

# Advanced Machine Learning

## Imbalanced Learning: Cost-Sensitive Learning Part 2



Confusion matrix		
	True class	
	$y = 1$	$y = -1$
Pred. $\hat{y} = 1$	TP	FP
class $\hat{y} = -1$	FN	TN

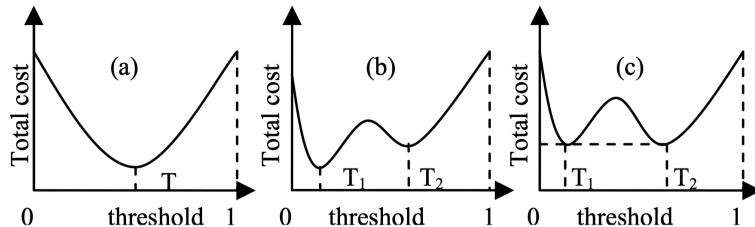
Cost matrix		
	True class	
	$y = 1$	$y = -1$
Pred. $\hat{y} = 1$	$C(1, 1)$	$C(1, -1)$
class $\hat{y} = -1$	$C(-1, 1)$	$C(-1, -1)$

### Learning goals

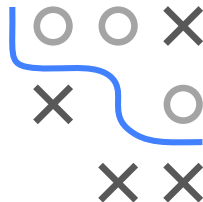
- Empirical thresholding
- Model-agnostic MetaCost

## EMPIRICAL THRESHOLDING: BINARY CASE

- Theoretical threshold from MECP not always best, due to e.g. wrong model class, finite data, etc.
- Simply measure costs on data with different thresholds
- Then pick best threshold (Fig.1 in [Sheng et al. 2006](#)):



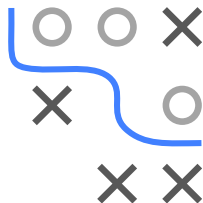
- What if two equal local minima? We prefer the one with wider span
- Do this on validation data / over cross-val to avoid overfitting!





# EMPIRICAL THRESHOLDING: MULTICLASS

- In the standard setting, we predict class  $h(\mathbf{x}) = \arg \max_k \pi_k(\mathbf{x})$ .
- Let's use  $g$  thresholds  $c_k$  now
- Re-scale scores  $\mathbf{s} = (\frac{\pi(\mathbf{x})_1}{c_1}, \dots, \frac{\pi(\mathbf{x})_g}{c_g})^\top$ ,
- Predict class  $\arg \max_k \pi_k(\mathbf{x})$ .
- Compute empirical costs over cross-validation
- Optimize over  $g$  (actually:  $g - 1$ ) dimensional threshold vector  $(c_1, \dots, c_g)^\top$  to produce minimal costs





# METACOST: ALGORITHM

**Input:**  $\mathcal{D} = \{(\mathbf{x}^{(i)}, y^{(i)})\}_{i=1}^n$  training data,  $B$  number of bagging iterations,  $\pi(\mathbf{x})$  probabilistic classifier,  $\mathbf{C}$  cost matrix, empty dataset  $\tilde{\mathcal{D}} = \emptyset$

# Bagging: Classifier is trained on different bootstrap samples.

**for**  $b = 1, \dots, B$  **do**

$\mathcal{D}_b \leftarrow$  Bootstrap version of  $\mathcal{D}$

$\pi_b \leftarrow$  train classifier on  $\mathcal{D}_b$

**end for**

# Relabeling: Find classifiers for which  $\mathbf{x}^{(i)}$  is OOB and compute  $\pi_b$  by averaging over predictions. Determine new label  $\tilde{y}^{(i)}$  w.r.t. to the cost minimal class.

**for**  $i = 1, \dots, n$  **do**

$\tilde{M} \leftarrow \bigcup_{m: \mathbf{x}^{(i)} \notin \mathcal{D}_m} \{m\}$

**end for**

**for**  $j = 1, \dots, g$  **do**

$\pi_j(\mathbf{x}^{(i)}) \leftarrow \frac{1}{|\tilde{M}|} \sum_{m \in \tilde{M}} \pi_j(\mathbf{x}^{(i)} \mid f_m)$  for each  $i$

**end for**

**for**  $i = 1, \dots, n$  **do**

$\tilde{y}^{(i)} \leftarrow \arg \min_k \sum_{j=1}^g \pi_j(\mathbf{x}^{(i)}) C(k, j)$

$\tilde{\mathcal{D}} \leftarrow \tilde{\mathcal{D}} \cup \{(\mathbf{x}^{(i)}, \tilde{y}^{(i)})\}$

**end for**

# Cost Sensitivity: Train on relabeled data.

$f_{\text{meta}} \leftarrow$  train  $f$  on  $\tilde{\mathcal{D}}$

