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```
% Joel Lubinitsky - 02/04/15  
% MAE 321 - HW 3.3
```

```
clear all  
close all  
clc
```

Problem 4:

Calculate the natural frequency and damping ratio for the system in Figure P1.91 given the values $m = 10$ kg, $c = 100$ kgs, $k_1 = 4000$ N/m, $k_2 = 200$ N/m, and $k_3 = 1000$ N/m. Assume that no friction acts on the rollers. Is the system overdamped, critically damped, or underdamped?

Unknown: ζ

Known

```
mass = 10;  
coefficientDamping = 100;  
stiffness1 = 4000;  
stiffness2 = 200;  
stiffness3 = 1000;
```

Calculations

$$\zeta = \frac{c}{c_{cr}}$$

$$c_{cr} = 2\sqrt{k_{eff}m}$$

$$k_{eff} = k_1 + \frac{k_2 k_3}{k_2 + k_3}$$

Therefore,

$$\zeta = \frac{c}{2\sqrt{k_1 + \frac{k_2 k_3}{k_2 + k_3}}m}$$

```
stiffnessEffective = stiffness1 + stiffness2 * stiffness3 / (stiffness2 + stiffness3);  
coefficientDampingCritical = 2 * sqrt(stiffnessEffective * mass);  
ratioDamping = coefficientDamping / coefficientDampingCritical
```

ratioDamping =

0.2449

Results

System is underdamped because $\zeta < 1$

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