

Derivative free optimization and evolutionary strategies

Exercise 1: Coordinate descent

Minimize Ridge regression, i.e.,

$$\min_{\boldsymbol{\theta}} \frac{1}{2} \|\mathbf{X}\boldsymbol{\theta}\|_2^2 + \frac{1}{2} \|\boldsymbol{\theta}\|_2^2$$

via coordinate descent.

Exercise 2: CMA-ES

Assume we have drawn the current population $\mathbf{x}_{1:\lambda}$ from the bivariate Gaussian distribution $\mathcal{N}(\mathbf{m}^{[0]}, \mathbf{C}^{[0]})$ with $\mathbf{m}^{[0]} = (1, 1)^\top$, $\mathbf{C}^{[0]} = \mathbf{I}$, such that

Id	x_1	x_2	Fitness value
1	1.14	0.24	0.67
2	1.54	-0.86	0.41
3	2.1	2.16	0.09
4	1.5	2.69	0.09
5	1.25	0.51	0.47
6	0.92	2.19	0.15

We want to do a simplified CMA-ES update step:

- Assume the parent number $\mu = 3$.
- Find $\mathbf{m}^{[1]}$ by updating $\mathbf{m}^{[0]}$ in the mean weighted¹ direction of $\mathbf{x}_{1:\mu}$ with stepsize 0.5.
- Compute \mathbf{C}_μ , the (unweighted) sample covariance of $\mathbf{x}_{1:\mu}$ w.r.t. $\mathbf{m}^{[0]}$, and compute

$$\mathbf{C}^{[1]} = (1 - c) \cdot \mathbf{C}^{[0]} + c \cdot \mathbf{C}_\mu$$

with $c = 0.1$.

¹Simply scale the fitness values such that they sum up to one.