



Computer vision

2D Camera Calibration

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2D Camera Calibration

Overview:

- Introduction
- Coordinate systems
- Camera parameters
- Calibration pattern
- Find calibration points
- Camera Calibration
- Pixel to world coordinate
- Correct for optical distortion

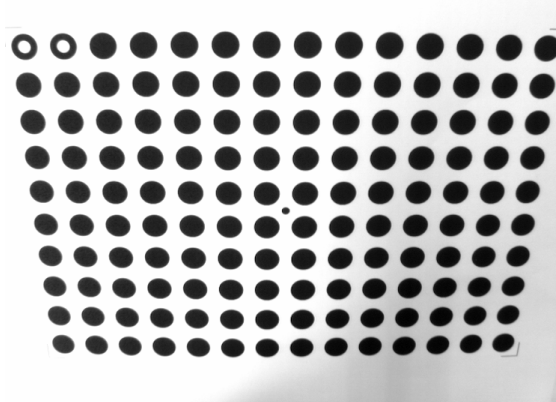
28-aug-08

2D Camera Calibration

2

Introduction

Problems in measuring the real size of 2D objects



28-aug-08

2D Camera Calibration

3

Introduction

Some problems in measuring the real size of 2D objects:

- Camera is tilted
- Dimensions of pixels horizontal and vertical are different
- Distance of object from camera
- Focal length of lens
- Lens distortion
- Mismatch frequency of frame grabber and analogue camera (*)
- Non-alignment of optical axis of camera ccd and lens

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4

Coordinate systems

Pixel coordinates:

- Measured from the image
- Unit in pixels
- Origin: top left corner
- X values increase from left to right
- Y values increase from top to bottom

World coordinates:

- User defined

In order to measure the real size of objects there must be a mapping from each pixel coordinate to a world coordinate.

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5

Camera parameters

Camera parameters:

- Interior parameters:
determined by the internal geometry of the camera and the properties of the frame grabber
- Exterior parameters:
determined by the position and orientation of the camera relative to the world coordinate system

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6

Interior parameters

- **Geometry of ccd chip:**
 - **dx:** center-to-center distance of pixels in x direction
 - **dy:** center-to-center distance of pixels in y direction
- **Principal point (alignment of optical axis of ccd and lens) :**
 - **xp:** x-coordinate for principal point, relative to center of image
 - **yp:** y-coordinate for principal point, relative to center of image
- **Camera constant:**
 - **f:** \leq focal length, at infinity = focal length
- **Lens distortion coefficients:**
 - **kappa1:** first order lens distortion coefficient
 - **kappa2:** second order lens distortion coefficient
 - **kappa3:** third order lens distortion coefficient
- **Frame grabber property:**
 - **sx:** scale factor for timing digitizer

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7

Exterior parameters

- **Rigid body transform:**
 - **Rx:** rotation around x-axis
 - **Ry:** rotation around y-axis
 - **Rz:** rotation around z-axis
 - **Tx:** translation in x direction
 - **Ty:** translation in y direction
 - **Tz:** translation in z direction

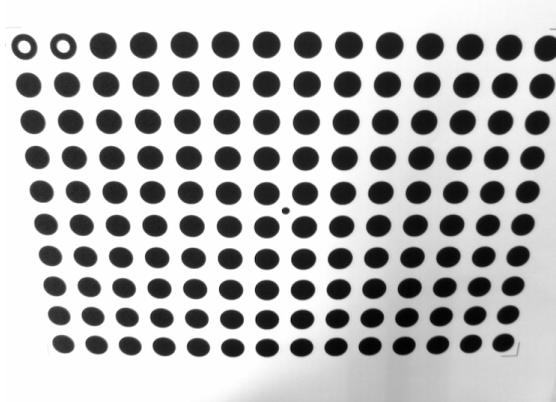
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8

Calibration Pattern

A fixed pattern of circles is used to calibrate the camera



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9

Find calibration points

**camera findcalpoints imageName nrRows nrCols minPixels
maxPixels**

This operator examines a binary image with imageName in order to find the calibration points.

A fixed pattern of circles is expected with nrCols circles vertical and nrRows circles horizontal.

Each circle has minimal minPixels and maximal maxPixels. The positions of the calibration points are displayed on the screen.

28-aug-08

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10

Demonstration Find calibration points

Demonstration:

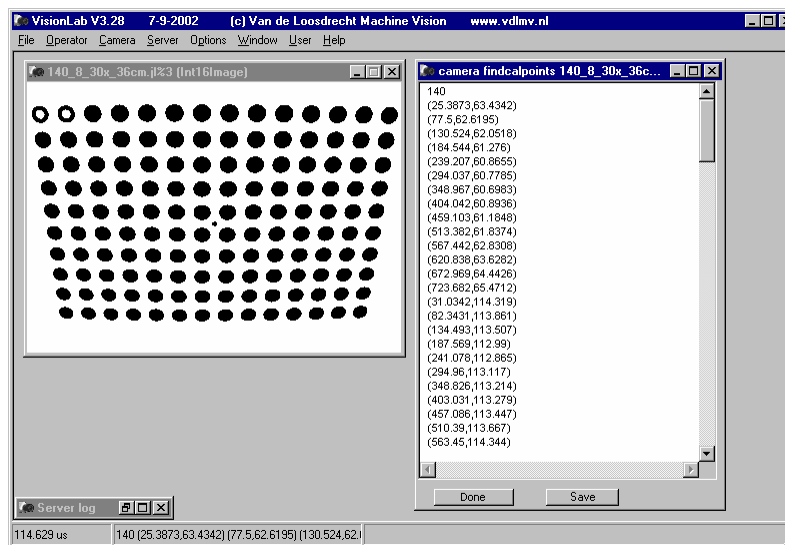
- Open image 140_8_30x_36cm.jl
- ThresholdIsoData DarkObject
- camera findcalpoints 10 14 300 2000
- Examine results

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11

Demonstration Find calibration points



28-aug-08

2D Camera Calibration

12

Camera Calibration

The 140 calibration points are used to find optimal values for the 15 camera parameters.

So there are 140 equations with 15 unknown parameters. The parameter space has 15 dimensions and consists of polynomial and goniometric equations.

This non-linear optimisation problem is solved in VisionLab with a combination of a Genetic Algorithm and Hill Climbing.

28-aug-08

2D Camera Calibration

13

Demonstration Camera Calibration

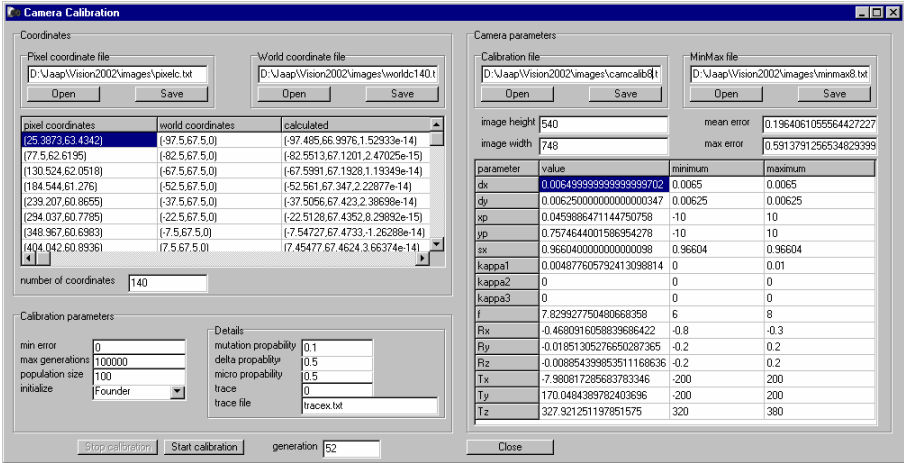
- Open dialog camera calibration
 - Pixel coordinate file: pixelc.txt
 - World coordinate file: worldc140.txt
 - Calibration file: camcalib8.txt
 - MinMax file: minmax8.txt
- Start calibration with:
 - Population size = 100
 - Mutation prop = 0.1
 - Delta prop = 0.5
 - Micro prop = 0.5

28-aug-08

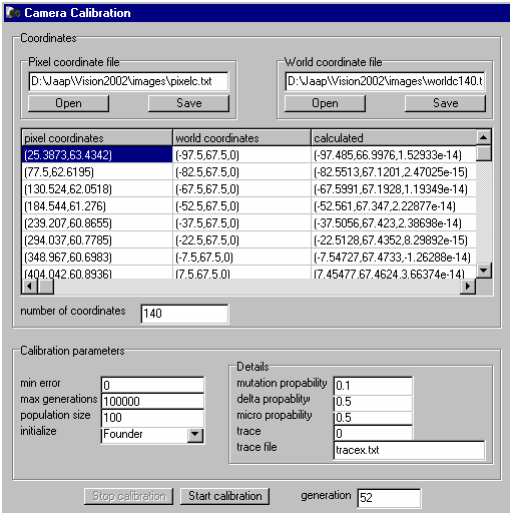
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14

Demonstration Camera Calibration



Left part Camera Calibration screen



Right part Camera Calibration screen

Camera parameters

Calibration file

D:\Jaap\Vision2002\images\camcalib8.t

OpenSave

MinMax file

D:\Jaap\Vision2002\images\minmax8.txt

OpenSave

image height

540

image width

748

mean error

0.1964061055564427227

max error

0.5913791256534829399

parameter	value	minimum	maximum
dx	0.00649999999999999702	0.0065	0.0065
dy	0.006250000000000000347	0.00625	0.00625
xp	0.0459886471144750758	-10	10
yp	0.7574644001586954278	-10	10
sx	0.96604000000000000098	0.96604	0.96604
kappa1	0.004877605792413098814	0	0.01
kappa2	0	0	0
kappa3	0	0	0
f	7.829927750480668358	6	8
Rx	-0.4680916058839686422	-0.8	-0.3
Ry	-0.01851305276650287365	-0.2	0.2
Rz	-0.008854399853511168636	-0.2	0.2
Tx	-7.980817285683783346	-200	200
Ty	170.0484389782403696	-200	200
Tz	327.921251197851575	320	380

Close

Pixel to world coordinate

camera pixelctoworldc pixelCoord camcalibfile

This operator translates a pixelCoordinate to a worldCoordinate using a calibration file camcalibfile.

Demonstration Pixel to world coordinate

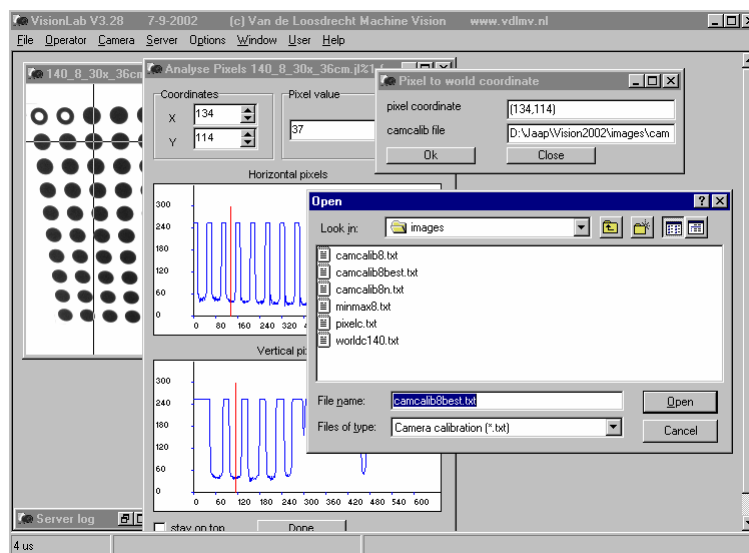
- Open image 140_8_30x_36cm.ji
- Find coordinate of pixel to convert to world coordinate
- Use in camera menu function Pixel to world coordinate
 - Fill in chosen pixel coordinate
 - Click on camcalib file field and select camera calibration file camcalib8best.txt
 - Execute function and see result in result bar

28-aug-08

2D Camera Calibration

19

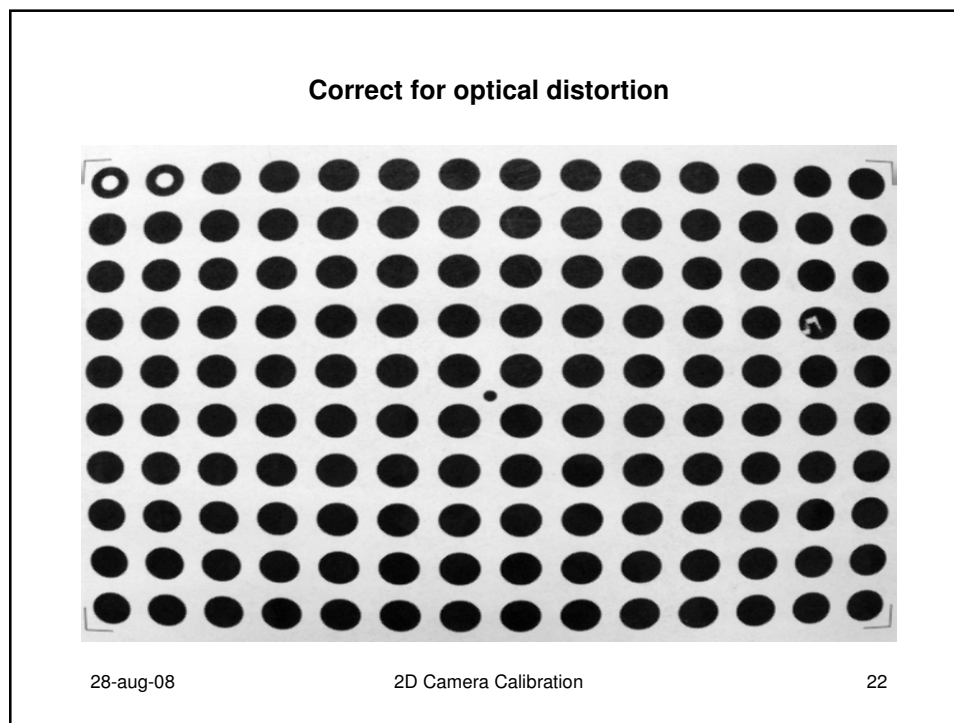
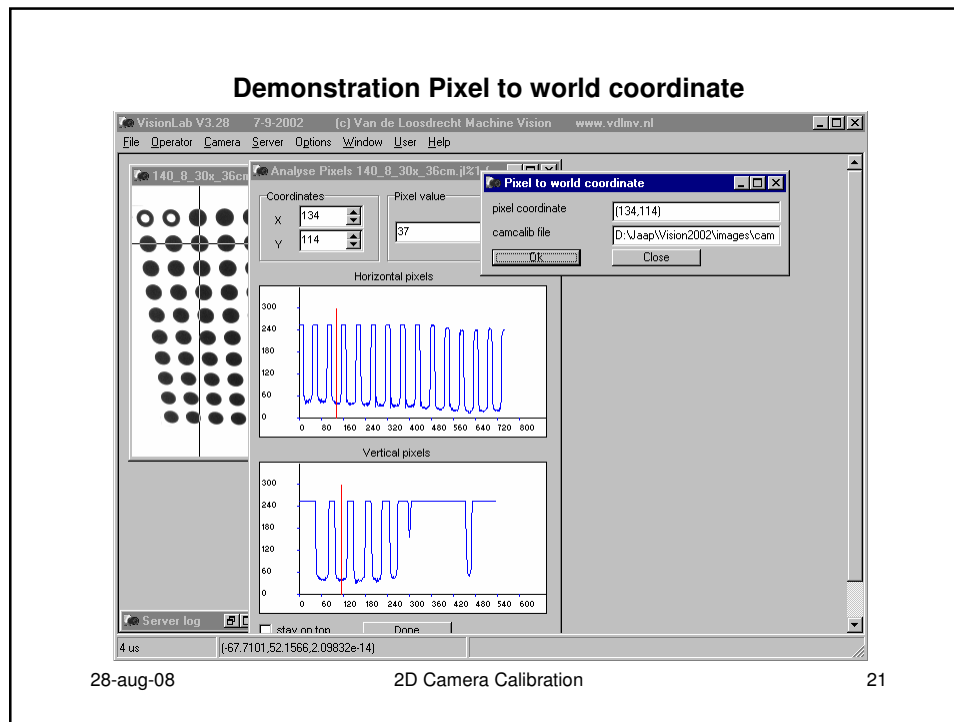
Demonstration Pixel to world coordinate



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20



Correct for optical distortion (*)

CorrectXYCoord (xyCoord, heightImage, widthImage, principal_point, sx, dx, dy, kappa1, kappa2, kappa3)

Camera CorrectCoord2D (Coord2D, heightImage, widthImage, principal_point, sx, dx, dy, kappa1, kappa2, kappa3)

This operators corrects the "barrel shape" lens distortion for one pixel coordinate

Camera CamDistortion (srcImage, destImage, principal_point, sx, dx, dy, kappa1, kappa2, kappa3)

This operator corrects the "barrel shape" lens distortion in the whole image

28-aug-08

2D Camera Calibration

23

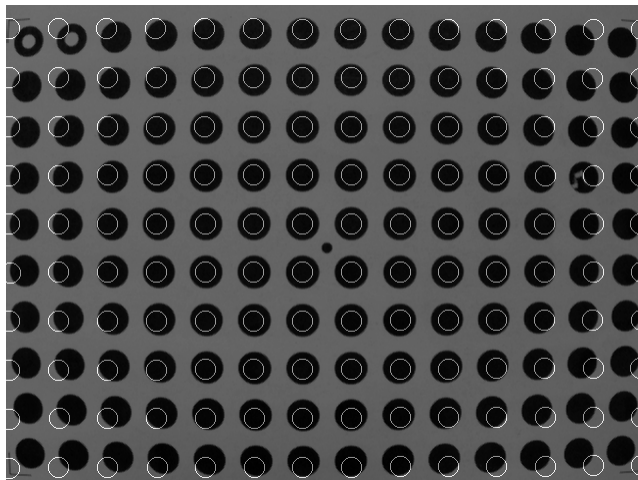
Demonstration Correct for optical distortion

- Close open images
- (note image taken with different camera as previous example, we are now interested only in the optical distortion)
- Show position of centre circles:
 - run script correct_distortion.js
- Open file distortion.jl
- (Show corrected image:
 - CamDistortion (0,0) 1 0.0099 0.0099 0.00555 0 0)

28-aug-08

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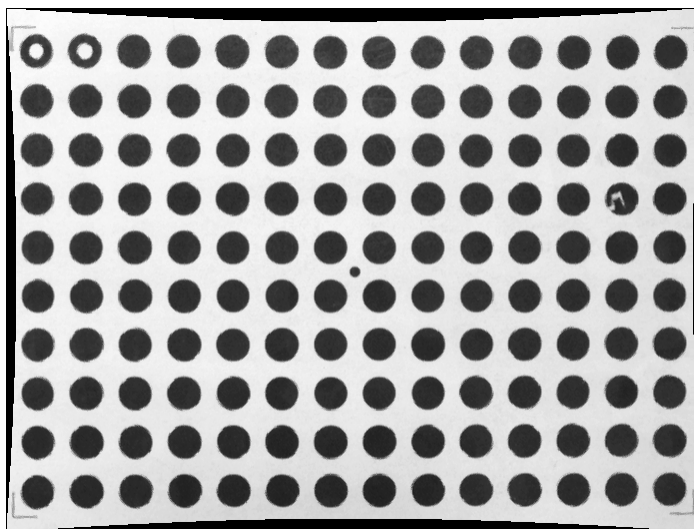
24

Positions of centre circles

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25

Corrected image

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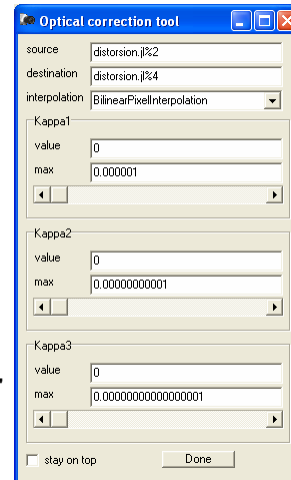
2D Camera Calibration

26

Optical correction tool

Used for interactively correcting optical distortions.

Note: Note the kappa's for this operator are different from the kappa's used by CamDistortion.
 This operator performs "the inverse operation" and is much faster than CamDistortion.
 See Geometry menu.

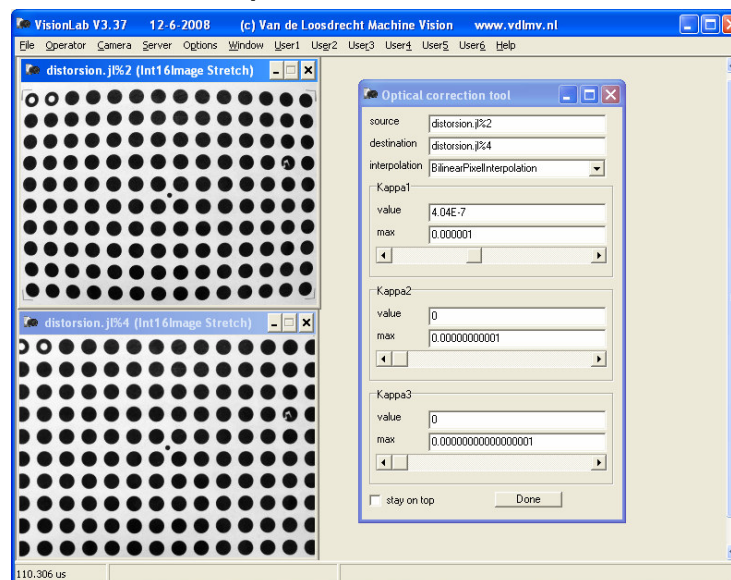


28-aug-08

2D Camera Calibration

27

Optical correction tool

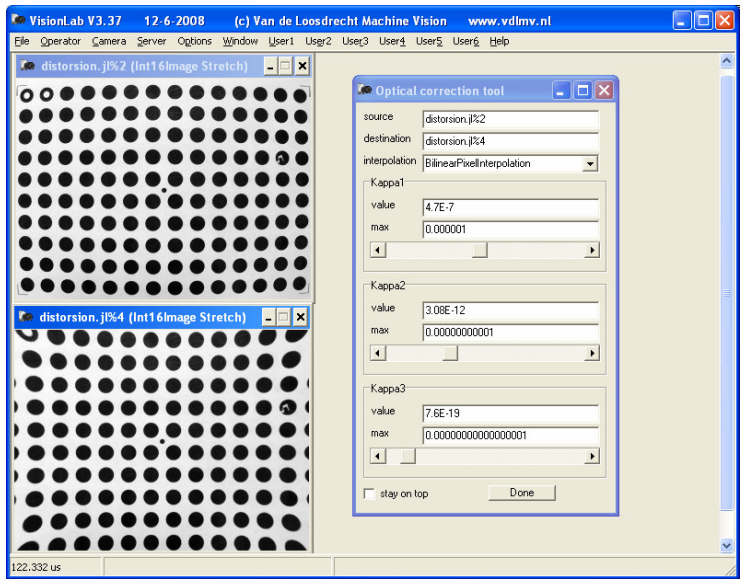


28-aug-08

2D Camera Calibration

28

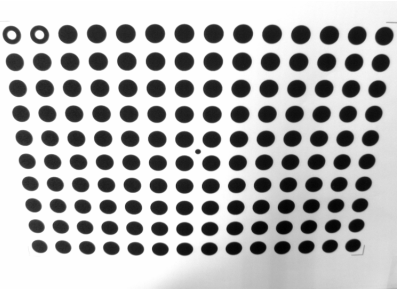
Optical correction tool



The screenshot shows the VisionLab V3.37 interface with the Optical correction tool. The tool is used to correct optical distortion in images. It displays two images: 'distorsion.j%2 (Int16Image Stretch)' and 'distorsion.j%4 (Int16Image Stretch)'. The tool settings include source, destination, interpolation, and Kappa1, Kappa2, Kappa3 values.

28-aug-08 2D Camera Calibration 29

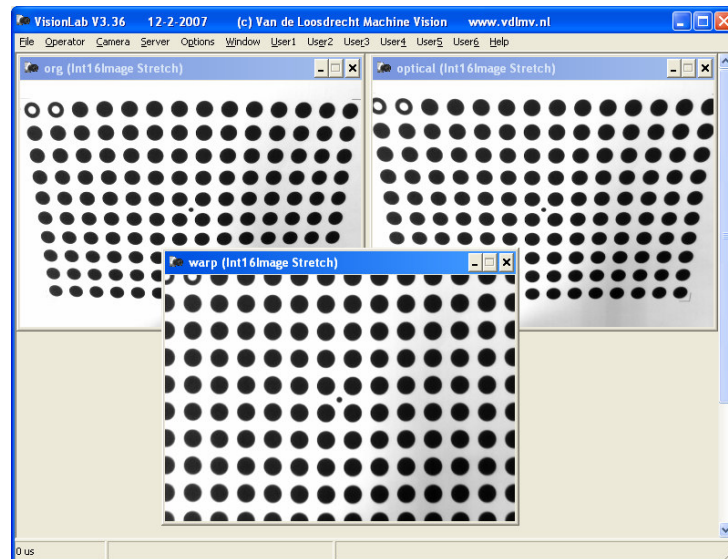
Exercise correct distortion



- Use image 140_8_30x_36cm.jl
- Correct both optical distortion and distortion by tilting

Answer: correct_opt_warp.jls

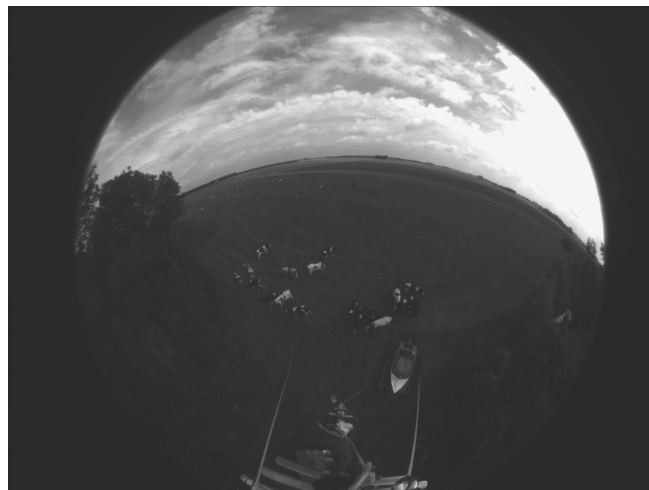
28-aug-08 2D Camera Calibration 30

Original -> Optical correction -> Warp

28-aug-08

2D Camera Calibration

31

Fish Eye lens

28-aug-08

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32

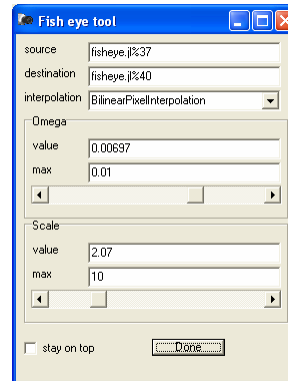
Fish Eye Tool

Used for interactively correcting Fish Eye distortions.

If omega is positive an image taken with a fish eye objective will be stretched flat. With a negative omega a normal image can be transformed to a fish eye image.

A good starting point for experimenting with a value for omega = $\pi / (\text{diameter fish eye circle in pixels})$.

The scale factor specifies a the zoom factor.

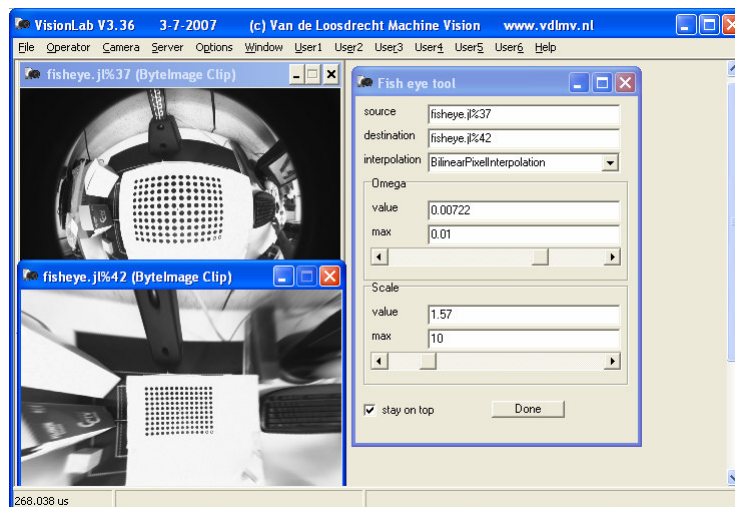


28-aug-08

2D Camera Calibration

33

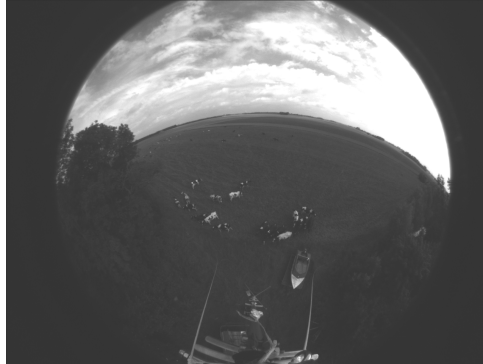
Fish Eye Tool (on image fisheye.jl)



28-aug-08

2D Camera Calibration

34

Exercise correct distortion

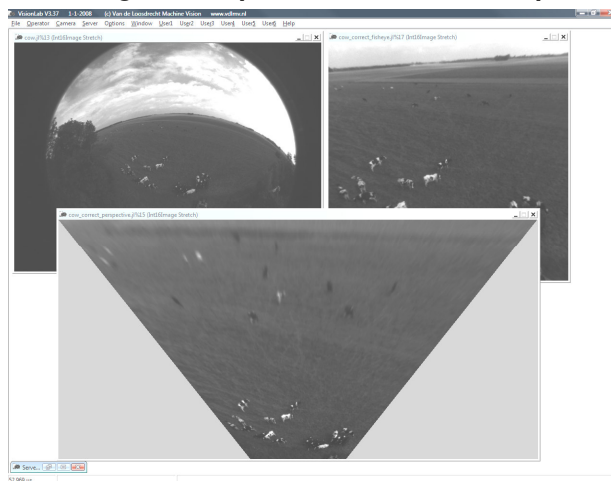
- Use image cow.jpg
- Correct both optical distortion and distortion by tilting

Answer: cow_correct.js

28-aug-08

2D Camera Calibration

35

Original -> Optical correction -> Warp

- All objects are of the same size, regardless of the distance to the camera
- Advantage: Binary or Greyscale filters can have fixed sizes

28-aug-08

2D Camera Calibration

36

Fish Eye correction operator (*)

**FishEye srcImage destImage height width omega scale border
interpolation**

Menu: Operator | Geometry

This operator performs a FishEye transform. If omega is positive an image taken with a fish eye objective will be stretched flat. With a negative omega a normal image can be transform to a fish eye image.

A good starting point for experimenting with a value for omega = π / (diameter fish eye circle in pixels) .

The scale factor specifies a the zoom factor.

The parameters height and width determine the size of the destination image.

The specified border value will be used as result pixel if information outside the source image is necessary for the calculation.

28-aug-08

2D Camera Calibration

37