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```
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% MAE 321 - HW 8.2  
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```

```
clear all  
close all  
clc
```

## Problem 2:

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For the example we did in class on 4 March, use Matlab to plot the transmissibility ratio for a range of damping coefficients. Use at least 5 values of  $c$ , and they should mostly span the range for underdamped responses. Include figures both for the transmissibility plotted as a function of the base excitation frequency, and as a function of the frequency ratio. (reminder:  $m = 100\text{kg}$ ,  $k = 2000\text{N/m}$ ,  $Y = 0.03\text{m}$ ,  $\omega_b = 6\text{rad/s}$ )

## Known

---

$m$ ,  $k$ ,  $Y$ ,  $\omega_b$

```
mass          = 100; % kg  
stiffness     = 2000; % N/m  
amplitudeBase = 0.03; % m  
num = 1000;  
frequencyBase = linspace(0, 10, num); % rad/s
```

## Calculations

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$$\omega_n = \sqrt{\frac{k}{m}}$$

$$r = \frac{\omega_b}{\omega_n}$$

$$\zeta = \frac{c}{2\sqrt{km}}$$

$$\frac{X}{Y} = \left[ \frac{1 + (2\zeta r)^2}{(1 - r^2)^2 + (2\zeta r)^2} \right]^{1/2}$$

```
frequencyNatural = sqrt(stiffness / mass);  
ratioFrequency   = frequencyBase ./ frequencyNatural;  
ratioDamping     = @(c) c / (2 * sqrt(stiffness * mass));
```

```

ratioTrans      = @(c) sqrt((1 + (2 .* ratioDamping(c) .* ratioFrequency) .^ 2) ./...
                        ((1 - ratioFrequency .^ 2) .^ 2 ...
                        + (2 .* ratioDamping(c) .* ratioFrequency) .^ 2));

coefficientDamping = linspace(200, 800, 5);
transmissibility   = zeros(num, 5);

for n = [1 : 5]

    transmissibility(:, n) = ratioTrans(coefficientDamping(n));

end

```

## Plots

```

figure(1)
hold on
xlabel('Base Frequency, \omega_b')
ylabel('Transmissibility Ratio, X/Y')
title('Transmissibility vs Base Frequency')
axis([0 frequencyBase(end) 0 3])

plot(frequencyBase, transmissibility(:, 1), '-', 'color', [0 0 0])
plot(frequencyBase, transmissibility(:, 2), '--', 'color', [0 0 0])
plot(frequencyBase, transmissibility(:, 3), '.', 'color', [0 0 0])
plot(frequencyBase, transmissibility(:, 4), ':', 'color', [0 0 0])
plot(frequencyBase, transmissibility(:, 5), '-.', 'color', [0 0 0])

legend('c = 200', 'c = 350', 'c = 500', 'c = 650', 'c = 800')

figure(2)
hold on
xlabel('Frequency Ratio, r')
ylabel('Transmissibility Ratio, X/Y')
title('Transmissibility vs Frequency Ratio')
axis([0 ratioFrequency(end) 0 3])

plot(ratioFrequency, transmissibility(:, 1), '-', 'color', [0 0 0])
plot(ratioFrequency, transmissibility(:, 2), '--', 'color', [0 0 0])
plot(ratioFrequency, transmissibility(:, 3), '.', 'color', [0 0 0])
plot(ratioFrequency, transmissibility(:, 4), ':', 'color', [0 0 0])
plot(ratioFrequency, transmissibility(:, 5), '-.', 'color', [0 0 0])

legend('c = 200', 'c = 350', 'c = 500', 'c = 650', 'c = 800')

```



