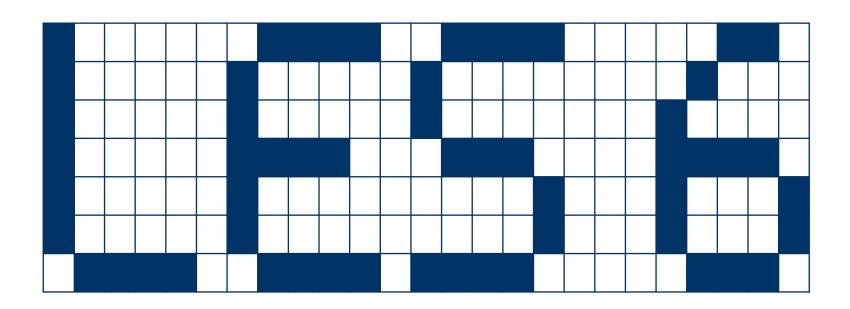




EVD1 – Vision operators







Nonlinear filters:

- Operate on greyscale images
- Are mainly used to remove noise
- But there are also other uses (dilation, erosion, edge detection)

Properties of Nonlinear filters:

- Computes a nonlinear function over a window of pixels
- Replaces one pixel within this window
- Window size is always odd, so there is a center pixel

Examples of Nonlinear filters:

- Average filter
- Harmonic filter
- Maximum filter
- Median filter

- Midpoint filter
- Minimum filter
- Range filter





Function prototype:





Average filter: Calculates the arithmetic mean of the pixels within the window

Window size (n) = 3

0	1	1	3	1	
	2	3	3	2	
	2	1	3	1	
	0	2	2	1	

$$\frac{1}{p_{(y,x)}} = \frac{1}{n^2} \sum_{i=-n/2}^{i=n/2} \sum_{j=-n/2}^{j=n/2} p(y+i,x+j)$$

$$p_{(1,1)} = \frac{1}{3^2} \times (1+1+3+2+3+9+2+1+3) = 2,7$$

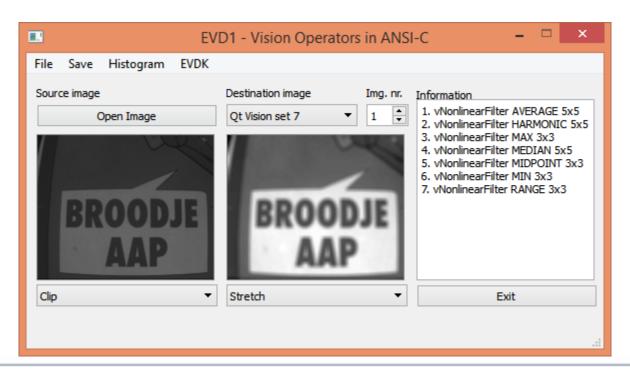
$$p_{(1,2)} = \frac{1}{3^2} \times (1+3+1+3+9+2+1+3+1) = 2,7$$





Average filter:

- Used to remove single noise pixels
- High noise values infuence all neighbour pixels
- Larger window means more blurring effect and loss of edge information

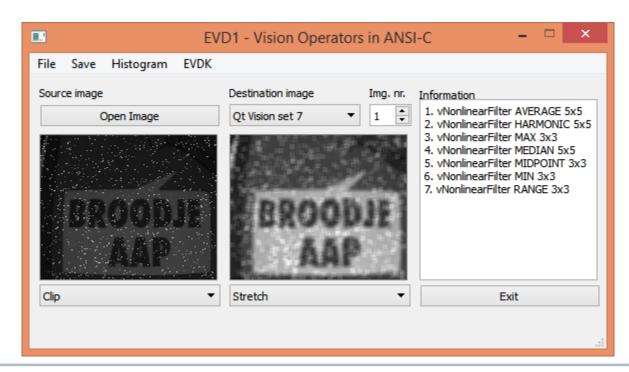






Average filter:

- Used to remove single noise pixels
- High noise values infuence all neighbour pixels
- Larger window means more blurring effect and loss of edge information

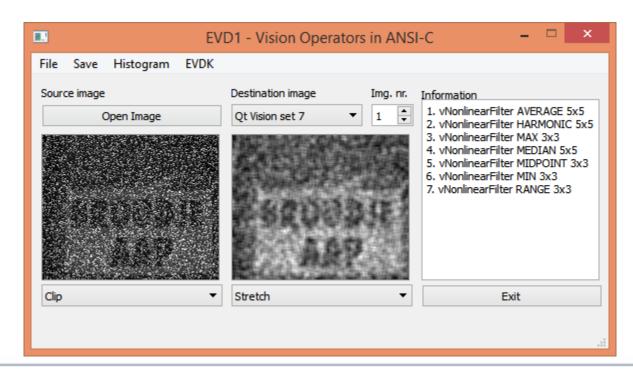






Average filter:

- Used to remove single noise pixels
- High noise values infuence all neighbour pixels
- Larger window means more blurring effect and loss of edge information







Harmonic mean filter: Calculates the average of rates of the pixels within the window

$$p_{(y,x)} = \frac{n^2}{\sum_{i=-n/2}^{i=n/2} \sum_{j=-n/2}^{j=n/2} \left(\frac{1}{p(y+i,x+j)}\right)}$$

$$p_{(1,1)} = \frac{3^2}{\frac{1}{1} + \frac{1}{1} + \frac{1}{3} + \frac{1}{2} + \frac{1}{3} + \frac{1}{9} + \frac{1}{2} + \frac{1}{1} + \frac{1}{3}} = 1,8^{\frac{er \text{ gets}}{1}}$$

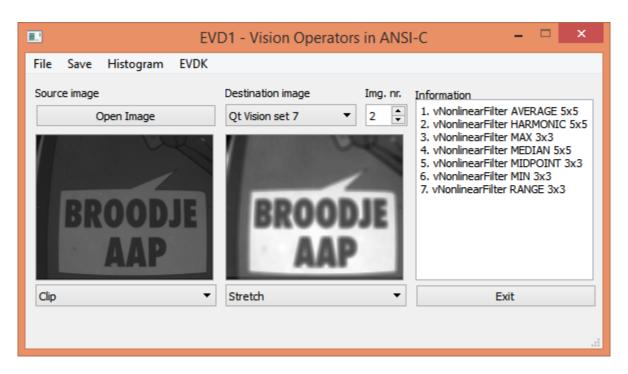
$$p_{(1,2)} = \frac{3^2}{\frac{1}{1} + \frac{1}{3} + \frac{1}{1} + \frac{1}{3} + \frac{1}{1} + \frac{1}{3} + \frac{1}{1} + \frac{1}{3} + \frac{1}{1}} = 1,6$$





Harmonic mean filter:

- Used to remove positive outlier noise pixels
- Larger window means more blurring effect and loss of edge information

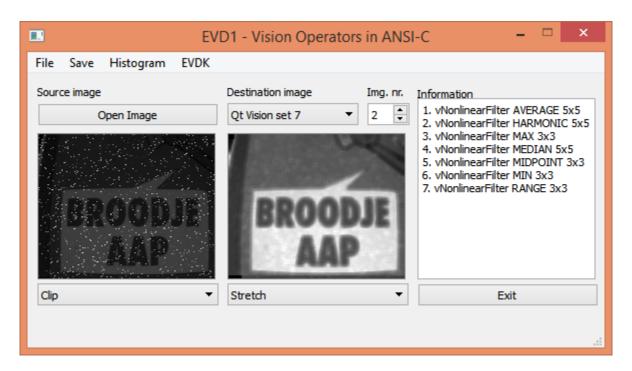






Harmonic mean filter:

- Used to remove positive outlier noise pixels
- Larger window means more blurring effect and loss of edge information

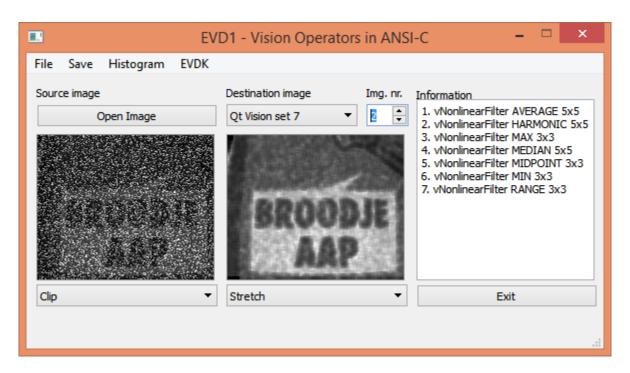






Harmonic mean filter:

- Used to remove positive outlier noise pixels
- Larger window means more blurring effect and loss of edge information







Max filter: Selects the maximum pixel value from the window

0
1 1 3 1
2 9 9 2
2 1 3 1
0 2 2 1

$$p_{(y,x)} = \max \left[window(y+i, x+j) \right]_{i=-n/2}^{i=n/2} j=n/2$$

$$p_{(1,1)} = \max[1,1,3,2,3,9,2,1,3] = 9$$

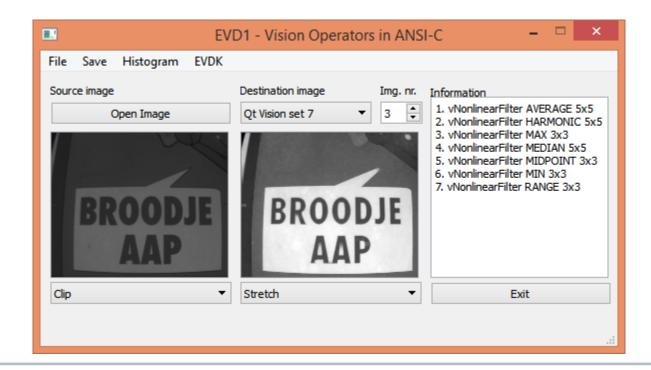
$$p_{(1,2)} = \max[1,3,1,3,9,2,1,3,1] = 9$$





Maximum filter:

- Used to remove <u>lower</u> value noise pixels
- Can also be used for binary dilation

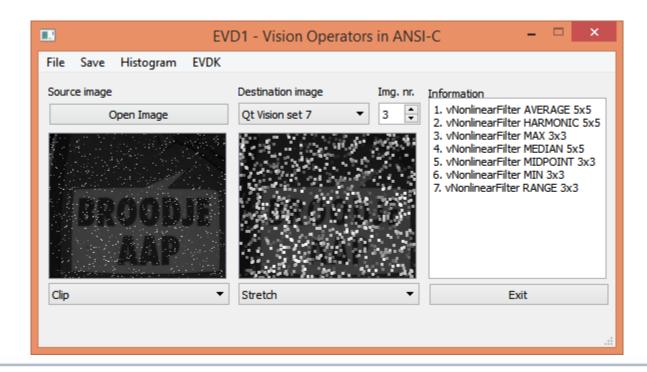






Maximum filter:

- Used to remove <u>lower</u> value noise pixels
- Can also be used for binary dilation

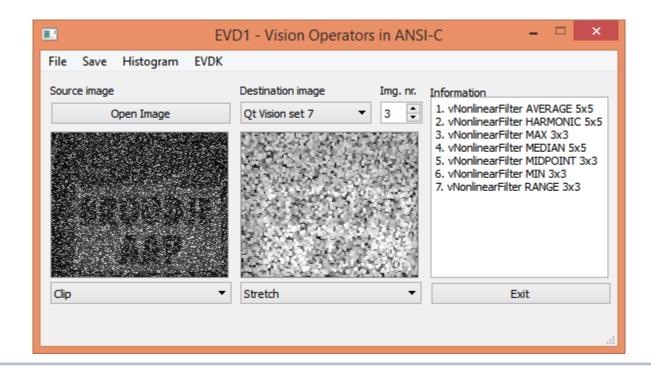






Maximum filter:

- Used to remove <u>lower</u> value noise pixels
- Can also be used for binary dilation







Min filter: Selects the minimum pixel value from the window

0
1 1 3 1
2 1 1 2
2 1 3 1
0 2 2 1

$$p_{(y,x)} = \min \left[window(y+i,x+j) \right]_{i=-n/2}^{i=n/2} j=-n/2$$

$$p_{(1,1)} = \min[1,1,3,2,3,9,2,1,3] = 1$$

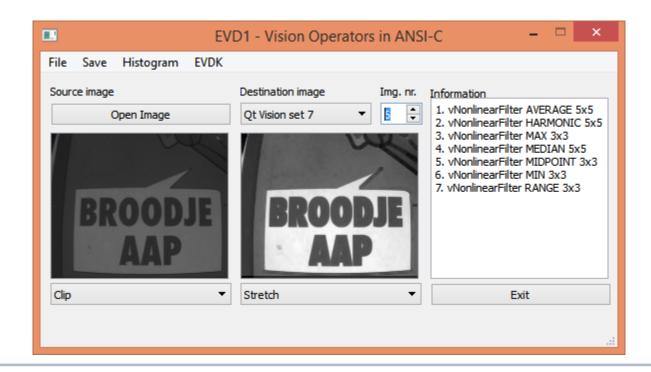
$$p_{(1,2)} = \min[1,3,1,3,9,2,1,3,1] = 1$$





Minimum filter:

- Used to remove <u>positive</u> value noise pixels
- Can also be used for binary erosion

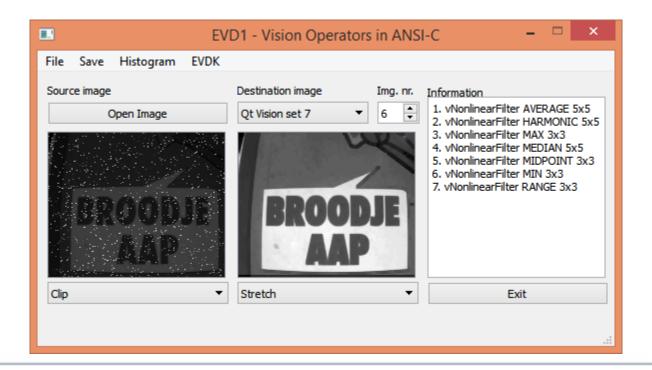






Minimum filter:

- Used to remove <u>positive</u> value noise pixels
- Can also be used for binary erosion

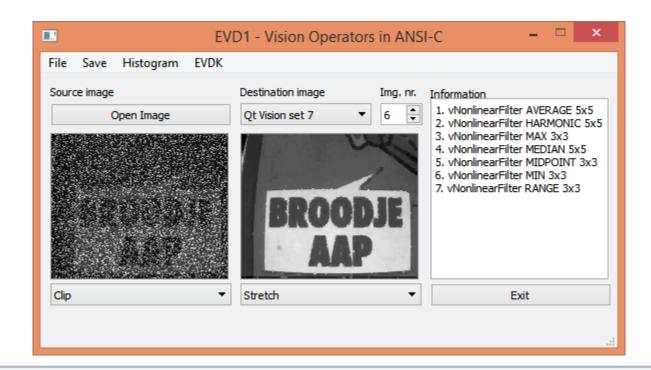






Minimum filter:

- Used to remove <u>positive</u> value noise pixels
- Can also be used for binary erosion







Midpoint filter: Calculates the average of the maximum and minimum pixel value within the window

0
1 1 3 1
2 5 5 2
2 1 3 1
0 2 2 1

$$p_{(1,1)} = \frac{9+1}{2} = 5$$

$$p_{(1,2)} = \frac{9+1}{2} = 5$$

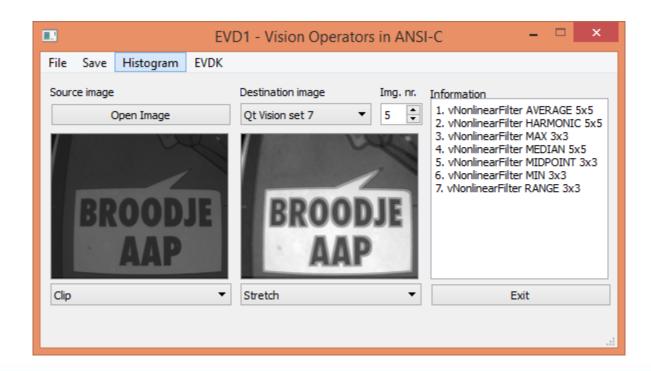
$$p_{(y,x)} = \frac{\max\left[window(y+i,x+j)\right]_{i=-n/2}^{i=n/2} j=n/2}{2} + \min\left[window(y+i,x+j)\right]_{i=-n/2}^{i=n/2} j=n/2}{2}$$





Midpoint filter:

Used to remove short tailed noise pixels

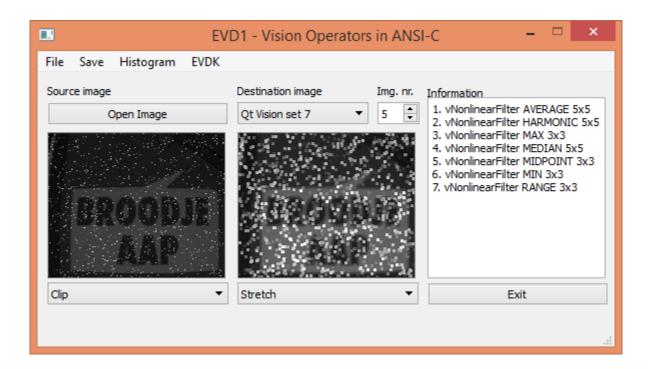






Midpoint filter:

Used to remove short tailed noise pixels

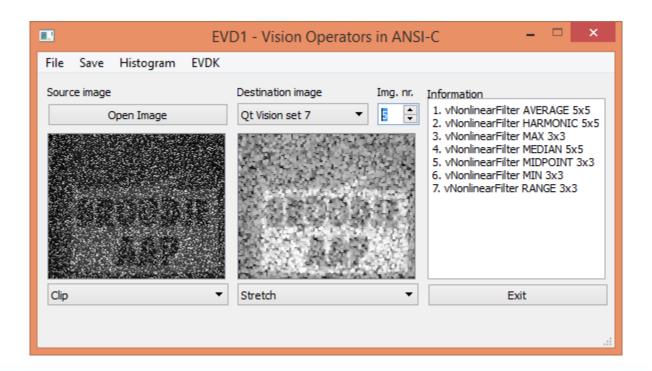






Midpoint filter:

Used to remove short tailed noise pixels







Median filter: Selects the median pixel value from the window

(by sorting the pixels and selecting the center value)

 0
 1
 1
 3
 1
 ...
 ...

 2
 2
 2
 2
 ...
 ...

 2
 1
 3
 1
 ...
 ...

 0
 2
 2
 1
 ...
 ...

$$p_{(y,x)} = median \left[window(y+i,x+j) \right]_{i=-n/2}^{i=n/2} j=-n/2$$

$$p_{(1,1)} = \text{median}[1,1,3,2,3,9,2,1,3] = median[1,1,1,2,2,3,3,3,9] = 2$$

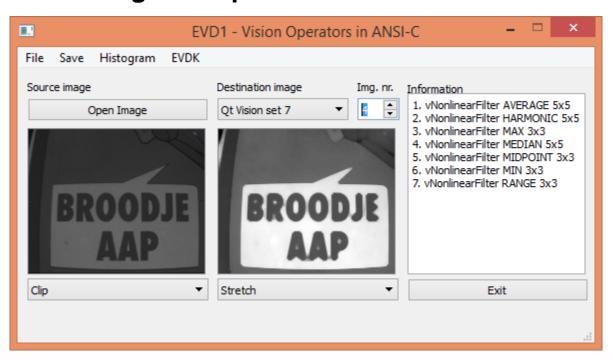
$$p_{(1,2)} = \text{median}[1,3,1,3,9,2,1,3,1] = median[1,1,1,1,2,3,3,3,9] = 2$$





Median filter:

- Used to remove outlier noise
- Used to remove <u>tailed</u> noise pixels
- Performs much better than the average filter, because edges are preserved

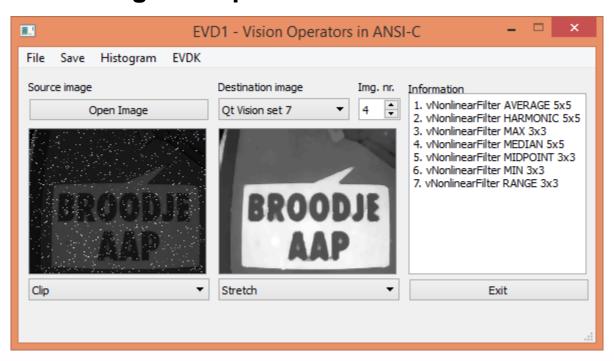






Median filter:

- Used to remove outlier noise
- Used to remove <u>tailed</u> noise pixels
- Performs much better than the average filter, because edges are preserved

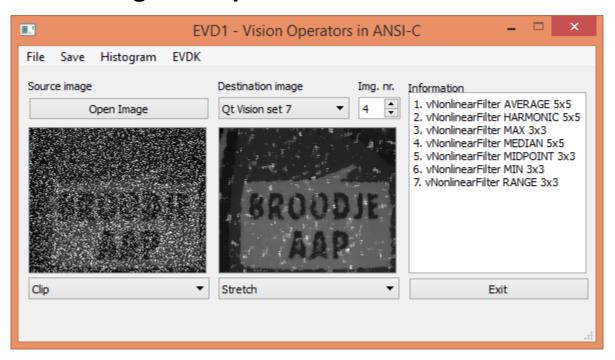






Median filter:

- Used to remove outlier noise
- Used to remove <u>tailed</u> noise pixels
- Performs much better than the average filter, because edges are preserved







Rangefilter: Calculates the difference of the maximum and minimum pixel value within the window

	0				
0	1	1	3	1	
	2	8	8	2	
	2	1	3	1	
	0	2	2	1	

$$p_{(1,1)} = 9 - 1 = 8$$

 $p_{(1,2)} = 9 - 1 = 8$

$$p_{(1,2)} = 9 - 1 = 8$$

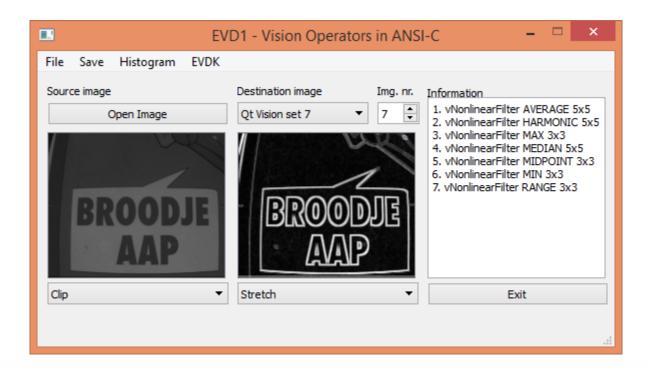
$$p_{(y,x)} = max \left[window(y+i,x+j) \right]_{i=-n/2}^{i=n/2} j=n/2 - min \left[window(y+i,x+j) \right]_{i=-n/2}^{i=n/2} - min \left[window(y+i,x+j) \right]_{i=-n/2}$$





Range filter:

Used to find edges (if there is no noise)

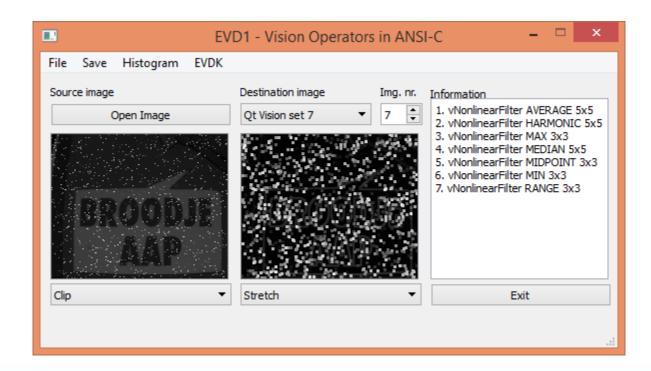






Range filter:

Used to find edges (if there is no noise)

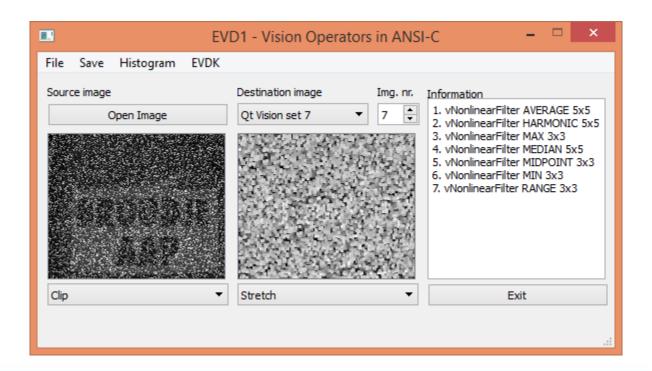






Range filter:

Used to find edges (if there is no noise)







How to handle edge pixels?

1	đ	1	3	1	
P	1	1	3	1	
2	2	3	9	2	
2	2	1	3	1	
	0	2	2	1	

- 1. Do not handle them at all!
- 2. Only use available pixels
- 3. Extend edges

Example:

Average
$$p_{(0,0)} = \frac{1}{4} \times (1+1+2+3) = 1,75$$





Opdracht

Implement the function vNonlinearFilter()

Aangezien we met een variabel window moeten kunnen werken is het erg rekenintensief om ervoor te zorgen dat het src image ook de dst moet kunnen zijn.

Alléén voor deze operator: src ≠ dst

Dat betekent dat op de target deze operator als eerste aangeroepen moet worden!





Opdracht

Geef in je logboek een verklaring voor alle filters waarom het filter juist wel of geen goed resultaat geeft bij het 'filters' plaatje met veel ruis.

