658.5}$	5	5
1	GS-pruned	-126097.03	0.12	0.93	879.83	141	5
2	DGS	-126800.73	0.12	0.93	3369.75	5	5
2	$\operatorname{DGS-clp}$	-126715.08	0.12	0.928	3369.75	5	5
2	GS-tw	-126770.5	0.12	0.93	638.1	5	5
2	GS- clp	-126598.4	0.12	0.93	638.1	5	5
2	GS-pruned	-126820.89	0.12	0.93	835.69	134	5
3	DGS	-124402.12	0.12	0.93	3935.6	5	5
3	$\operatorname{DGS-clp}$	-124379.2	0.126	0.929	3935.6	5	5
3	GS-tw	-124590.43	0.13	0.93	673.5	5	5
3	GS- clp	-124452.15	0.12	0.93	673.5	5	5
3	GS-pruned	-124662.1	0.12	0.93	854.26	152	5
4	DGS	-126101.27	0.12	0.93	3783.08	5	5
4	$\operatorname{DGS-clp}$	-126009.97	0.12	0.928	3783.08	5	5
4	GS-tw	-126162.79	0.121	0.93	669.1	5	5
4	GS- clp	-125892.6	0.12	0.93	669.1	5	5
4	GS-pruned	-126195.54	0.12	0.93	887.45	148	5
5	DGS	-125751.19	0.12	0.93	3686.68	5	5
5	DGS-clp	-125685.3	0.121	0.929	3686.68	5	5
5	GS-tw	-125914.8	0.12	0.93	$\boldsymbol{658.2}$	5	5
5	GS- clp	-125760.31	0.12	0.93	$\boldsymbol{658.2}$	5	5
5	GS-pruned	-126091.93	0.12	0.93	876.82	138	5
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