

Simulating Competing Risk Survival Settings

With High-Dimensional Data

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2023-05-13

BioWiMium

Simulation setup is part of ongoing project

Motivation

- Variable selection in high-dimensional settings with competing risks
- Focus more on high-dimensional setting

Outcome

• 2 competing events, censoring approx. equal prevalence

Generating Survival Times (I)



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BIOINFORMATICS

ORIGINAL PAPER

Vol. 25 no. 7 2009, pages 890–896 doi:10.1093/bioinformatics/btp088

Gene expression

Boosting for high-dimensional time-to-event data with competing risks

Harald Binder^{1,2,*}, Arthur Allignol^{1,2}, Martin Schumacher² and Jan Beyersmann^{1,2}

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Received on October 16, 2008; revised on January 19, 2009; accepted on February 12, 2009

Advance Access publication February 25, 2009

Associate Editor: Joaquin Dopazo

Binder et al. (2009)

Generating Survival Times (II)



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Adapting Prediction Error Estimates for Biased Complexity Selection in High-Dimensional Bootstrap Samples

Harald Binder & Martin Schumacher

Universität Freiburg i. Br.

Nr. 100

December 2007



Generating Survival Times to Simulate Cox Proportional Hazards Models

Ralf Bender¹, Thomas Augustin², Maria Blettner¹

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Bender et al. (2005)



- N = 400, p = 5000, 16 informative (12 per event)
- Organized in 4 blocks of correlated variables & uncorrelated noise

Blocks

- Block 1: $ho \approx 0.5$
- Block 2: ho pprox 0.35
- Block 3: $\rho \approx 0.05$
- Block 4: ho pprox 0.32
- $\bullet \ \ {\rm Rest:} \ \rho \approx 0$

- $$\begin{split} \bullet & j=1,\dots,p \text{ and } i=1,\dots,N \\ \bullet & \epsilon_{ij} \sim \mathcal{N}(0,1) \text{ and } U_{i\{1,2,3\}} \sim \mathcal{U}(0,1) \end{split}$$

$$x_{ij} = \begin{cases} -1 + \epsilon_{ij} & \text{for } i \leq 0.5n \text{ and } j \leq 0.05p \\ 1 + \epsilon_{ij} & \text{for } i > 0.5n \text{ and } j \leq 0.05p \\ 1.5 \cdot \mathbf{1}\{U_{i1} < 0.4\} + \epsilon_{ij} & \text{for } 0.05p < j \leq 0.1p \\ 0.5 \cdot \mathbf{1}\{U_{i2} < 0.7\} + \epsilon_{ij} & \text{for } 0.1p < j \leq 0.2p \\ 1.5 \cdot \mathbf{1}\{U_{i3} < 0.3\} + \epsilon_{ij} & \text{for } 0.2p < j \leq 0.3p \\ \epsilon_{ij} & \text{for } j > 0.3p \end{cases}$$

- ullet Cause-specific hazards for events k=1,2 and coefficients $oldsymbol{eta}^{(k)}$
- $\beta_j^{(k)} = \pm 0.5$ for effect variables

Blocks

- Block 1 ("Mutual"):
 - 4 variables with positive effect in both of $\boldsymbol{\beta}^{(1,2)}$
- Block 2 ("Reversed"):
 - 4 variables with positive effect in $\boldsymbol{\beta}^{(1)}$ and negative in $\boldsymbol{\beta}^{(2)}$
- Block 3 ("Disjoint"):
 - ullet 3.1: 4 variables with negative effect in $oldsymbol{eta}^{(1)}$ only
 - ullet 3.2: 4 (other) variables with positive effect in $oldsymbol{eta}^{(2)}$ only

• Cox-exponential model for events k = 1, 2:

$$\lambda^{(k)}(x) = \lambda_k \exp(\mathbf{x}^T \boldsymbol{\beta}^{(k)})$$

- $\lambda_{1,2}$: Constant baseline hazards for event times $T_i^{(k)}$
- ullet λ_C : Analogue for censoring times C_i
- \bullet Default setting: $\lambda_1=\lambda_2=\lambda_C=0.1$

$$T_i^{(k)} = \frac{-\log(U_i)}{\lambda_k \exp(\mathbf{x}_i^T \boldsymbol{\beta}^{(k)})} \qquad C_i = \frac{-\log(U_i)}{\lambda_C}$$

$$U_i \sim \mathcal{U}(0,1) \implies -\log(U_i) \sim \text{Exponential}(\lambda = 1)$$

Assign observed event times t_i and censoring δ_i indicator accordingly

$$t_i = \min(T_i^{(1)}, T_i^{(2)}, C_i) \qquad \qquad \delta_i = \begin{cases} 0 & \text{if } t_i = C_i \\ 1 & \text{if } t_i = T_i^{(1)} \\ 2 & \text{if } t_i = T_i^{(2)} \end{cases}$$

П

- $\pmb{\beta}^{(k)}$ sparse with 12 non-zero entries, $\sum_{i=1}^p \beta_j^{(k)} = 2$
- $\bullet \ \exp(\mathbf{x}_i^T \pmb{\beta}^{(k)})$ in range of $[10^{-4}, 10^3]$

Event prevalences

Mean event counts and prevalence after 100 replicates with N=400:

| δ | n (min - max) | % (min - max) |
|---|-------------------|-----------------------|
| 0 | 118.0 (97 - 136) | 29.5% (24.2% - 34.0%) |
| 1 | 165.1 (142 - 190) | 41.3% (35.5% - 47.5%) |
| 2 | 116.9 (93 - 141) | 29.2% (23.2% - 35.2%) |

Thanks for listening!



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Next up: Backup slides with code

```
X <- matrix(rnorm(n * p), nrow = n, ncol = p)</pre>
ui1 <- runif(n); ui2 <- runif(n); ui3 <- runif(n)
j seq <- seq len(p)</pre>
block1 <- which(j seq <= 0.05 * p)
X[seq len(n/2), block1] < -1 + X[seq len(n/2), block1]
X[-seq len(n/2), block1] \leftarrow 1 + X[-seq_len(n/2), block1]
block2 <- which((j seq > (0.05 * p)) & (j seq <= (0.1 * p)))
X[, block2] \leftarrow 1.5 * (ui1 < 0.4) + X[, block2]
block3 <- which((0.1 * p < j_seq) & (j_seq <= 0.2 * p))
X[, block3] \leftarrow 0.5 * (ui2 < 0.7) + X[, block3]
block4 \leftarrow which((0.2 * p < j seq) & (j seq <= 0.3 * p))
X[, block4] \leftarrow 1.5 * (ui3 < 0.3) + X[, block4]
```

```
ce < -0.5
# first block
j block1 <- which(j seq <= 0.05 * p)</pre>
beta1[j block1[1:4]] <- ce
beta2[j block1[1:4]] <- ce
# second block
j block2 <- which((j seq > (0.05 * p)) & (j seq <= (0.1 * p)
beta1[j block2[1:4]] <- ce
beta2[j block2[1:4]] <- -ce
# third block
j_block3 < - which((0.1 * p < j_seq) & (j_seq <= 0.2 * p))
beta1[j block3[1:4]] <- -ce
beta2[j block3[5:8]] <- ce # offset by 4
```

Event Times: Code



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```
lp1 <- X %*% beta1
lp2 <- X %*% beta2
Ti1 <- -log(runif(n)) / (lambda1 * exp(lp1))
Ti2 <- -log(runif(n)) / (lambda2 * exp(lp2))
Ci <- -log(runif(n)) / lambda c
ti <- pmin(Ti1, Ti2, Ci)
di <- as.integer(Ti1 <= Ci | Ti2 <= Ci)</pre>
di[which(Ti2 <= Ti1 & Ti2 <= Ci)] <- 2
```

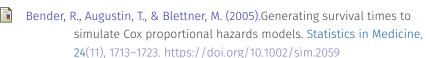
Thank you for your attention

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