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**FACULTY
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Bachelor's thesis

Probabilistic algorithms for computing the LTS estimate

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March 4, 2019

Acknowledgements

THANKS to everybody

Declaration

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In Prague on March 4, 2019

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Citation of this thesis

Jenč, Martin. *Probabilistic algorithms for computing the LTS estimate*. Bachelor's thesis. Czech Technical University in Prague, Faculty of Information Technology, 2019.

Abstrakt

V několika větách shrňte obsah a přínos této práce v českém jazyce.

Klíčová slova LTS odhad, lineární regrese, optimalizace, nejmenších čtverců, usekané čtverce, metoda nejmenších čtverců, outliers

Abstract

The least trimmed squares (LTS) method is a robust version of the classical method of least squares used to find an estimate of coefficients in the linear regression model. Computing the LTS estimate is known to be NP-hard, and hence suboptimal probabilistic algorithms are used in practice.

Keywords LTS, linear regression, robust estimator, least trimmed squares, ordinary least squares, outliers, outliers detection

Contents

Introduction	1
1 The Least trimmed squares	3
1.1 Robust statistics	3
1.2 Description	3
1.3 Computation	3
2 Algorithms	5
2.1 FAST-LTS	5
2.2 Exact algorithm	6
2.3 Feasible solution	6
2.4 MMEA	6
2.5 Branch and bound	6
2.6 Adding row	6
3 Experiments	7
3.1 Data	7
3.2 Performance	7
3.3 Outlier detection	7
Conclusion	9
Bibliography	11
A Datasets	13
B Contents of enclosed CD	15

List of Figures

Introduction

The Least trimmed squares

1.0.1 Objective function

1.0.1.1 something

1.1 Robust statistics

1.2 Description

1.3 Computation

Algorithms

2.1 FAST-LTS

In this section we'll describe FAST-LTS algorithm and it's main properties. The main idea of this algorithm is based on the fact that from one approximation of the algorithm we can compute another which can have lower objective function.

Thoerem 1: [1] Let $w_0 \dots w_p$ be the LTS estimate. for each data sample we can compute $\|y - wx\|$

Hlavní myšlenka tohoto algoritmu spočívá ve faktu,

Vyberte si šablonu podle druhu práce (bakalářská, diplomová), jazyka (Dejatiná, angličtina) a kódování (ASCII, UTF-8, ISO-8859-2 nebo latin2 a nebo Windows-1250).

V Deskové variantě naleznete šablony v souborech pojmenovaných · ch ve formátu práce kódování.tex. Typ práce máří"e bá · t:

BP bakalářská práce,

DP diplomová (magisterská) práce.

Kódování zdrojového souboru (L^AT_EX), ve kterém chcete psát, máří"e bá · t:

UTF-8 kódování Unicode,

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Windows-1250 znaková sada 1250 Windows.

V pážňpadě nejistoty ohledně kódování doporuďujeme následujícň postup:

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2. ALGORITHMS

2. V opaĎnĎm pĚĚnpadĚ postupujte dĚle podle toho, jakĚ operaĎnĎ systĚm pouĚíváte:

- v pĚĚnpadĚ Windows pouĚijte Ěablonu pro kĚsdovĚnĚ Windows-1250,
- jinak zkuste pouĚít Ěablonu pro kĚsdovĚnĚ ISO-8859-2.

V anglickĚ variantĚ jsou Ěablony pojmenovanĚ podle typu prĚce, moĚnosti jsou:

bachelors bakalĚĚskĚ prĚce,

masters diplomovĚ (magisterskĚ) prĚce.

2.2 Exact algorithm

2.3 Feasible solution

2.4 MMEA

2.5 Branch and bound

2.6 Adding row

Experiments

- 3.1 Data
- 3.2 Performance
- 3.3 Outlier detection

Conclusion

Bibliography

- [1] Rybicka, J. *LaTeX pro začátečníky*. Brno: Konvoj, third edition, ISBN 80-7302-049-1.

Datasets

GUI Graphical user interface

XML Extensible markup language

Contents of enclosed CD

	readme.txt	the file with CD contents description
	exe	the directory with executables
	src	the directory of source codes
	wbdcm	implementation sources
	thesis	the directory of \LaTeX source codes of the thesis
	text	the thesis text directory
	thesis.pdf	the thesis text in PDF format
	thesis.ps	the thesis text in PS format