

Лабораторная работа 4

Вариант 13

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Целью работы является исследование свойств некоторых видов сетей с радиальными базисными элементами, алгоритмов обучения, а также применение сетей в задачах классификации и аппроксимации функции.

```
In [1]: import matplotlib.pyplot as plt
import numpy as np
import keras
from keras import layers
import tensorflow as tf
```

Классификация

```
In [2]: def ellipse(t, a, b, x0, y0):
    x = x0 + a*np.cos(t)
    y = y0 + b*np.sin(t)
    return x, y

def parabola(t, p, x0, y0):
    x = x0 + t ** 2 / (2. * p)
    y = y0 + t
    return x, y

epochs = 500
```

```
In [3]: t = np.linspace(0, 2*np.pi, 200)
x1, y1 = ellipse(t, 0.3, 0.3, 0, 0)

x2, y2 = ellipse(t, 0.7, 0.7, 0, 0)

x3, y3 = parabola(t, 1, -0.8, 0)
```

Описываем класс RBF слоя

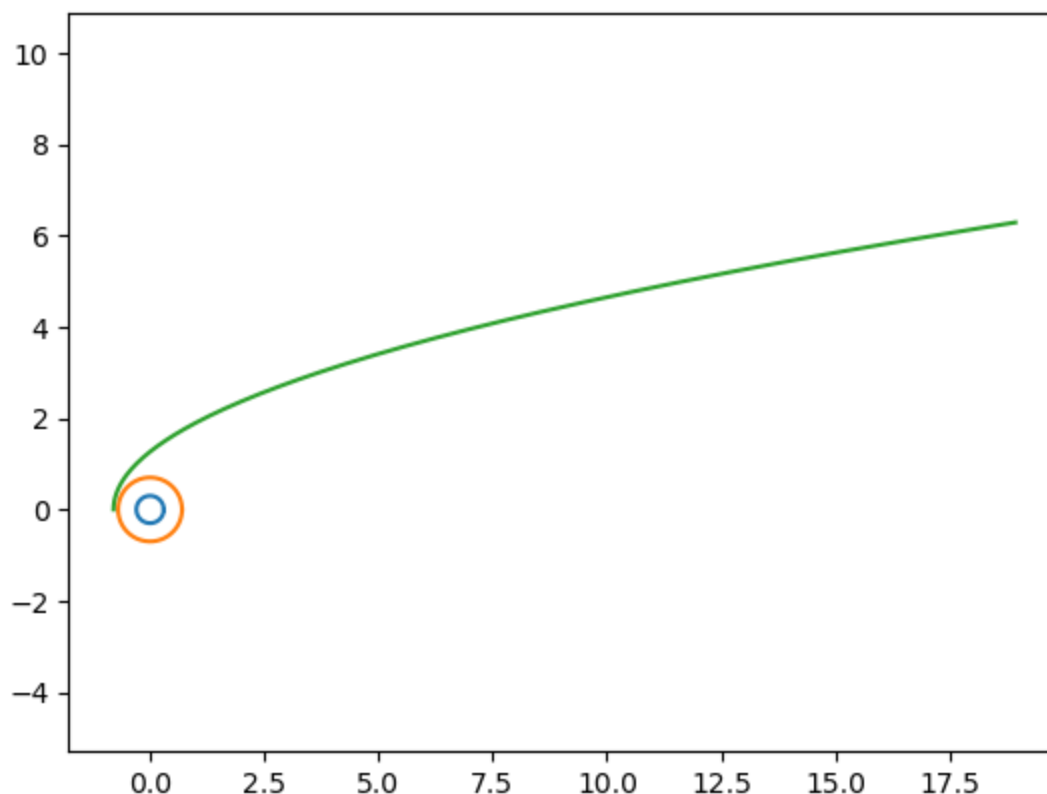
```
In [4]: class RBF(layers.Layer):
    def __init__(self, units, **kwargs):
        self.units = units
        super(RBF, self).__init__(**kwargs)

    def build(self, input_shape):
        self.mu = self.add_weight(
            shape=(input_shape[1], self.units), initializer="random_normal", trainable=True
        )
        self.sigm = self.add_weight(
            shape=(self.units,) , initializer="random_normal", trainable=True
        )
        super().build(input_shape)

    def call(self, inputs):
        l_norm = tf.reduce_sum((tf.expand_dims(inputs, axis=2) - self.mu) ** 2, axis = 1)
        return tf.exp(l_norm*self.sigm)
```

```
In [5]: plt.plot(x1,y1)
plt.plot(x2,y2)
plt.plot(x3,y3)
plt.axis('equal')
```

```
Out[5]: (-1.7869604401089358, 19.92616924228765, -1.049136367826184, 6.632343482179861)
```



Готовим датасет

```
In [6]: data1 = [[cords, [1, 0, 0]] for cords in zip(x1, y1)]
data2 = [[cords, [0, 1, 0]] for cords in zip(x2, y2)]
data3 = [[cords, [0, 0, 1]] for cords in zip(x3, y3)]
dataset = data1 + data2 + data3
np.random.shuffle(dataset)
```

```
In [7]: train_percent = 0.8
train_num = int(train_percent * len(dataset))
train_X = [x[0] for x in dataset[:train_num]]
train_y = [x[1] for x in dataset[:train_num]]
test_X = [x[0] for x in dataset[train_num:]]
test_y = [x[1] for x in dataset[train_num:]]
```

Создаем модель

```
In [8]: model = keras.Sequential([
    RBF(10,input_dim=2),
    layers.Dense(3,activation='sigmoid', name="sigmoid")
])
```

Компилируем модель

```
In [9]: model.compile(loss='mse', optimizer='adam', metrics=['mae'])
```

Тренируем модель

```
hist = model.fit(train_X,train_y,batch_size=len(dataset)//10,epochs=epochs)
```

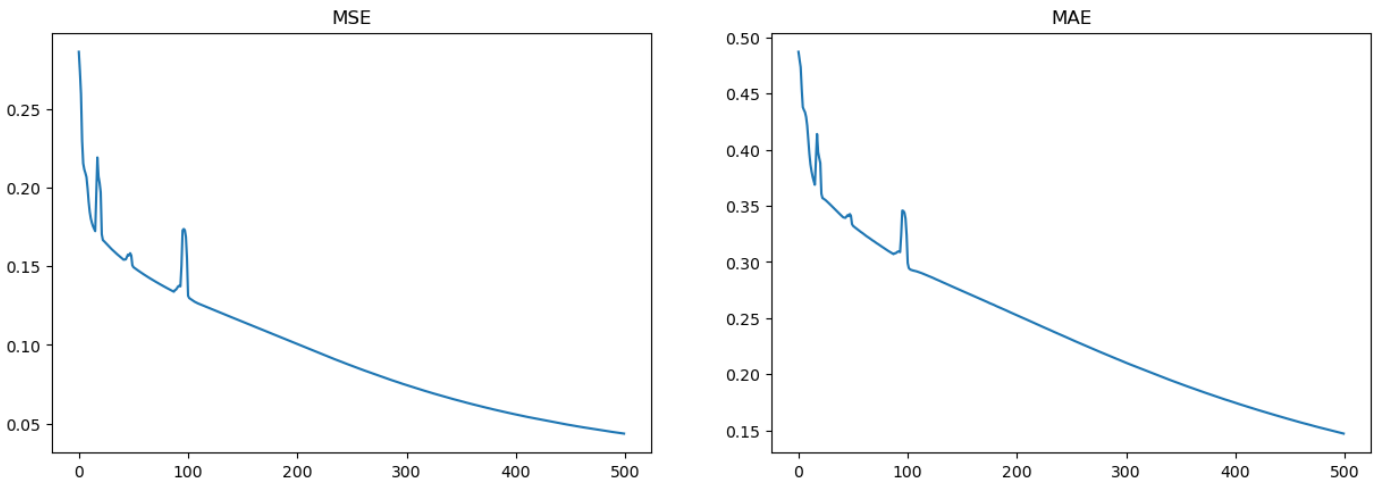
In []:

```
In [11]: fig, ax = plt.subplots(1, 2)
fig.set_figwidth(15)

ax[0].set_title('MSE')
ax[1].set_title('MAE')

ax[0].plot(range(epochs), hist.history['loss'])
ax[1].plot(range(epochs), hist.history['mae'])
```

Out[11]: [



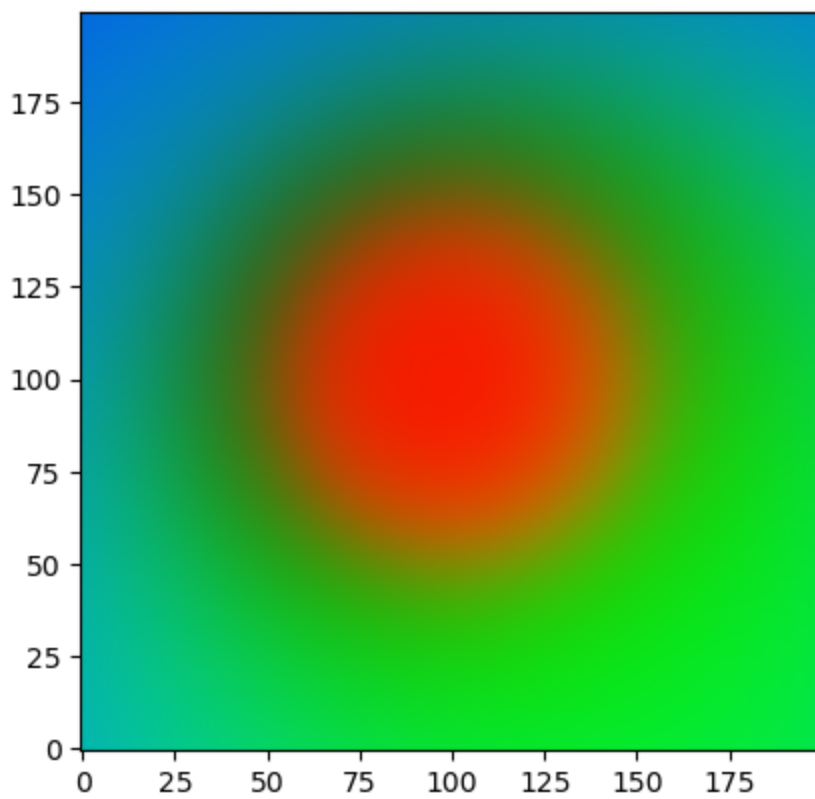
Создаем поле точек и скалярное поле

```
In [12]: pole = []
for y in np.linspace(-1,1,200):
    for x in np.linspace(-1,1,200):
        pole.append((x,y))
```

```
In [13]: pred = model.predict(pole)
z = []
for i in range(200):
    z.append(pred[i*200: (i+1)*200])
```

1250/1250 [=====] - 1s 711us/step

```
In [14]: fig, ax = plt.subplots()
ax.imshow(z)
ax.invert_yaxis()
```



Аппроксимация функции

```
In [15]: def func(t):
         return np.cos(t**2 - 2*t + 3)
```

```
In [16]: h = 0.02
         X = np.arange(0, 5+h, h)
         y = func(X)
```

Создаем модель

```
In [38]: model2 = keras.Sequential([
         RBF(30, input_dim=1),
         layers.Dense(1, activation='linear', name='linear')
         ])
```

Компилируем модель

```
In [39]: model2.compile(loss='mse', optimizer='adam', metrics=['mae'])
```

Тренируем модель

```
In [ ]: hist2 = model2.fit(X, y, batch_size=10, epochs=1000)
```

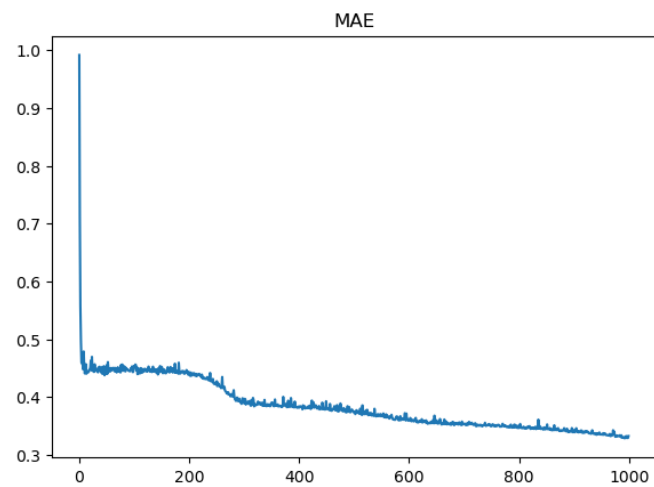
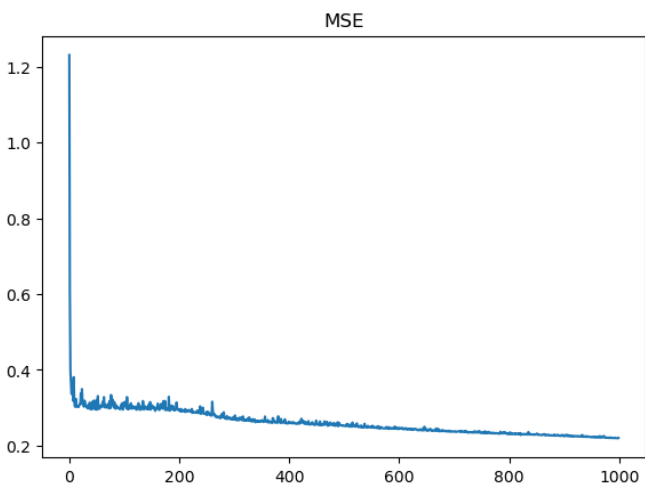
```
In [41]: fig, ax = plt.subplots(1, 2)
         fig.set_figwidth(15)

         ax[0].set_title('MSE')
         ax[1].set_title('MAE')

         ax[0].plot(range(1000), hist2.history['loss'])
         ax[1].plot(range(1000), hist2.history['mae'])
```

[<matplotlib.lines.Line2D at 0x2268307f5b0>]

Out[41]:

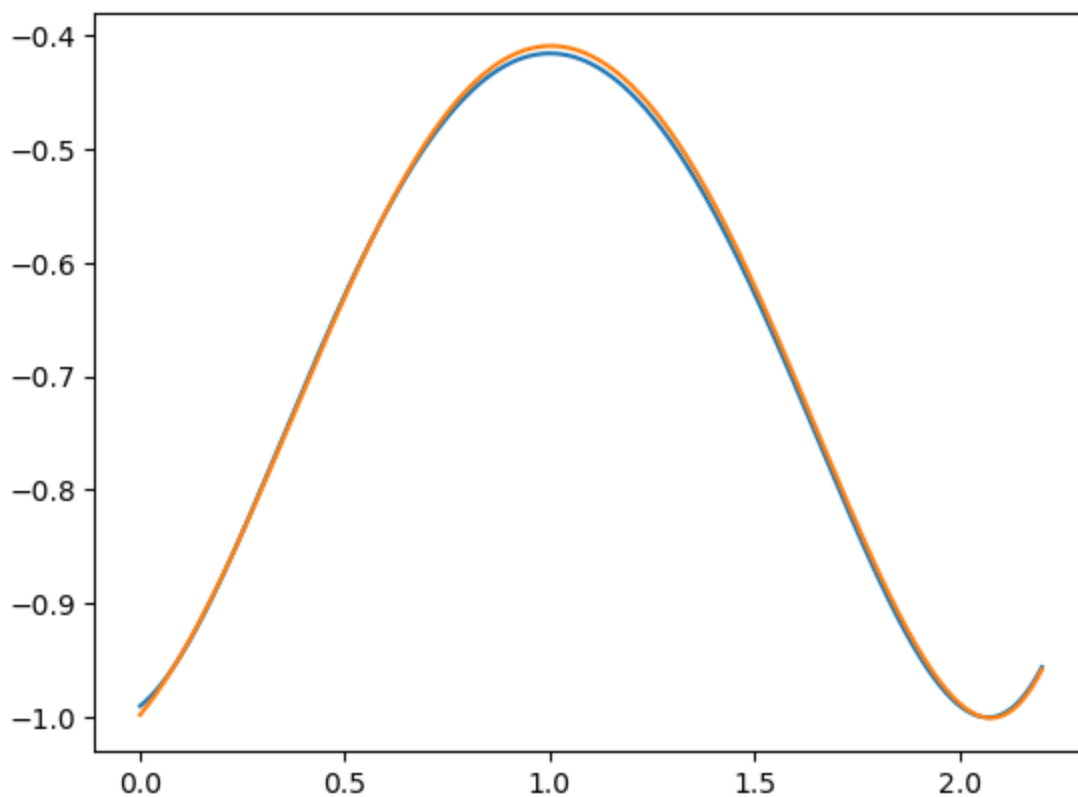


Аппроксимируем функцию

```
In [33]: t = np.linspace(0, 2.2, 2000)
y_ans = func(t)
y_pred = model2.predict(t)
plt.plot(t, y_ans)
plt.plot(t, y_pred)
```

63/63 [=====] - 0s 790us/step

Out[33]: [<matplotlib.lines.Line2D at 0x226fbf0a3a0>]



In []: