COMPUTER SCIENCE MENTORS

September 28, 2020 to October 1, 2020

Lists

Lists Introduction:

for item in 1st:

do things

Lists are type of sequence, which means they are an ordered collection of values that has both length and the ability to select elements.

```
>>> lst = [1, False, [2, 3], 4] \# a list can contain anything
>>> len(lst)
>>> lst[0]
                 # Indices of a list only go up to the len(lst)
>>> lst[4]
Error: list index out of range
We can iterate over lists using their index, or iterate of elements directly
for index in range(len(lst)):
        # do things
```

List comprehensions are a useful way to iterate over lists when your desired result is a

```
new_list2 = [<expression> for <element> in <sequence> if <</pre>
   condition>1
```

We can use **list splicing** to create a copy of a certain portion or all of a list

1. What would Python display? Draw box-and-pointer diagrams for the following:

```
>>> a = [1, 2, 3]
>>> a
[1, 2, 3]
>>> a[2]
3
>>> b = a
>>> a = a + [4, [5, 6]]
>>> a
[1, 2, 3, 4, [5, 6]]
>>> b
[1, 2, 3]
>>> c = a
>>> a = [4, 5]
>>> a
[4, 5]
>>> C
[1, 2, 3, 4, [5, 6]]
>>> d = c[3:5]
>>> c[3] = 9
>>> d
[4, [5, 6]]
>>> c[4][0] = 7
>>> d
[4, [7, 6]]
>>> c[4] = 10
>>> d
[4, [7, 6]]
>>> C
[1, 2, 3, 9, 10]
```

2. Draw the environment diagram that results from running the code.

```
def reverse(lst):
    if len(lst) <= 1:
        return lst
    return reverse(lst[1:]) + [lst[0]]

lst = [1, [2, 3], 4]
rev = reverse(lst)</pre>
```

https://goo.gl/6vPeX9 We call reverse recursively 3 times and open 3 new frames, each time passing through a shallow copy of the list without the first element lst[1:]. We then return the list '[4]' back up after hitting the base case of a length 1 list. At each level, we take the list returned from the smaller recursive call and append 'lst[0]' to the end of returned list. When you pass in a list as an argument to a function the new frame's argument points to the same list passed in (does not create a new list) List slices create shallow copies (a new list is created but any pointers in the new list still point to the same thing that the original list that was sliced is pointing to) Keep in mind that the return value of the reverse function is a new list because of the '+ [lst[0]]'

3. Write a function that takes in a list nums and returns a new list with only the primes from nums. Assume that is_prime(n) is defined. You may use a while loop, a for loop, or a list comprehension.

```
def all_primes(nums):
    result = []
    for i in nums:
        if is_prime(i):
            result = result + [i]
    return result

List comprehension:
    return [x for x in nums if is_prime(x)]
```

Data Abstraction Overview:

Abstraction allows us to create and access different types of data through a controlled, restricted programming interface, hiding implementation details and encouraging programmers to focus on how data is used, rather than how data is organized. The two fundamental components of a programming interface are a constructor and selectors.

- 1. Constructor: The interface that creates a piece of data; e.g. calling t = tree(3) creates a new tree object and assigns it to t.tree() is a constructor.
- 2. Selectors: The interface by which we access attributes of a piece of data; e.g. calling branches(t) and is_leaf(t) return different attributes of a tree (a list of branches and whether the tree is a leaf, respectively). branches() and is_leaf() are both selectors.

Through constructors and selectors, a data type can hide its implementation, and a programmer doesn't need to *know* its implementation to *use* it.

1. The following is an **Abstract Data Type (ADT)** for elephants. Each elephant keeps track of its name, age, and whether or not it can fly. Given our provided constructor, fill out the selectors:

```
def elephant(name, age, can_fly):
    """
    Takes in a string name, an int age, and a boolean can_fly.
    Constructs an elephant with these attributes.
    >>> dumbo = elephant("Dumbo", 10, True)
    >>> elephant_name(dumbo)
    "Dumbo"
    >>> elephant_age(dumbo)
    10
    >>> elephant_can_fly(dumbo)
    True
    """
    return [name, age, can_fly]

def elephant_name(e):
    return e[0]

def elephant_age(e):
    return e[1]
```

```
def elephant_can_fly(e):
    return e[2]
```

2. This function returns the correct result, but there's something wrong about its implementation. How do we fix it?

```
def elephant_roster(elephants):
    """
    Takes in a list of elephants and returns a list of their
        names.
    """
    return [elephant[0] for elephant in elephants]

elephant[0] is a Data Abstraction Violation (DAV). We should use a selector instead. The corrected function looks like:
    def elephant_roster(elephants):
        return [elephant_name(elephant) for elephant in elephants]
```

3. Fill out the following constructor for the given selectors.

```
def elephant(name, age, can_fly):
    return [[name, age], can_fly]
def elephant_name(e):
    return e[0][0]
def elephant_age(e):
    return e[0][1]
def elephant_can_fly(e):
    return e[1]
```

4. How can we write the fixed elephant_roster function for the constructors and selectors in the previous question?

No change is necessary to fix elephant_roster since using the elephant selectors "protects" the roster from constructor definition changes.

5. **(Optional)** Fill out the following constructor for the given selectors.

```
def elephant(name, age, can_fly):
    11 11 11
    >>> chris = elephant ("Chris Martin", 38, False)
    >>> elephant_name(chris)
    "Chris Martin"
    >>> elephant_age(chris)
    >>> elephant_can_fly(chris)
    False
    >> chris("size")
    "Breaking abstraction barrier!"
    def select(command)
        if command == "name":
            return name
        elif command == "age":
            return age
        elif command == "can_fly":
            return can_fly
        return "Breaking abstraction barrier!"
    return select
def elephant name(e):
    return e("name")
def elephant_age(e):
    return e("age")
def elephant_can_fly(e):
    return e("can_fly")
```

What are trees?

A tree has a root label and a sequence of branches. Each branch of a tree is a tree. A tree with no branches is called a leaf. Any tree contained within a tree is called a sub-tree of that tree (such as a branch of a branch). The root of each sub-tree of a tree is called a node in that tree. Trees are a recursive data abstraction, since trees have branches that are trees themselves

Because of this, it often makes sense to solve tree problems using recursion:

- 1. Base case is often when we reach a leaf node
- 2. Recursive case is often when we still need to recurse down, e.g. we haven't hit a leaf yet. Recursive calls need to break the problem into smaller parts, which for trees often means passing in each branch as an input.

When trying to understand and solve tree problems, it is helpful to draw out the tree.

Things to remember:

```
def tree(label, branches=[]):
    return [label] + list(branches)

def label(tree):
    return tree[0]

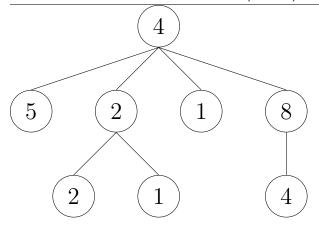
def branches(tree):
    return tree[1:] #returns a list of branches
```

Note: You don't have to worry too much about how trees are actually represented as lists—that's the power of abstraction at work!

As shown above, the tree constructor takes in a label and a list of branches (which are themselves trees).

```
tree(4,
    [tree(5),
    tree(2,
        [tree(2),
        tree(1)]),
    tree(1),
    tree(8,
        [tree(4)])])
```

This creates a tree that looks like this (see next page):



1. Let t be the tree depicted above. What do the following expressions evaluate to? If the expressions evaluates to a tree, format your answer as tree(..., ...). (Note that the Python interpreter wouldn't display trees like this. This is just so you think about trees as an ADT instead of worrying about their implementation.)

```
>>> label(t)
4
>>> branches(t)[1]
tree(2, [tree(2), tree(1)])
>>> branches(branches(t)[1])[1]
tree(1)
```

2. Write the function sum_of_nodes which takes in a tree and outputs the sum of all the elements in the tree.

```
def sum_of_nodes(t):
    """
    >>> t = tree(...) # Tree from question 1.
    >>> sum_of_nodes(t) # 4 + 5 + 2 + 1 + 8 + 2 + 1 + 4 = 27
    27
    """

    total = label(t)
    for branch in branches(t):
        total += sum_of_nodes(branch)
    return total

Alternative solution:
    return label(t) +\
        sum([sum_of_nodes(b) for b in branches(t)])
```

Explanation:

Given that trees are an inherently recursive data type, we can approach this problem similar to a recursion problem.

The first thing we want to look at is the base case. The smallest possible input is just passing in a leaf into the function. In this case our return should just be the label of the leaf so we save that as variable "total".

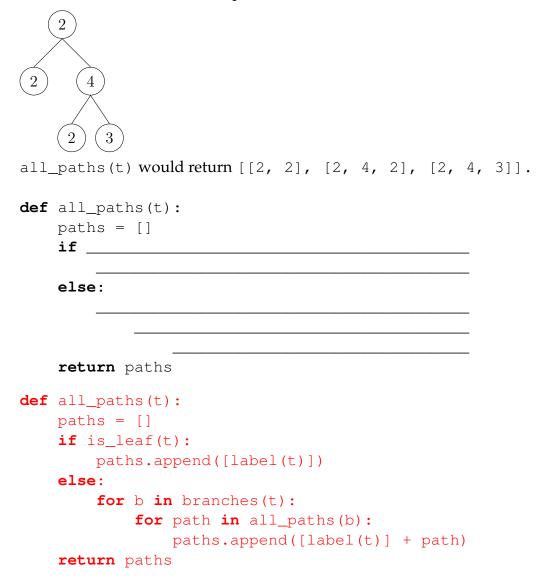
Now we approach the recursive element of the problem where we need to look at all the branches of the tree. All the branches are also trees and we need to find the sums of the branches to add to our total so we can call our function on each branch.

To individually get each branch, we use a for loop iterating over branches(t) and call the function on each branch. Once we have the result of calling the function, we can add it to our total result which is keeping track of the total sum.

Finally, we can return the total. The reason why we don't need a base case of 'if is_leaf(t)' is because our for loop will only run if there are branches and if it is a leaf, it will not run and will skip it and just return the total value which is just the label of the tree.

Note: 'for branch in branches(t)' is a useful way to recurse through a tree and is commonly used in many tree problems! The alternate solution contains the same logic but makes effective use of list comprehension. 'sum' is a useful built-in function in Python to return the sum of a list.

3. Write a function, all_paths that takes in a tree, t, and returns a list of paths from the root to each leaf. For example, if we called all_paths(t) on the following tree:



Explanation:

We begin by making a list to contain all the paths.

If the tree is a leaf, the root is a leaf, so the only path is [label(t)].

Otherwise, for each branch in the tree, we can use recursion to generate all the paths that extend from that branch to a leaf.

Finally, we combine the root label with each branch-starting path to make it a path from the root to a leaf.

Append every path like this to paths, and we have created a list of all paths!

Challenge Problems

Note: These problems are meant to be challenging and may take a long time. Please attempt the previous questions on the worksheet first.

1. Fill in the methods below according to the doctests.

```
def gen_list(n):
    11 11 11
    Returns a nested list structure of n elements where the
    ith element is a list from 0 (inclusive) to i (exclusive).
    >>> gen_list(3)
    [[0], [0, 1], [0, 1, 2]]
    >>> gen_list(5)
    [[0], [0, 1], [0, 1, 2], [0, 1, 2, 3], [0, 1, 2, 3, 4]]
    return
For an additional challenge, try out the following:
def gen increasing(n):
    11 11 11
    Returns a nested list structure of n elements where the
    ith element of each list is one more than the previous
    element (even if the previous is in a prior sublist).
    >>> gen_increasing(3)
    [[0], [1, 2], [3, 4, 5]]
    >>> gen_increasing(5)
    [[0], [1, 2], [3, 4, 5], [6, 7, 8, 9], [10, 11, 12, 13,
    1411
    11 11 11
    return
Hint: You can sum ranges. E.g. sum (range (3)) gives us 0 + 1 + 2 = 3.
def gen_list(n):
    return [[i for i in range(j+1)] for j in range(n)]
def gen increasing(n):
        return [[i for i in range(sum(range(j+1)), sum(range(j
           +1)) + j+1) for j in range (n)
```

2. A character tree is a tree where the characters along a path of the tree form a word (as defined in the English dictionary). A path through a tree is a list of adjacent node values that starts from any node and ends with a leaf value.

Imagine you're playing a version of Scrabble and you really want to win. Implement scrabble_tree which takes in a character tree. The function will then find all words in the character tree and return the word with the highest value. You may use the pre-defined functions is_word(word) and score(word). You can assume that all characters in the character tree are lower cased.

The function <code>is_word(word)</code> returns True if word is a valid dictionary word and False otherwise. Additionally, you are given a function <code>score(word)</code>, which returns the score of word in a game of Scrabble. You do not need to worry about how these functions are implemented.

Note: If all characters have a weight of 1, then this problem is the same as finding the longest string of the character tree.

(a) First, implement the function word_exists, which takes in a word word and a character tree t. The function will return True if characters along a path from the root of t to a leaf spells word. Otherwise, it returns False.

```
def word_exists(word, t):
    if len(word) == 1:
        return
elif ______:
    return False
return ____(
```

(b) Now, implement the function scrabble_tree. You may use the function you defined in part a, as well as the provided functions is_word(word) and score. You may also want to use the built-in Python function filter.

The function filter takes in a single argument function as its first parameter and a sequence as its second parameter. The function will then test which elements of the sequence is True using the provided function.

```
>>> lst = [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]
>>> evens = list(filter(lambda x: x % 2 == 0, lst))
>>> evens
[2, 4, 6, 8, 10]
```

Note: We have to call list on the output of filter because filter returns an object (which will be covered in a later part of this course).

```
def scrabble tree(t):
       11 11 11
      We assume that all characters have a score of 1.
      >>> t1 = tree('h', [tree('j', [tree('i')])])
      >>> scrabble_tree(t1)
       'hi'
      >>> t2 = tree('i', [tree('l', [tree('l')])])
      >>> t3 = tree('h', [tree('i'), t2])
      >>> scrabble_tree(t3)
       'hill'
       11 11 11
      def find_all_words(t):
          if _____:
              return
          all words = []
          for b in branches(t):
              words_in_branch = _____
              words_from_t = [
              filter_from_t =
              all_words =
          return _____
      clean words = [
      return max(_____, key=
def word_exists(word, t):
   if len(word) == 1:
       return is_leaf(t) and word[0] == label(t)
   if word[0] != label(t):
       return False
   return any([word_exists(word[1:], b) for b in branches(t)
      ])
def scrabble tree(t):
   def find all words(t):
       if is_leaf(t):
```

```
return [label(t)]
all_words = []
for b in branches(t):
    words_in_branch = find_all_words(b)
    words_from_t = [label(t) + w for w in
        words_in_branch]
    filter_from_t = list(filter(lambda w: word_exists(
        w, t), words_from_t))
    all_words = all_words + words_in_branch +
        filter_from_t
    return all_words
clean_words = [word for word in find_all_words(t)if
    is_word(word)]
return max(clean_words, key=lambda w: score(w))
```