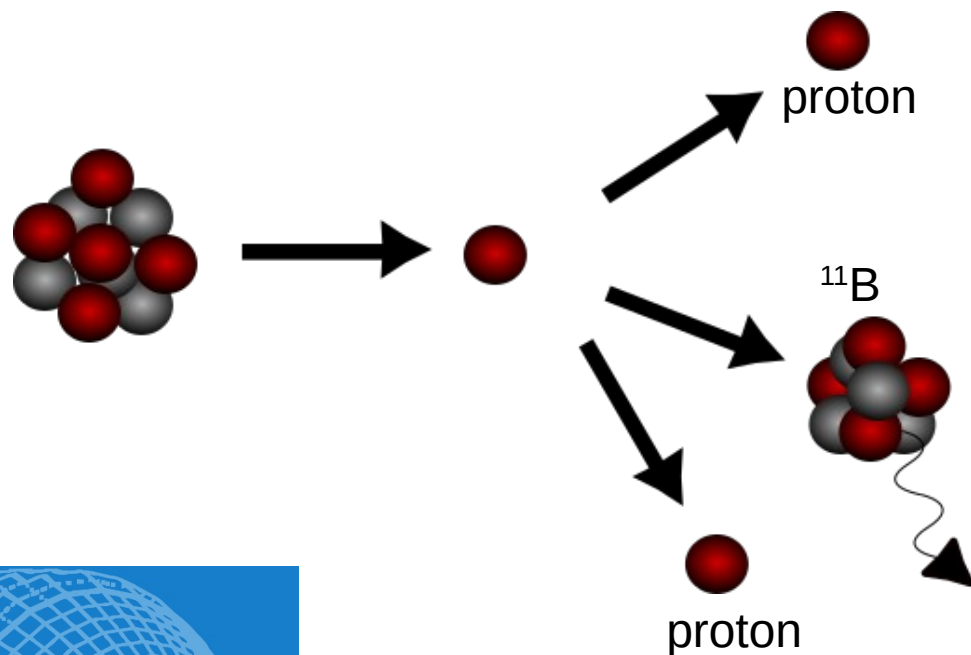
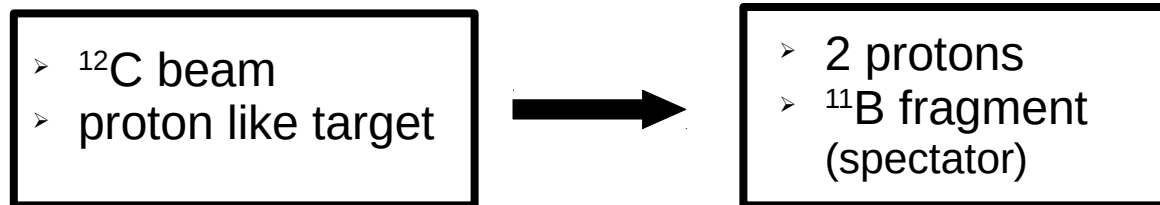
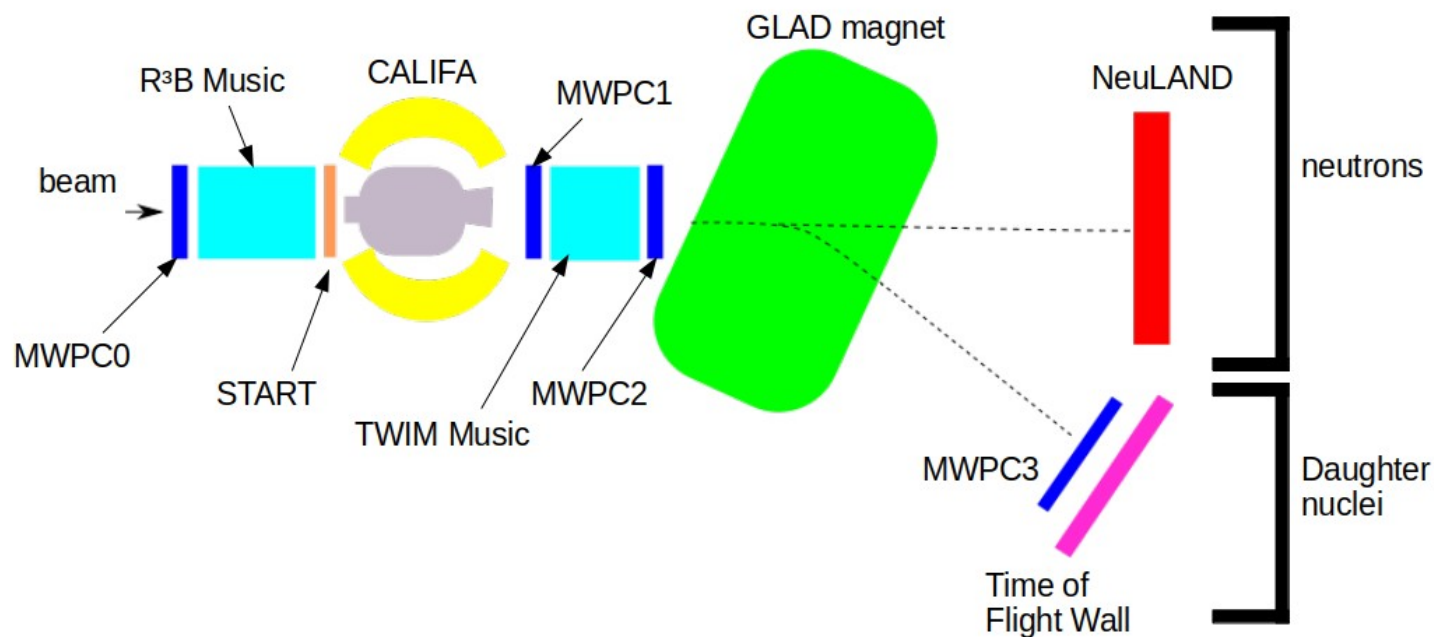


$^{12}\text{C}(p,2p)^{11}\text{B}$ reaction:



SETUP:

Beam energy: 400 AMeV
Beamtype: ^{12}C
Target: CH_2

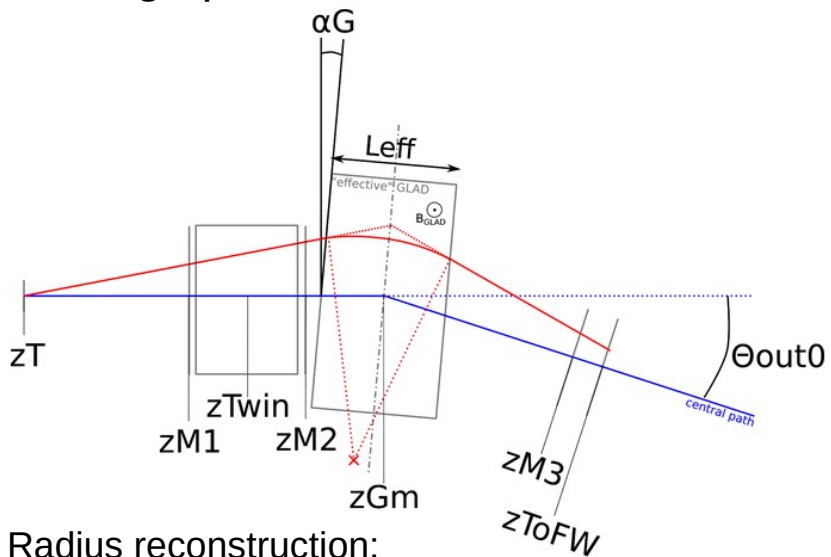




Fragment Particle Identification



Flightpath reconstruction:

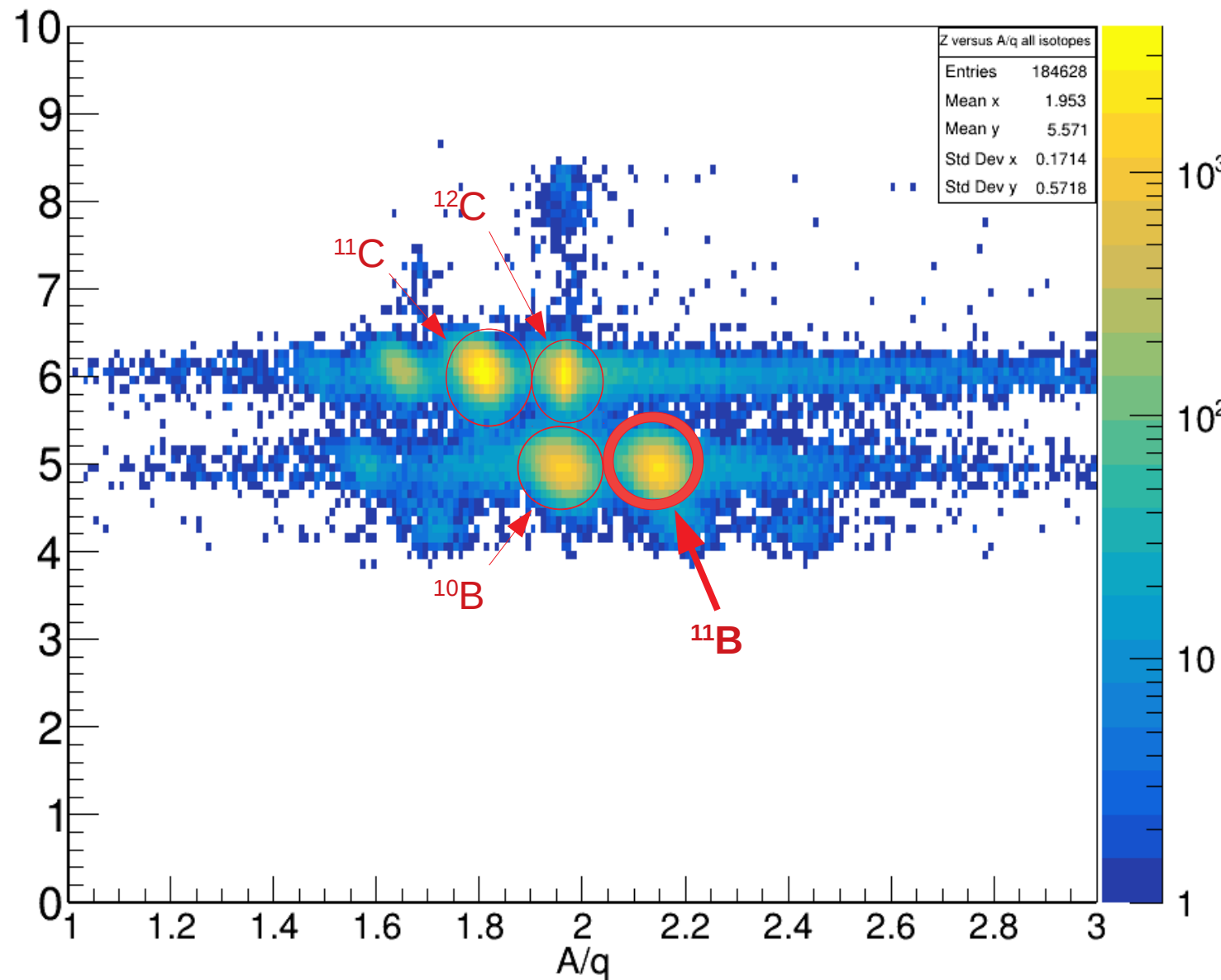


Radius reconstruction:

$$R = \frac{L_{eff}}{2 \sin\left(\frac{\theta_{in} + \theta_{out}}{2}\right)}$$

$$B * \rho = \frac{\beta * \gamma * M}{q}$$

Z (charge)

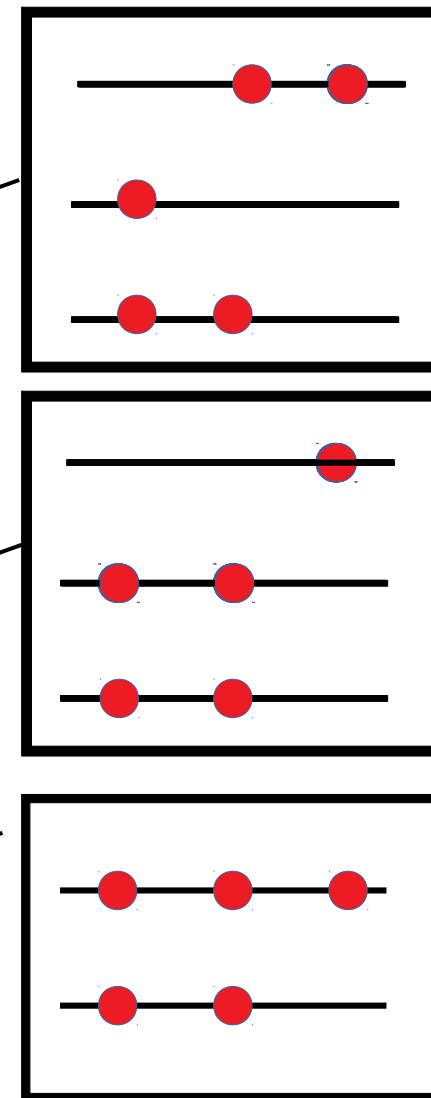
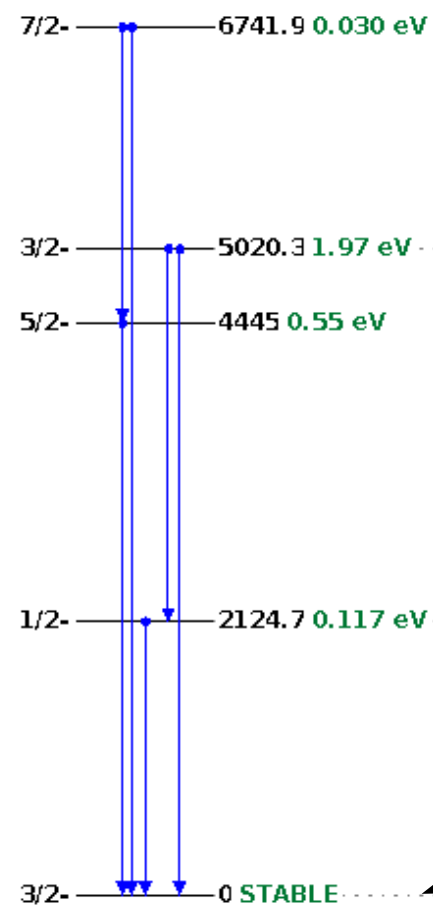
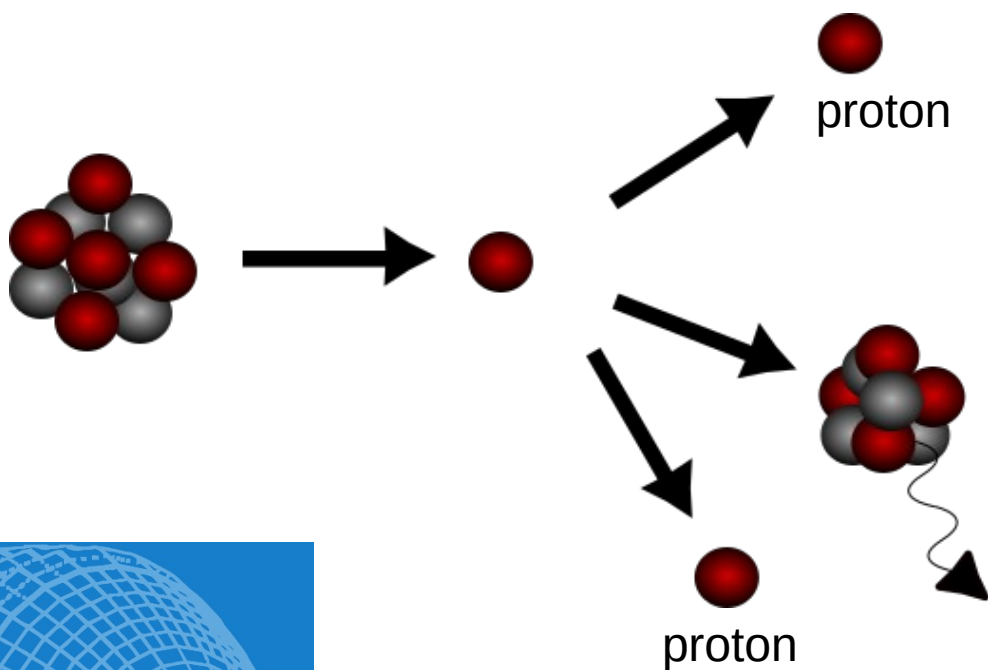




$^{12}\text{C}(p,2p)^{11}\text{B}$ reaction

Two Proton Identification:

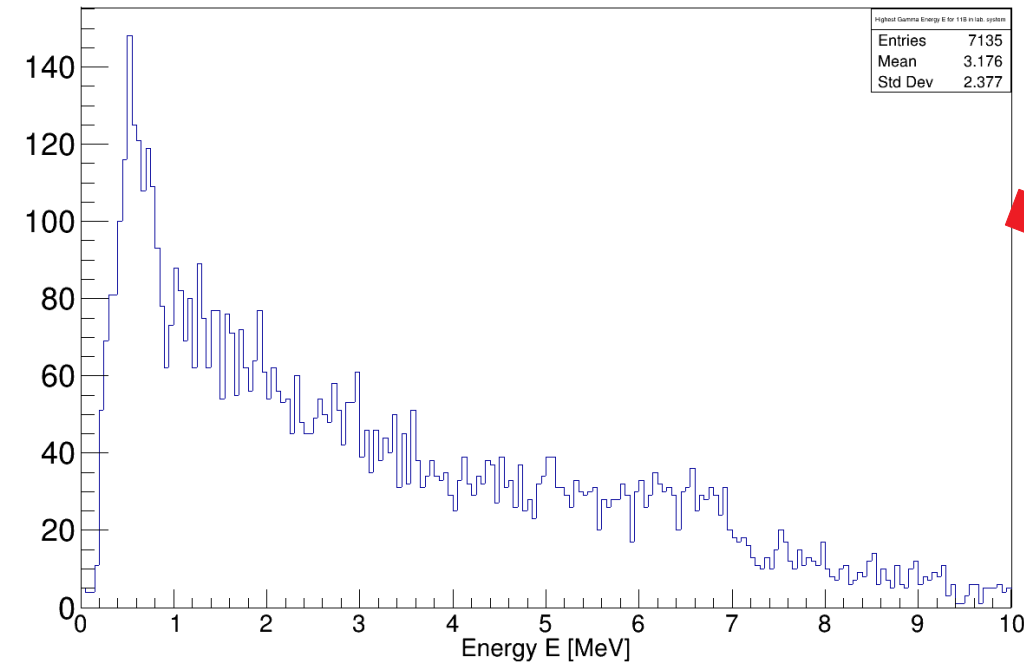
→ two hits with $E_{\text{hit}} > 30 \text{ MeV}$





Gamma Spectrum of ^{11}B

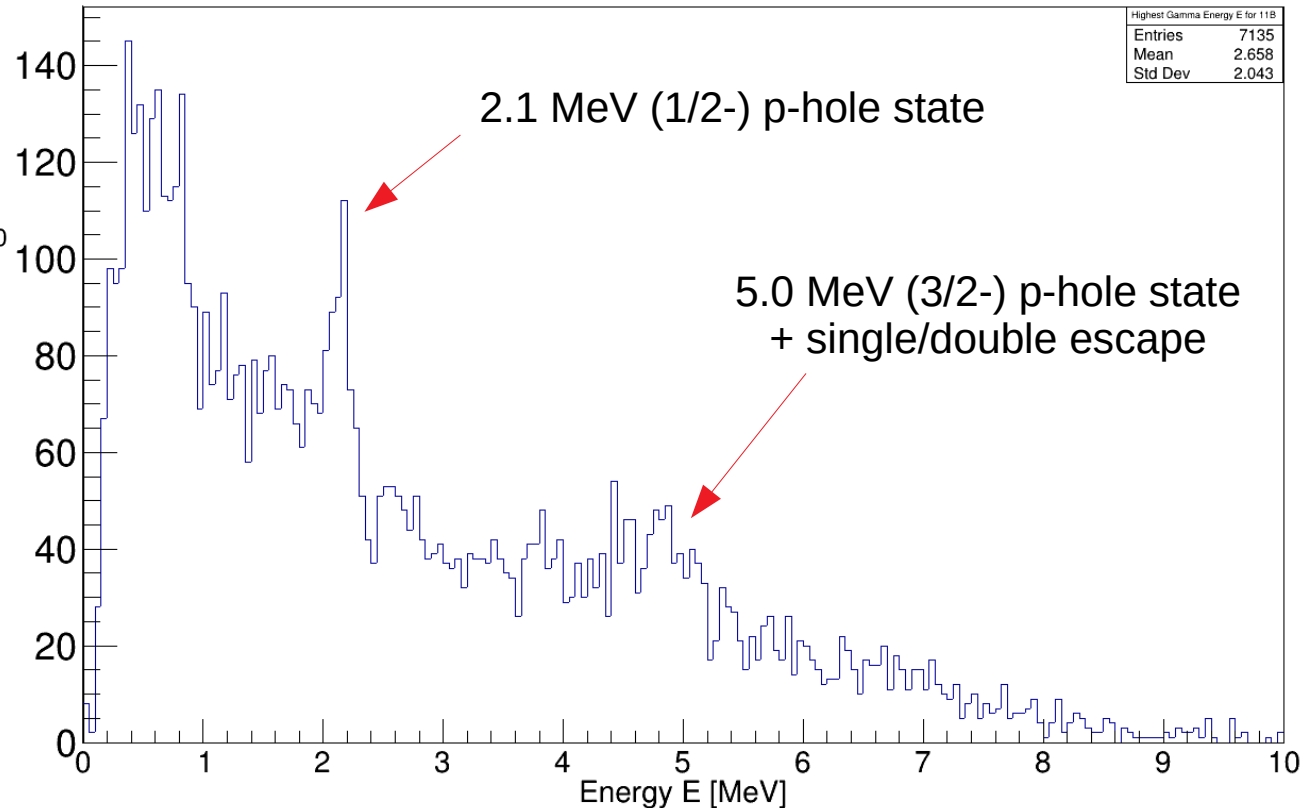
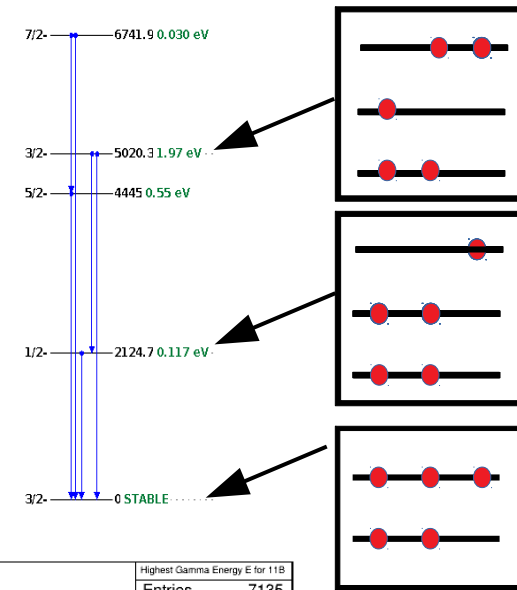
laboratory system



Doppler Correction:

$$E_{\gamma} = \gamma E_{lab} (1 - \beta \cos(\theta))$$

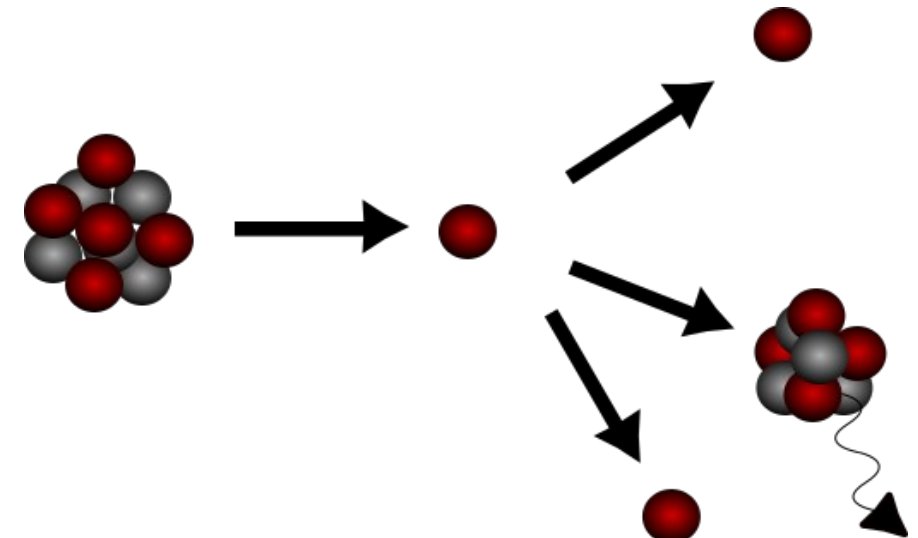
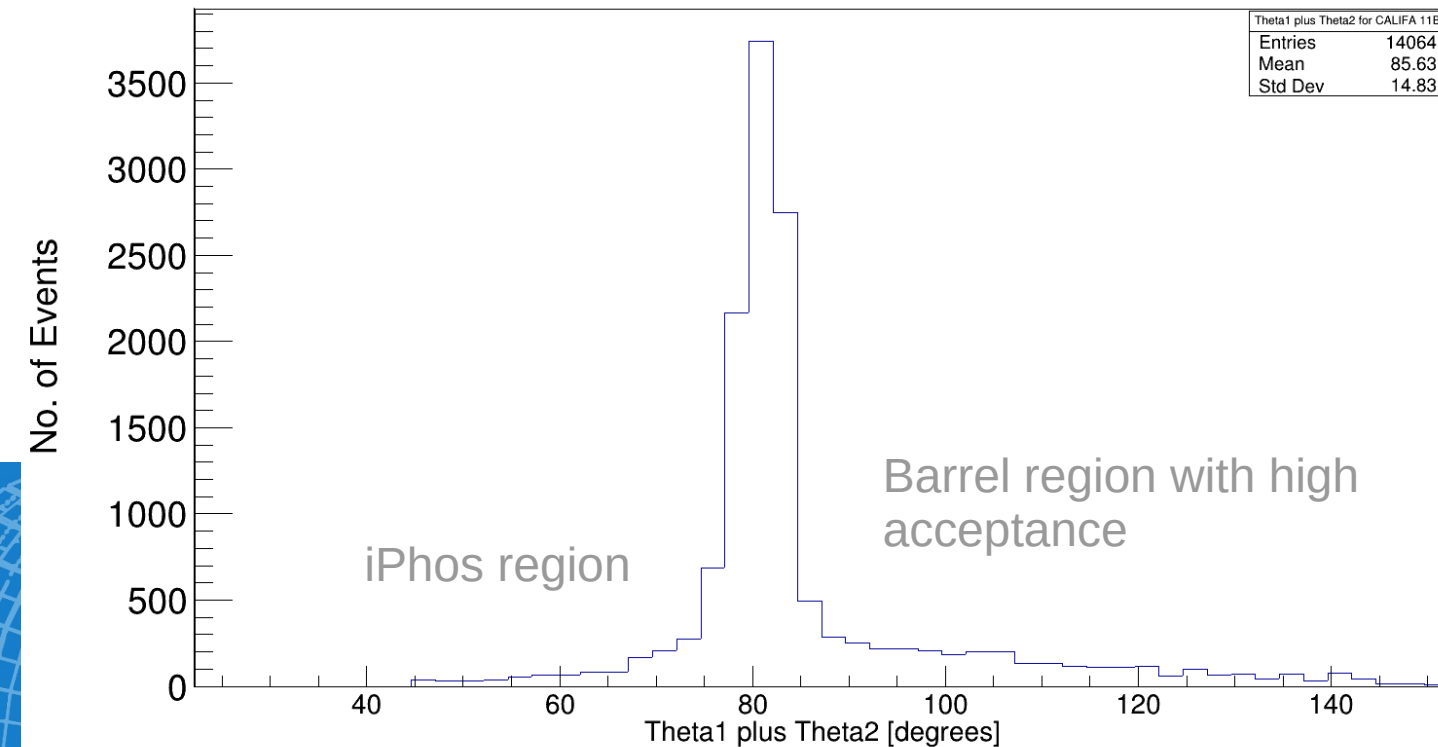
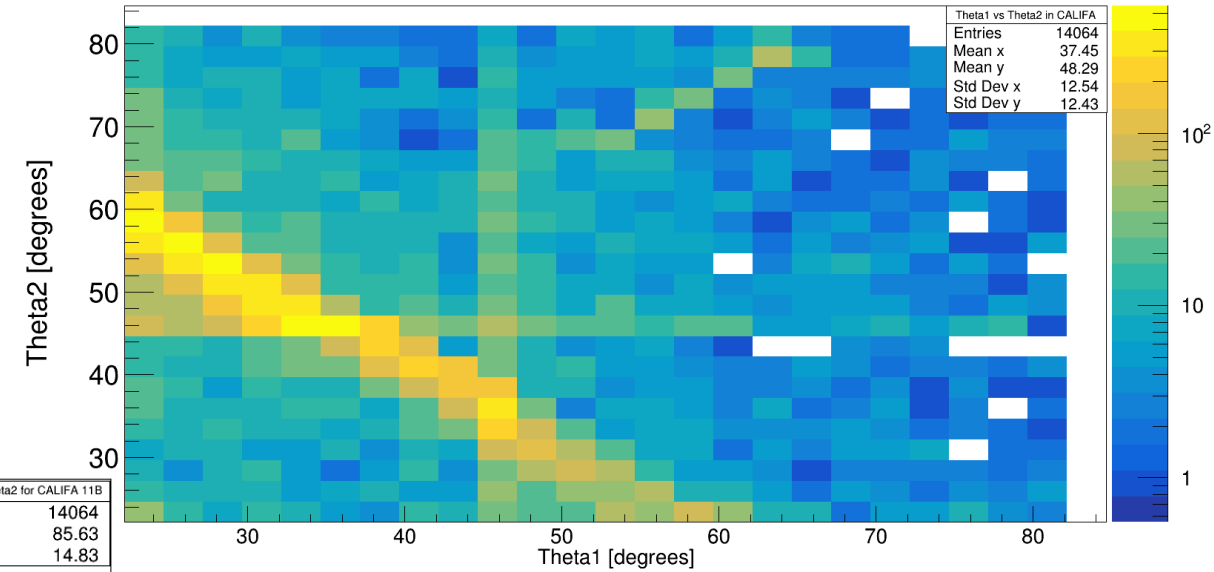
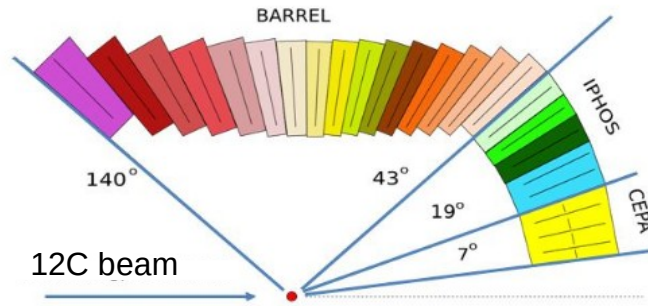
^{11}B rest frame





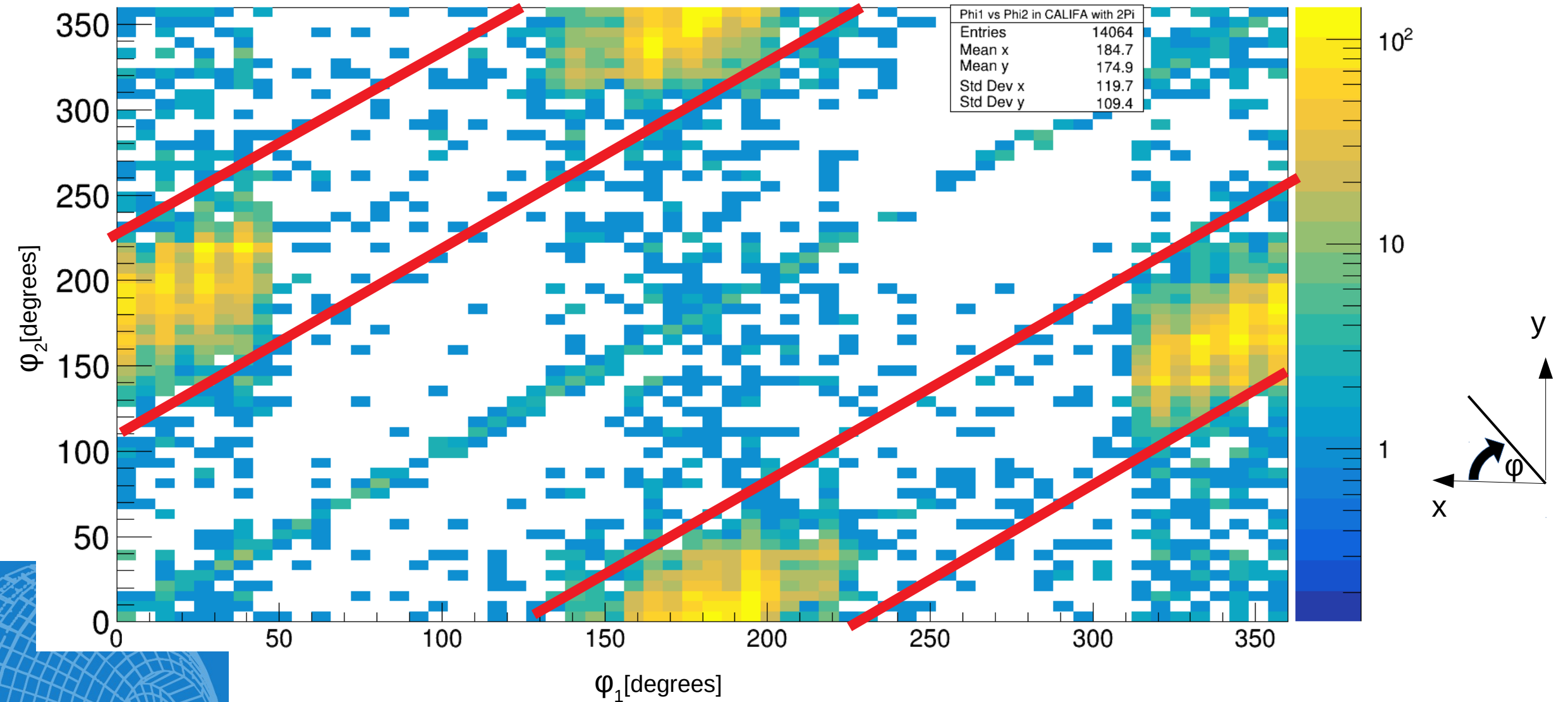
Polar Angular Distribution of protons for $^{12}\text{C}(p,2p)^{11}\text{B}$

Theta1 vs Theta2 in CALIFA





Arzimuthal Distribution of protons for $^{12}\text{C}(p,2p)^{11}\text{B}$



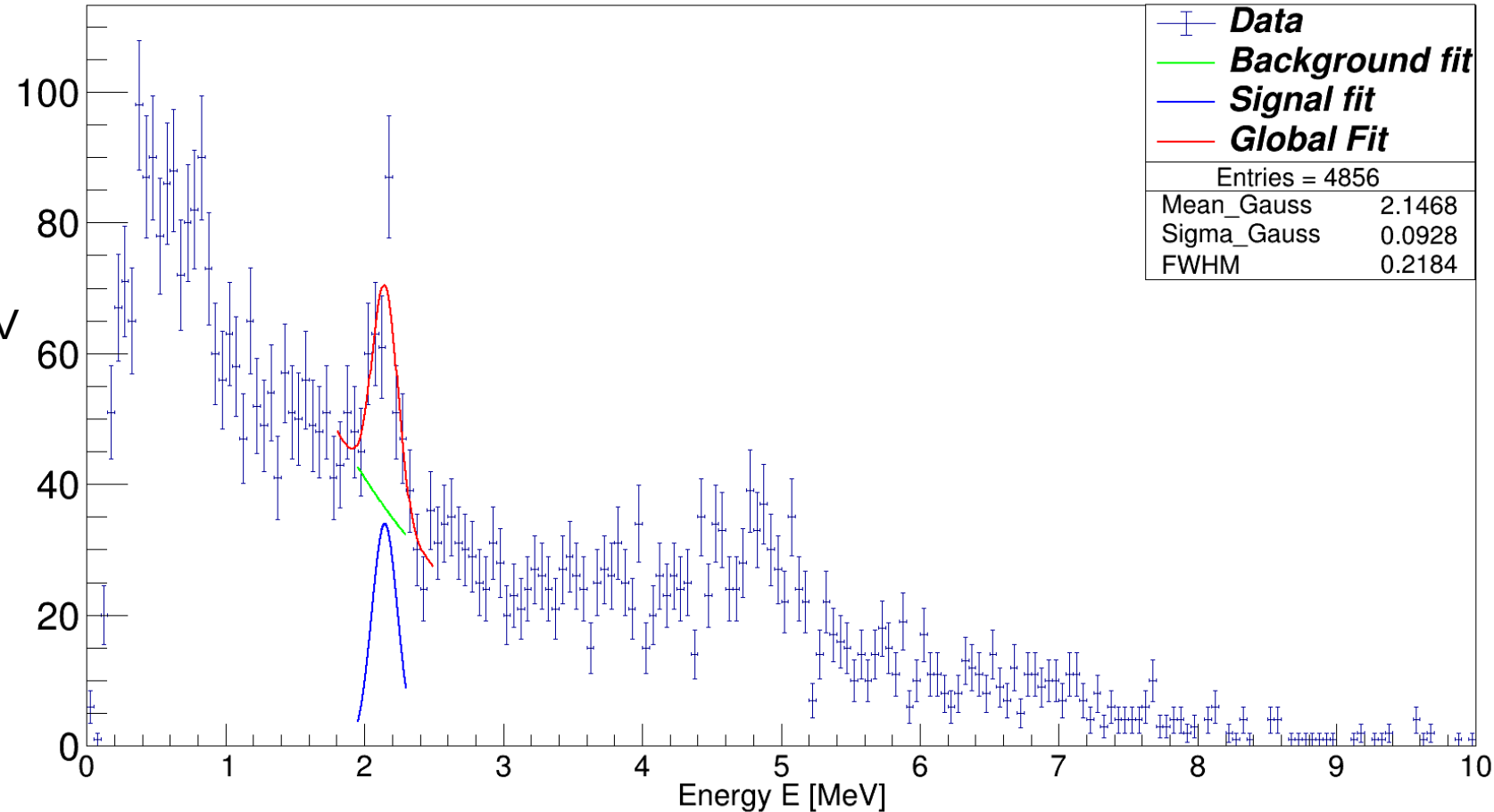


Gamma Spectrum with Angular Cuts

CALIFA Gamma Energy Spectrum

Event selection criteria for CALIFA:

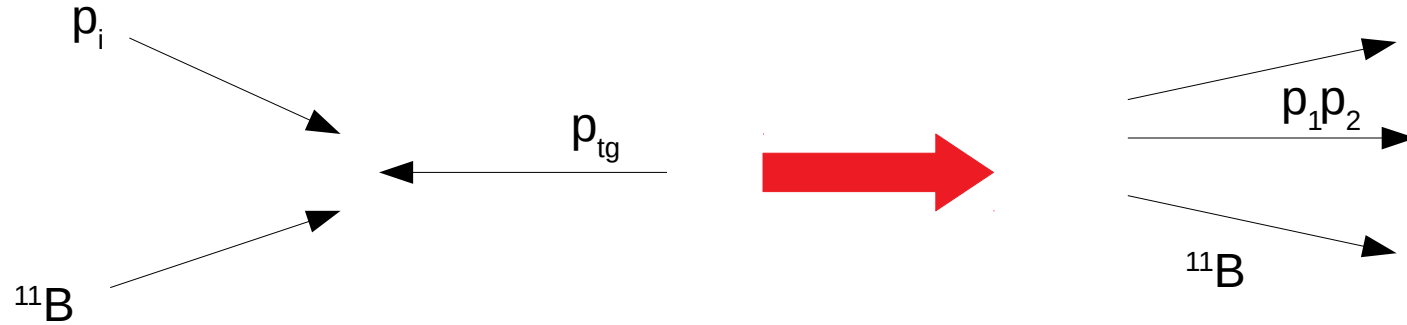
- 11B fragment identification
- two hits (protons) with $E_{\text{hit}} > 30$ MeV
- $\theta_1 + \theta_2 < 90^\circ$
- $\Delta\phi = 180^\circ \pm 40^\circ$



TODO: make bkg from 1 to 3 and add also plots with hit-multiplicities...



Reconstruction of Inner Momenta



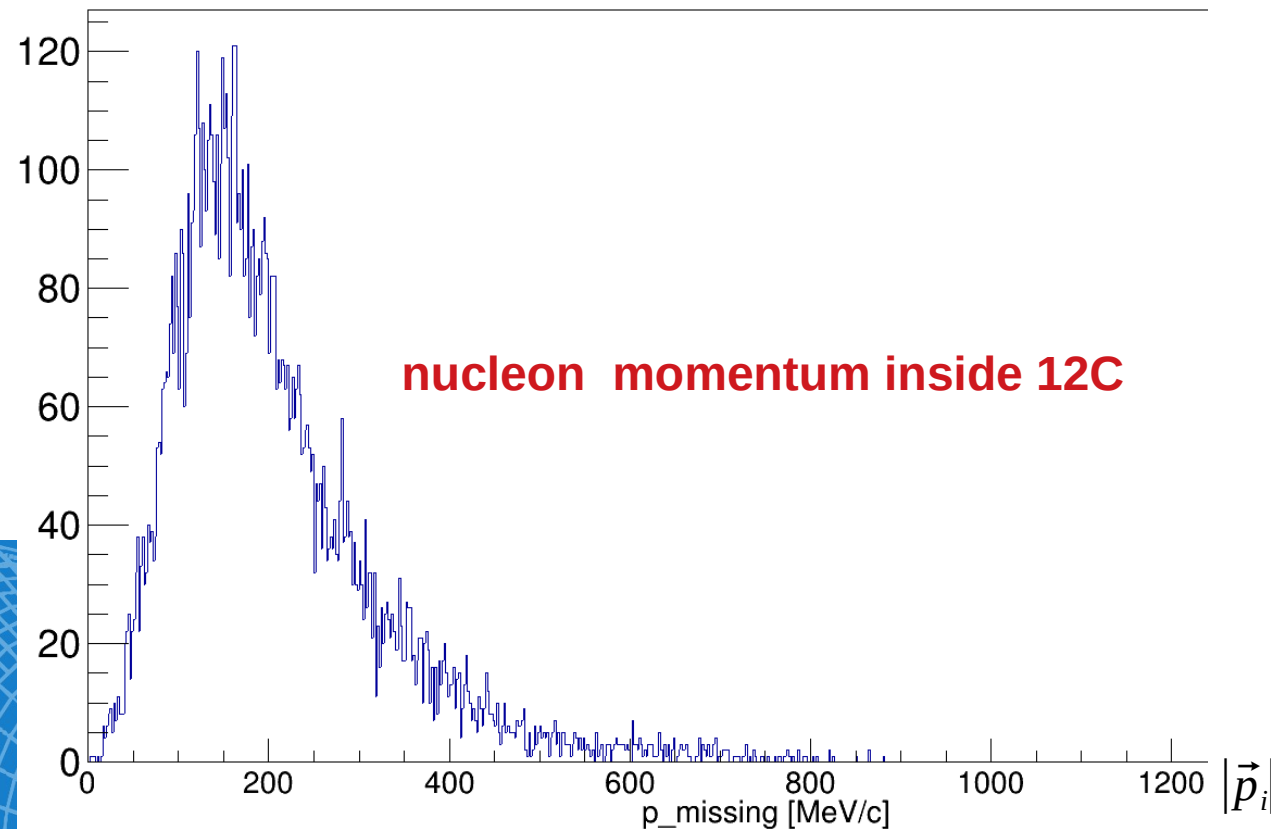
Momentum conservation relation:

$$\mathbf{p}_{12C} + \mathbf{p}_{tg} = \mathbf{p}_1 + \mathbf{p}_2 + \mathbf{p}_{11B}$$

assuming QE scattering in
mean field potential:

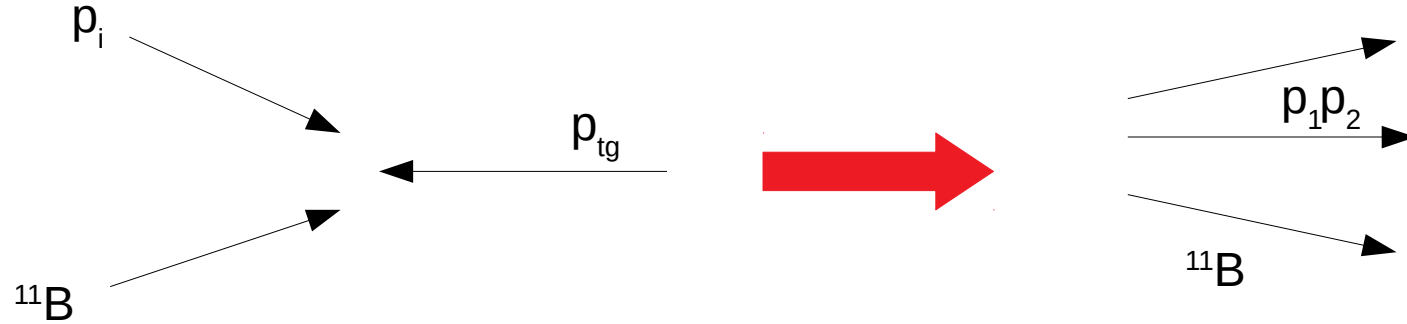
$$\mathbf{p}_{12C} = \mathbf{p}_i + \mathbf{p}_{11B}$$

$$\mathbf{p}_i \approx \mathbf{p}_{missing} = \mathbf{p}_1 + \mathbf{p}_2 - \mathbf{p}_{tg} \text{ (no ISI / FSI)}$$





Momentum components of p_i



Momentum conservation relation:

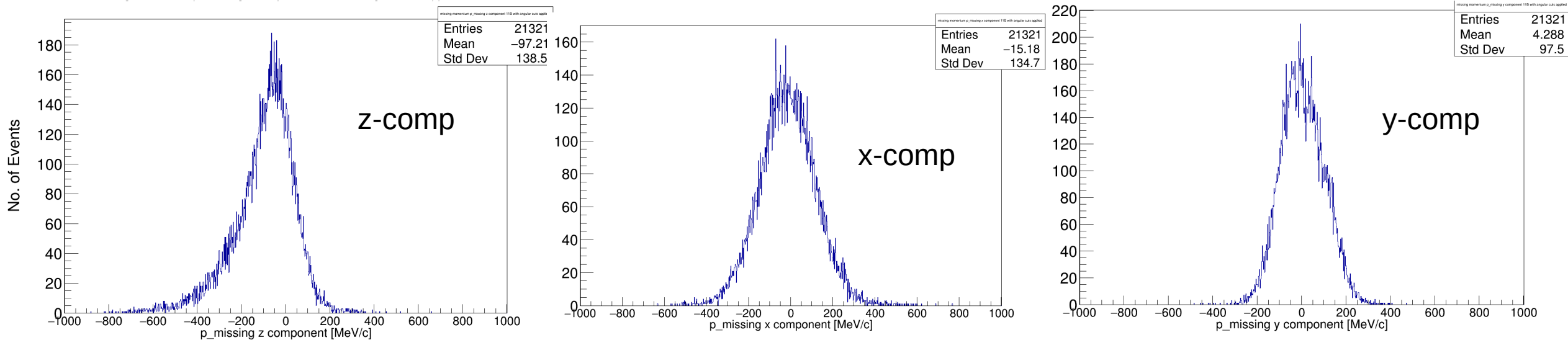
$$\mathbf{p}_{12C} + \mathbf{p}_{tg} = \mathbf{p}_1 + \mathbf{p}_2 + \mathbf{p}_{11B}$$

assuming QE scattering in
mean field potential:

$$\mathbf{p}_{12C} = \mathbf{p}_i + \mathbf{p}_{11B}$$

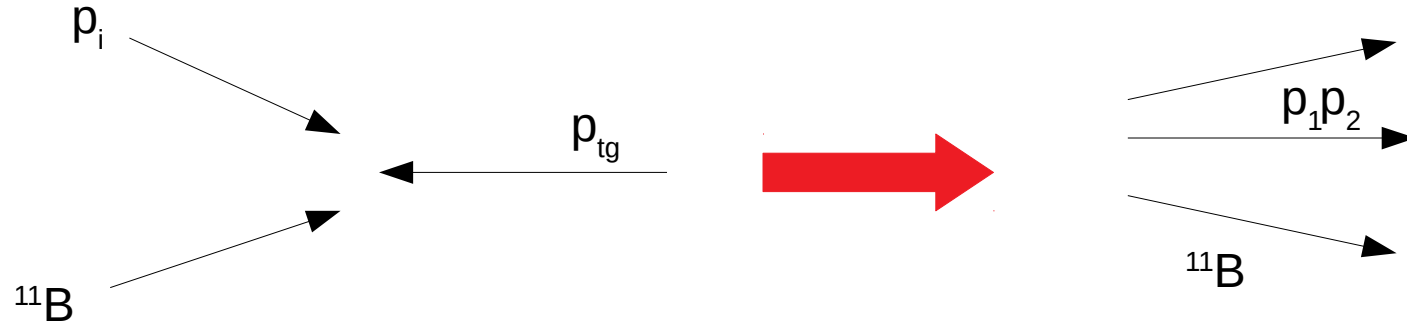
$$\mathbf{p}_i \approx \mathbf{p}_{missing} = \mathbf{p}_1 + \mathbf{p}_2 - \mathbf{p}_{tg} \text{ (no ISI/FSI)}$$

momentum-components (with angular cuts applied)





Missing Energy Distribution



$$p_i \approx p_{\text{missing}} = p_1 + p_2 - p_{tg} \text{ (no ISI / FSI)}$$

$$E_{\text{miss}} = m_p - e_{\text{miss}}$$

(where e_{miss} is the energy component of $\mathbf{p}_{\text{missing}}$)

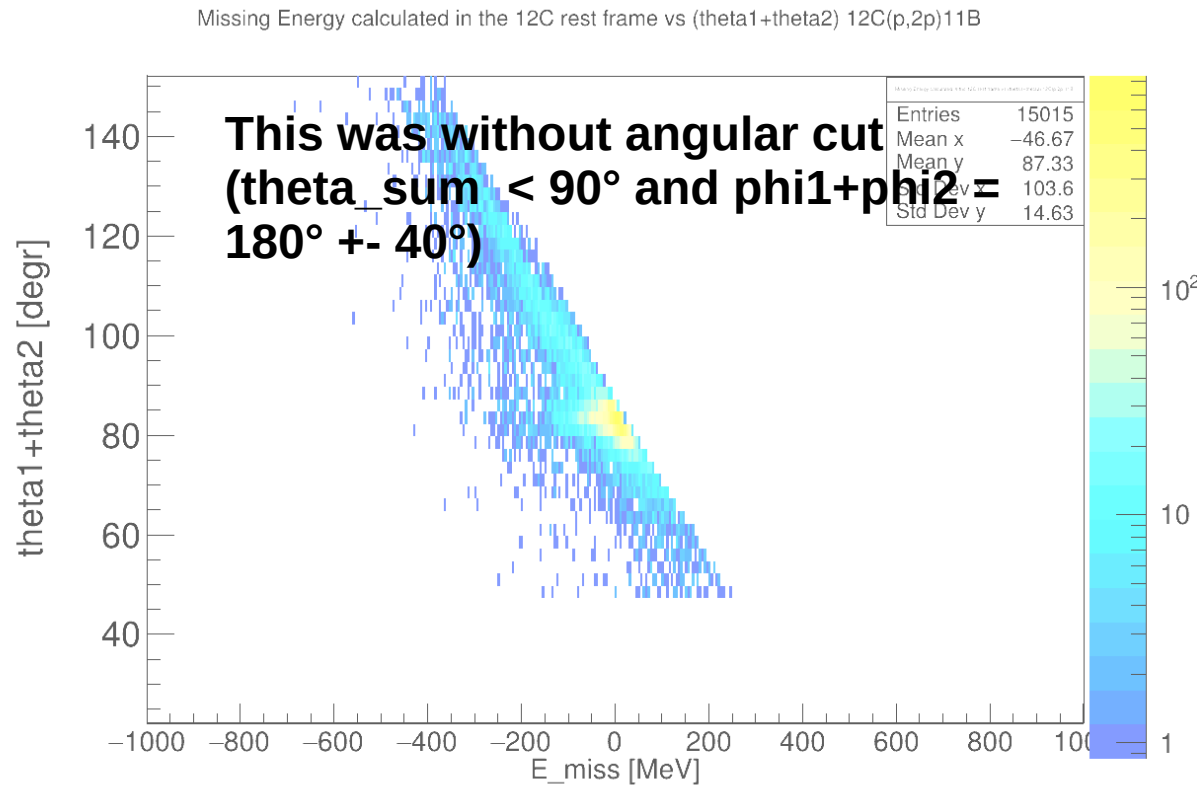
E_{miss} can be interpreted as $E_{\text{sep}} + E_{\text{mean_exc}}$:

$$E_{\text{miss}} = E_{\text{final}} - E_{\text{initial}}$$

$$E_{\text{miss}} = E_{\text{tgkin}} + m_{\text{tg}} + m_p - m_{p1} - E_{p1\text{kin}} - m_{p2} - E_{p2\text{kin}}$$

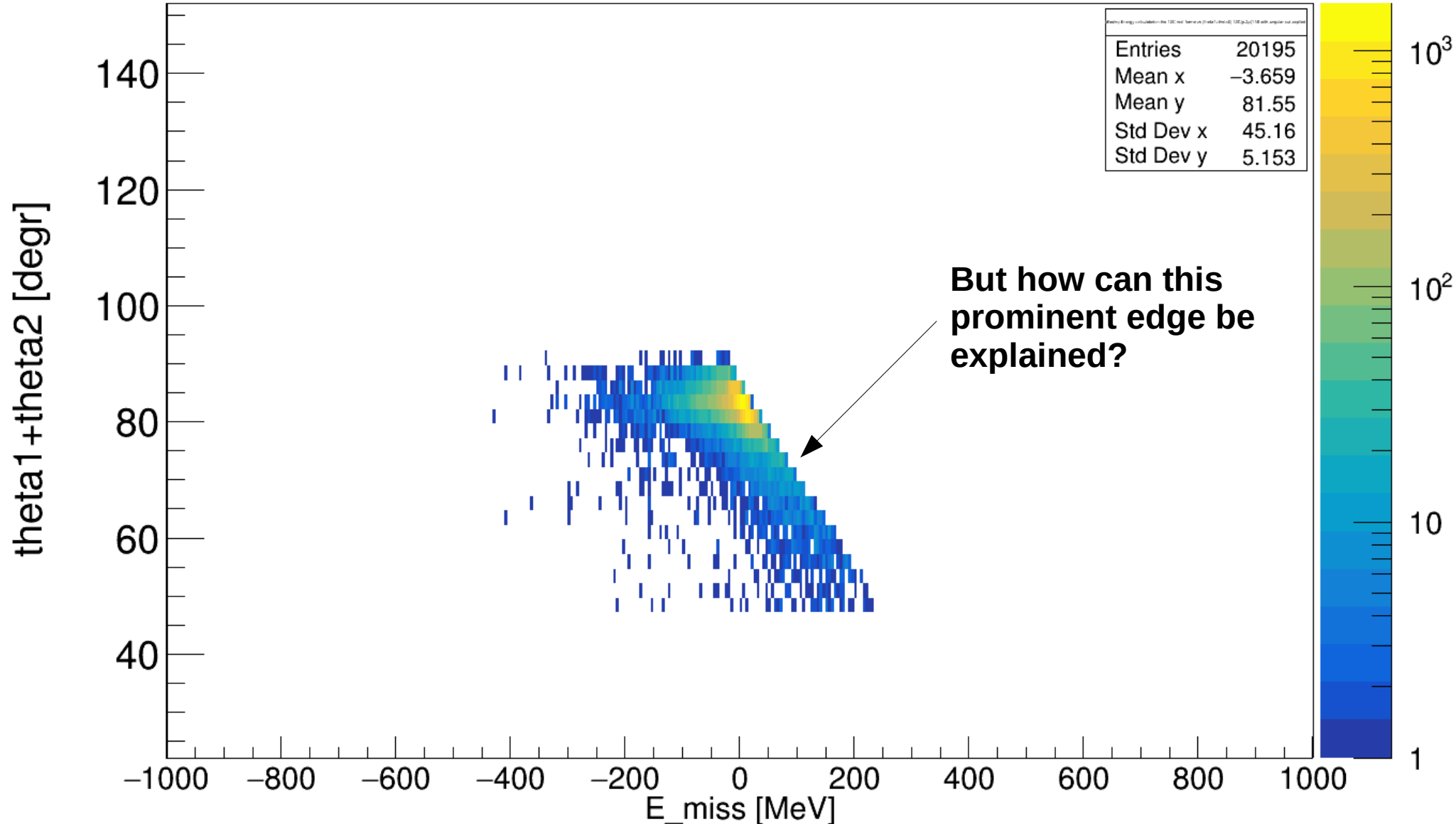
(where $m_p = m_{\text{tg}} = m_{p1} = m_{p2}$ as they are all protons)

$$E_{\text{miss}} = E_{\text{tgkin}} - E_{p1\text{kin}} - E_{p2\text{kin}} \text{ (in 12C cms)}$$



Missing Energy Distribution

Now with cut on angles: $\theta_{\text{sum}} < 90^\circ$ and $\phi_{\text{diff}} = 180^\circ \pm 40^\circ$





Analysis Missing Energy Distribution

Explicit calculation of the Missing Energy (in the 12C frame):

$$E_{\text{miss}} = E_{\text{tgin}} - E_{\text{p1kin}} - E_{\text{p2kin}}$$

$$E_{\text{miss}} = 400 - \underbrace{\left(\gamma * (E_{\text{kin1}} + 938) - \gamma * \beta * \sqrt{(E_{\text{kin1}} + 938)^2 - 938^2} * \cos(\theta_1) - 938 \right)}_{E'_{\text{p1}}} - \underbrace{\left(\gamma * (E_{\text{kin2}} + 938) - \gamma * \beta * \sqrt{(E_{\text{kin2}} + 938)^2 - 938^2} * \cos(\theta_2) - 938 \right)}_{E'_{\text{p2}}}$$

$E_{\text{kin1}} \qquad E_{\text{kin2}}$

$E_{\text{pot}_{\text{p1}}} \qquad E_{\text{pot}_{\text{p2}}}$



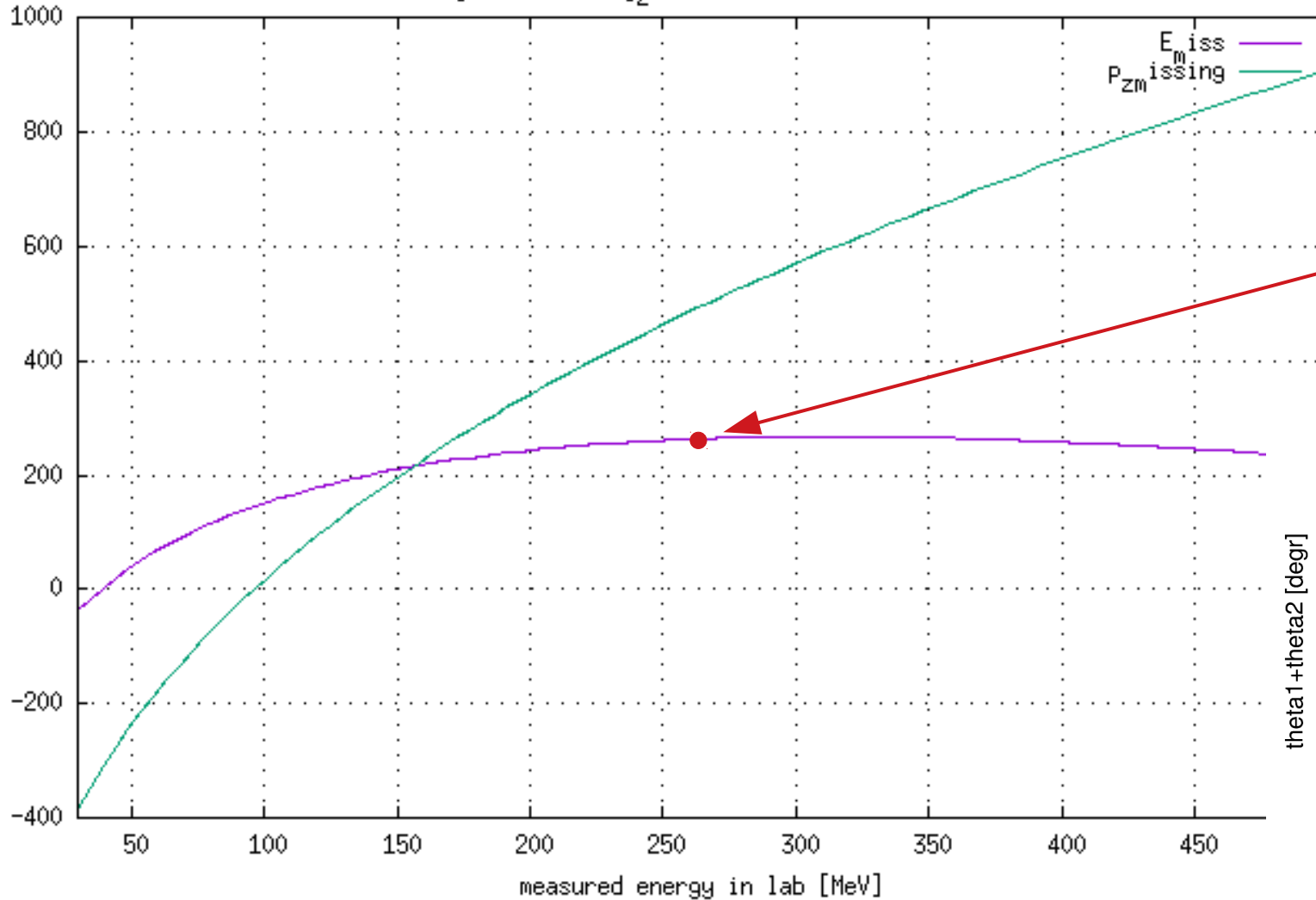


E_missing and p_z_missing for different opening angles



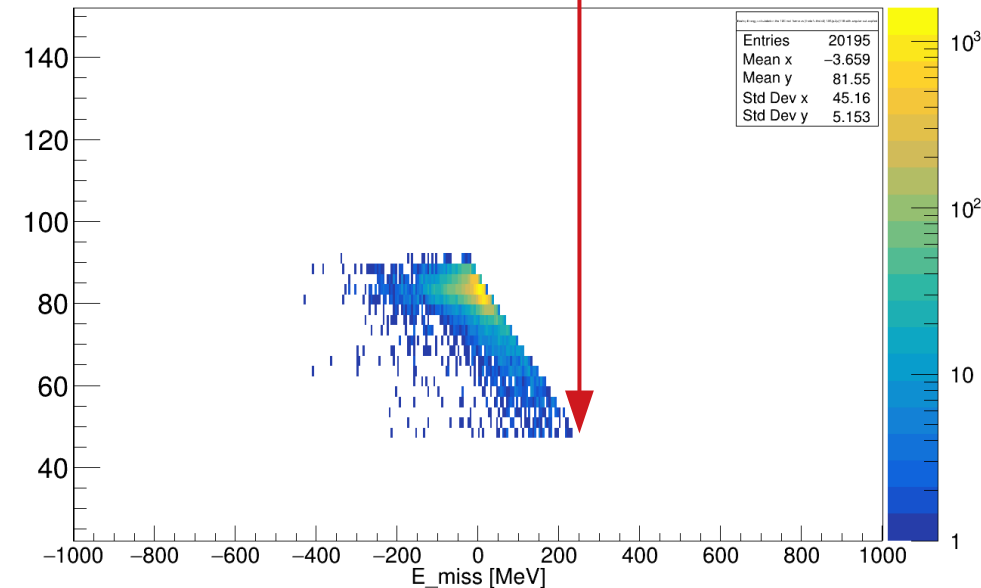
For simplicity let's say $\theta_1 = \theta_2$. That means for $\theta_{\text{sum}} = 44^\circ \rightarrow \theta_1 = \theta_2 = 22^\circ$

E_missing and p_missing_z versus measured energy in lab



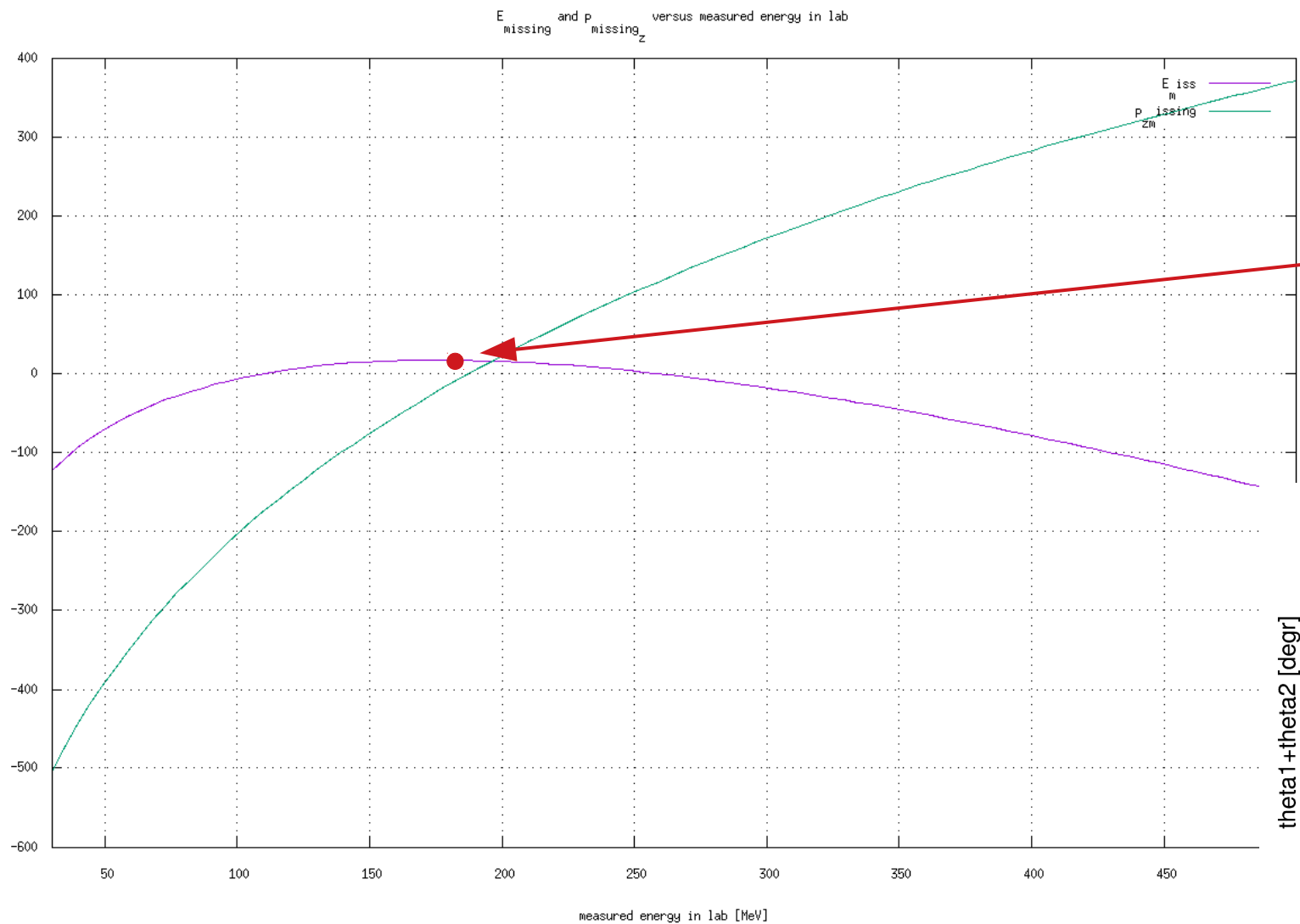
Maximum ≈ 270 MeV

theta1+theta2 [degr]

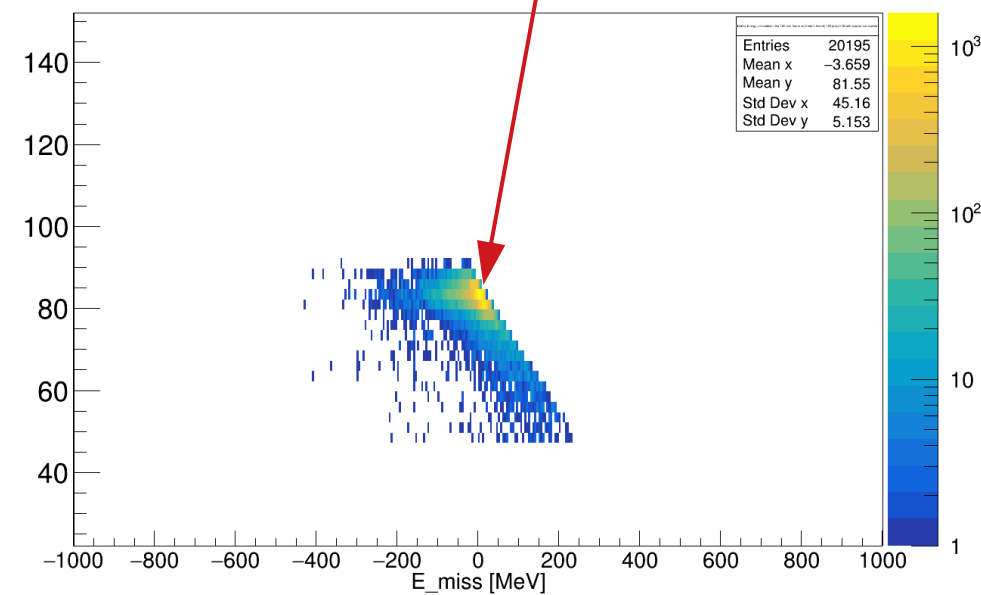




E_missing and p_z_missing for $\theta_1 = \theta_2 = 41^\circ$

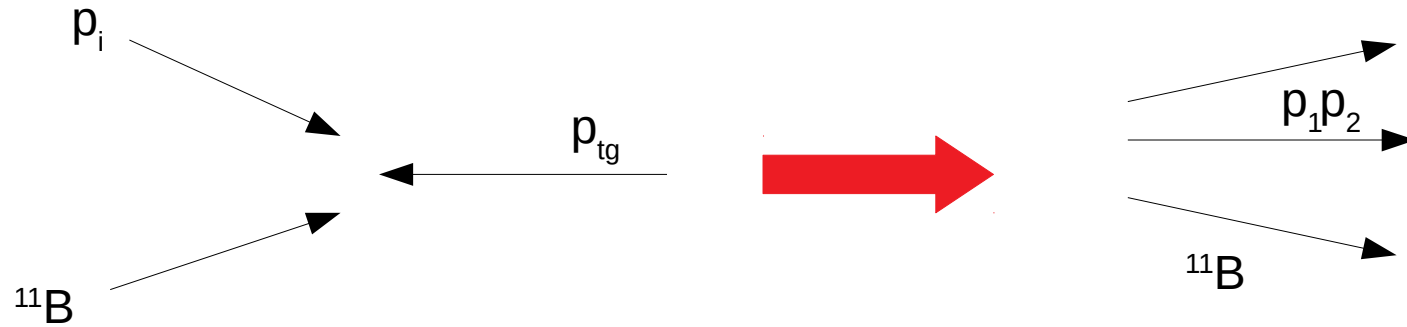


Maximum ≈ 20 MeV



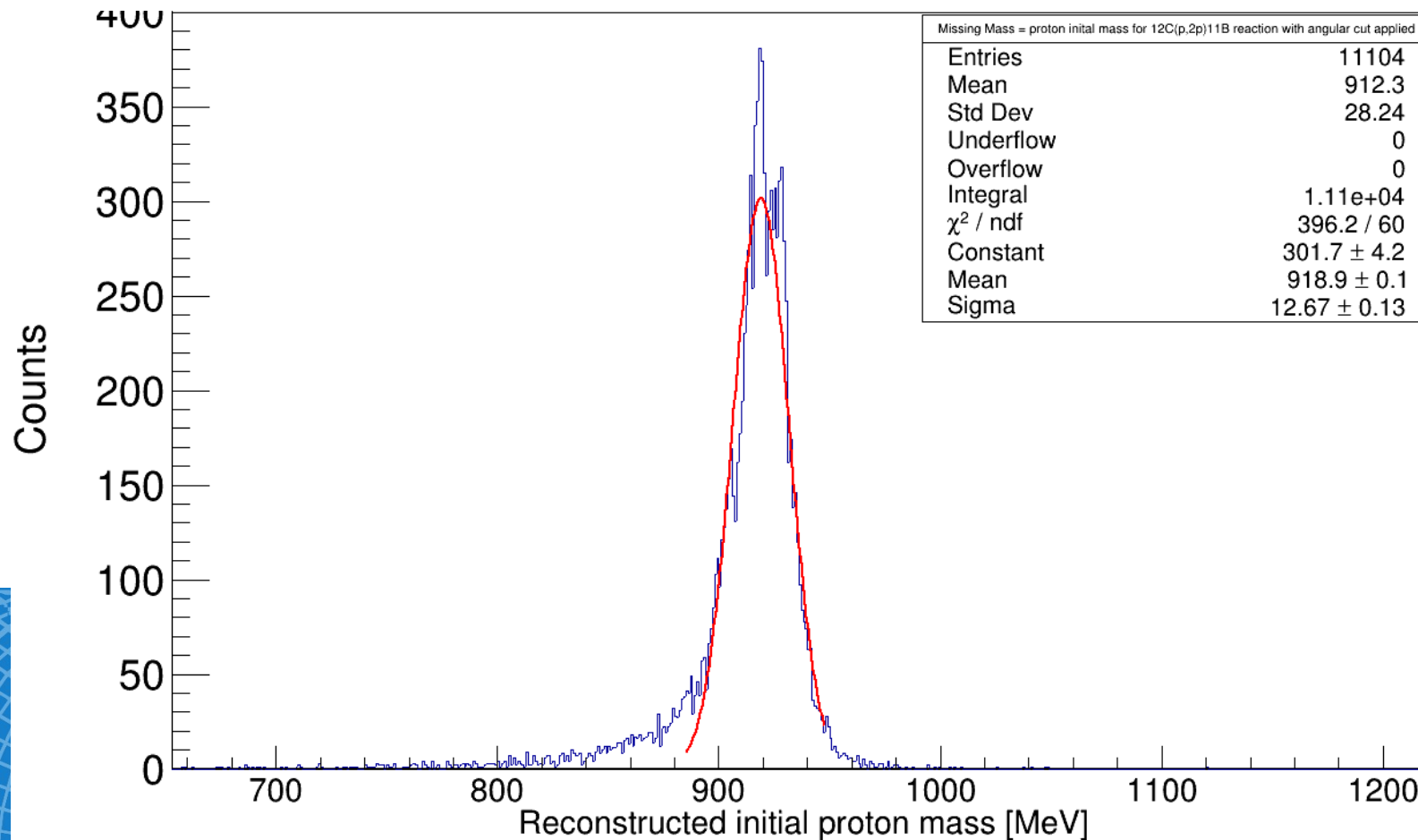


Mass reconstruction of p_i



$$p_i \approx p_{\text{missing}} = p_1 + p_2 - p_{\text{tg}} \text{ (no ISI/FSI)}$$

$$M_i = \sqrt{(p_1 + p_2 - p_{\text{tg}})^2}$$

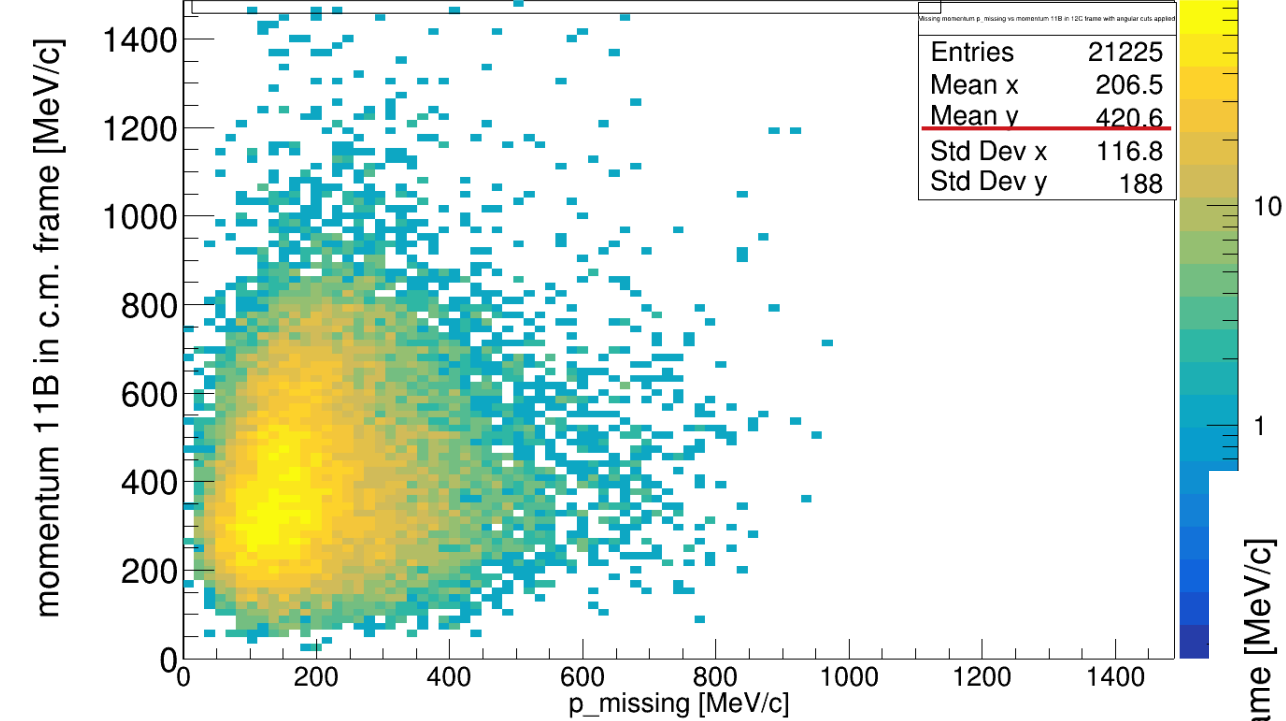


Looks ok, mean of 918 MeV is lower than expected....

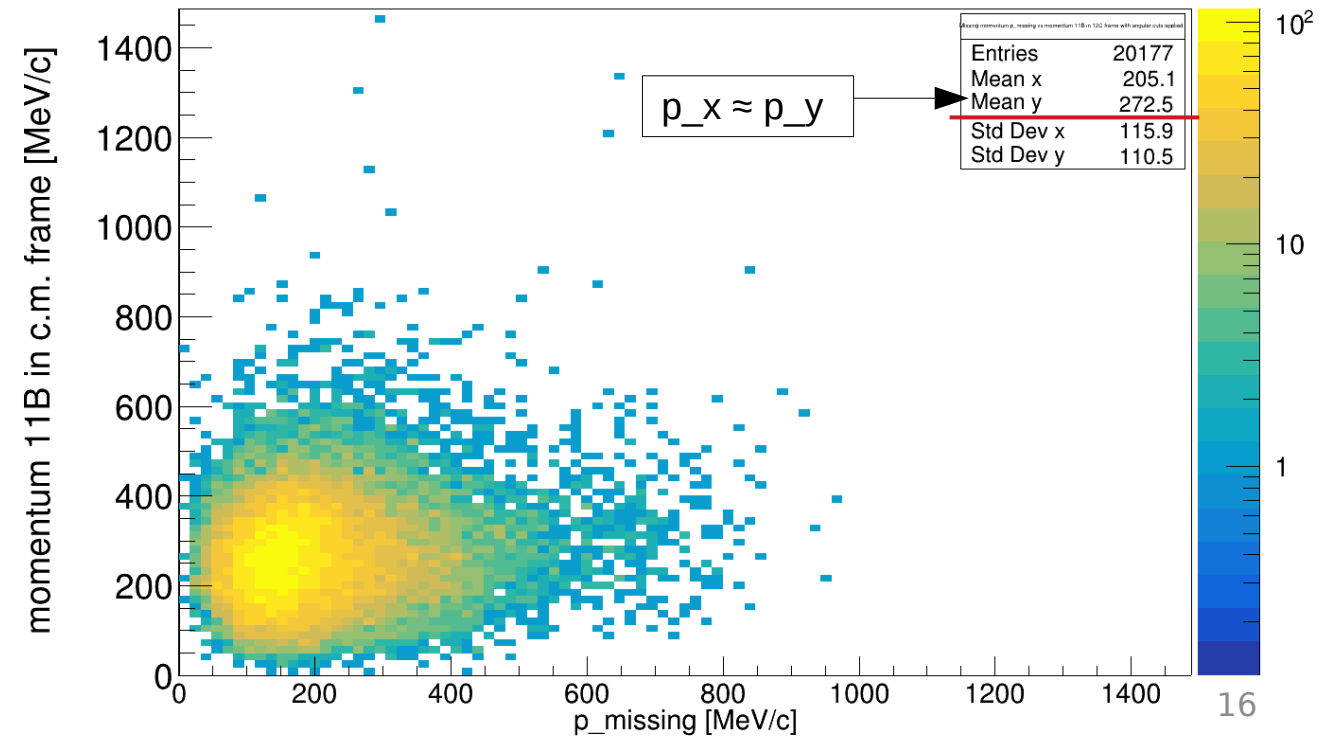


Momentum p_i vs p_{11B} in 12C

With y-information from MW1 and MW2

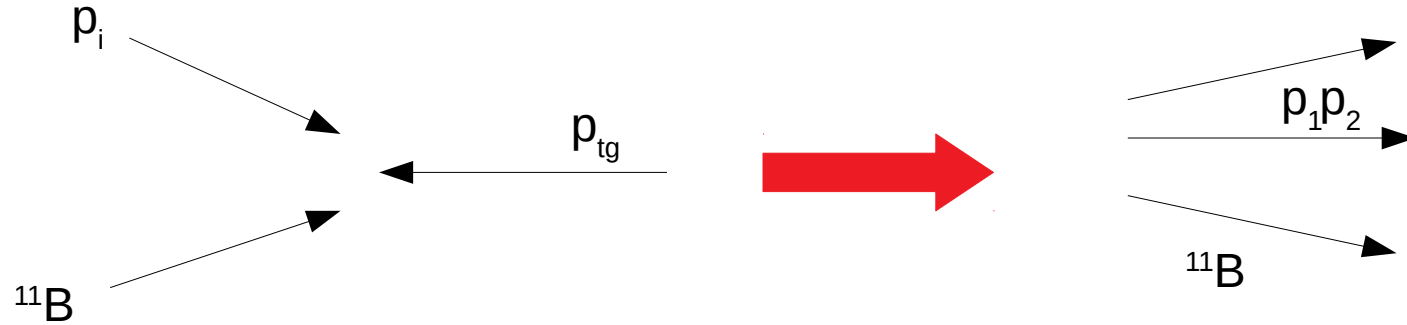


Now with y-info from MW1 and MW3





Missing mass reconstruction

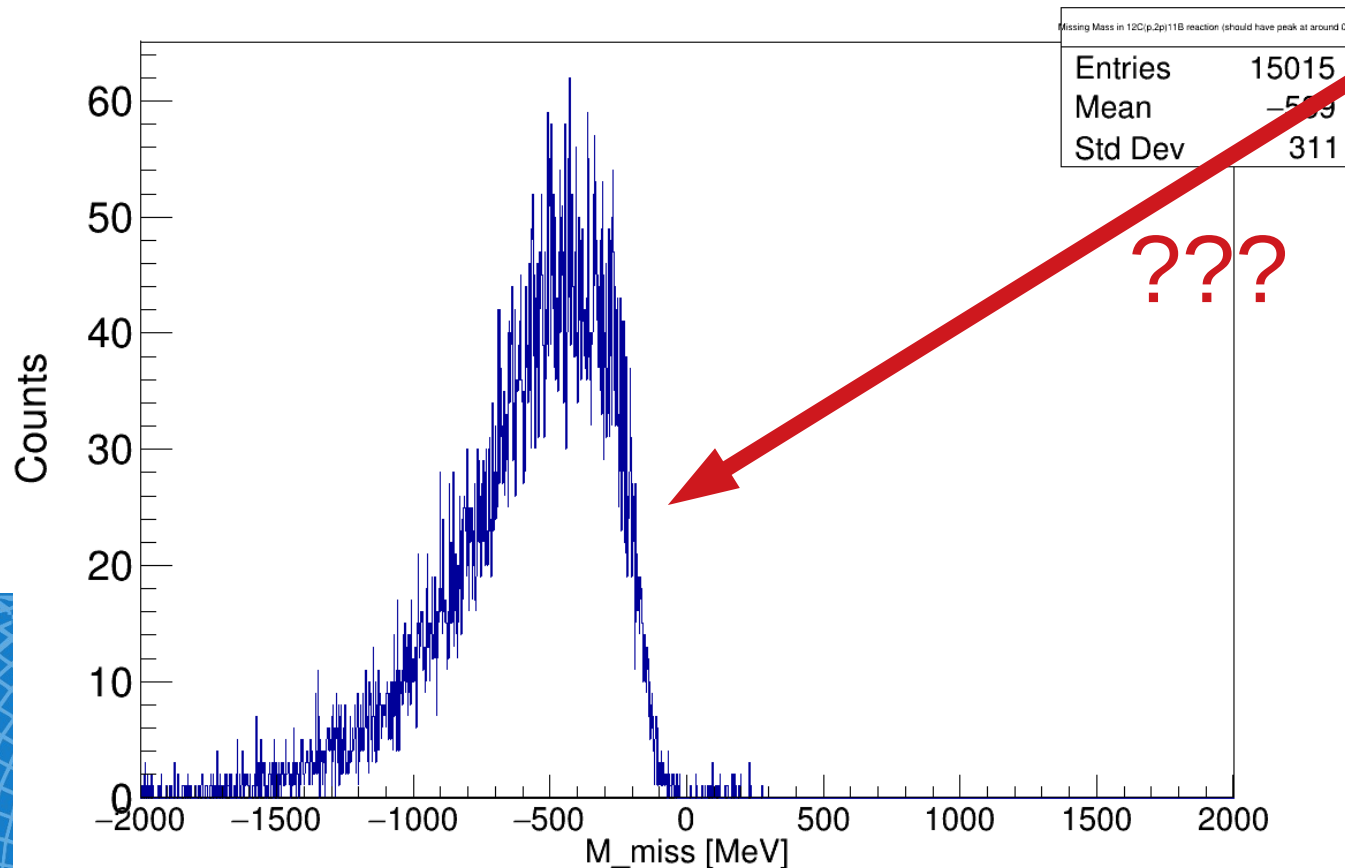


$$M_{miss} = \sqrt{(p_{12C} - p_i - p_{11B})^2}$$

should be ≈ 0

→ give better look at the 3-momentum distribution
(+- permutation at MW position??)

→ as the reconstruction of p_i works well it can be deduced that $11B$ reconstruction faulty....

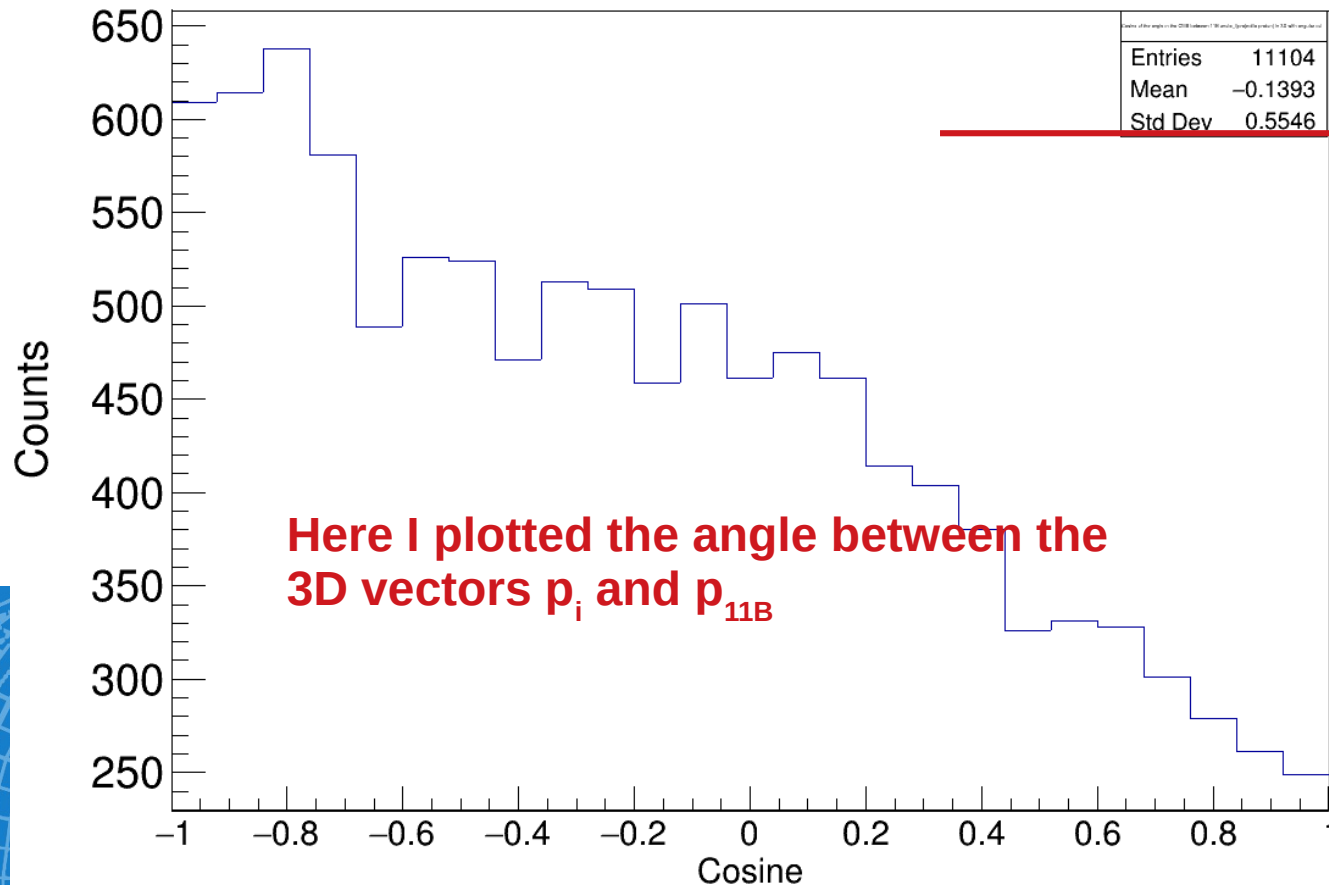




Inner angular distributions

In ^{12}C cms frame (using MW1 and MW2) :

Cosine of the angle in the CMS between ^{11}B and p_i (projectile proton) in 3D with angular cut

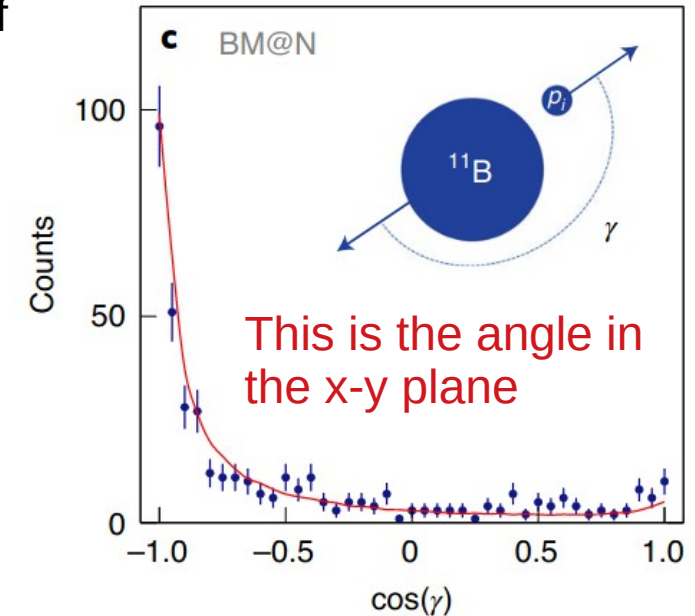
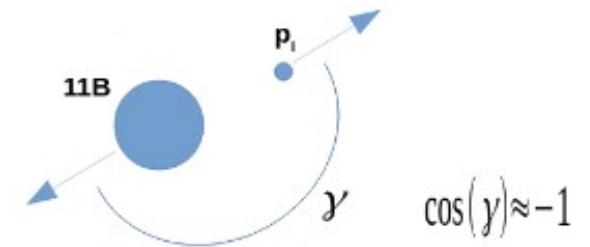


Not satisfactory....

See:

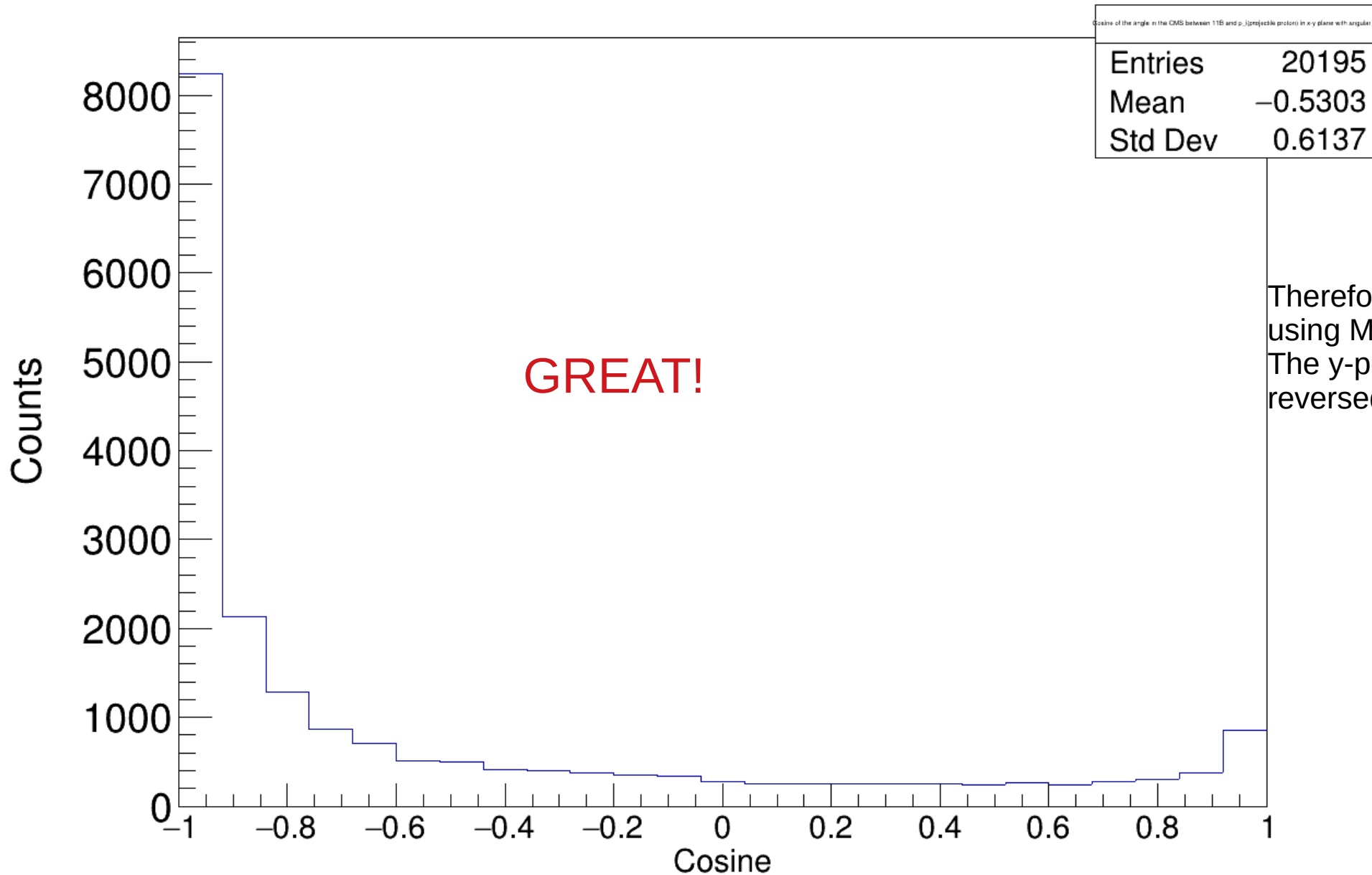
<https://www.nature.com/articles/s41567-021-01193-4.pdf>

$$p_{^{12}\text{C}} = p_i + p_{^{11}\text{B}}$$





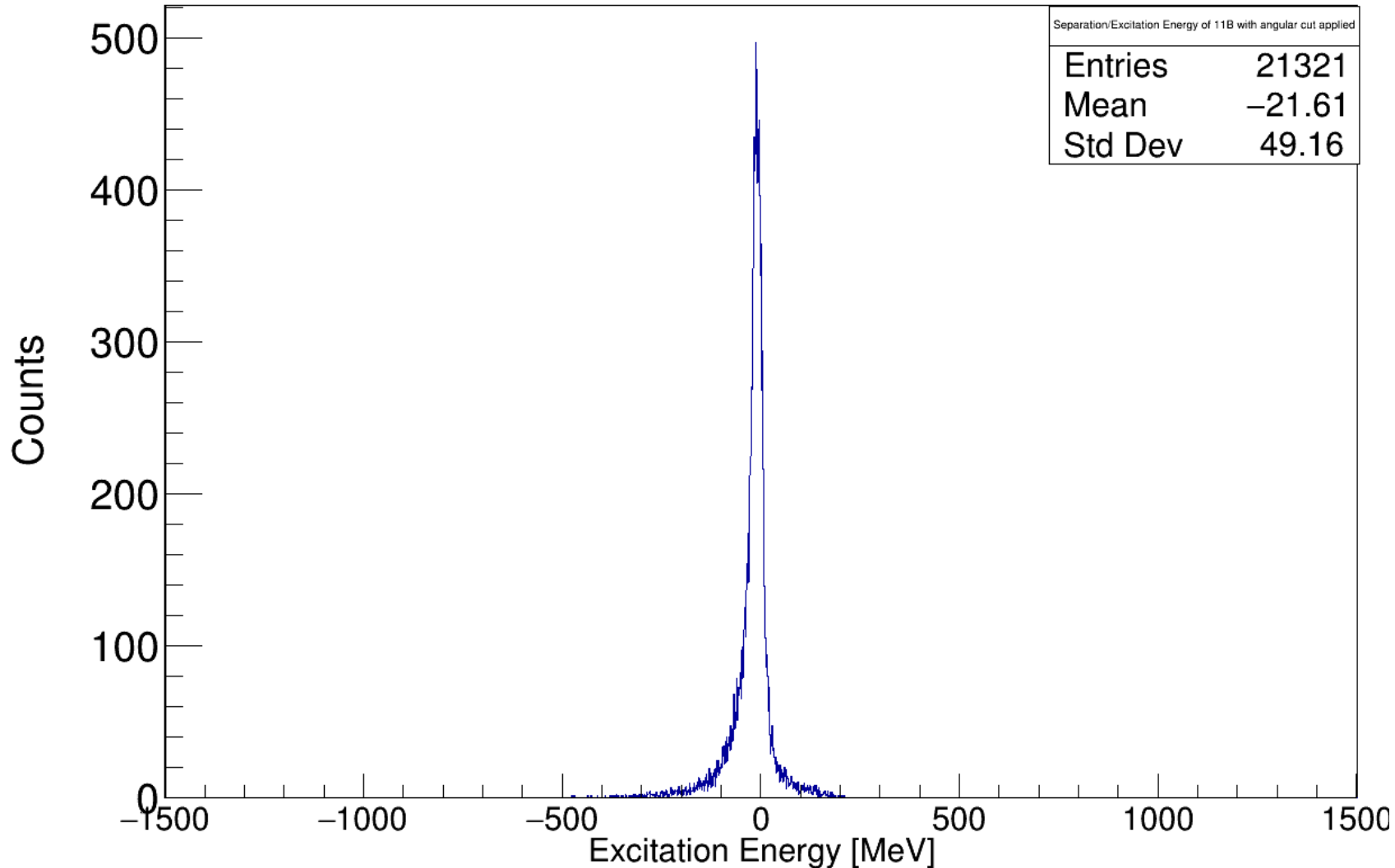
Angular Distribution in x-y plane



Therefore the y position was determined using MWPC3
The y-position of MWPC3 has been reversed (meaning $+y \rightarrow -y$ and $-y \rightarrow +y$)

Excitation Energy of ^{11}B

$$E_{exc} = \left(\underbrace{P_{^{12}\text{C}} + p_{tg} - p_1 - p_2}_{-p_i} \right) \cdot M - M_{^{11}\text{B}}$$

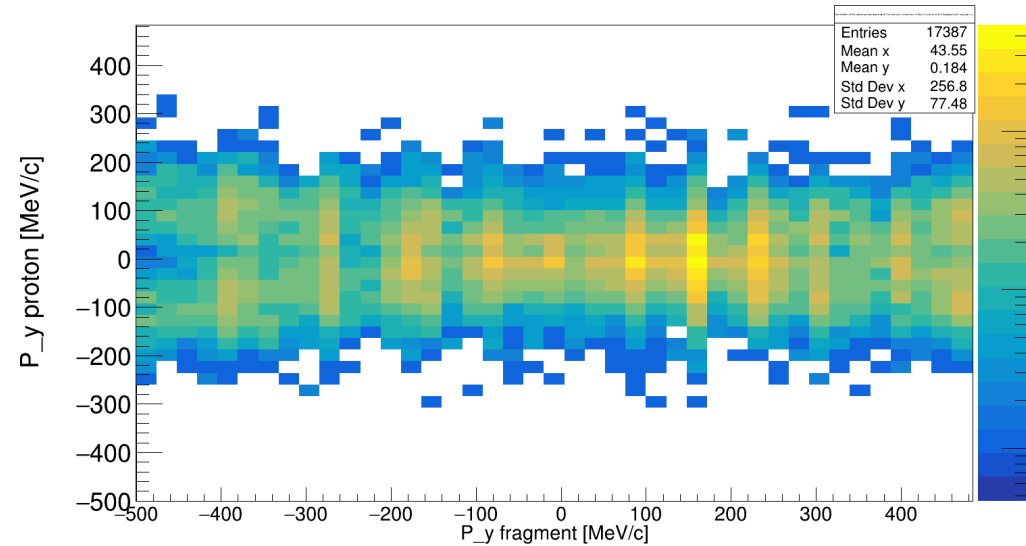


Is this formula valid?

With given formula:

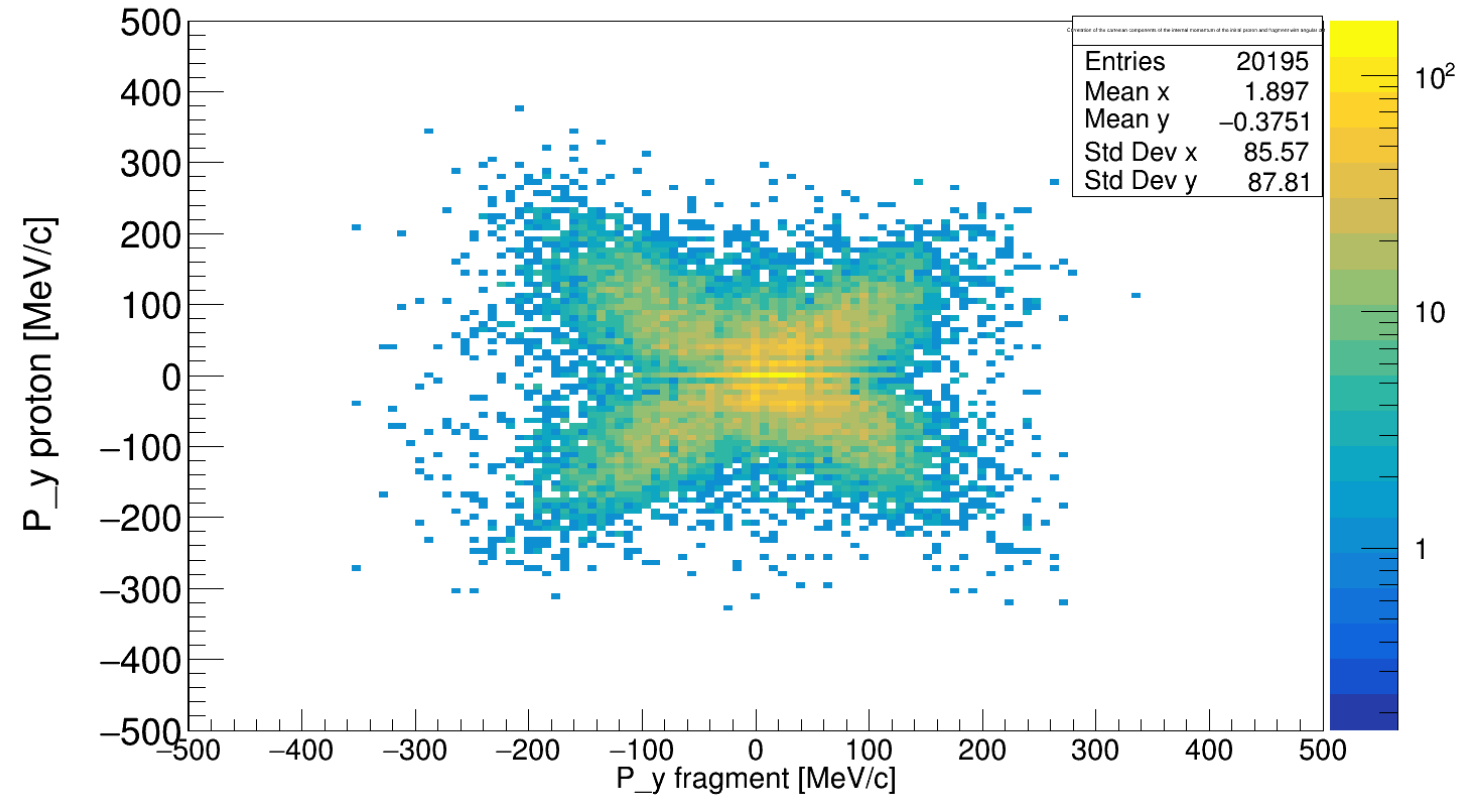
$$P_y = Q_k \times \sin\theta_k \sin(\varphi_k - \varphi_i),$$

This plot was with P_y _fragment reconstruction from MW1 and MW2



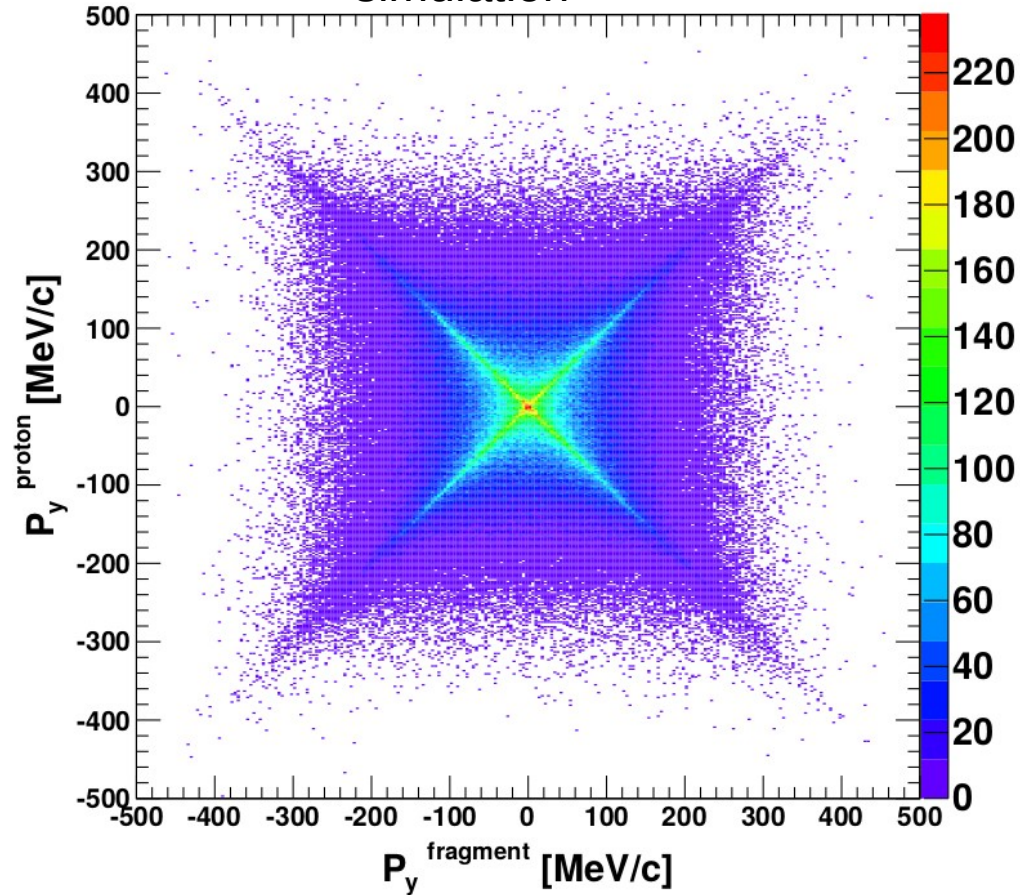
This is with P_y _fragment reconstruction from MW1 and MW3

Correlation of the cartesian components of the internal momentum of the initial proton and fragment with angular cut

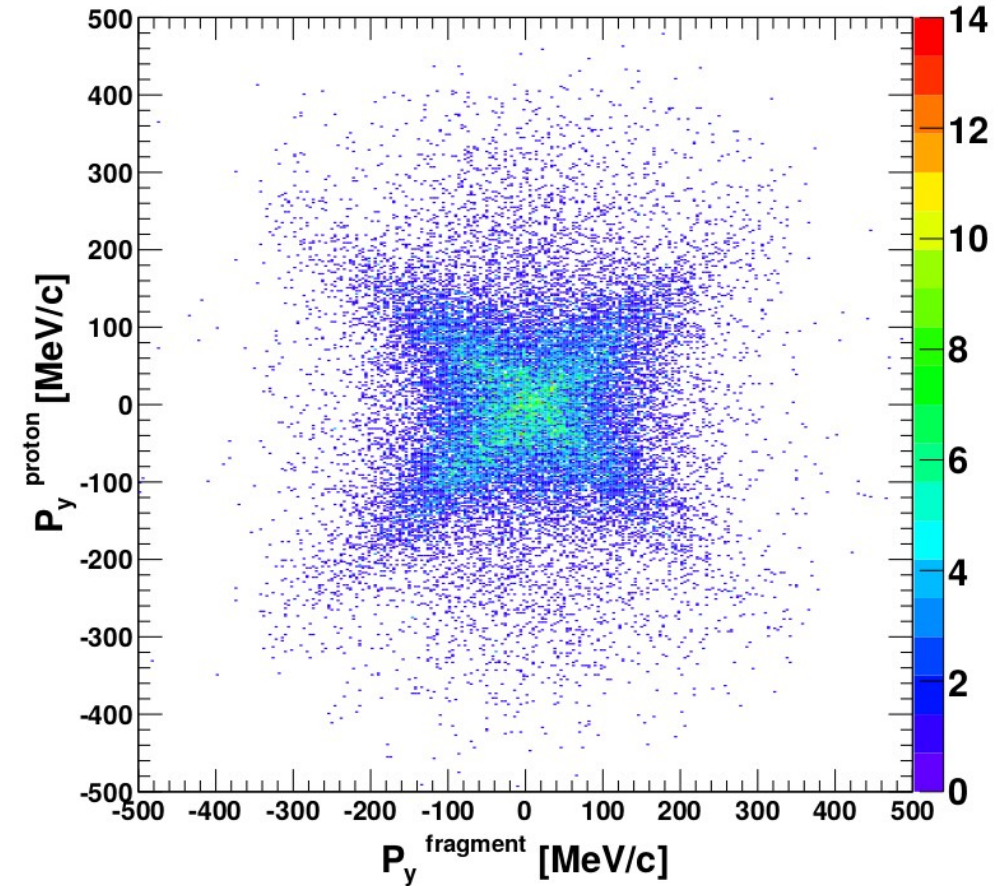


What we expect:

simulation



experiment





Explanation of $P_y = Q_k \times \sin\theta_k \sin(\varphi_k - \varphi_i),$



$Q_k \times \sin\theta_k \sin(\varphi_k - \varphi_i)$ Is a Cartesian component of the internal momentum of the internal momentum of the knocked out proton from ^{12}C perpendicular to the reaction plane.
The reaction plane is given by the ^{12}C momentum vector and the scattered target proton.

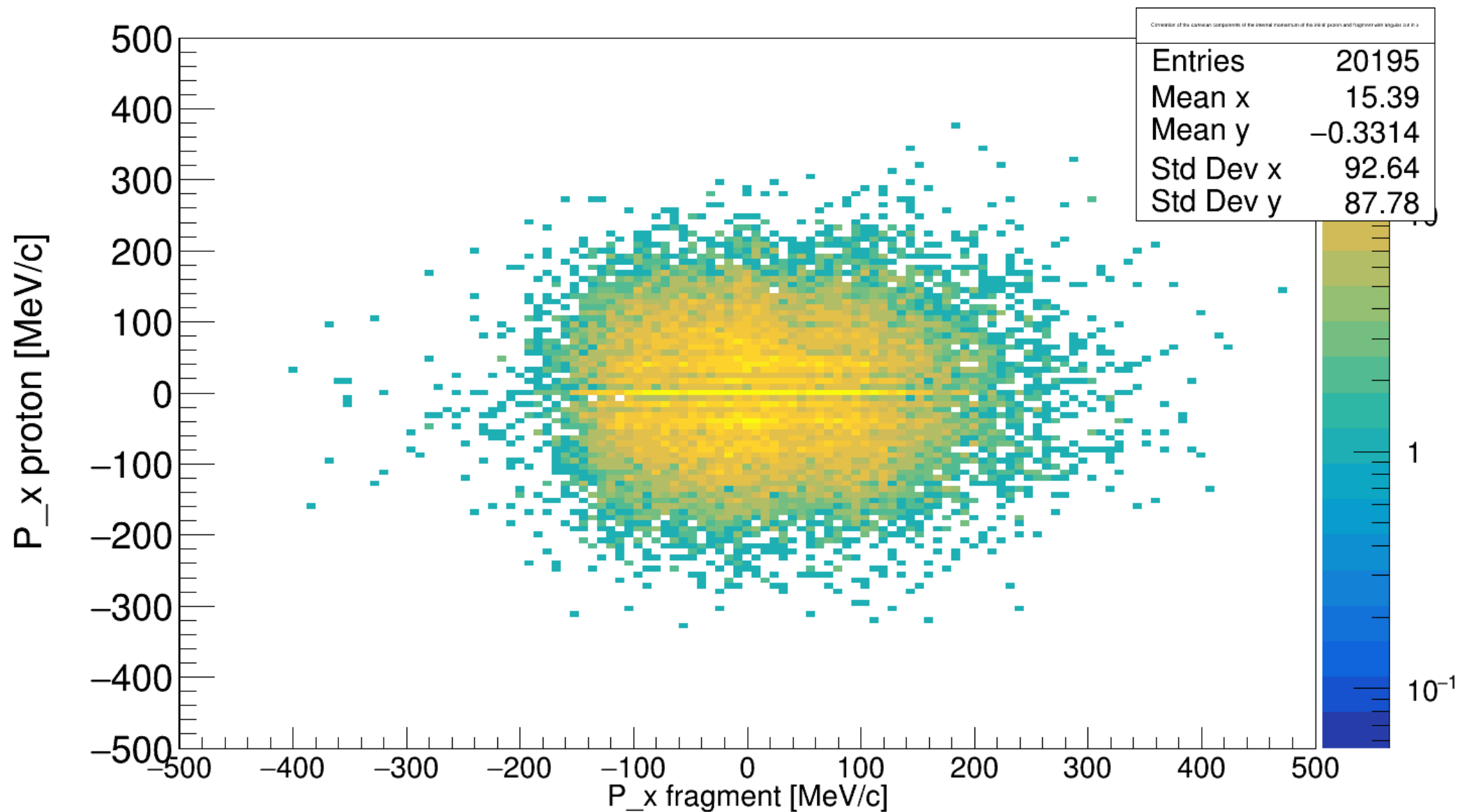
Can be plotted also against $P_{x_fragment}$ (see next slide). This is a blurred centered spot. This can be explained by:

- acceptance of CALIFA: no crystals in the $\phi \pm 90^\circ$ region , therefore the y component is dominant
- low precision for y position (can be partly solved using MW1.Y vs MW3.Y, but then straggling..)

For more details and derivation see:

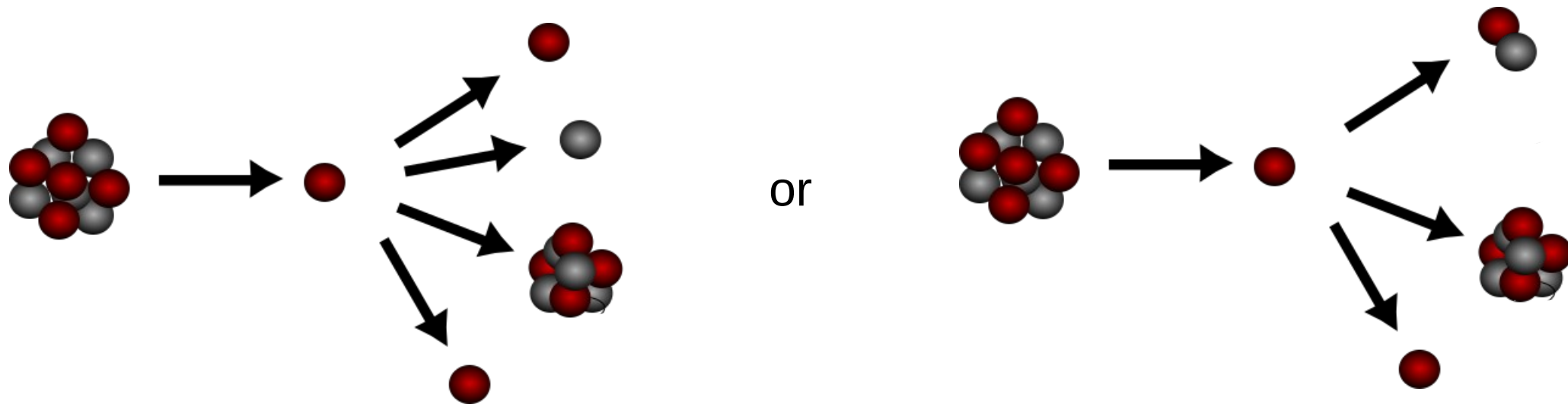
<https://www.sciencedirect.com/science/article/abs/pii/S0375947405008523>

Correlation of the cartesian components of the internal momentum of the initial proton and fragment with angular cut in x





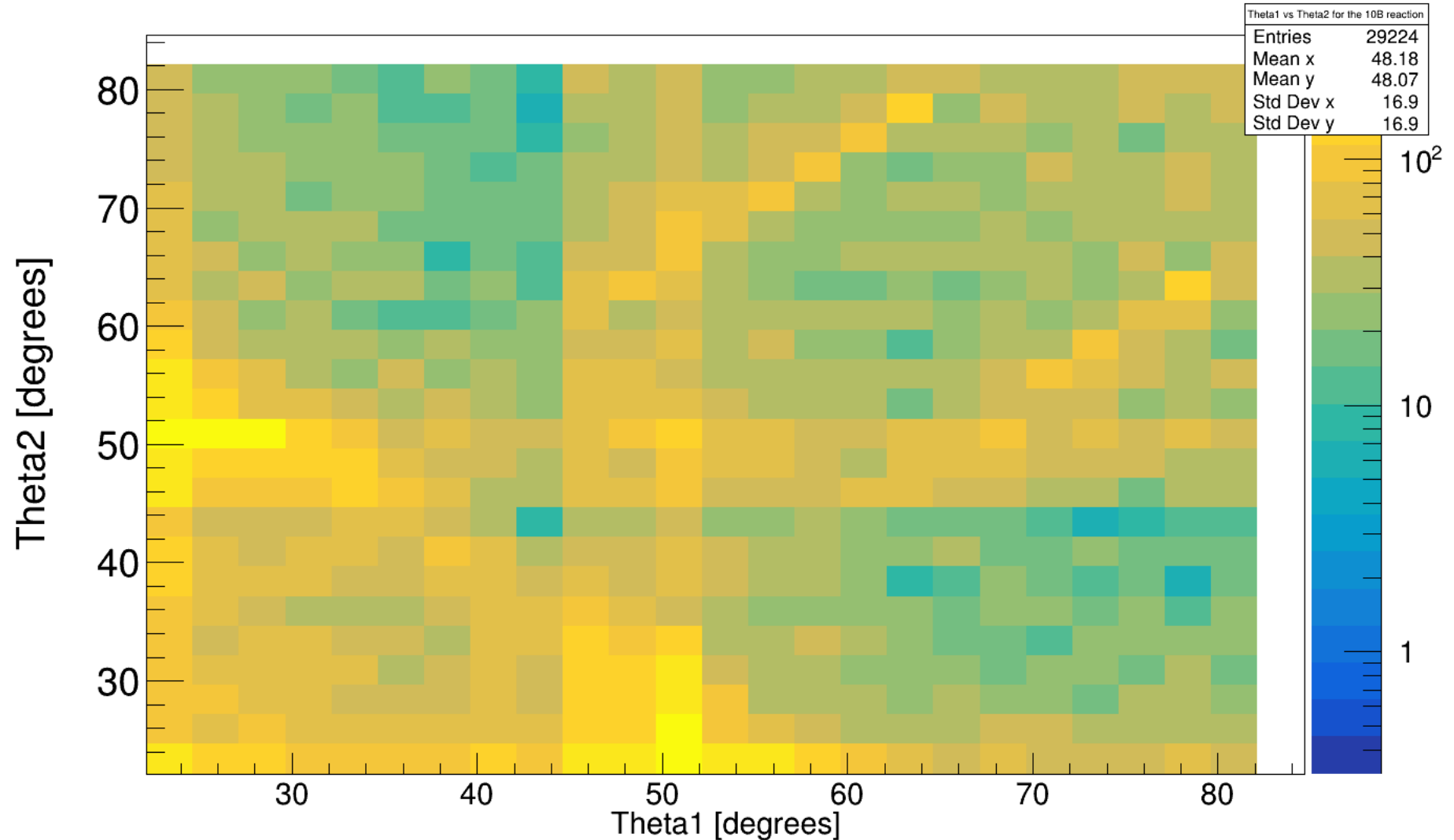
$^{12}\text{C}(\text{p}, \text{ppn}/\text{pd})^{10}\text{B}$ Reaction



First Angular and Momentum Plots ...

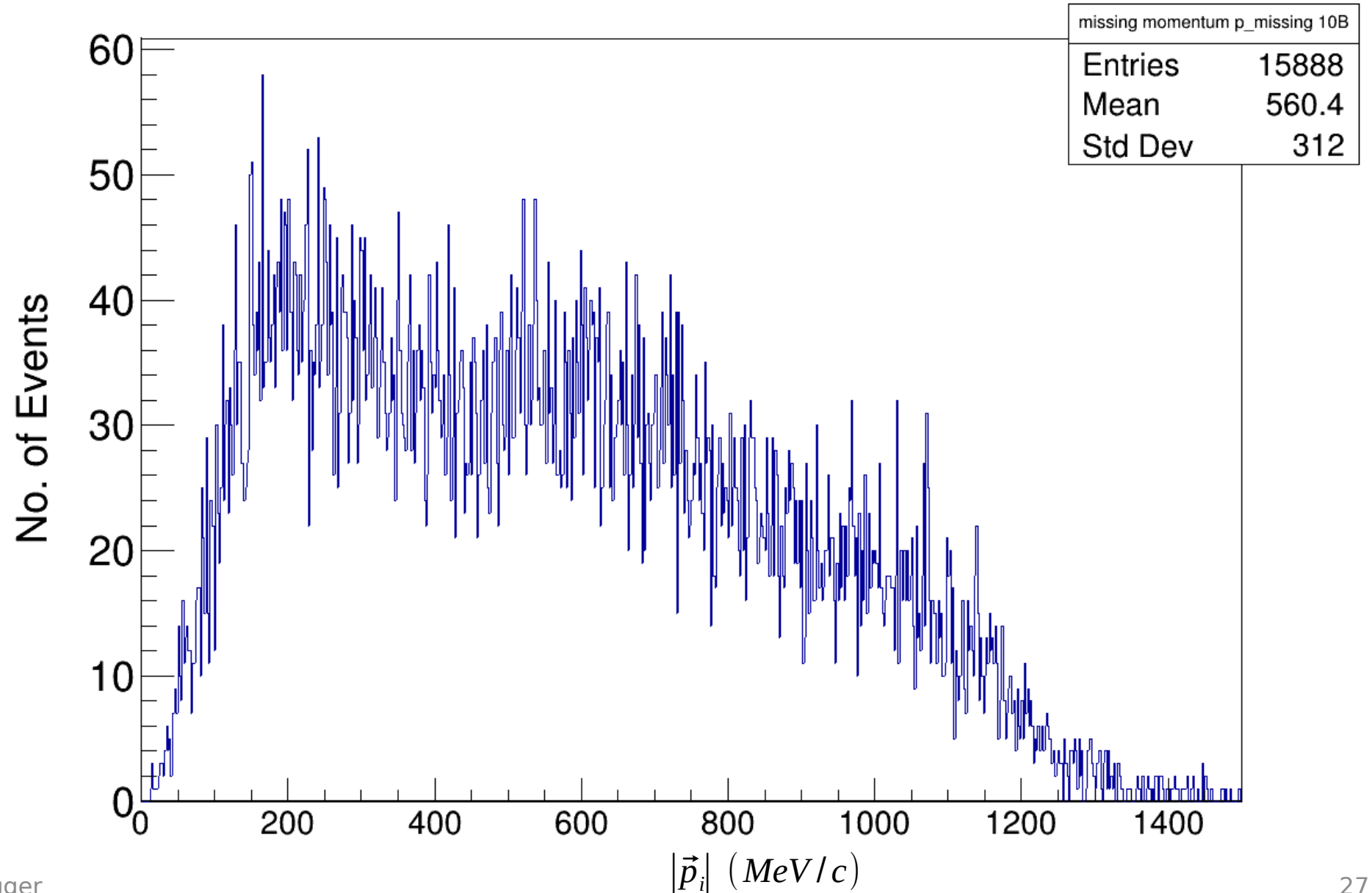
Without cut:

Theta1 vs Theta2 for the 10B reaction



Reconstruction of inner momentum p_i

$$\vec{p}_i = (\vec{p}_1 + \vec{p}_1 - \vec{p}_{tg})$$





Neutron Mass Reconstruction

$$M^2_{\text{missing}} = (\underbrace{p_{12C} + p_{tg}}_{\text{before reaction}} - \underbrace{p_1 + p_2 + p_{10B}}_{\text{after reaction}})^2$$

