



Computer Vision

Binary Morphology

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Noordelijke Hogeschool Leeuwarden and Van de Loosdrecht Machine Vision
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Binary Morphology

Overview:

- Erosion
- Dilation
- Opening
- Closing
- Hit and miss (*)
- Thinning (*)
- Thickening (*)
- Skeleton

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Erosion

Erosion (src, dest, mask)

The erosion operator initialises a destination image by sliding a mask across a source image.

The mask may be visualised as a probe that slides across the src image, testing the spatial nature of the image at every point x . Where the mask translated to x can be contained in the original image (by placing the centre (= origin) of the mask at x), then x belongs to the destination image.

Usage:

- to peel blobs
- to implement more complex operators

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Demonstration Erosion

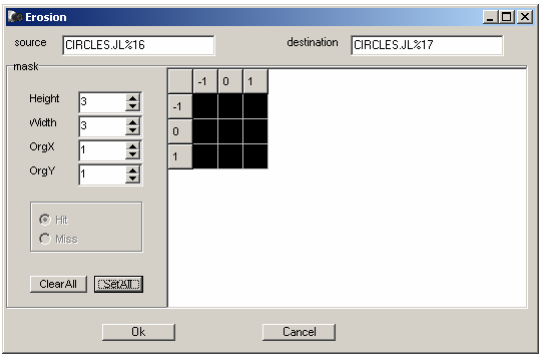
- Open image circles.jl
- Threshold 0 130
- Erosion 3x3 setall
- Result: a layer of 1 pixel is eroded from image
- Eroded image (= 2nd) subtracted from thresholded image gives the border of objects
- Successive erosions erodes the legs and objects

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Erosion 3x3 setall

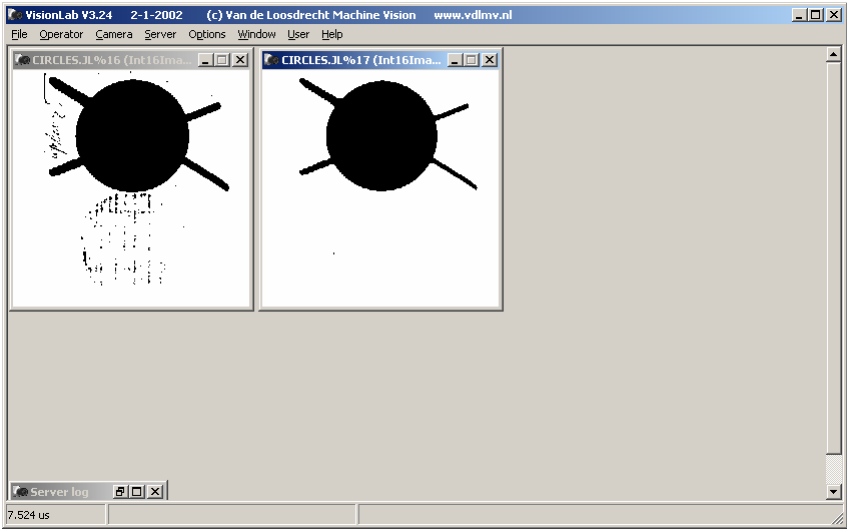


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Erosion 3x3 setall

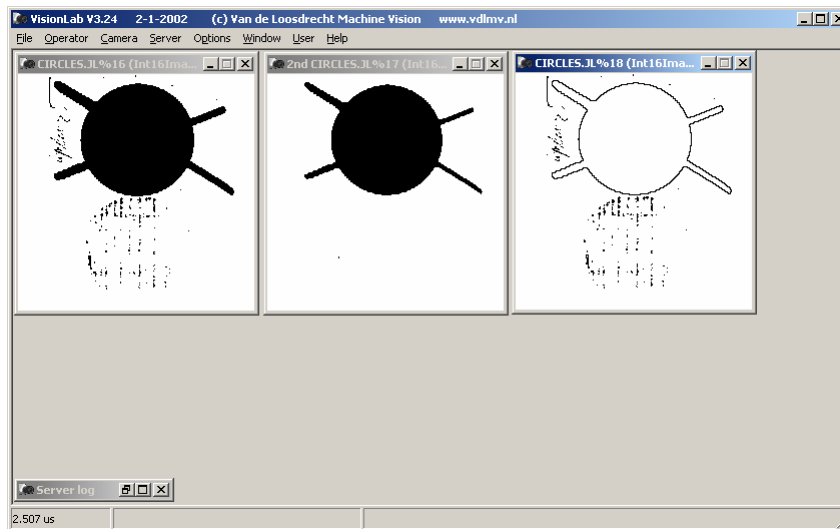


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**Eroded image (= 2nd) subtracted from Thresholded image
gives the border of objects**

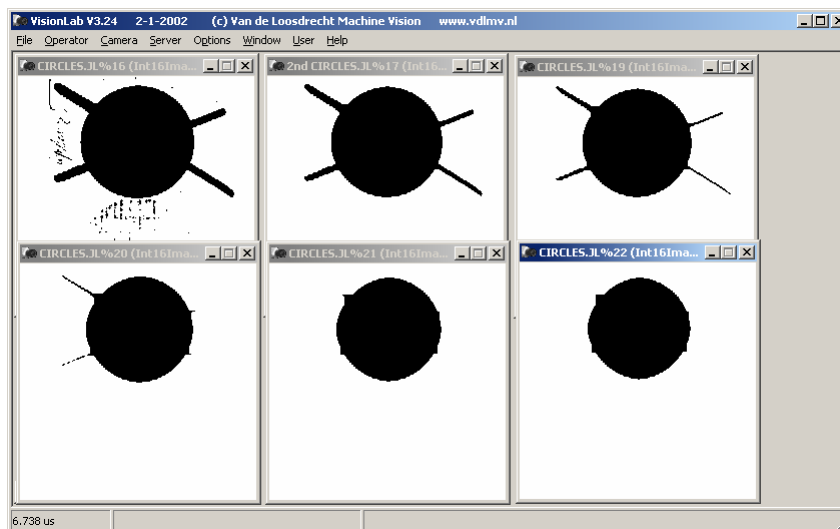


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Successive erosions erodes the legs and objects



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Demonstration Erosion

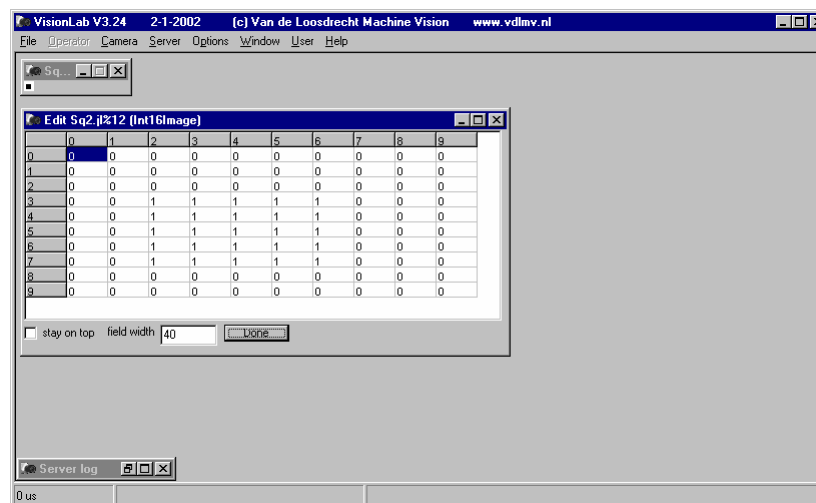
- Open image sq2.jl
- Show image with edit
- Erosion with 1 1 1
0 0 1
0 0 0
- Show result with edit
- Explain why top, right and left border are removed

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Image sq2.jl

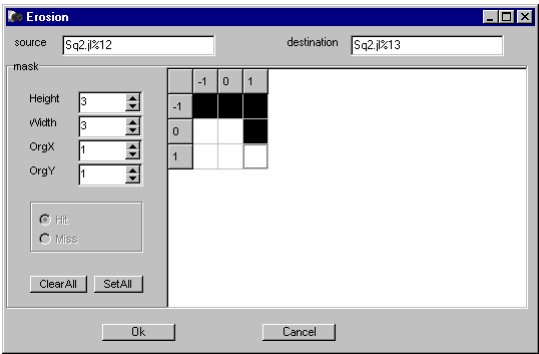


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Erosion mask

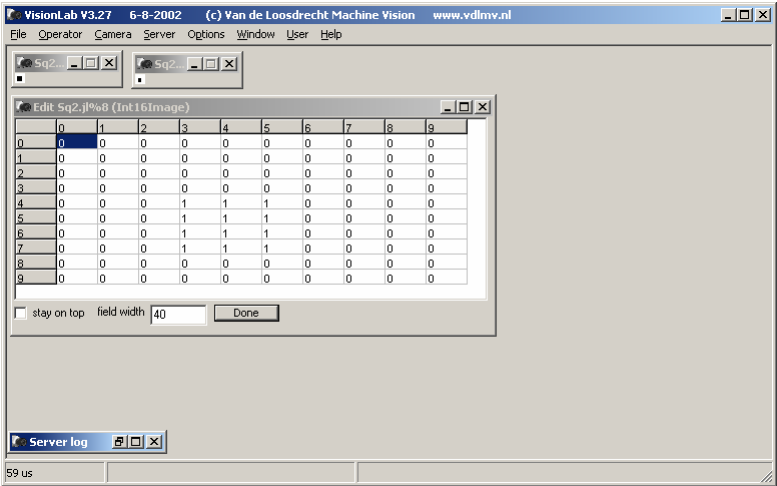


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Erosion



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Dilation

Dilation (src, dest, mask)

At the start of the operation the destination image is filled with background (=0) pixel values. The mask is swept over the source image. Every time the centre (= origin) of the mask touches an object (=1) pixel in the source image, the entire translated mask is OR-ed to the destination image.

Usage:

- to add a layer to blobs
- to implement more complex operators

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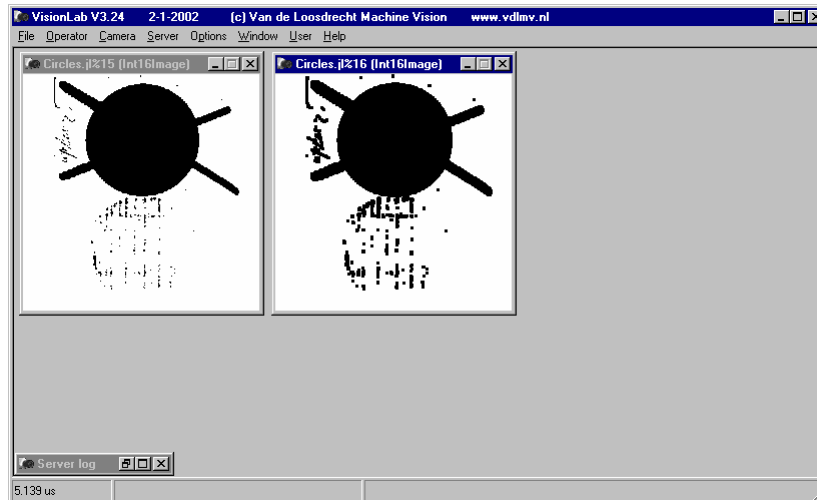
Demonstration Dilation

- Open image circles.jl
- Threshold 0 130
- Dilation 3x3 setall
- Result: a layer of 1 pixel is added to the image
- Thresholded image (= 2nd) subtracted from Eroded image gives a border around the objects
- With successive dilations the objects grow

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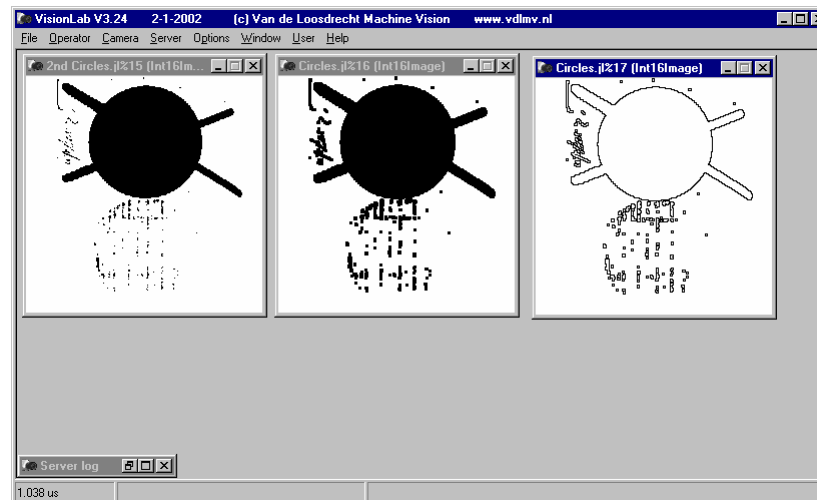
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Dilation 3x3 setall

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**Thresholded image (= 2nd) subtracted from Eroded image
gives a border around the objects**

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With successive dilations the objects grow



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Demonstration Dilation

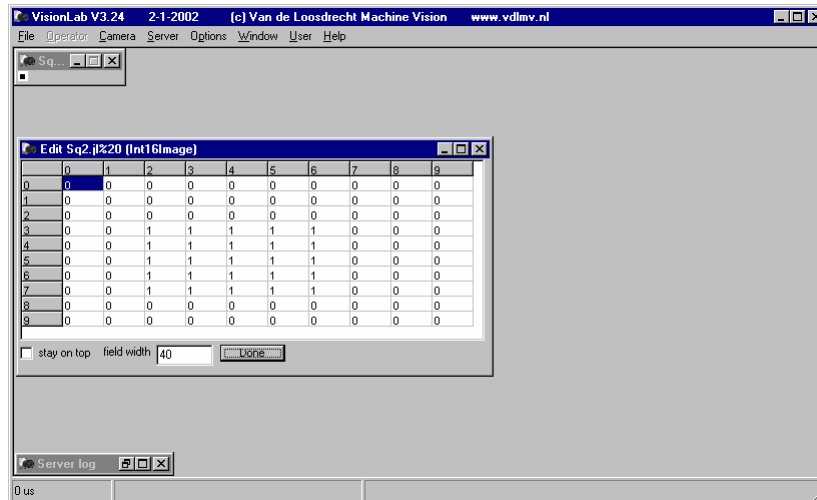
- Open image sq2.jl
- Show image with edit
- Dilation with $\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{bmatrix}$
- Show result with edit
- Explain why square is shifted one square to left bottom
- Same with Dilation with $\begin{bmatrix} 0 & 0 & 0 \\ 1 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$, result extra layer at left side

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Image sq2.jl

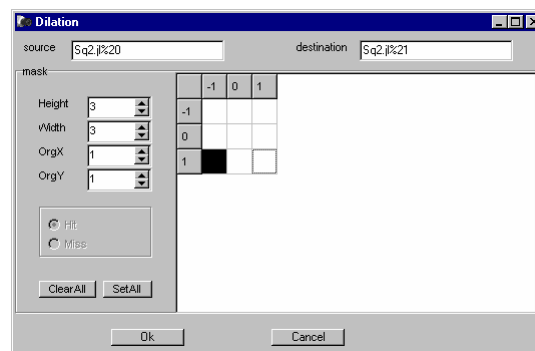


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First example Dilation

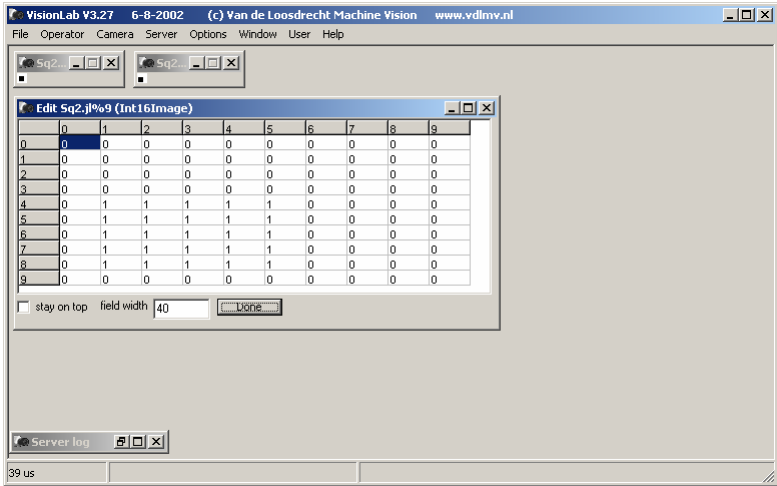


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First example Dilation

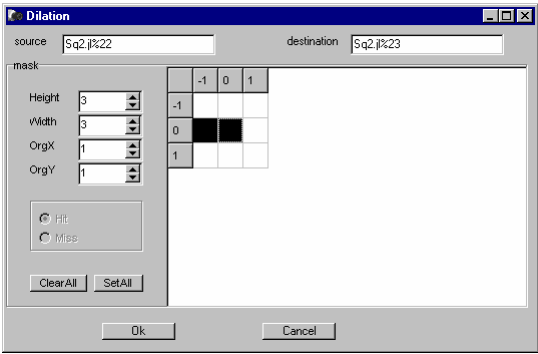


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Second example Dilation

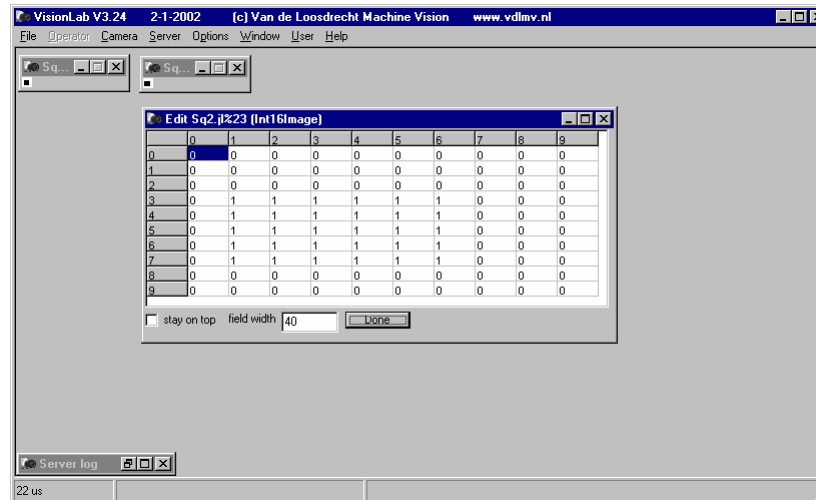


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Second example Dilation



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Opening

Opening (src, dest, mask)

The opening operator initialises a destination image as the result of an erosion on the source image with the mask followed by a dilation with the same mask.

Usage: smooths the contour by

- breaking narrow corridors
- eliminating small islands
- sharpening peaks
- small objects are removed and the original shape is almost retained

Opening operation is idempotent

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Demonstration Opening, removing small objects

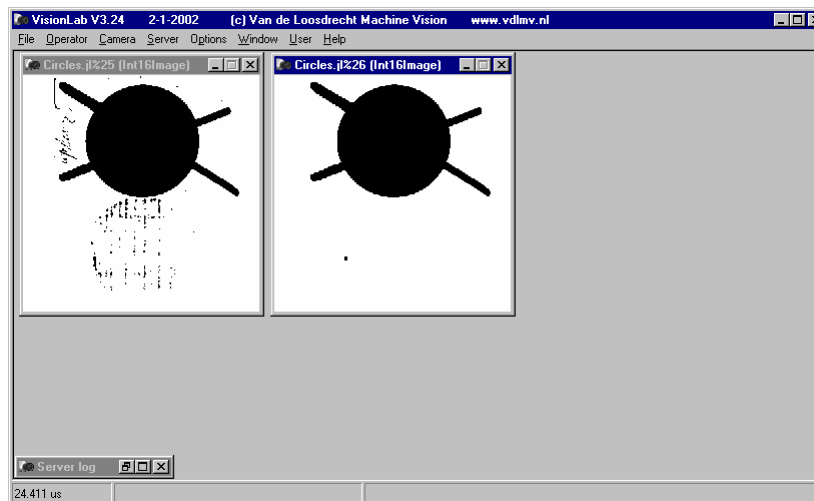
- Open image circles.jl
- Threshold 0 130
- Opening 3x3 setall
- Note small difference: difference between thresholded image and Opened image, right top leg, right edge (207,35), due to square shape erosion mask (*)
- 2nd time same opening has no effect

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Opening 3x3 setall, removing small objects

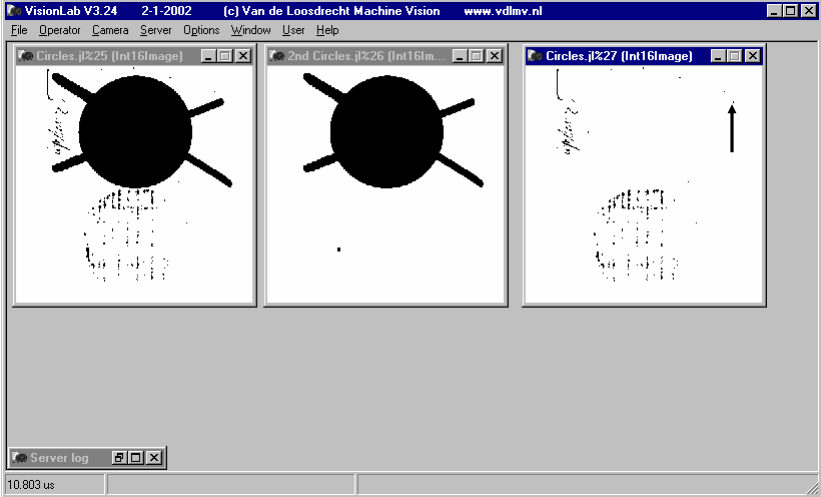


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Difference



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Demonstration Opening, sharpening of peaks

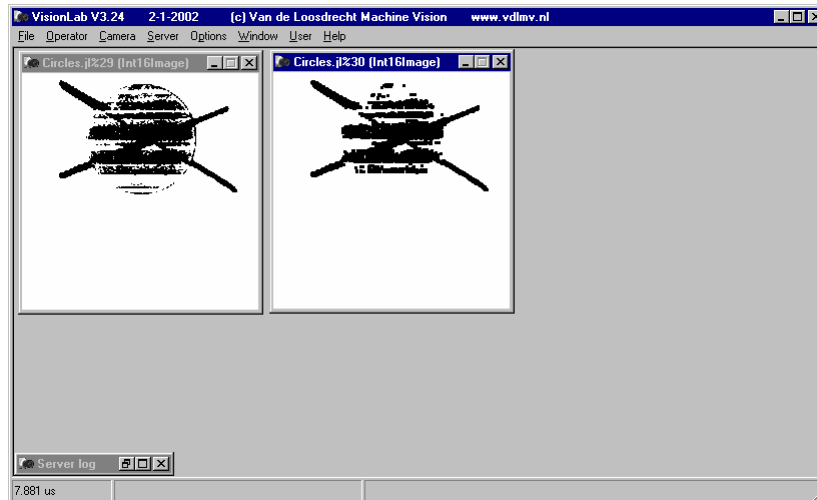
- Open image circles.jl
- Threshold 0 60
- Opening 3x3 setall
- Show sharpening of peaks
- Implementation:
 - Erosion, followed by
 - Dilation with same mask

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Opening 3x3 setall, sharpening of peaks



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Closing

Closing (src, dest, mask)

The closing operator initialises a destination image as the result of a dilation on the source image with the mask followed by an erosion with the same mask.

Usage: smooths the contour by

- filling narrow breaks
- eliminating small holes
- filling gaps

Closing operation is idempotent

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Demonstration Closing, filling gaps

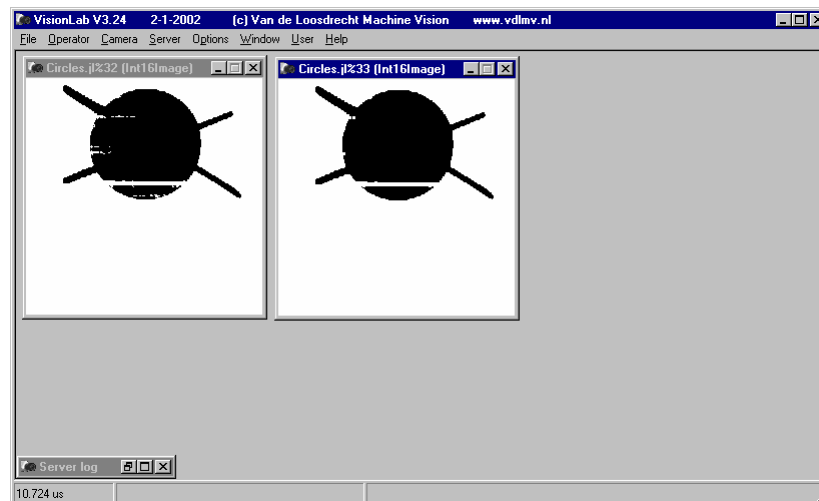
- Open image circles.jl
- Threshold 0 70
- Closing 3x3 setall
- 2nd time same closing has no effect
- Implementation:
 - Dilation, followed by
 - Erosion with same mask

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Closing 3x3 setall, filling gaps



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Demonstration Opening, find legs

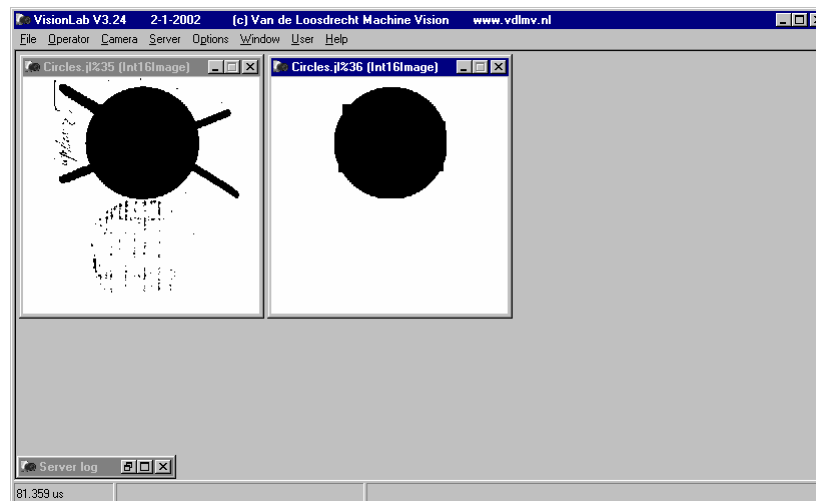
- Find the legs in threshold circles.jl 0 130:
- Opening 15x15 setall (org = 7,7), remove noise and legs
- Subtract Opened image (= 2nd) from thresholded image
- Opening 5x5 setall (org = 2,2) to remove noise

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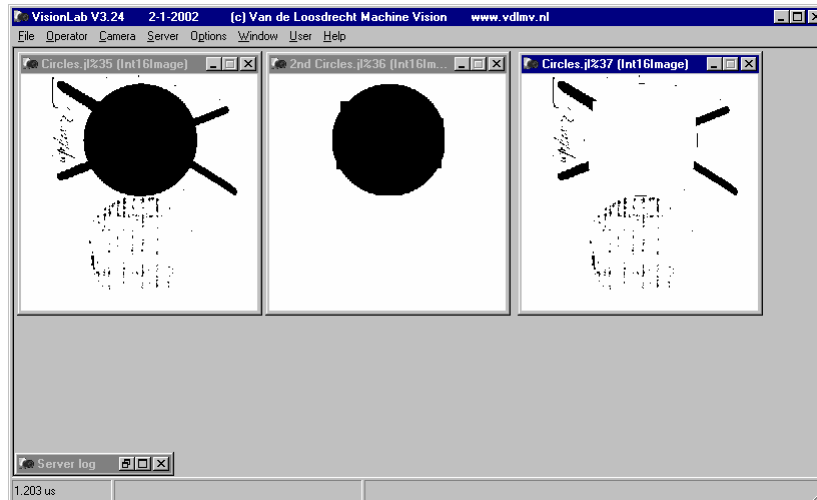
Opening 15x15 setall (org = 7,7), remove noise and legs



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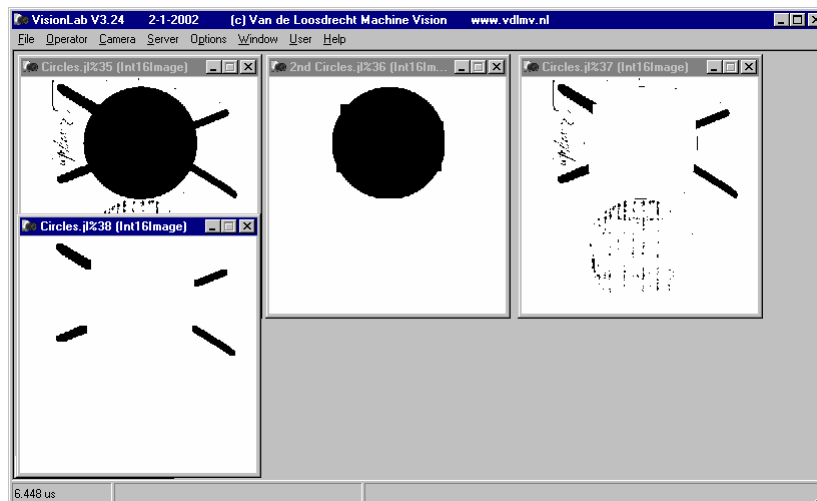
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Subtract Opened image (= 2nd) from Thresholded image

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Opening 5x5 setall (org = 2,2) to remove noise

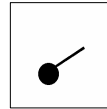
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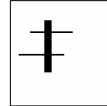
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Exercises with Opening and Closing

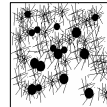
a) Use image `ballbar.jl`
Split ball from bar



b) Use image `bars.jl`
Split in one vertical bar and two horizontal bars



c) Use image `ballstripes.jl`
Filter the balls from the image



Answers:

- `ballbar.jls`
- `bars.jls`
- `ballstripes.jls`

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Hit and Miss (*)

HitAndMiss (src, dest, hitMask, missMask)

The destination image has pixels set to the object value ($\neq 1$) at positions where all objects in the hitmask are contained in the source image and none of the object pixels in the missmask are contained in the source image.

Usage: to find specific points of blobs like corners or borders.

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Demonstration Hit and Miss, find right border (*)

- Example find right border
 - Open file sq2.jl
 - Apply HitAndMiss with hitmask: 0 0 0 and missmask: 0 0 1

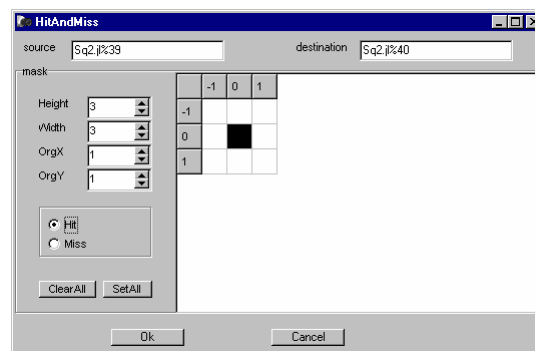
0 1 0	0 0 1
0 0 0	0 0 1

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Hit mask (*)

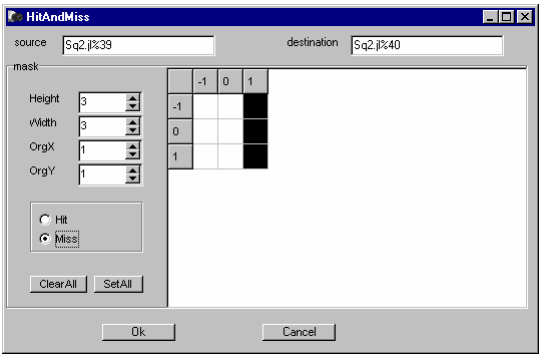


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Miss mask (*)

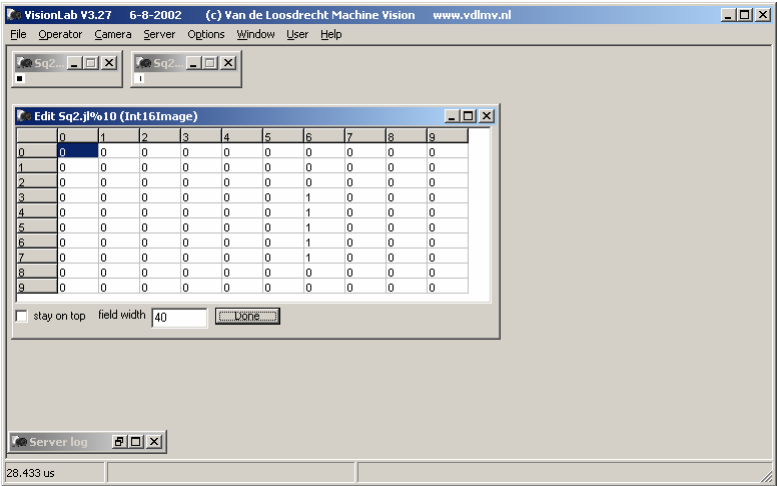


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Demonstration Hit and Miss, find right border (*)



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Demonstration Hit and Miss, find right top corner (*)

- Example find right top corner
 - Open file sq2.jl
 - Apply HitAndMiss with hitmask: 0 0 0 and missmask: 0 1 1

1 1 0
0 1 0

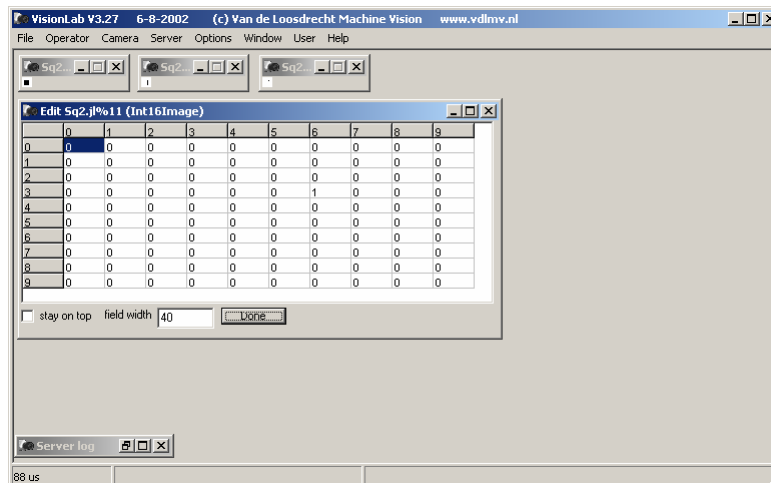
0 0 1
0 0 0

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Demonstration Hit and Miss, find right top corner (*)



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Hit and Miss (*)

Algorithm:

- **dest = src**
- **Not (dest)**
- **Erosion (dest, tmp, missMask)** // 'dilate' background
- **Erosion (src, dest, hitMask)** // erode objects
- **dest &= tmp;**

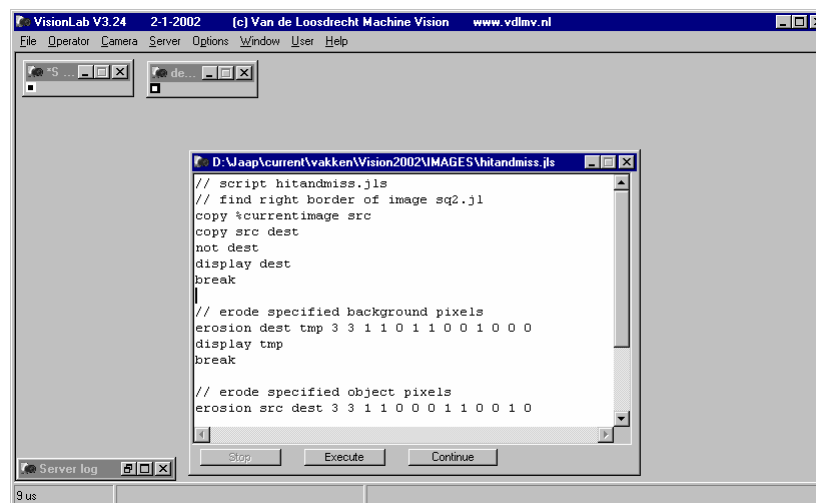
- see script hitandmiss.jls

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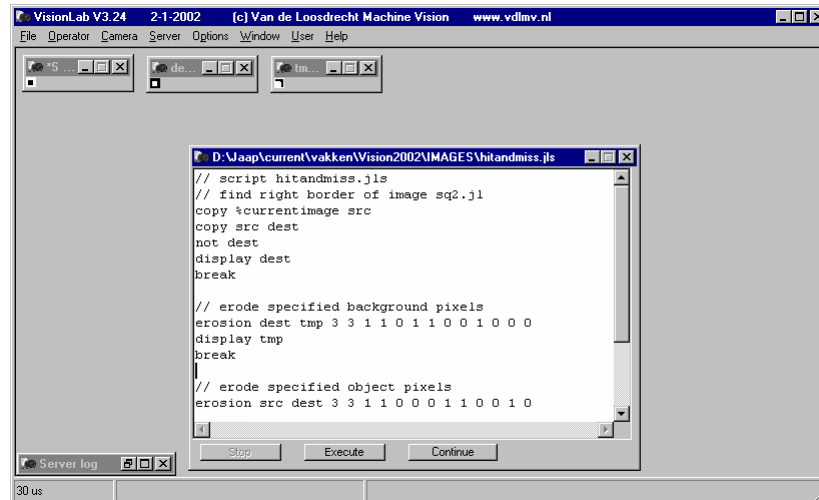
Not (dest) (*)



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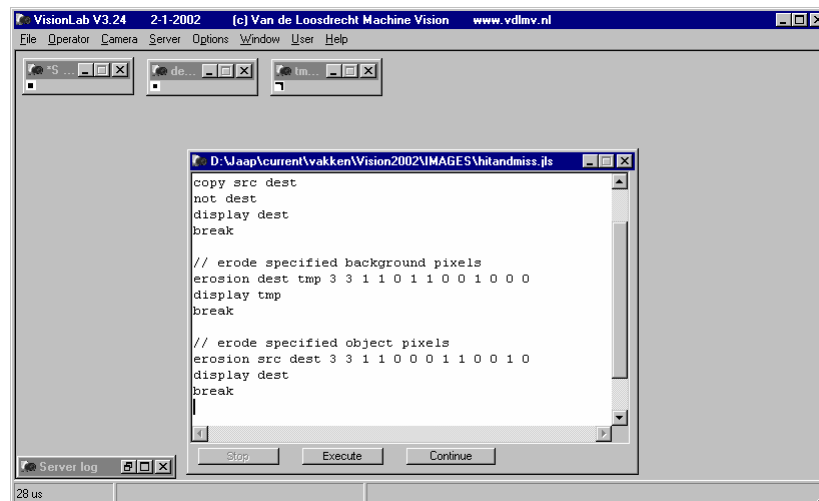
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Erosion (dest, tmp, missMask) (*)

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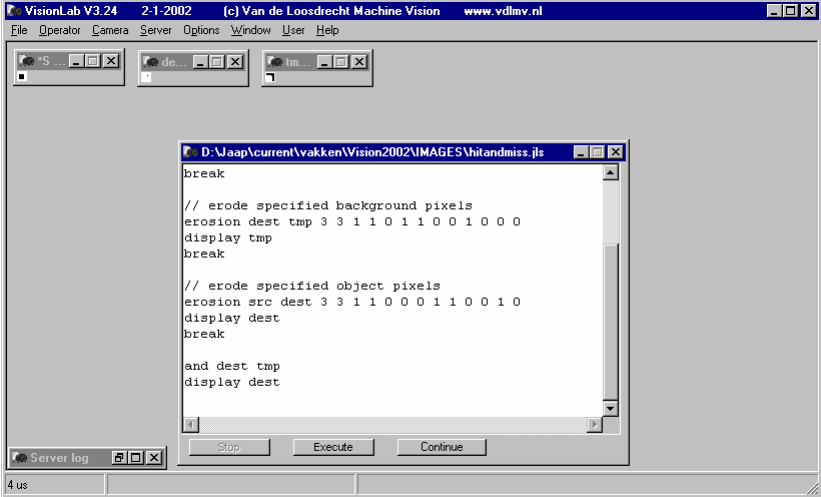
Erosion (src, dest, hitMask) (*)

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dest &= tmp; (*)



The screenshot shows the VisionLab V3.24 interface. A script window titled 'D:\Jaap\current\vakken\Vision2002\IMAGES\hitandmiss.js' is open, displaying the following code:

```
break
// erode specified background pixels
erosion dest tmp 3 3 1 1 0 1 1 0 0 1 0 0 0
display tmp
break
// erode specified object pixels
erosion src dest 3 3 1 1 0 0 0 1 1 0 0 1 0
display dest
break
and dest tmp
display dest
```

At the bottom of the script window, there are buttons for 'Stop', 'Execute', and 'Continue'. The status bar at the bottom left indicates '4 us'.

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Thinning (*)

Thinning (src, dest, hitMask, missMask)

The destination image is the same as the source image but object pixels which are covered by the hitmask and not covered by the missmask are excluded from the destination image.

In order to perform meaningful, the origin of the hitmask should be included in the hitmask and the origin of the missmask should be excluded from the missmask.

Usage: at selective points peeling the blobs.

Demonstration Thinning, remove right border (*)

- Open image sq2.jl
- Analyse image with Edit
- Apply Thinning with hitmask: 0 0 0 and missmask: 0 0 1

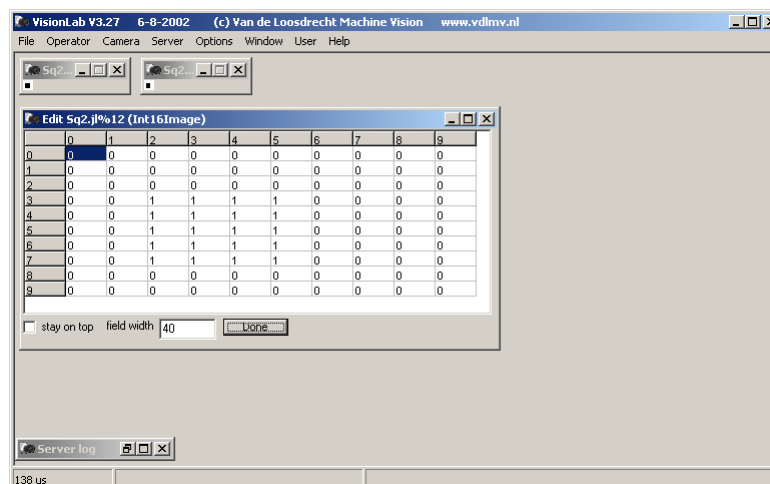
0 1 0	0 0 1
0 0 0	0 0 1
- Analyse result with Edit; right border has been removed

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Demonstration Thinning, remove right border (*)



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Demonstration Thinning, remove right top (*)

- Open image sq2.jl
- Analyse image with Edit
- Apply Thinning with hitmask: 0 0 0 and missmask: 0 1 1

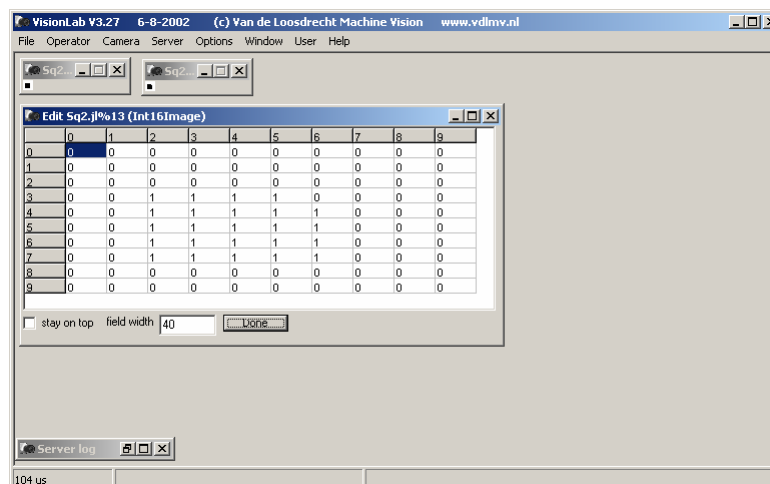
1 1 0	0 0 1
0 1 0	0 0 0
- Analyse result with Edit; right top has been removed

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Demonstration Thinning, remove right top (*)



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Thinning (*)

Algorithm:

- **HitAndMiss (src, tmp, hitMask, missMask)**
- **dest = src**
- **dest -= tmp** (exor is also possible)

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Thickening (*)

Thickening (src, dest, hitMask, missMask)

The destination image is the same as the source image but at special positions pixels are added.

These positions are where all objects in the hitmask are contained in the source image and none of the object pixels in the missmask are contained in the source image.

In order to perform meaningful, the origin of the hitmask should be excluded from the hitmask and the origin of the missmask should be included in the missmask.

Note: only the origin pixel is added.

Usage: add at selective points a layer to the blobs

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Demonstration Thickening (*)

- Open image sq2.jl
- Analyse image with Edit
- Apply Thickening with hitmask: 0 0 0 and missmask: 0 0 0

0 0 0	0 1 0
1 0 0	0 0 0

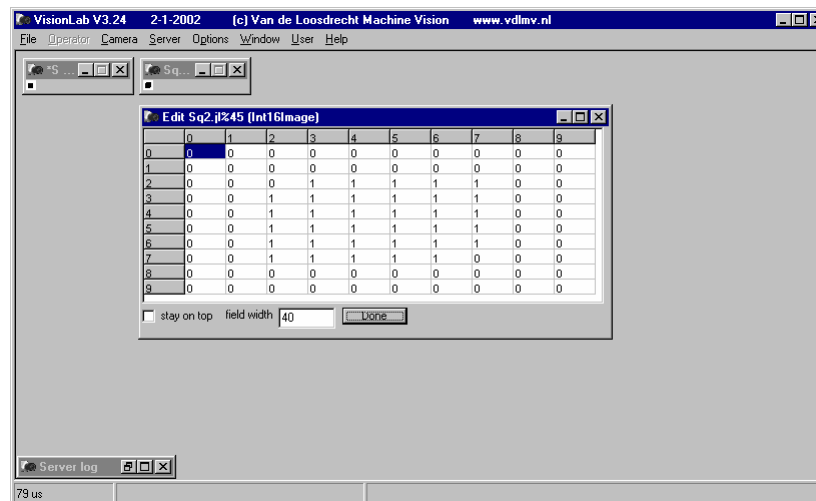
must be present
is not present and is added
- Analyse result with Edit; a layer is added at the top and the right side, note top left and bottom right.

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Demonstration Thickening (*)



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Thickening (*)

Algorithm:

- **HitAndMiss (src, dest, hitMask, missMask)**
- **dest |= src** (adding also possible)

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Skeleton

Skeleton (sourceImage, destinationImage)**Function:**

- **Calculates the skeleton of all blobs in a binary image**

Algorithm:

- **Iterative Thinning (= “grass burning”)**

Usage:

- **To get the ‘basic form’ of a blob**
- **Slow operation**

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Demonstration Skeleton sq.jl

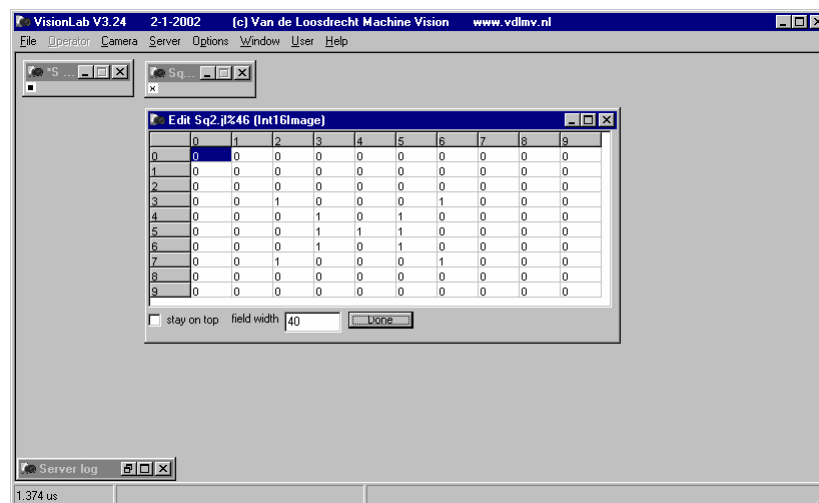
- Open image sq.jl
- Apply Skeleton
- Analyse result with Edit

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Demonstration Skeleton sq.jl



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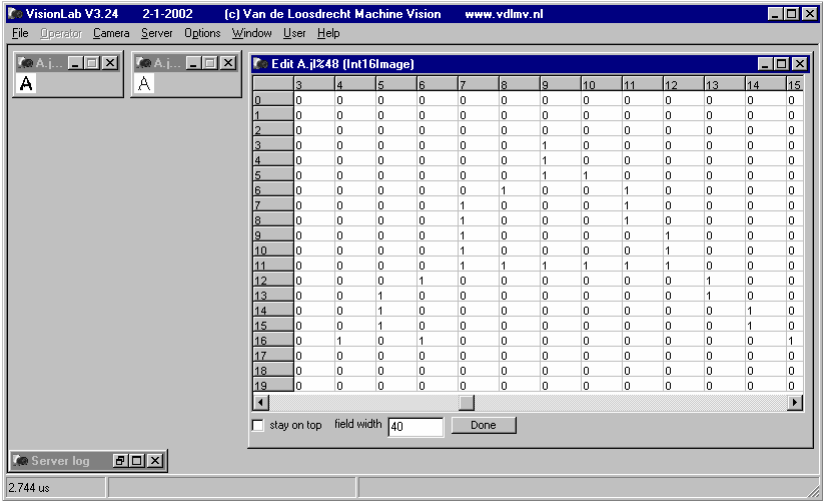
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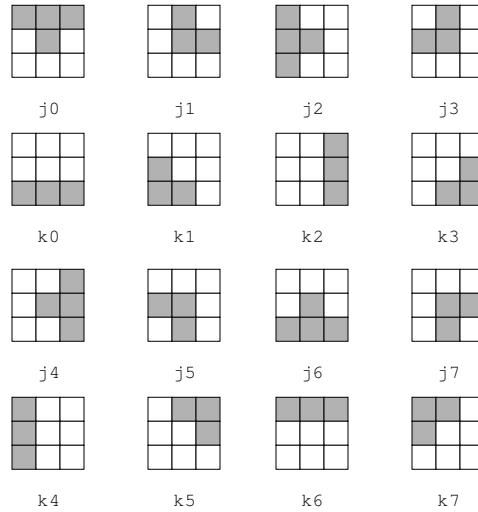
Demonstration Skeleton A.jl

- Open image A.jl
- Apply Skeleton
- Analyse result with Edit

Demonstration Skeleton A.jl



Skeleton implementation masks (*)



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Skeleton algorithm (*)

```

dest = src;
do {
    prevImage = dest;
    for (int i = 0; i < 8; i += 2) {
        Thinning (dest, tmp, j[i], k[i]);
        Thinning (tmp, dest, j[i+1], k[i+1]);
    }
} while (prevImage != dest);

```

Note:

- This is a very slow implementation
- Alternatives can be based on distance transform

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Demonstration Skeleton algorithm (*)

- Open image sq2.jl
- Thinning with masks j0 and k0,
eats middle of bottom border, but excludes the corners
- Thinning result with masks j1 and k1,
tries to eat left bottom corner, unless it is an isolated corner
- To see that Thinning with masks j1 and k1,
tries to eat left bottom corner, unless it is an isolated corner,
do this operation on sq2.jl

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Thinning with masks j0 and k0, (*) eats middle of bottom border, but excludes the corners

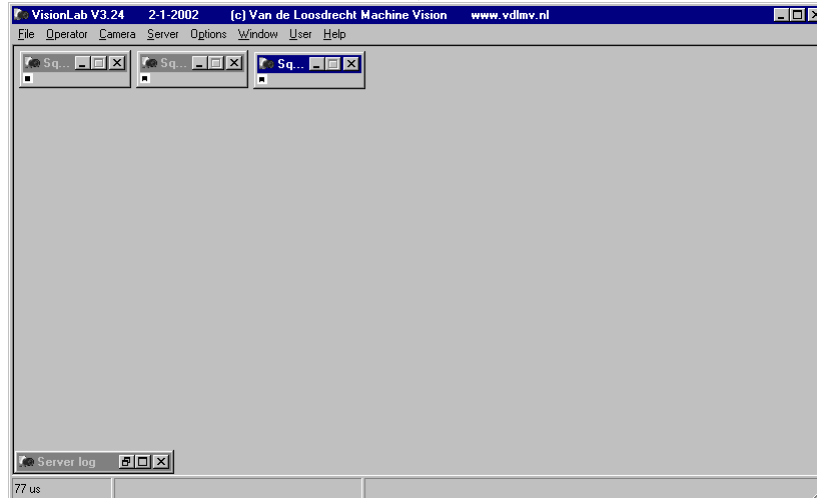


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Thinning result with masks j1 and k1, (*)
tries to eat left bottom corner, unless it is an isolated corner

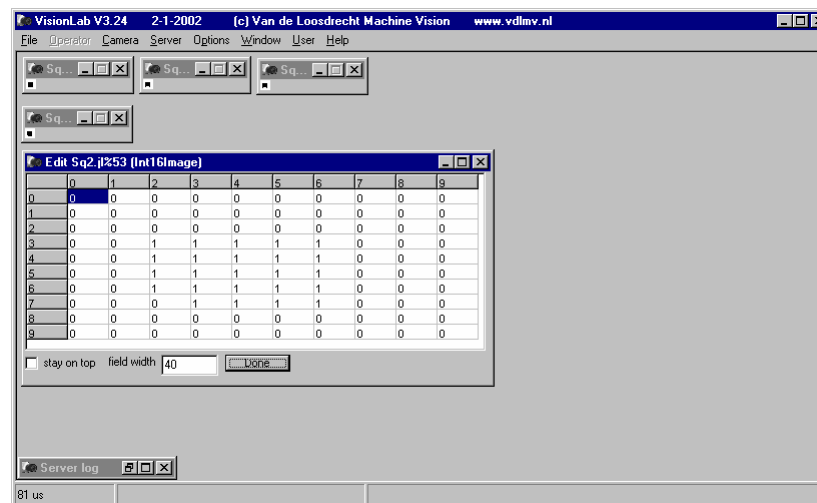


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Thinning with masks j1 and k1 on sq.jl, (*)
tries to eat left bottom corner, unless it is an isolated corner



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End points and branch points

In skeletons special points can be identified:

- end points (= one object neighbour)
- branch points (= more then two object neighbours)

NrOfNeighbours srcImage destImage connected

All background pixels will get the value 0.

All pixels belonging to a blob will get the value of its number of neighbours.

The parameter connected has the value EightConnected or FourConnected and determines how the blobs are connected.

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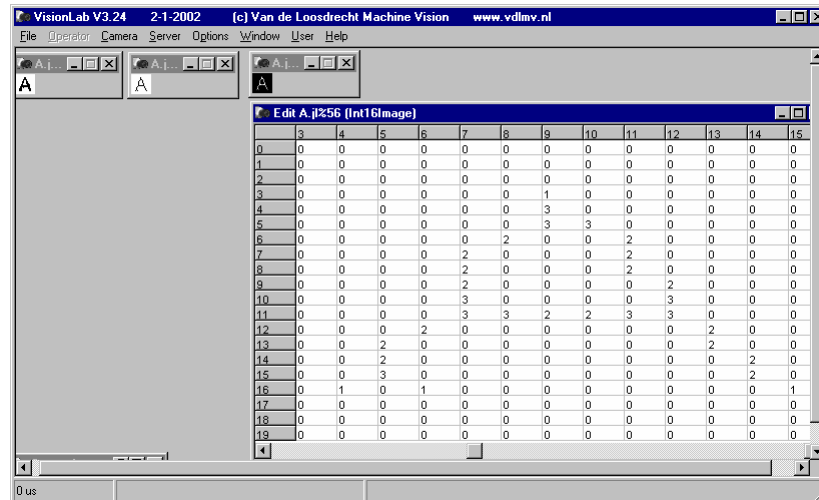
Demonstration finding endpoints

- Open image A.jl
- Skeleton
- NrOfNeighbours EightConnected (from the segmentation menu)
- Show results with edit
- Threshold 1 1,
to find endpoints, note there are 4 !

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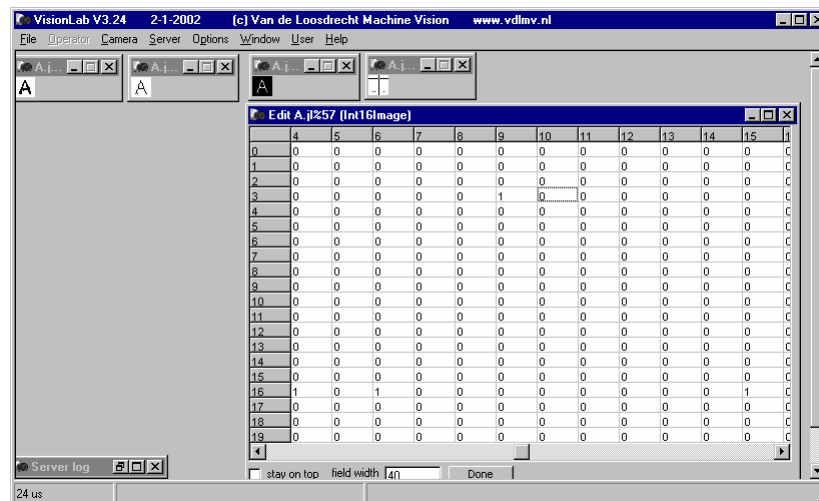
NrOfNeighbours

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Threshold 1 1, to find 4 endpoints



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Implementation of NrofNeighbours (*)

For EightConnected objects:

- Convolution with mask

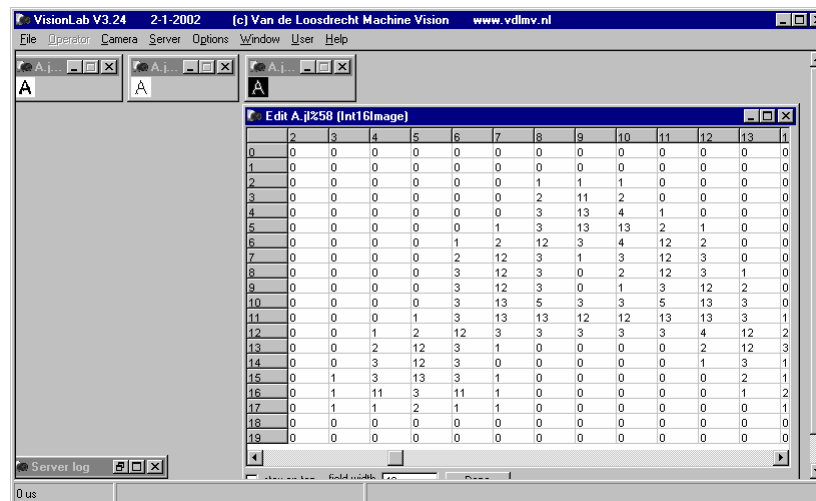
1	1	1
1	10	1
1	1	1
- $p < 10$: background pixel with p number of objects as neighbour
- $p > 10$: object pixel with $p - 10$ number of objects as neighbour
- Subtract 10 from all pixels
- Setselectedtovalue -10 -1 0

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Binary Morphology

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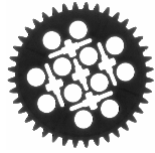
Convolution on skeleton (*)



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Binary Morphology

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Exercise count number of tooth on gear

- **Use image gear.jl**
- **Write script for counting number of teeth**

- **answer script gear.jls**

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Binary Morphology

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