



# Quasi Free Scattering with S444 Data (2020)

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Analysis WG Meeting  
22.07.2021

$^{12}\text{C}(p,2p)^{11}\text{B}$  reaction

$^{12}\text{C}(p,\text{ppn}/\text{pd})^{10}\text{B}$  reaction

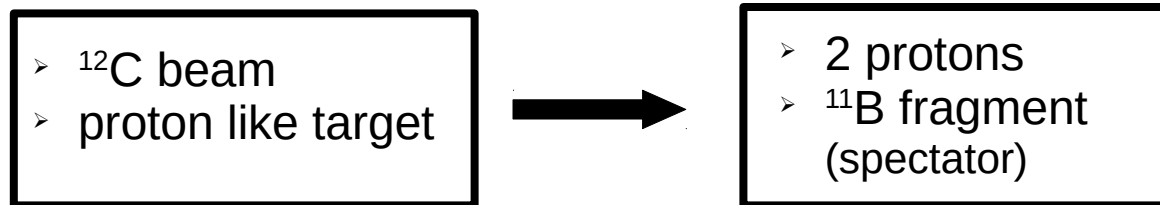
SRC Analysis



Supported by BMBF 05P15WOFNA and 05P19WOFN1.

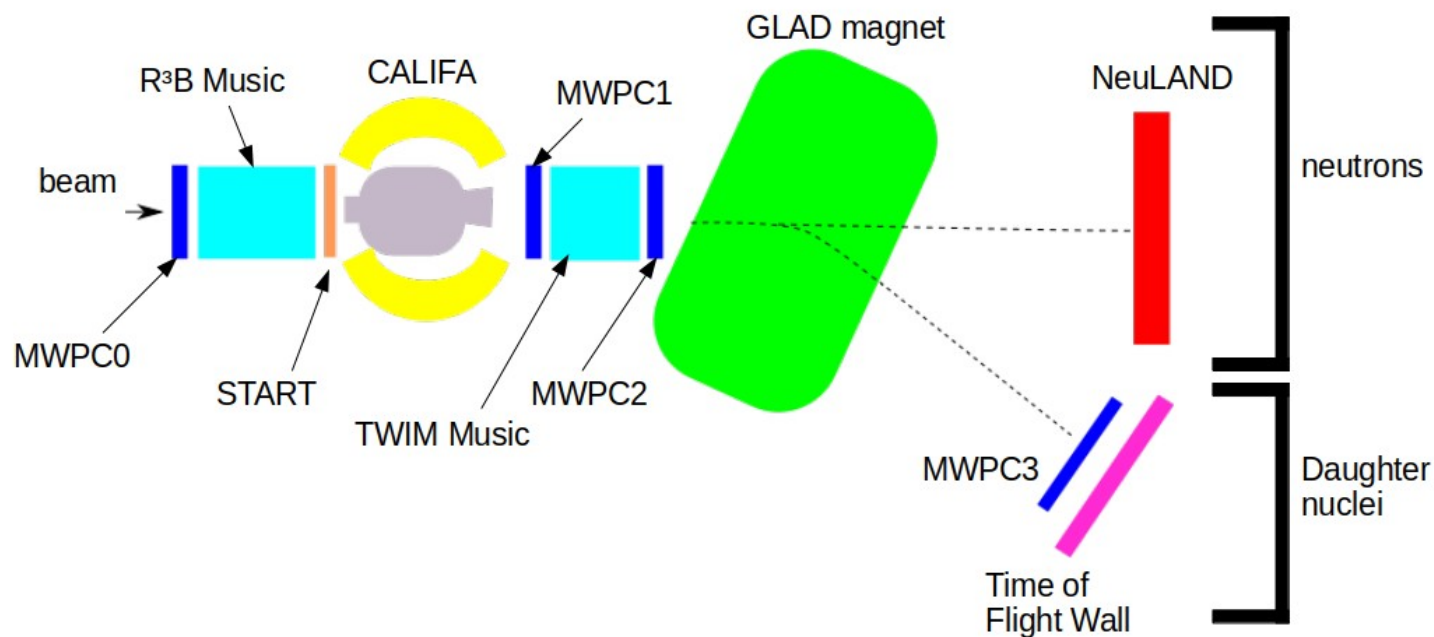
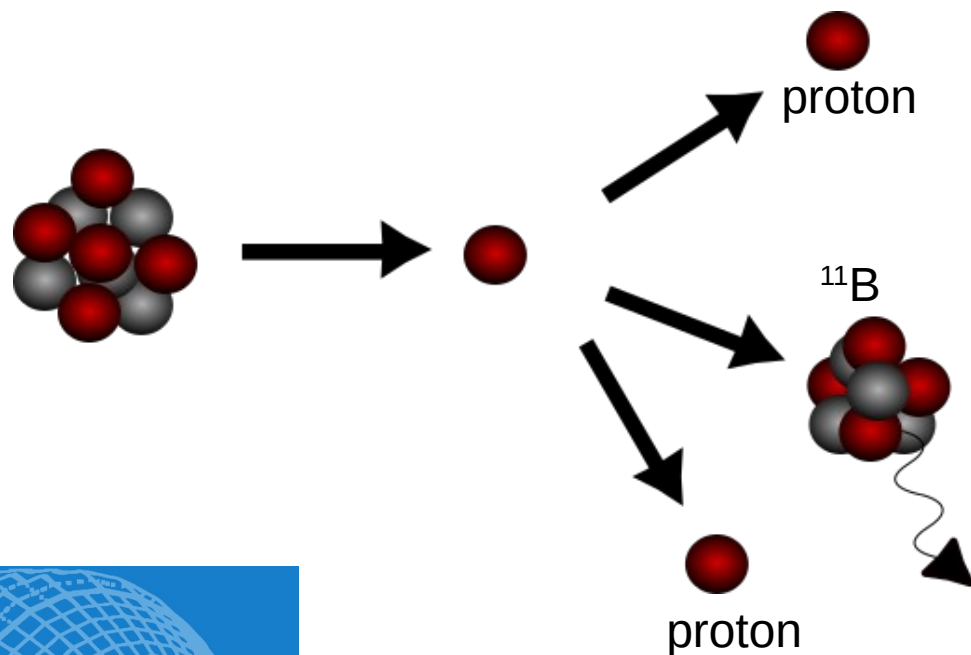
The results presented here are based on the experiment s444/s473, which was performed at the beam line/infrastructure Cave C at the GSI Helmholtzzentrum für Schwerionenforschung, Darmstadt (Germany) in the frame of FAIR Phase-0.

**$^{12}\text{C}(p,2p)^{11}\text{B}$  reaction:**



**SETUP:**

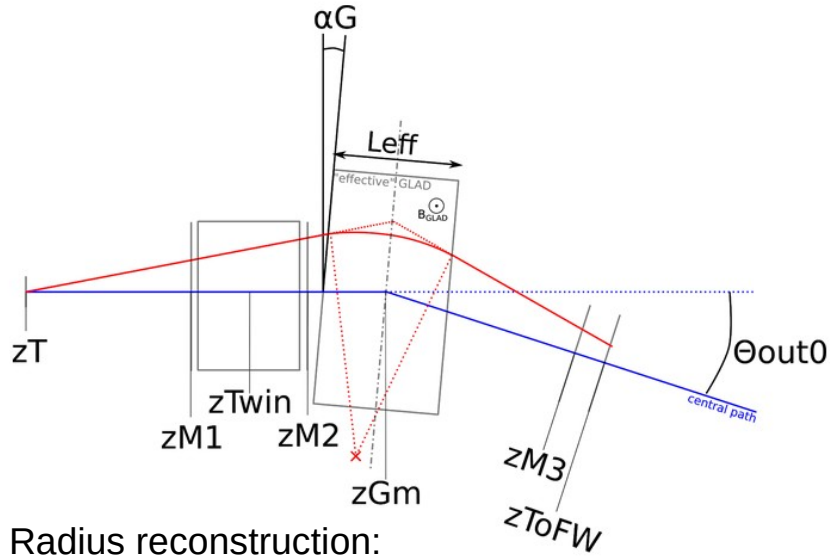
**Beam energy: 400 AMeV**  
**Beamtype:  $^{12}\text{C}$**   
**Target:  $\text{CH}_2$**





# Fragment Particle Identification

Flightpath reconstruction:

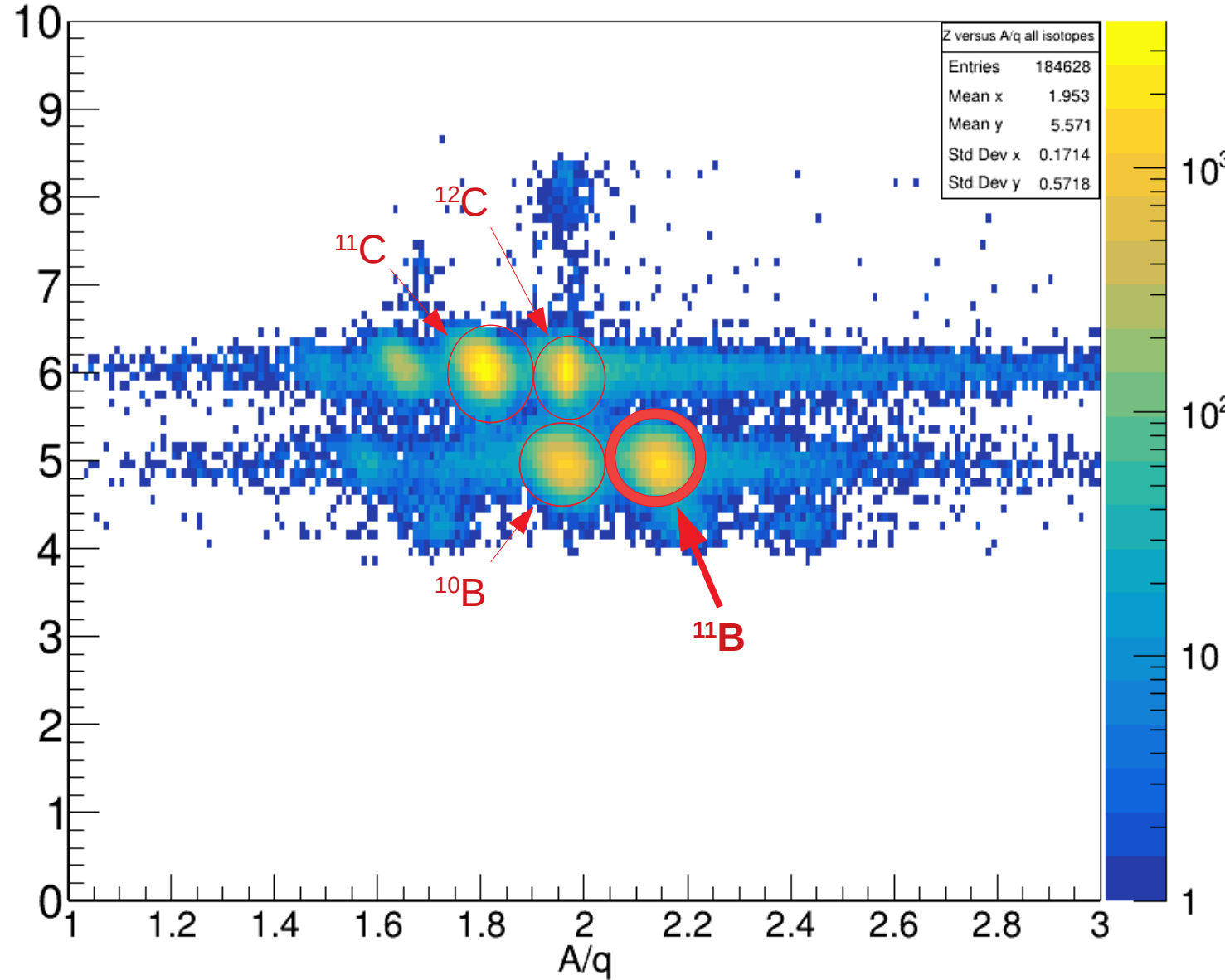


Radius reconstruction:

$$R = \frac{L_{eff}}{2 \sin\left(\frac{\theta_{in} + \theta_{out}}{2}\right)}$$

$$B * \rho = \frac{\beta * \gamma * M}{q}$$

Z (charge)

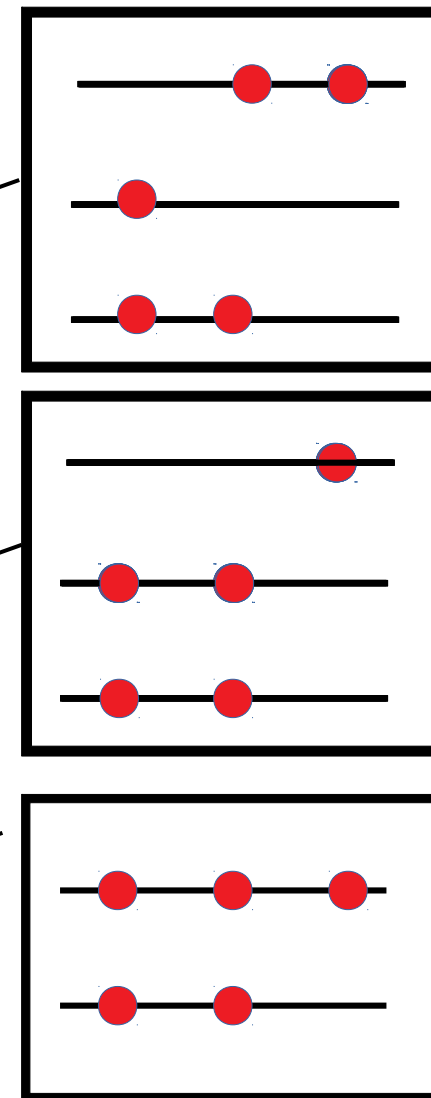
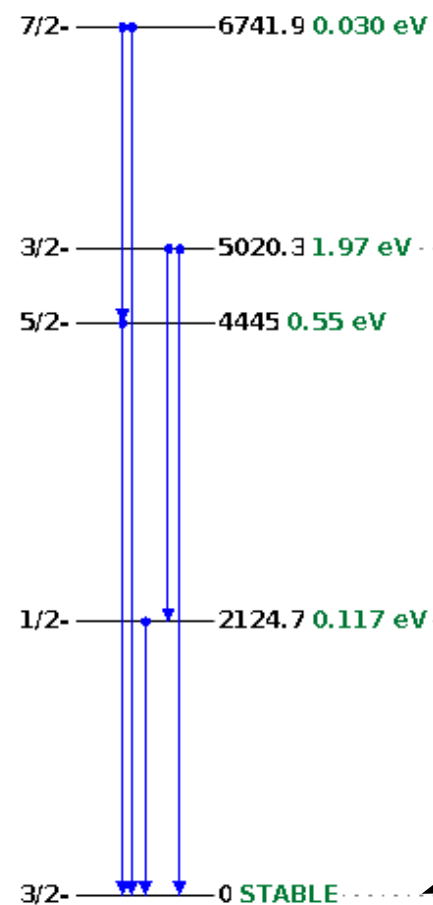
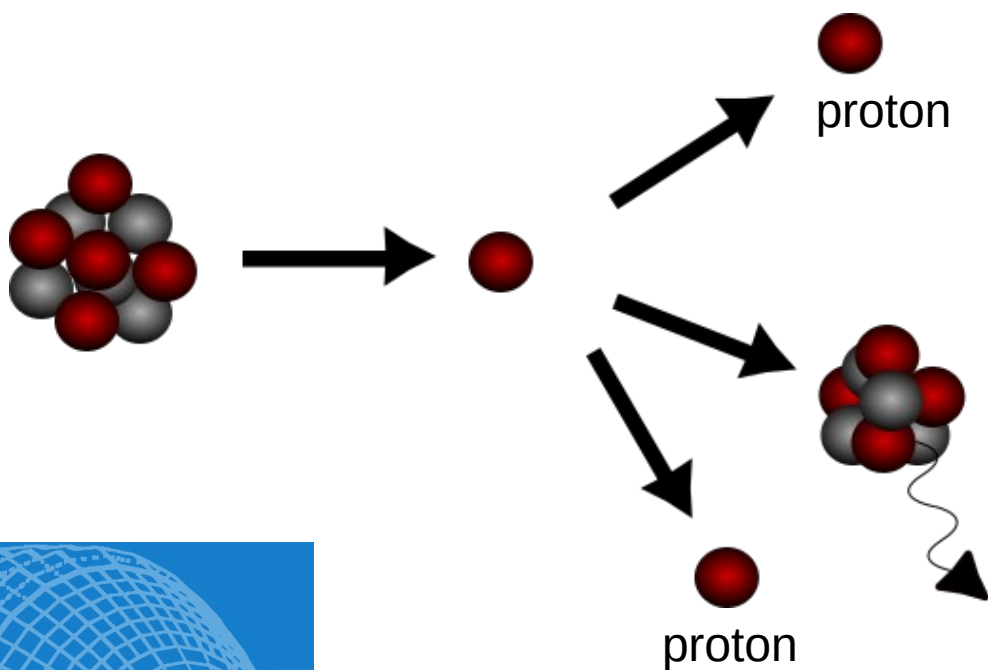




# $^{12}\text{C}(p,2p)^{11}\text{B}$ reaction

## Two Proton Identification:

→ two hits with  $E_{\text{hit}} > 30 \text{ MeV}$

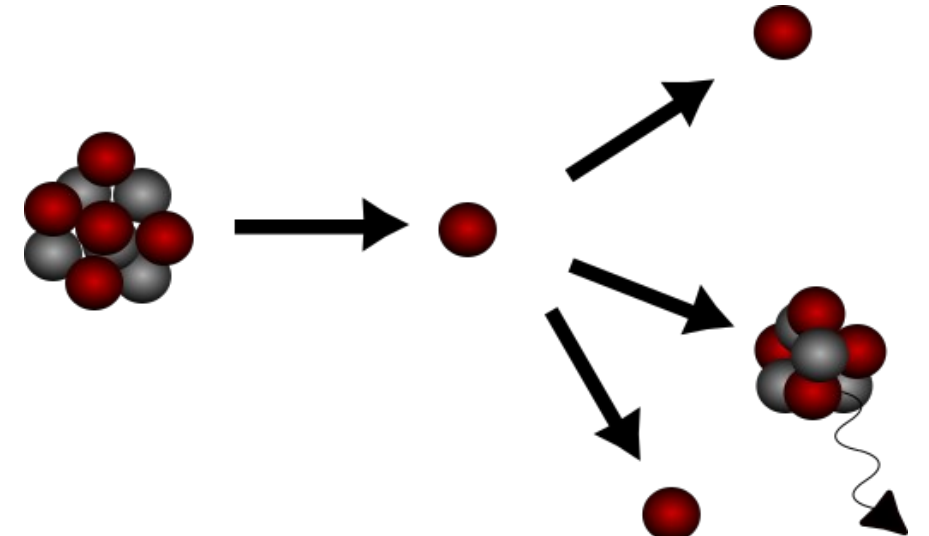
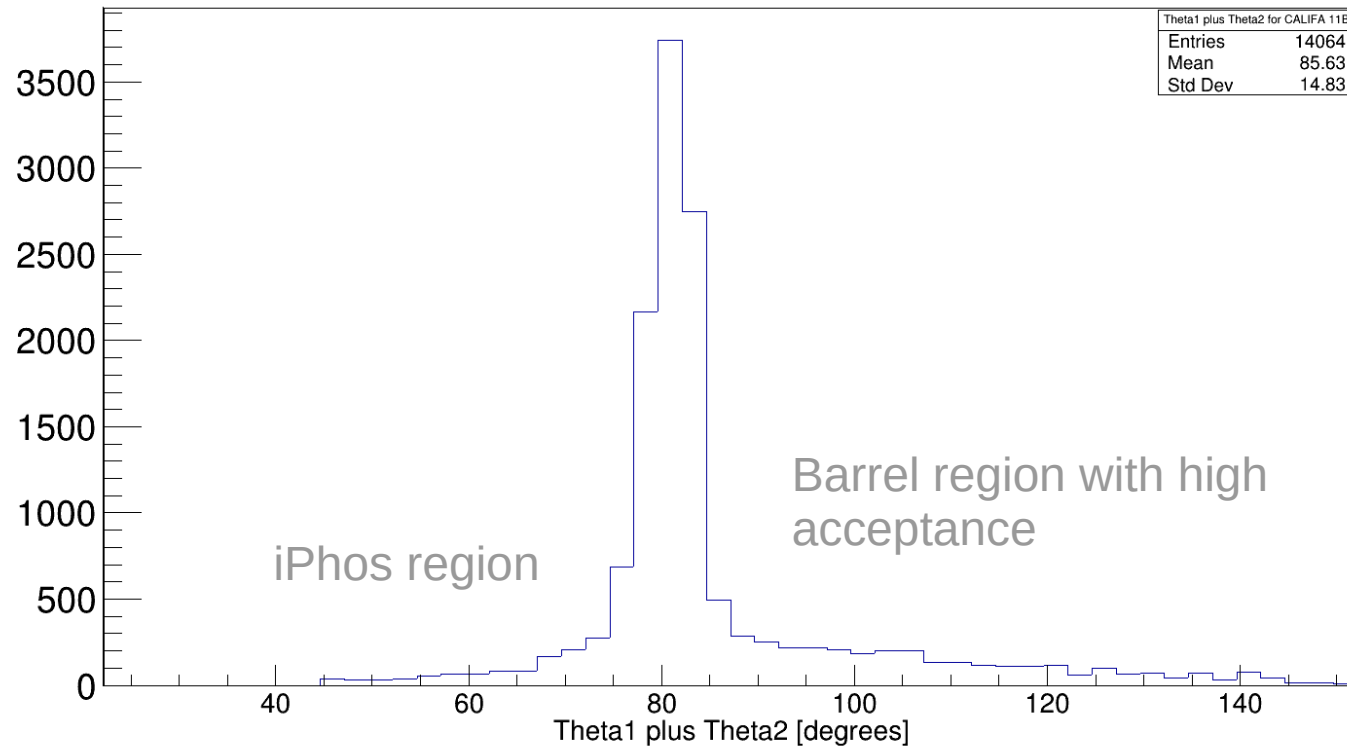
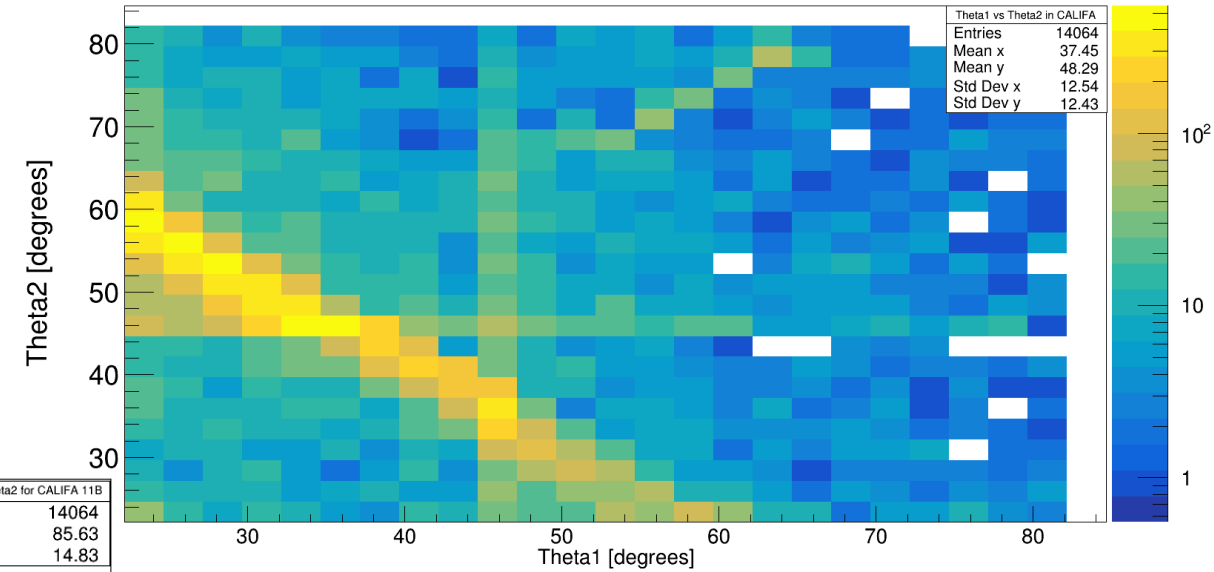
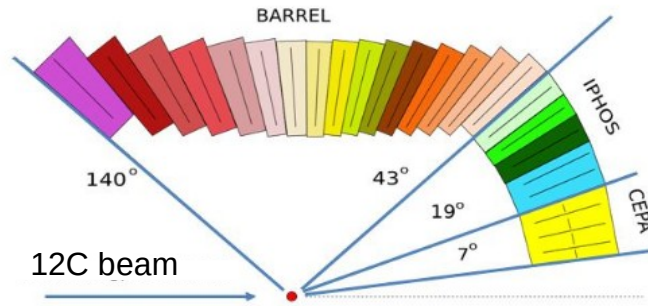




# Polar Angular Distribution of protons for $^{12}\text{C}(p,2p)^{11}\text{B}$

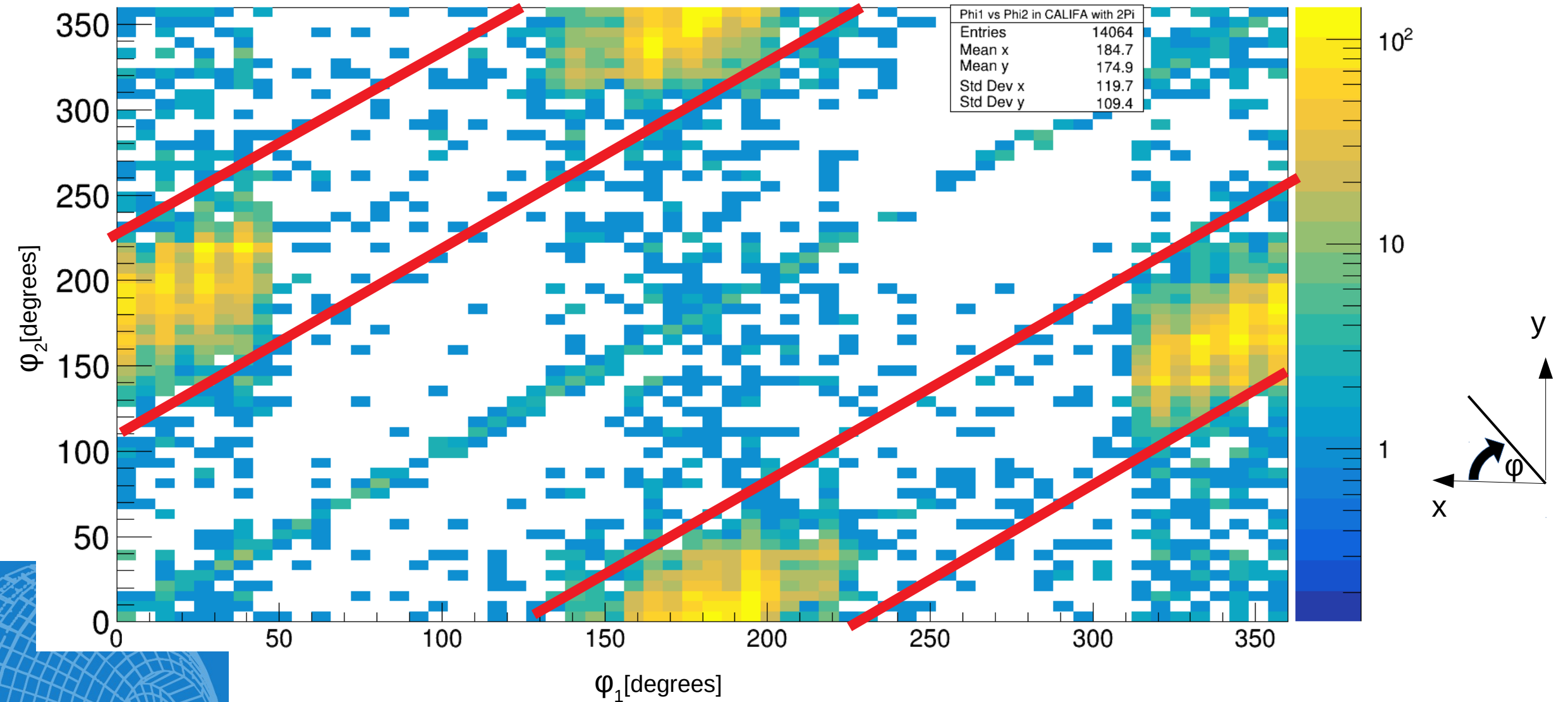


Theta1 vs Theta2 in CALIFA





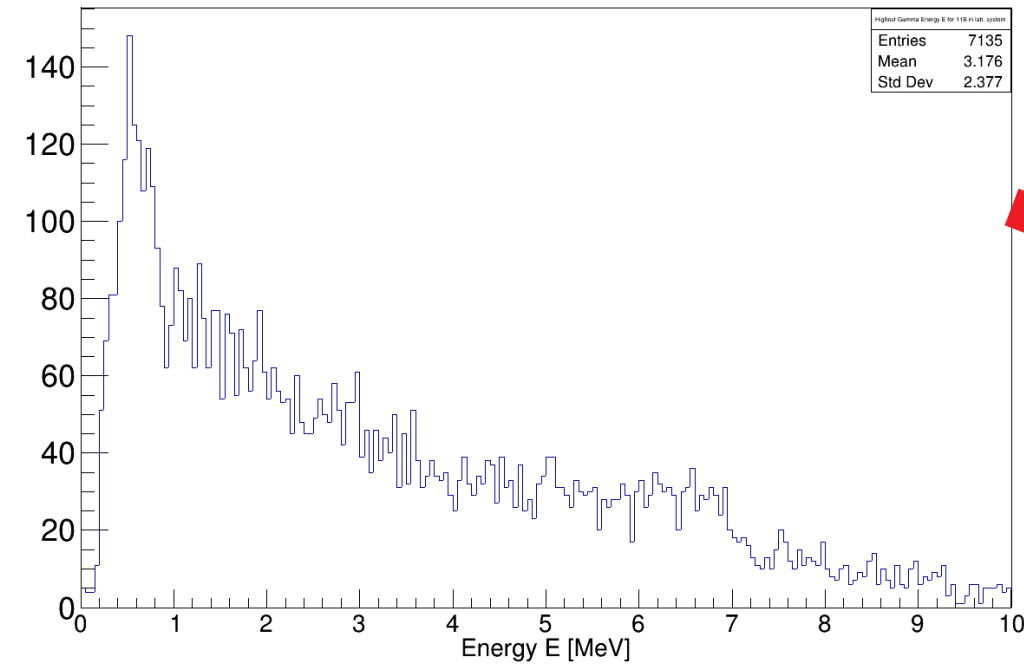
# Arzimuthal Distribution of protons for $^{12}\text{C}(p,2p)^{11}\text{B}$





# Gamma Spectrum of $^{11}\text{B}$

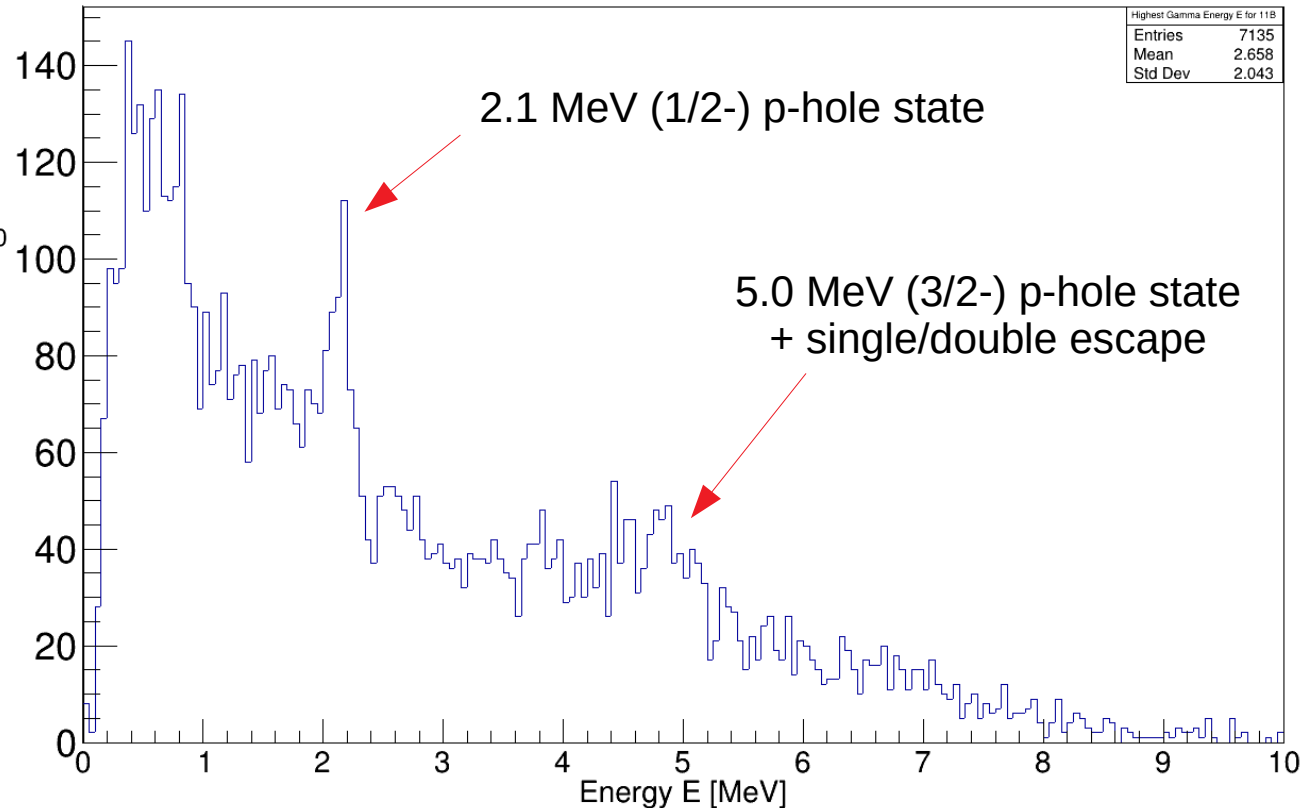
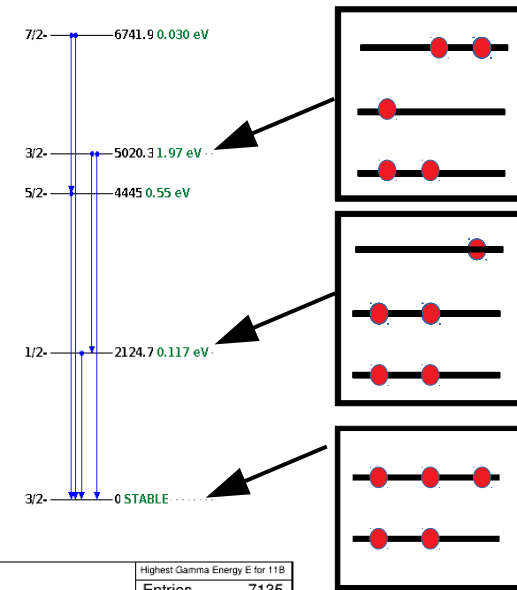
laboratory system



Doppler Correction:

$$E_{\gamma} = \gamma E_{lab} (1 - \beta \cos(\theta))$$

$^{11}\text{B}$  rest frame





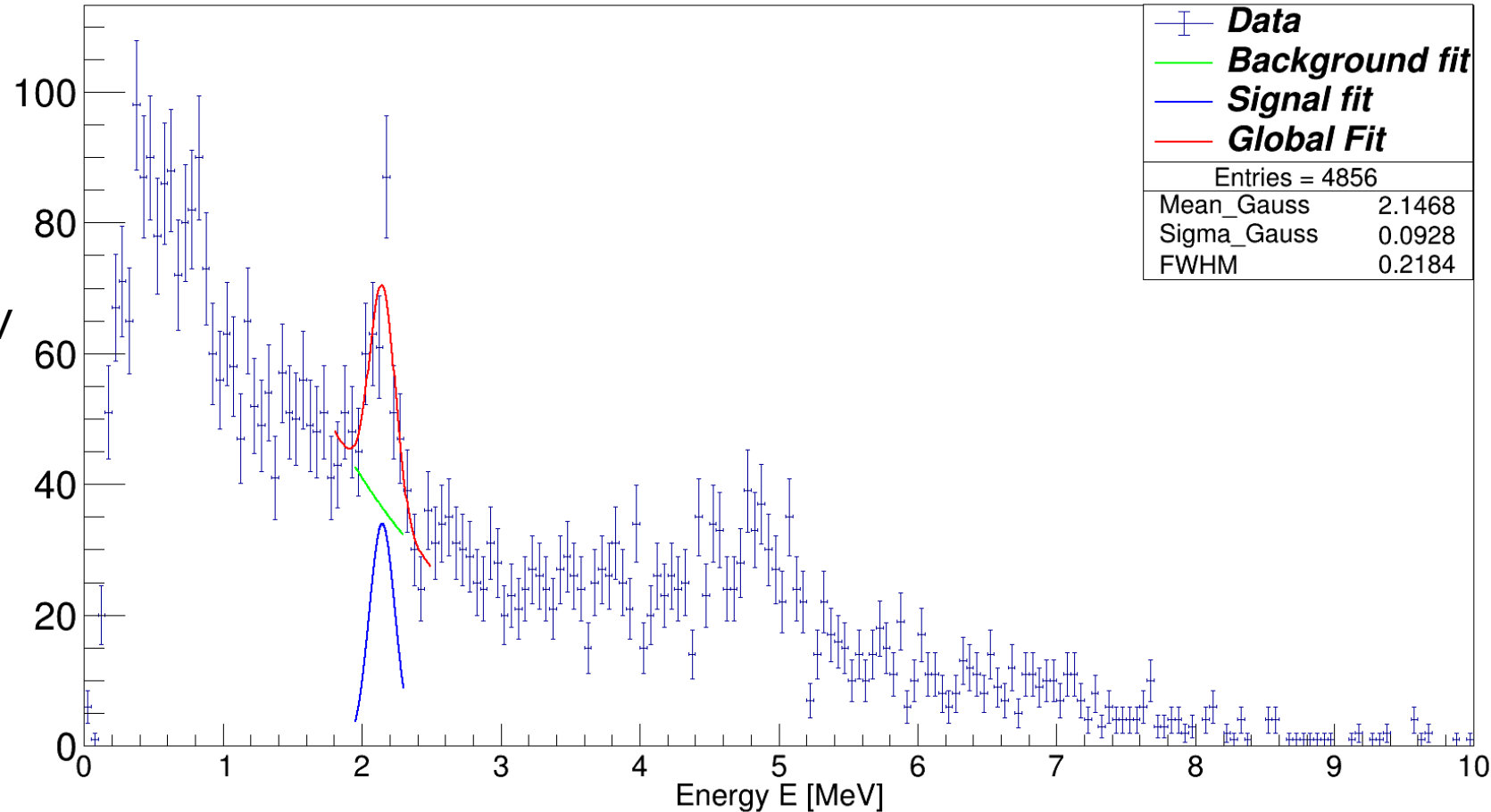


# Gamma Spectrum with Angular Cuts

CALIFA Gamma Energy Spectrum

Event selection criteria for CALIFA:

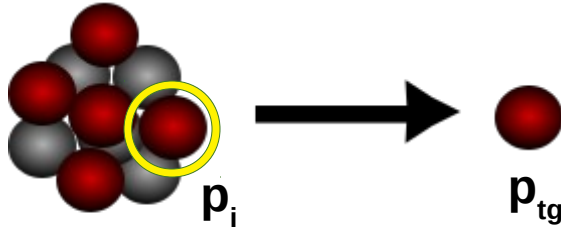
- 11B fragment identification
- two hits (protons) with  $E_{\text{hit}} > 30 \text{ MeV}$
- $\theta_1 + \theta_2 < 90^\circ$
- $\Delta\phi = 180^\circ \pm 40^\circ$



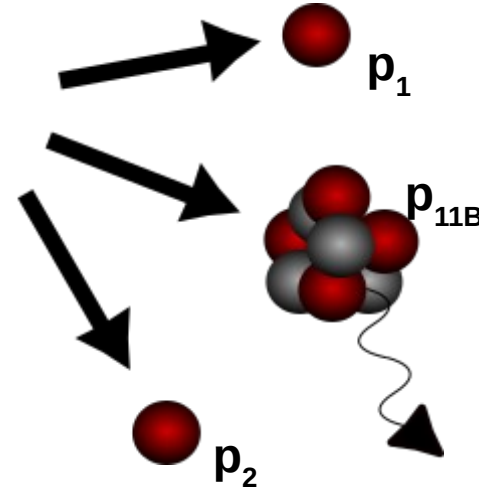


# Reconstruction of Inner Momenta

Before Scattering:



After Scattering:



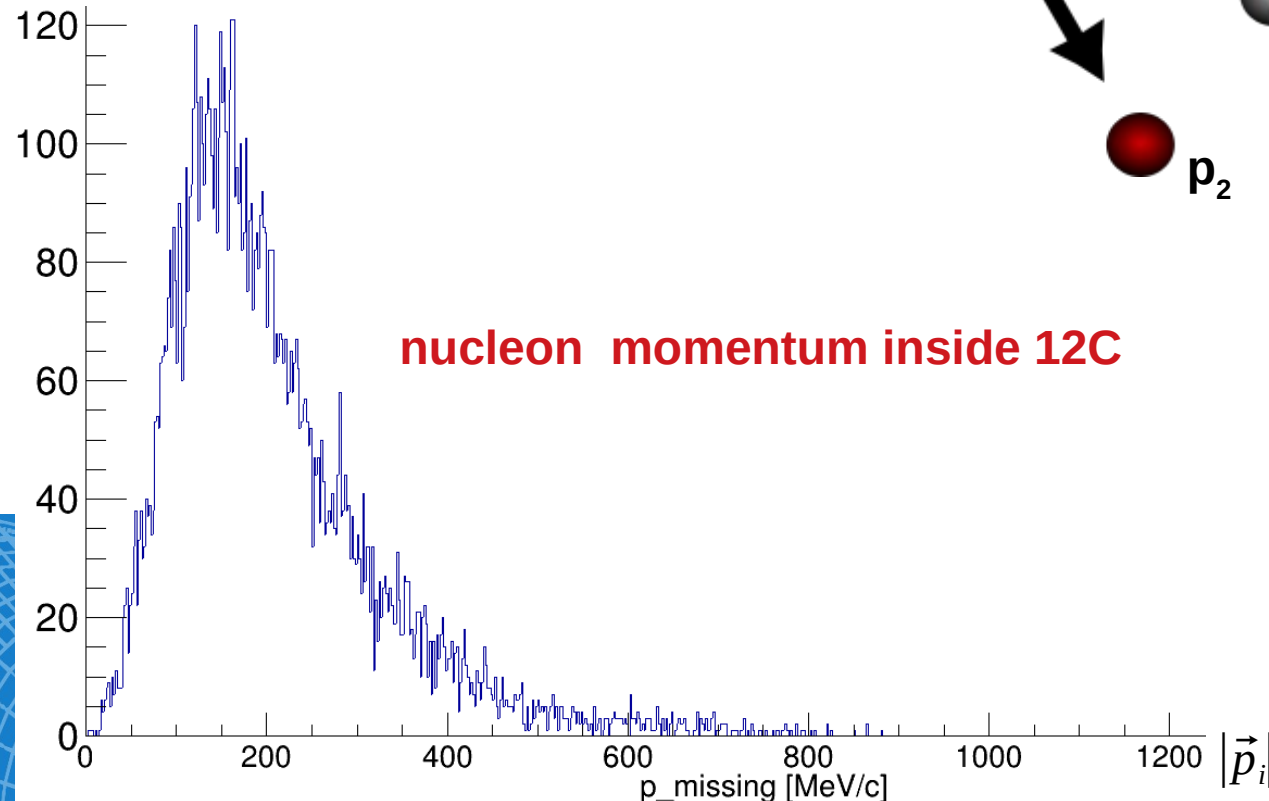
(Four-)Momentum conservation relation:

$$p_{12C} + p_{tg} = p_1 + p_2 + p_{11B}$$

assuming QE scattering in  
mean field potential:

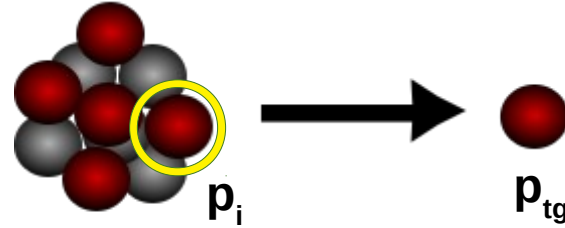
$$p_{12C} = p_i + p_{11B}$$

$$p_i \approx p_{missing} = p_1 + p_2 - p_{tg} \text{ (no ISI / FSI)}$$

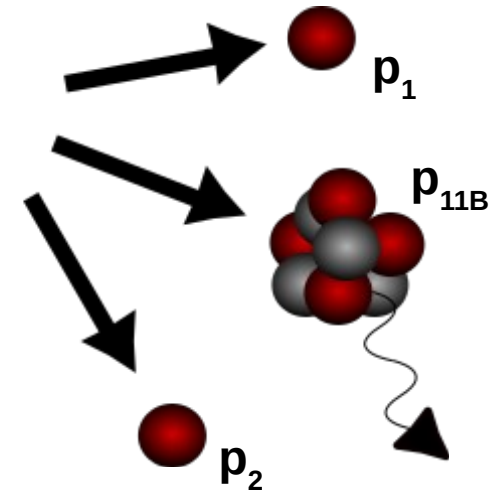


# Momentum components of $p_i$

Before Scattering:

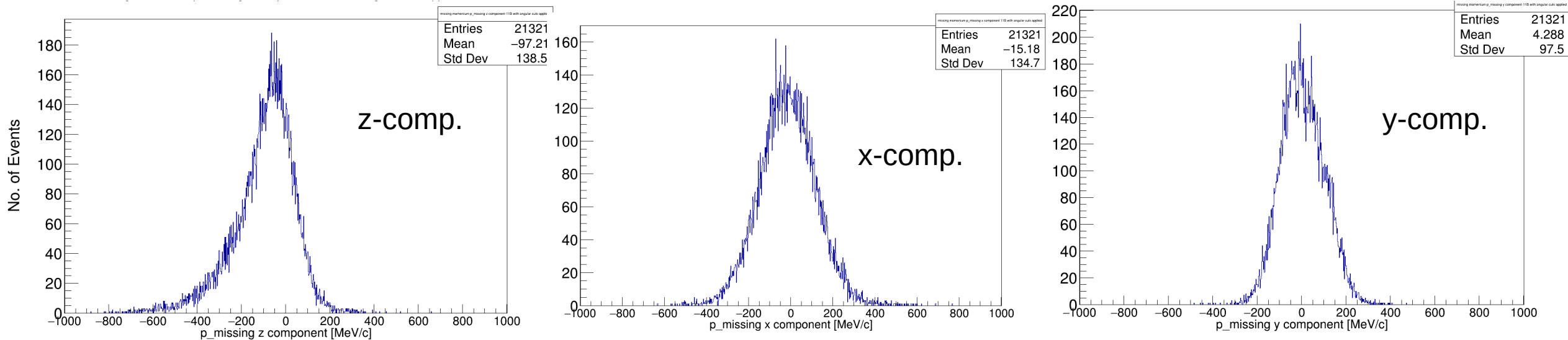


After Scattering:



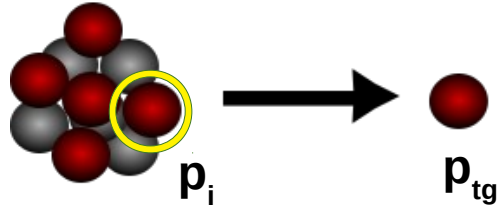
$$p_i \approx p_{\text{missing}} = p_1 + p_2 - p_{\text{tg}} \text{ (no ISI/FSI)}$$

$p_i$  Momentum-Components (with angular cuts applied)

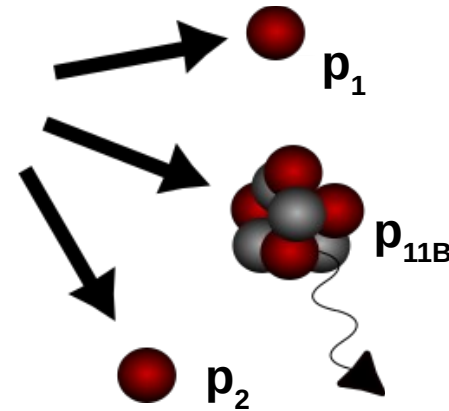


# Mass reconstruction of $p_i$

Before Scattering:

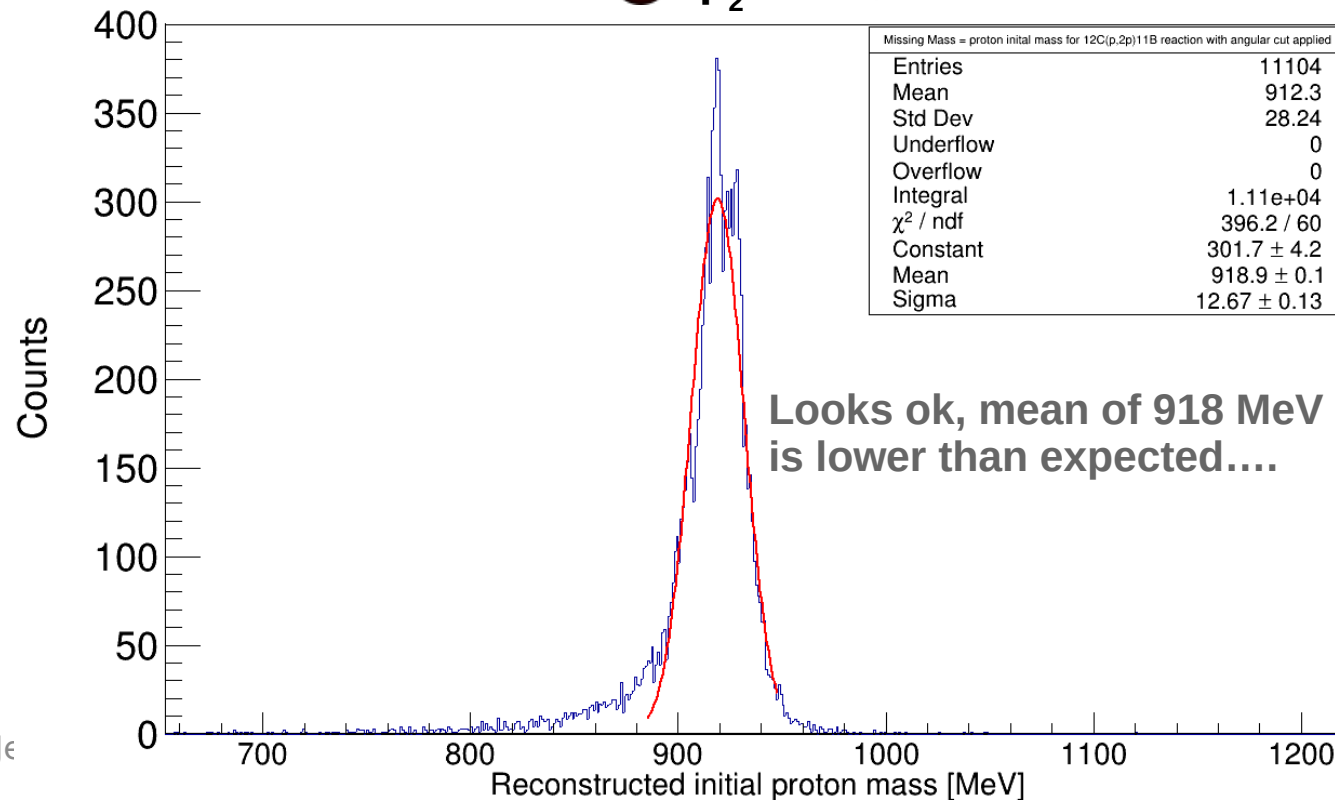


After Scattering:



$$p_i \approx p_{\text{missing}} = p_1 + p_2 - p_{\text{tg}} \text{ (no ISI/FSI)}$$

$$M_i = \sqrt{(p_1 + p_2 - p_{\text{tg}})^2}$$



## Definition of Missing Energy \*:

$$E_{\text{miss}} = m_p - e_{\text{miss}} = E_{\text{tgkin}} - E_{p1\text{kin}} - E_{p2\text{kin}} \quad (\text{in } 12\text{C cms})$$

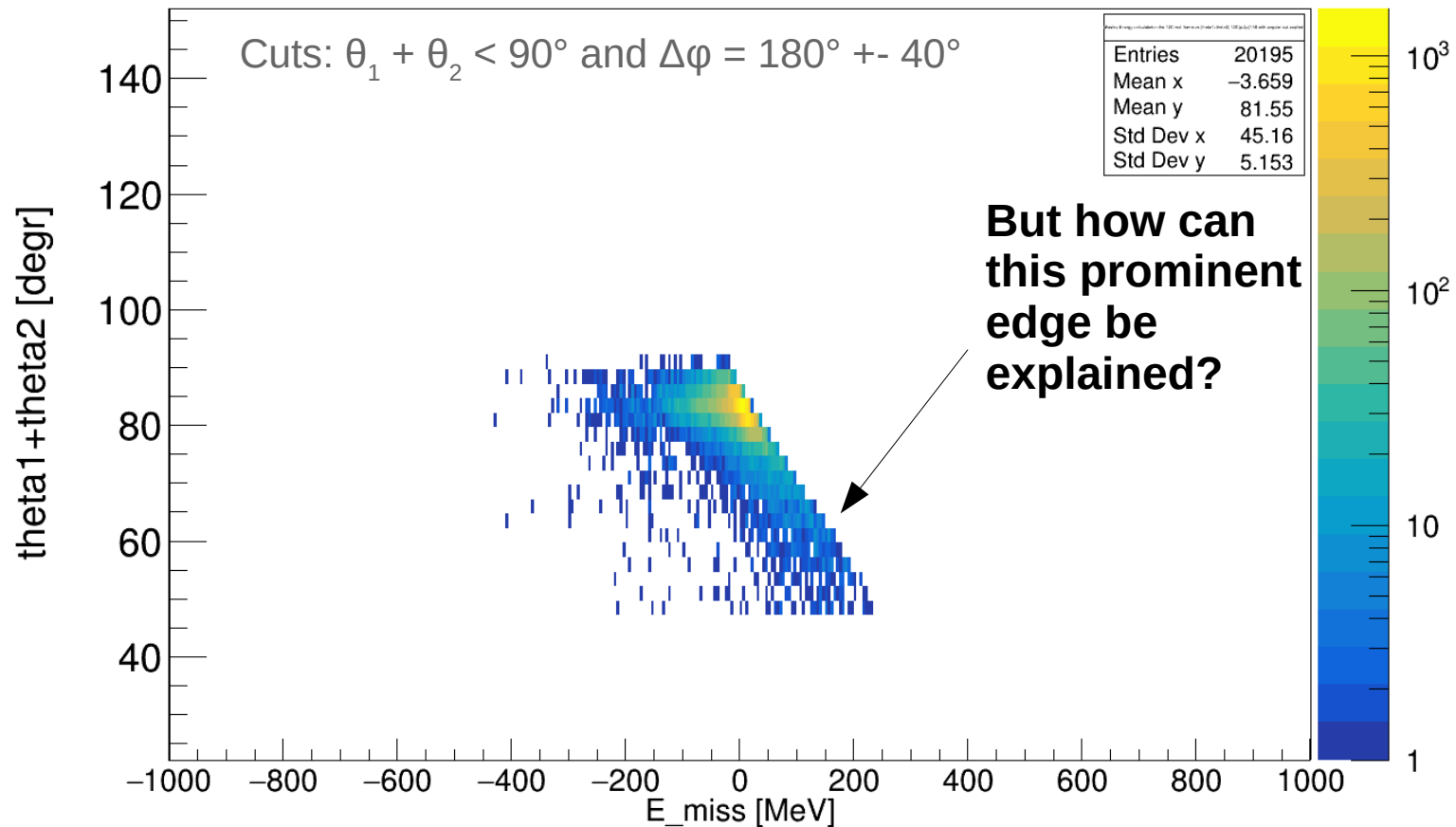
(where  $e_{\text{miss}}$  is the energy component of  $\mathbf{p}_{\text{missing}}$ )

$$\mathbf{p}_i \approx \mathbf{p}_{\text{missing}} = \mathbf{p}_1 + \mathbf{p}_2 - \mathbf{p}_{\text{tg}} \quad (\text{no ISI/FSI})$$

$$E_{\text{miss}} = E_{\text{initial}} - E_{\text{final}}$$



$$E_{\text{miss}} = E_{\text{Sep}} + \bar{E}_{\text{Exc}}$$



Explicit calculation of the Missing Energy (in the 12C frame):

$$E_{\text{miss}} = E_{\text{tgkin}} - E_{\text{p1kin}} - E_{\text{p2kin}}$$

$$E_{\text{miss}} = 400 - \underbrace{\left( \gamma * (E_{\text{kin1}} + 938) - \gamma * \beta * \sqrt{(E_{\text{kin1}} + 938)^2 - 938^2} * \cos(\theta_1) - 938 \right)}_{E'_{\text{p1}}} - \underbrace{\left( \gamma * (E_{\text{kin2}} + 938) - \gamma * \beta * \sqrt{(E_{\text{kin2}} + 938)^2 - 938^2} * \cos(\theta_2) - 938 \right)}_{E'_{\text{p2}}}$$

$\underbrace{E_{\text{tgkin}} \quad E_{\text{kin1}}}_{E_{\text{p1kin}}} \quad \underbrace{E_{\text{kin2}}}_{E_{\text{p2kin}}}$

$E_{\text{pot}_{\text{p1}}} \quad E_{\text{pot}_{\text{p2}}}$

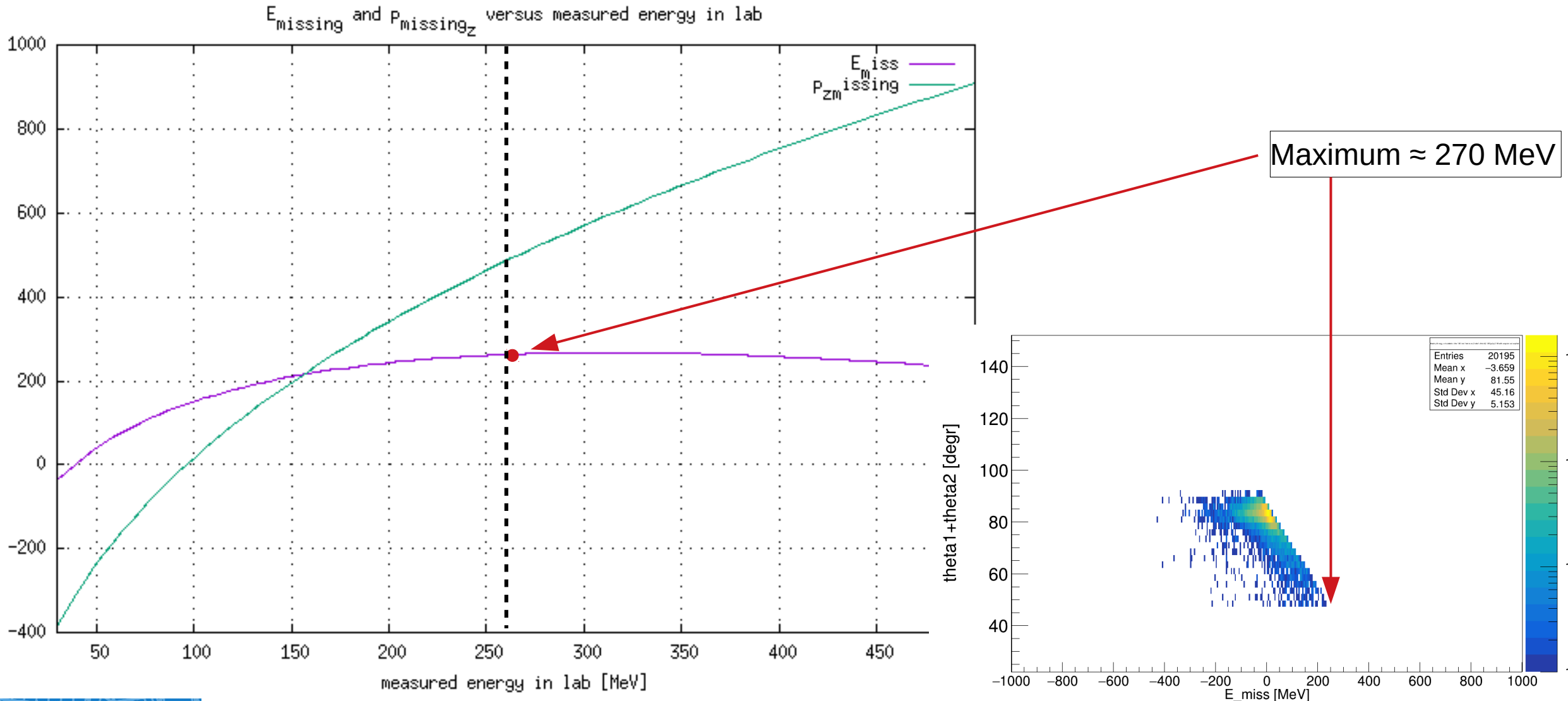




# E\_missing and p\_z\_missing for different opening angles

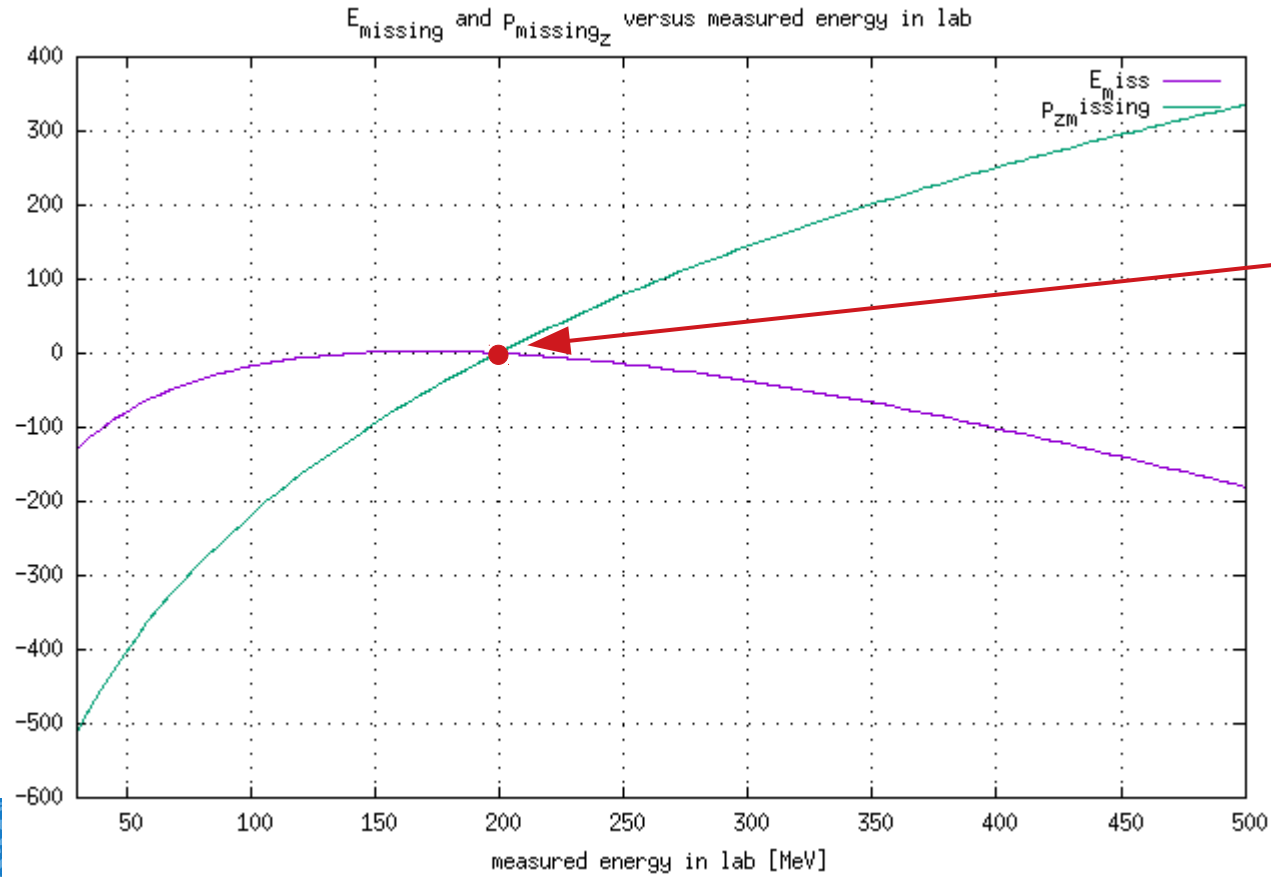


For simplicity let's say  $\theta_1 = \theta_2$  and  $E_{\text{kin1}} = E_{\text{kin2}}$ . That means for  $\theta_{\text{sum}} = 44^\circ \rightarrow \theta_1 = \theta_2 = 22^\circ$

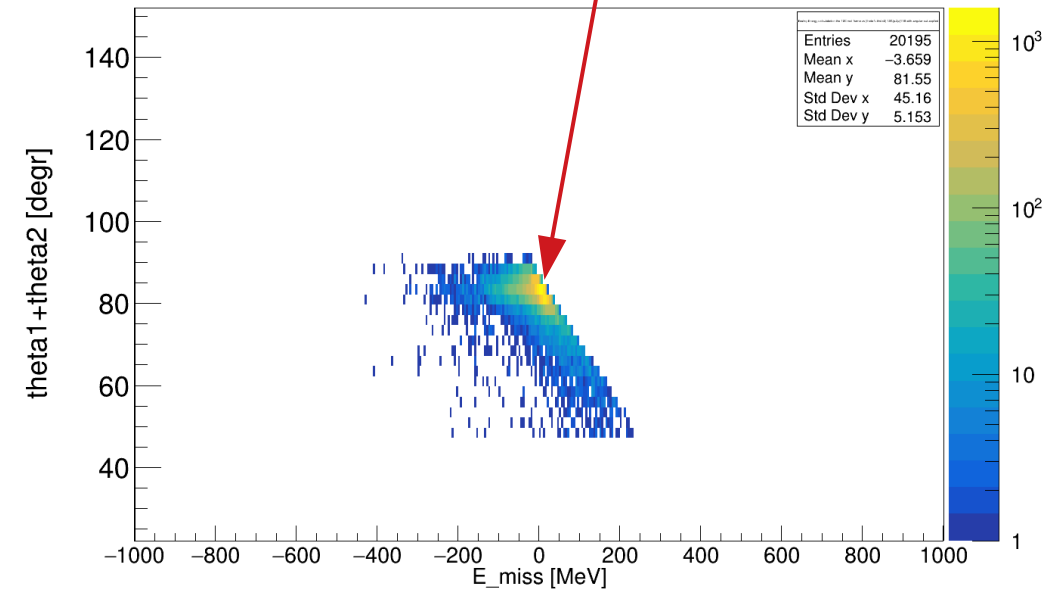




# E\_missing and p\_z\_missing for $\theta_1 = \theta_2 = 42^\circ$



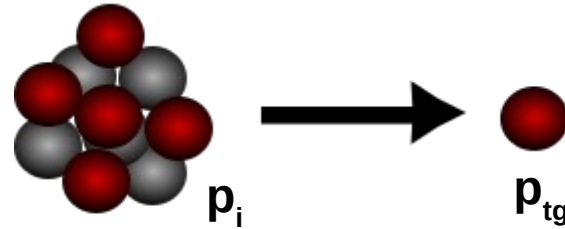
Quasi-Free Scattering reaction  
 $\approx 84^\circ$



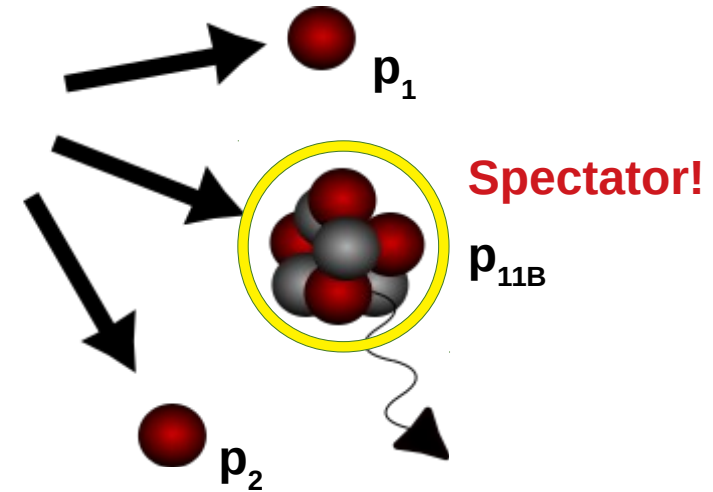


# Momentum components of $p_{11B}$

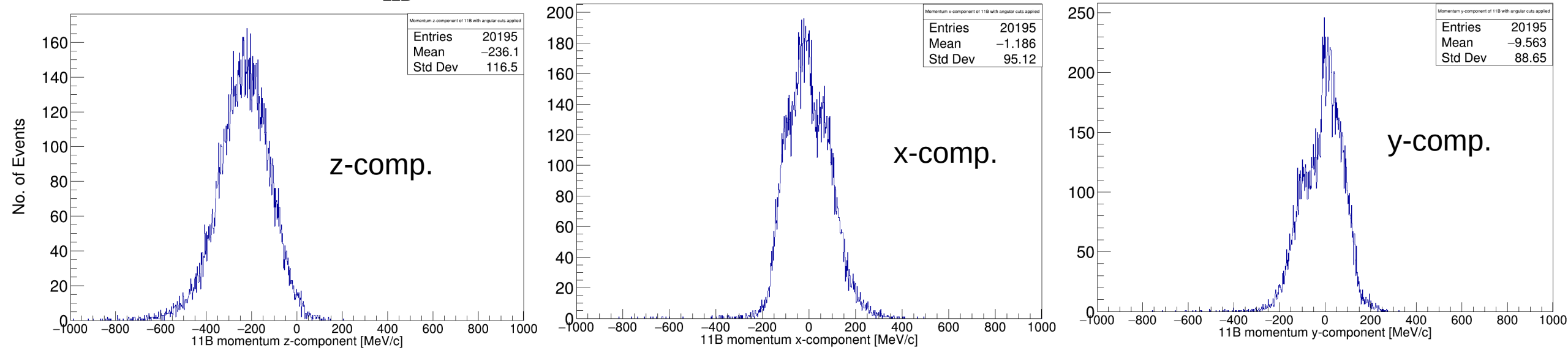
Before Scattering:



After Scattering:

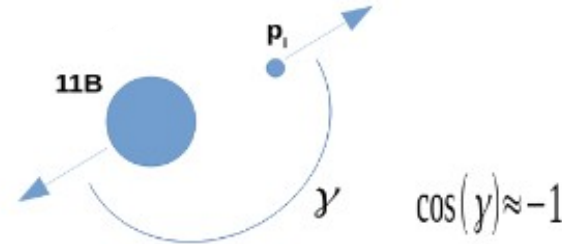


$p_{11B}$  Momentum-Components (with angular cuts applied)

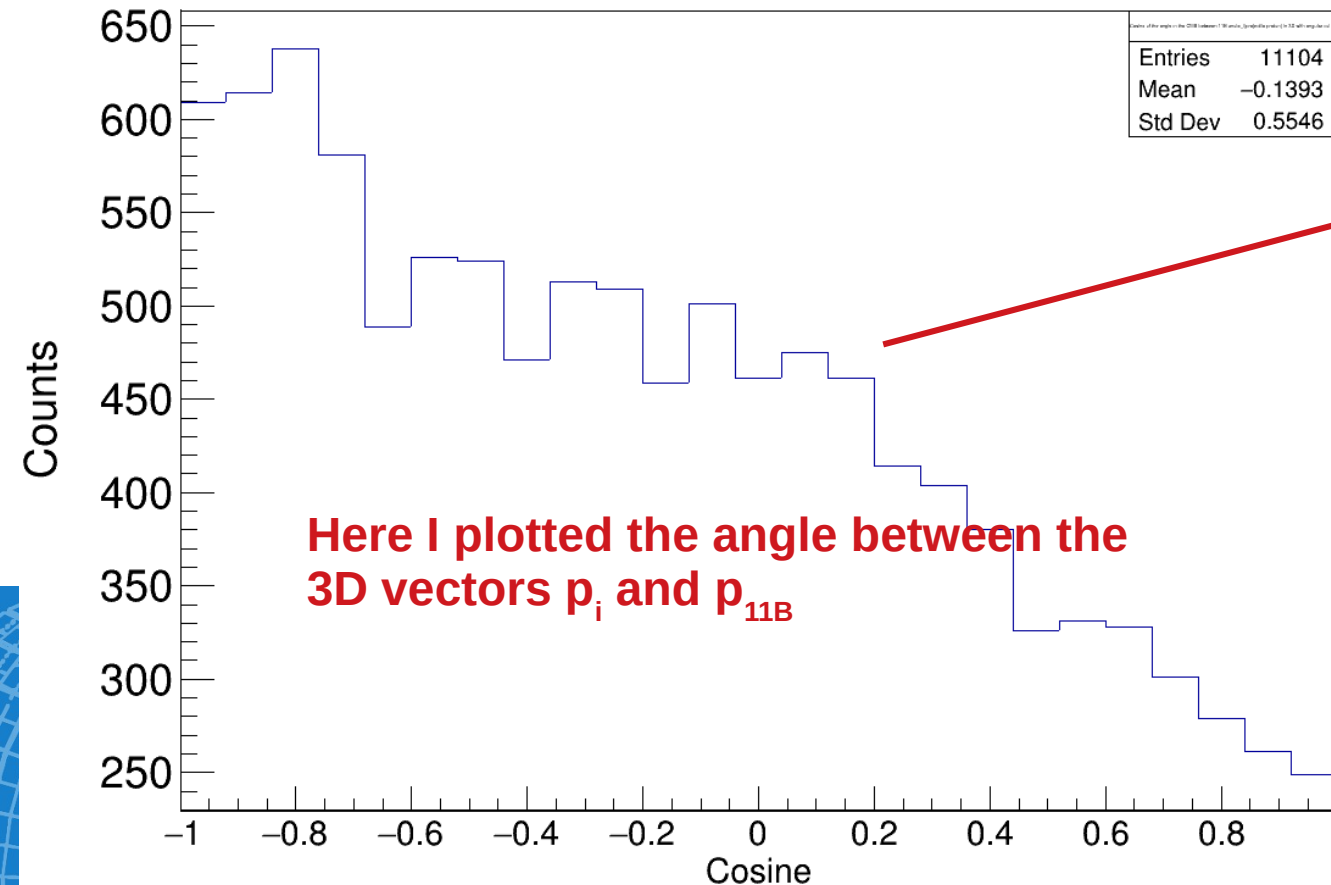


- $\mathbf{p}_i$  determined by angle and energy deposition of p1 and p2
- $\mathbf{p}_{11B}$  determined by ToF and tracking detectors (MWPCs)

(p11B\_y was calculated by y-position in MW1 and MW2)



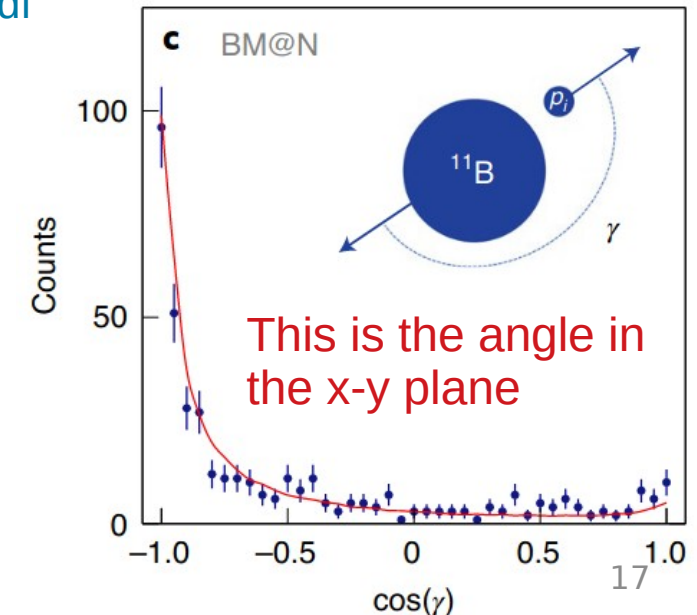
$$\mathbf{p}_{12C} = \mathbf{p}_i + \mathbf{p}_{11B}$$



Not satisfactory....

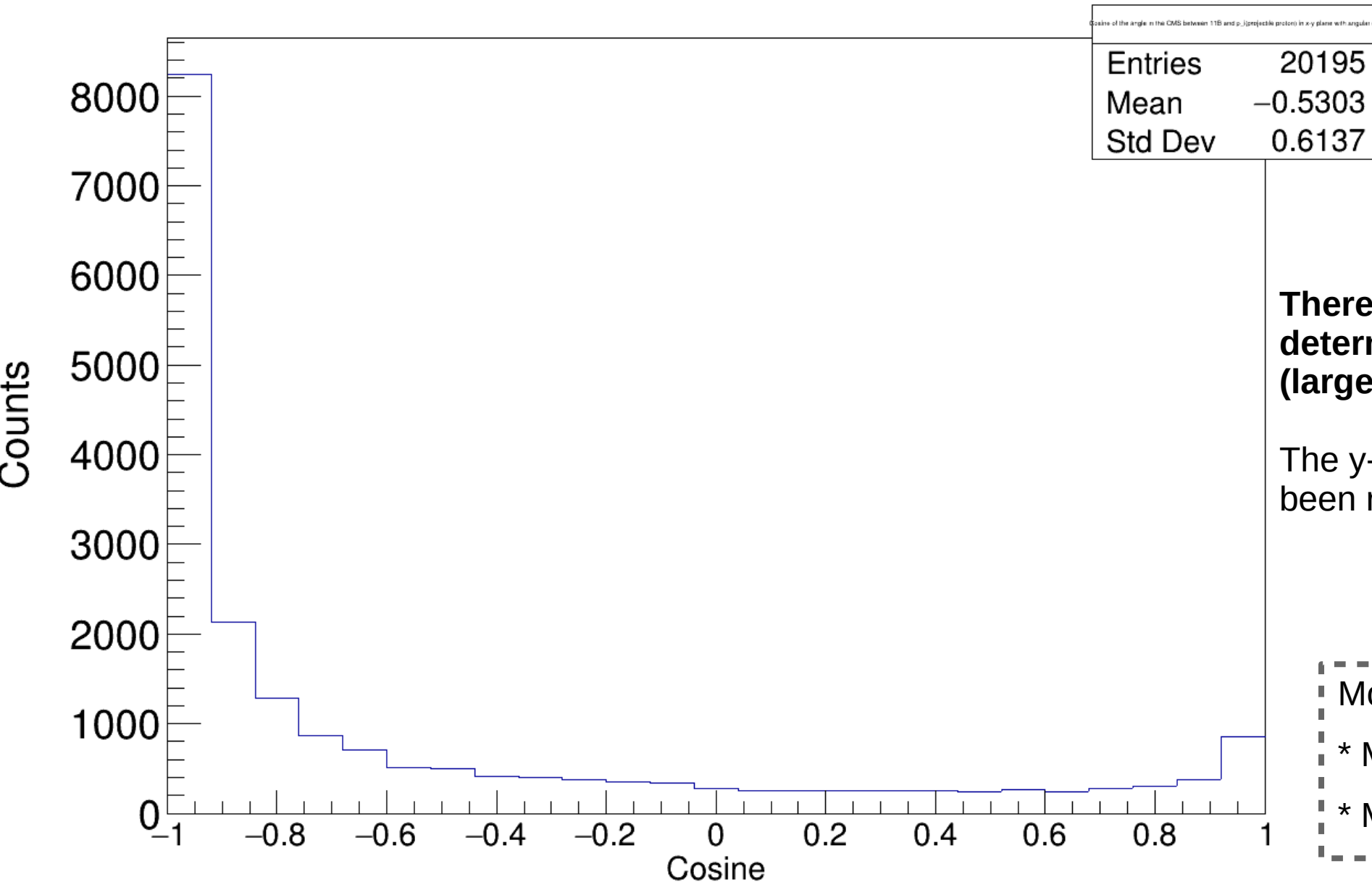
See:

<https://www.nature.com/articles/s41567-021-01193-4.pdf>





# Angular Distribution in x-y plane



**Therefore the y position was determined using MWPC3 (larger lever arm)**

The y-position of MWPC3 has been reversed (+y → -y and -y → +y)

Moreover:

\* MW0X inverted

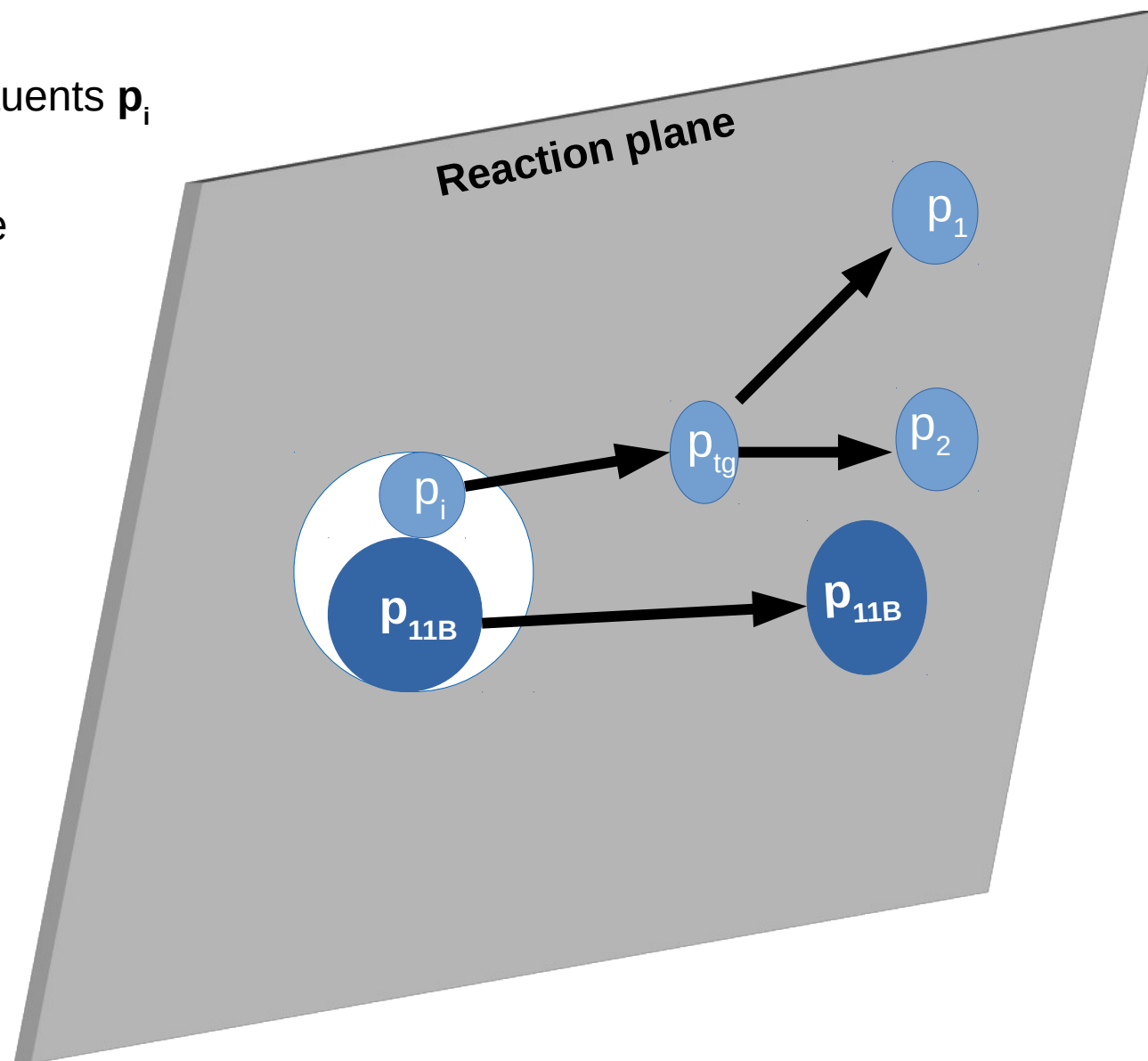
\* MW1Y and MW2Y swapped



# Spatial Correlation of the Reaction Products

Assuming no inner momenta of the  $^{12}\text{C}$  constituents  $\mathbf{p}_i$  and  $\mathbf{p}_{^{11}\text{B}}$ :

→ scattering would take place in reaction plane



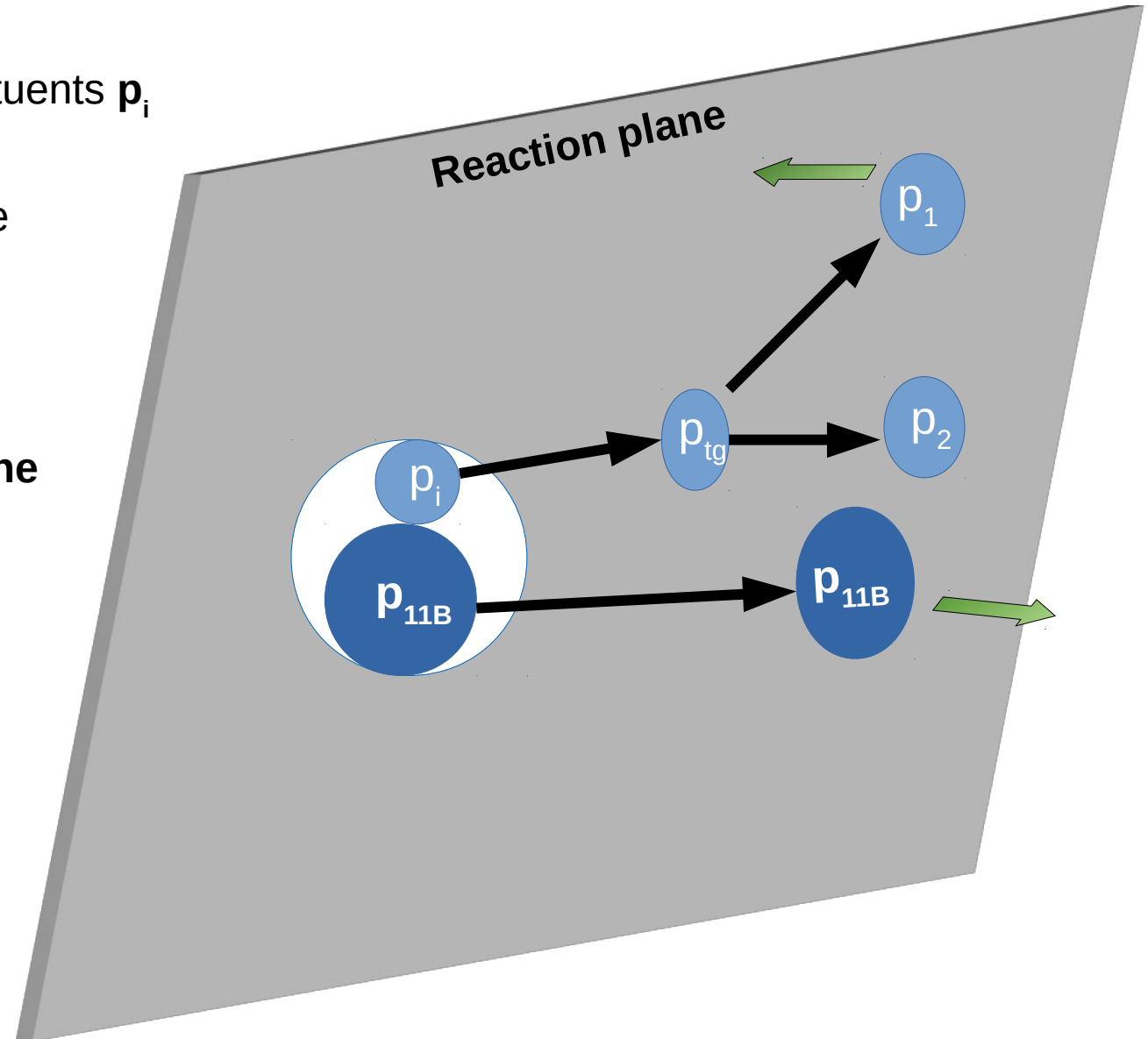
Assuming no inner momenta of the  $^{12}\text{C}$  constituents  $\mathbf{p}_i$  and  $\mathbf{p}_{^{11}\text{B}}$ :

→ scattering would take place in reaction plane

**BUT:**

$$|\vec{p}_i| \approx |\vec{p}_{^{11}\text{B}}| \neq 0$$

→ there are components perpendicular to the reaction plane!

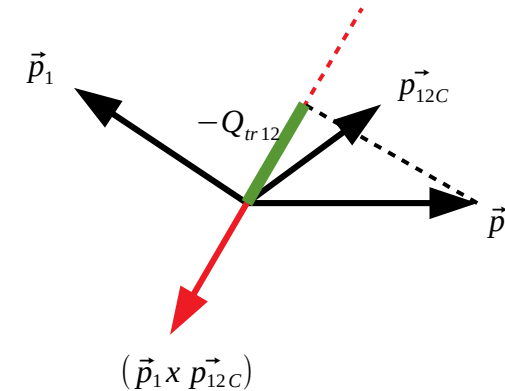
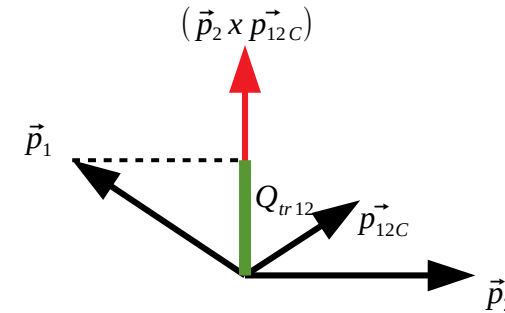


As measure of the overall perpendicular fraction to the reaction plane\*:

$$Q_{tr12} = \frac{\vec{p}_1 * (\vec{p}_2 \times \vec{p}_{12C})}{|\vec{p}_1| |\vec{p}_2 \times \vec{p}_{12C}|}$$

or

$$Q_{tr21} = \frac{\vec{p}_2 * (\vec{p}_1 \times \vec{p}_{12C})}{|\vec{p}_2| |\vec{p}_1 \times \vec{p}_{12C}|} = -Q_{tr12}$$

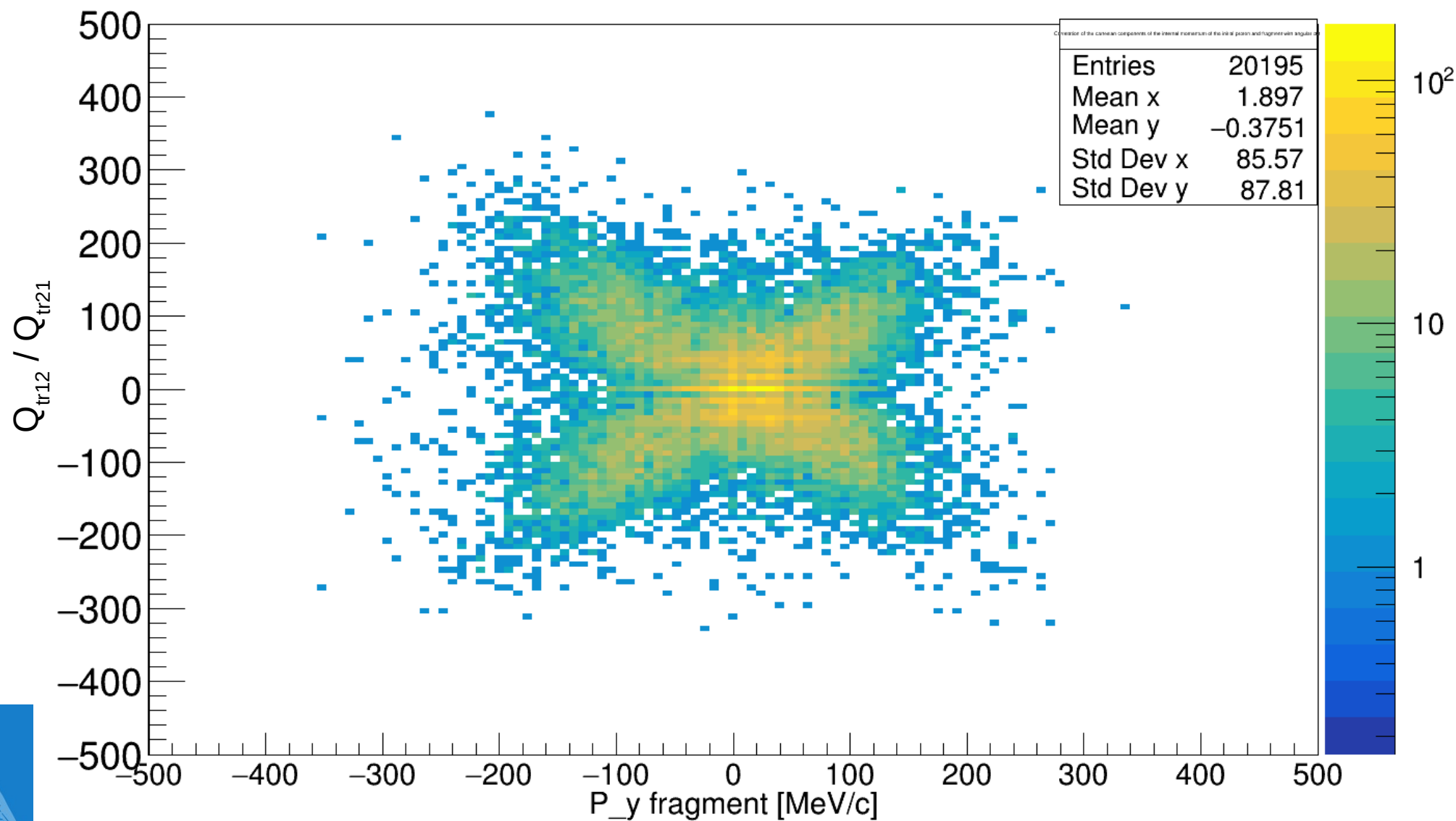


Due to momentum conservation:

$$Q_{tr12} = -Q_{trFragment}$$



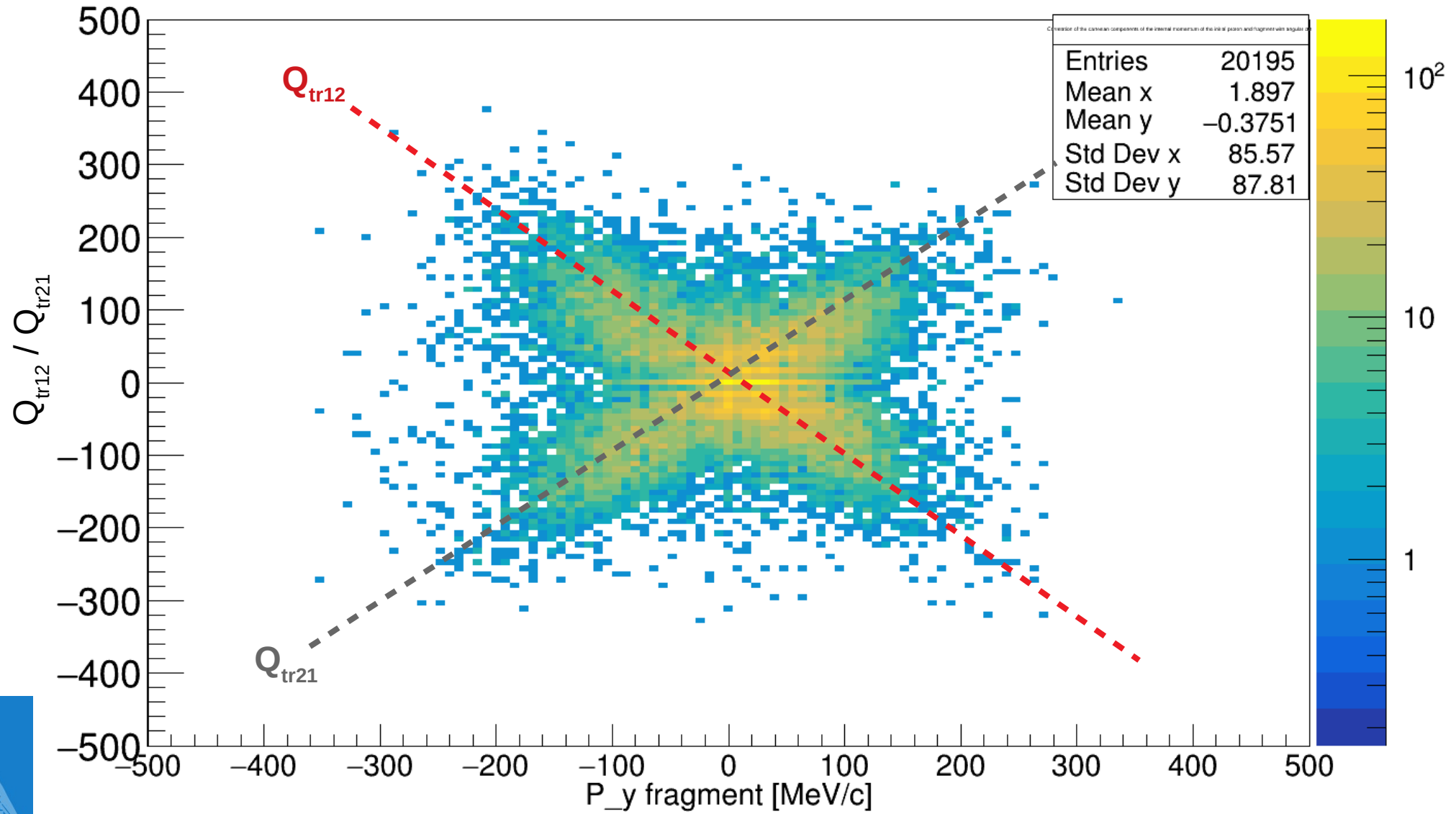
# $Q_{tr12}$ vs. $|\vec{p}_{y11B}|$





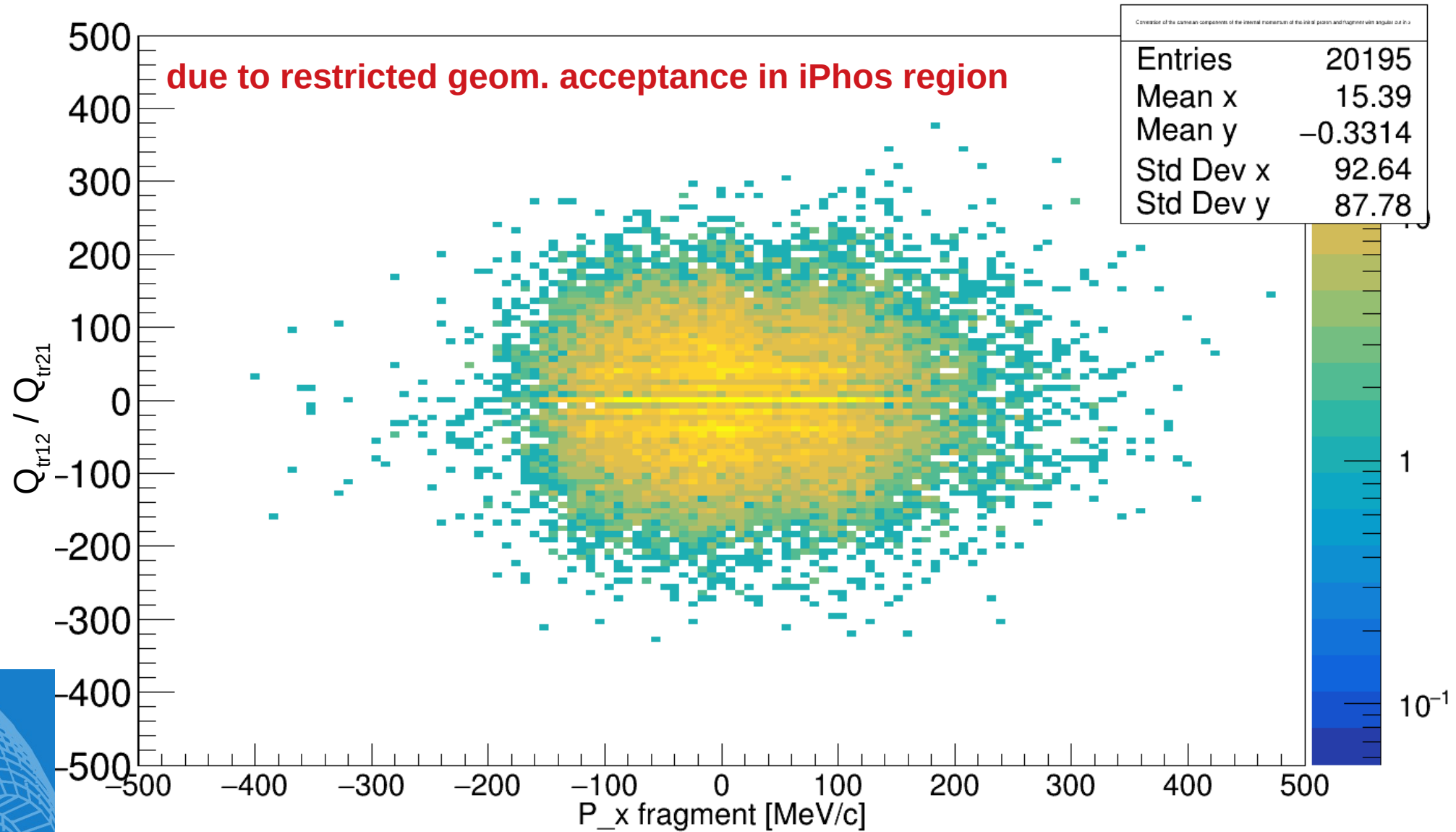


# $Q_{tr12}$ vs. $|\vec{p}_{y11B}|$



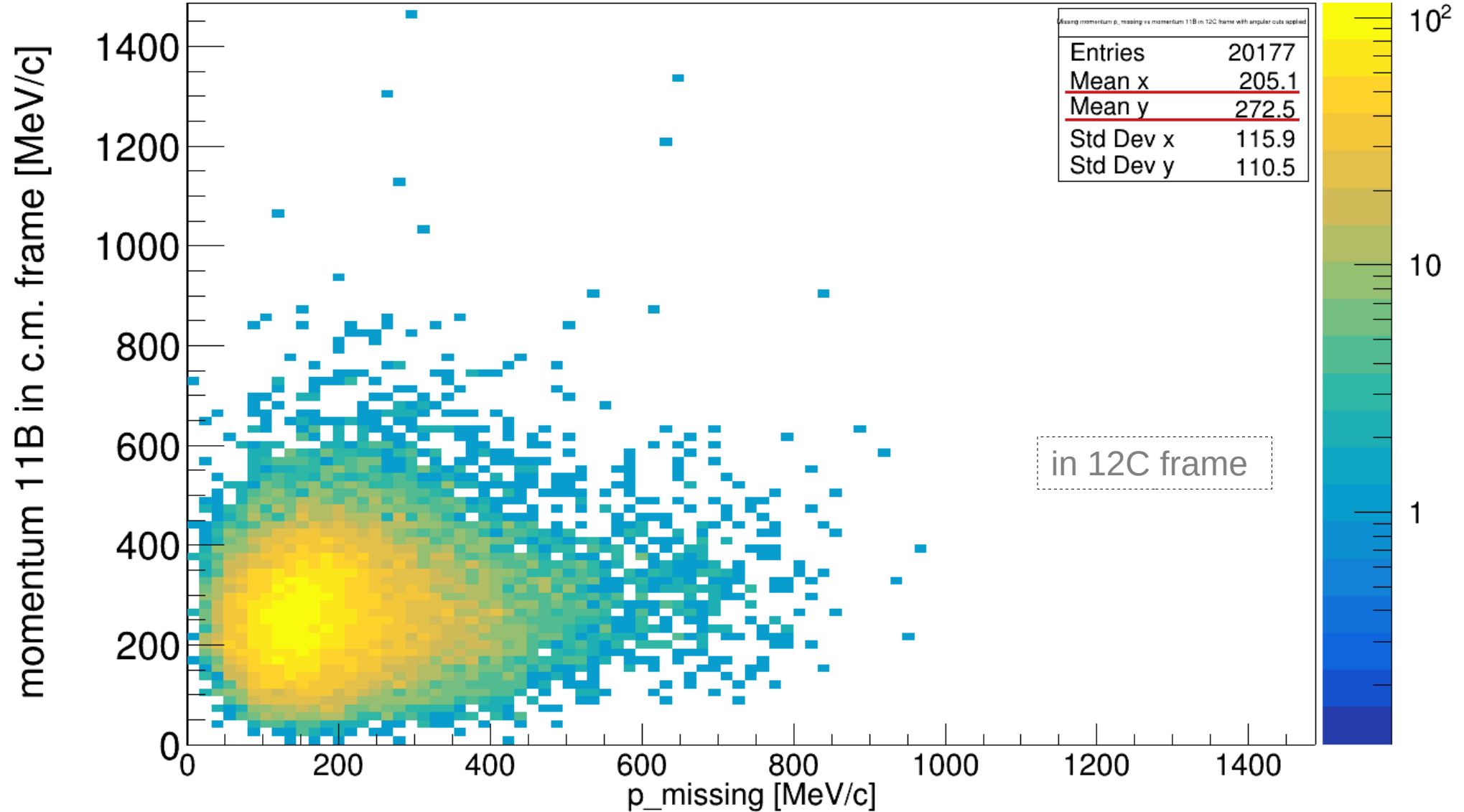


$Q_{\text{tr}12}$  vs.  $|\vec{p}_{\text{x}11\text{B}}|$

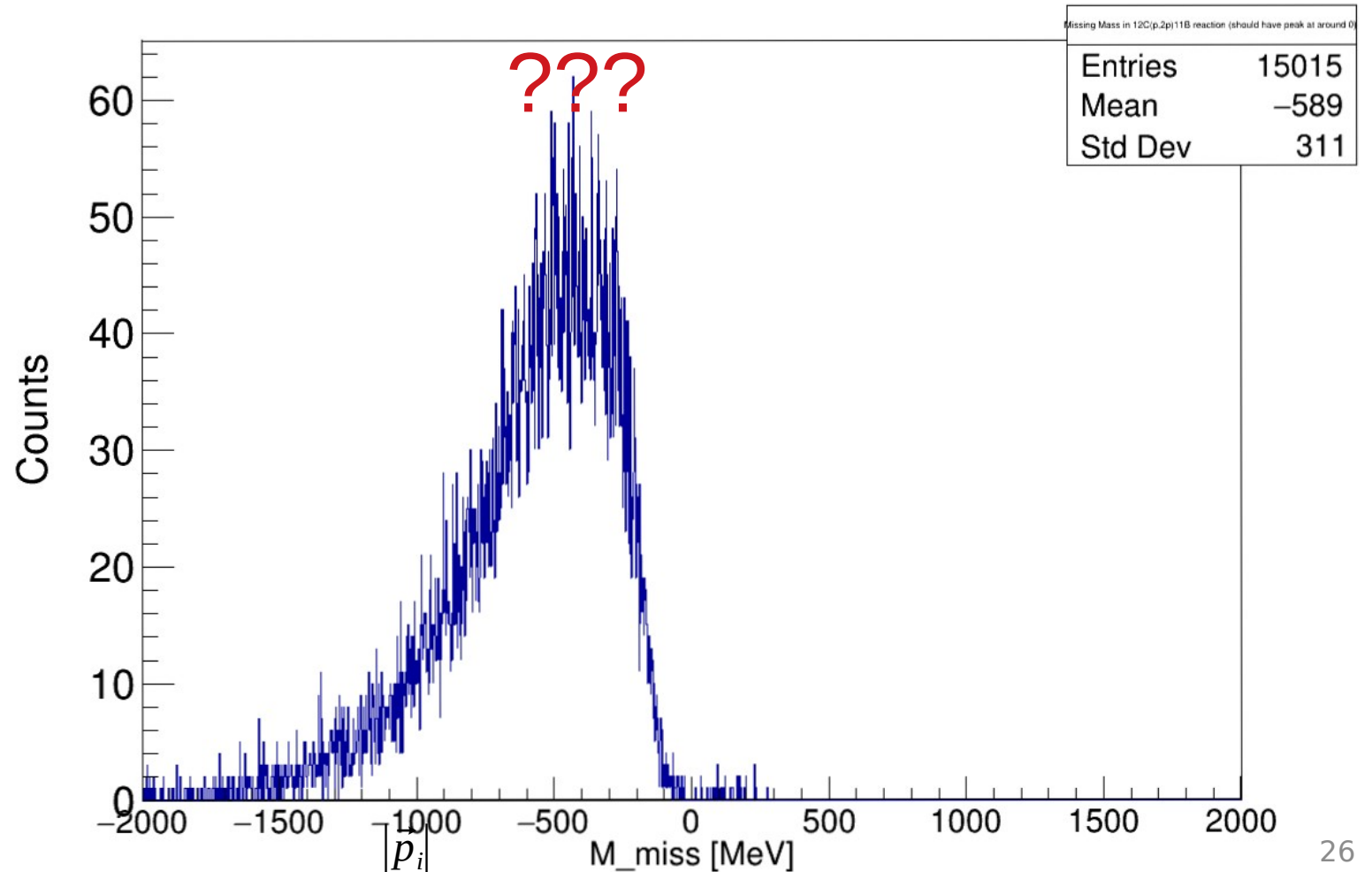
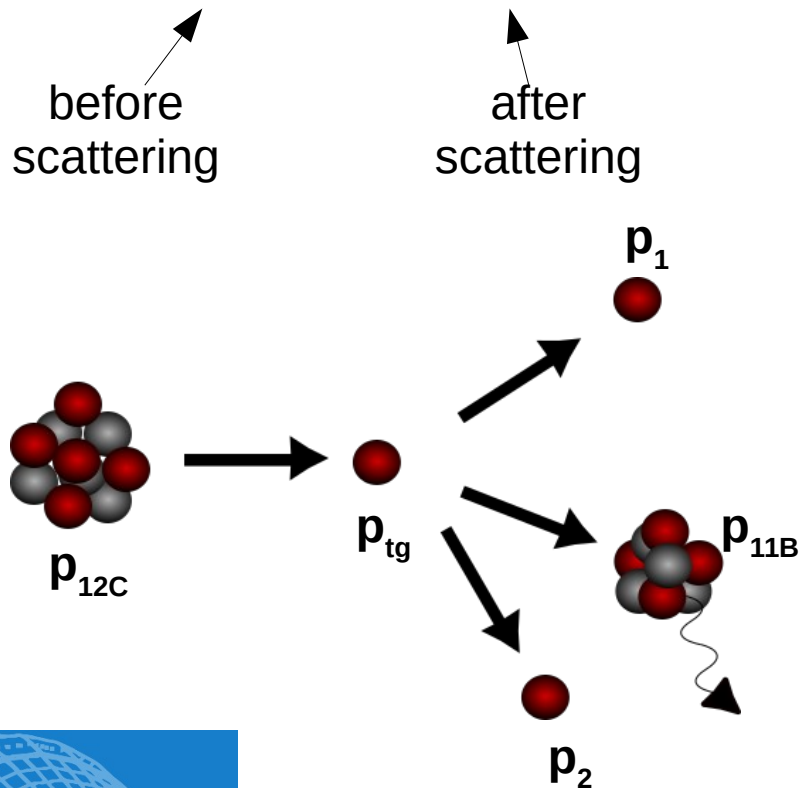




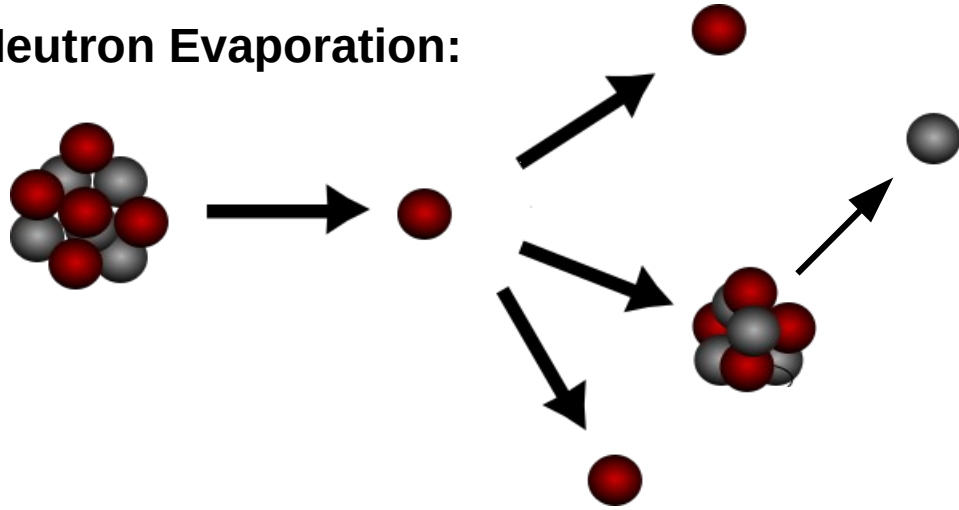
# Momentum $p_i$ vs $p_{11B}$ in 12C



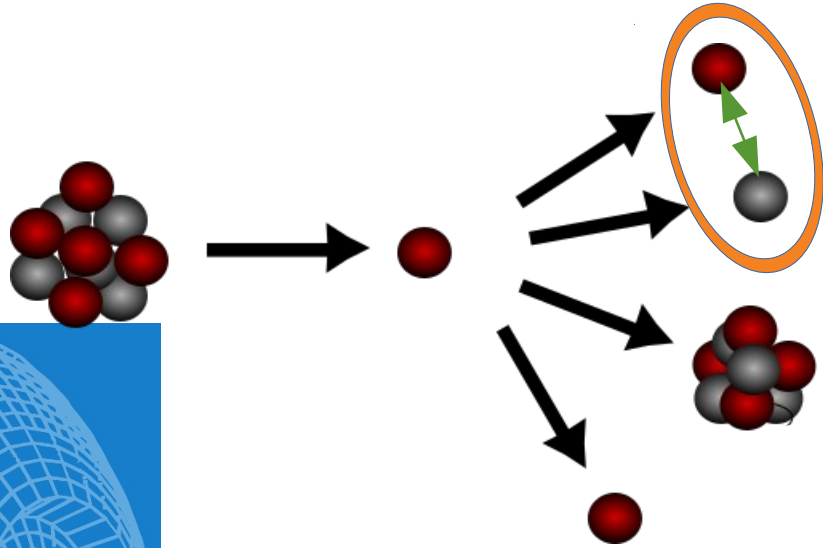
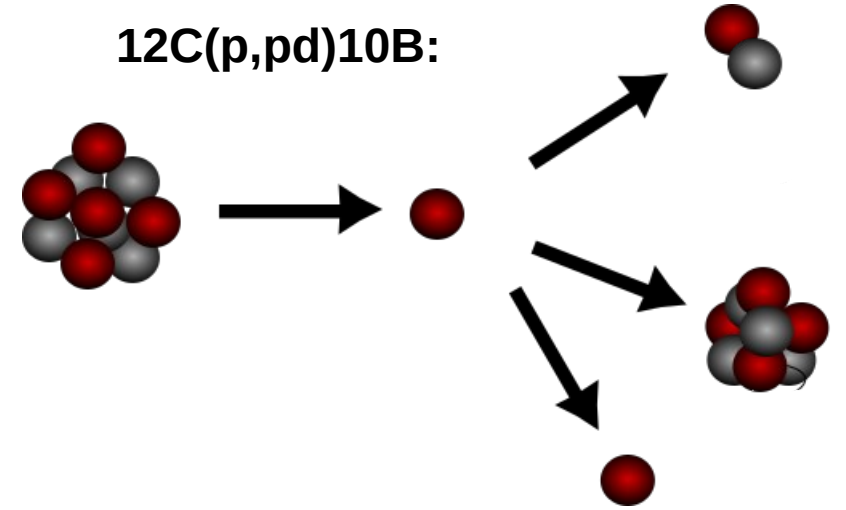
$$M_{\text{miss}} = \sqrt{(\underbrace{p_{12C} + p_{tg}}_{\text{before scattering}} - \underbrace{p_1 + p_2 + p_{11B}}_{\text{after scattering}})^2} \quad (\text{should be } \approx 0)$$



Neutron Evaporation:



12C(p,pd)10B:

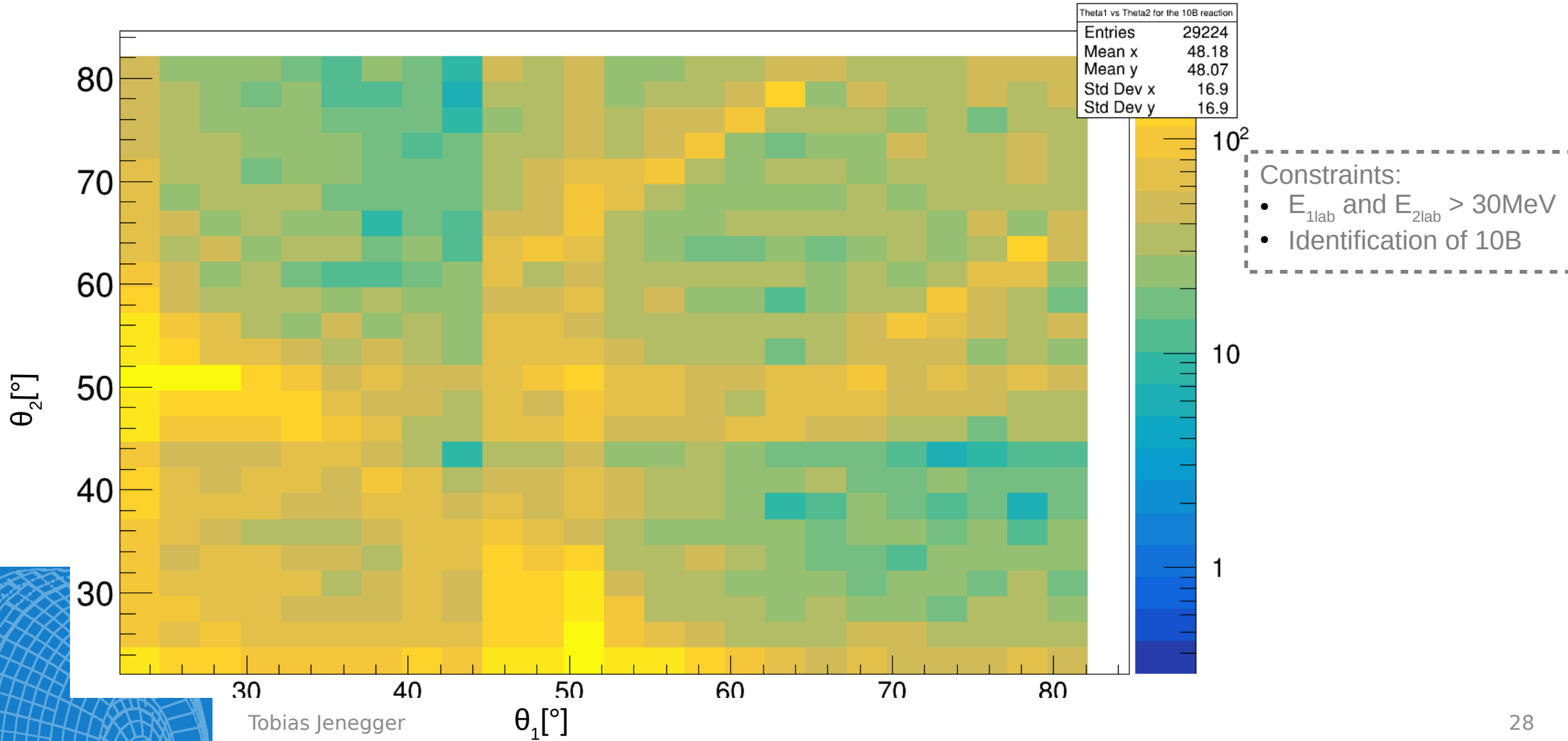


**Short-Range-Correlated (SRC) Pair:**

- possible explanation for the EMC – effect
- nucleon pairs with high relative and low c.m. momentum (compared to Fermi momentum  $k_F$ )

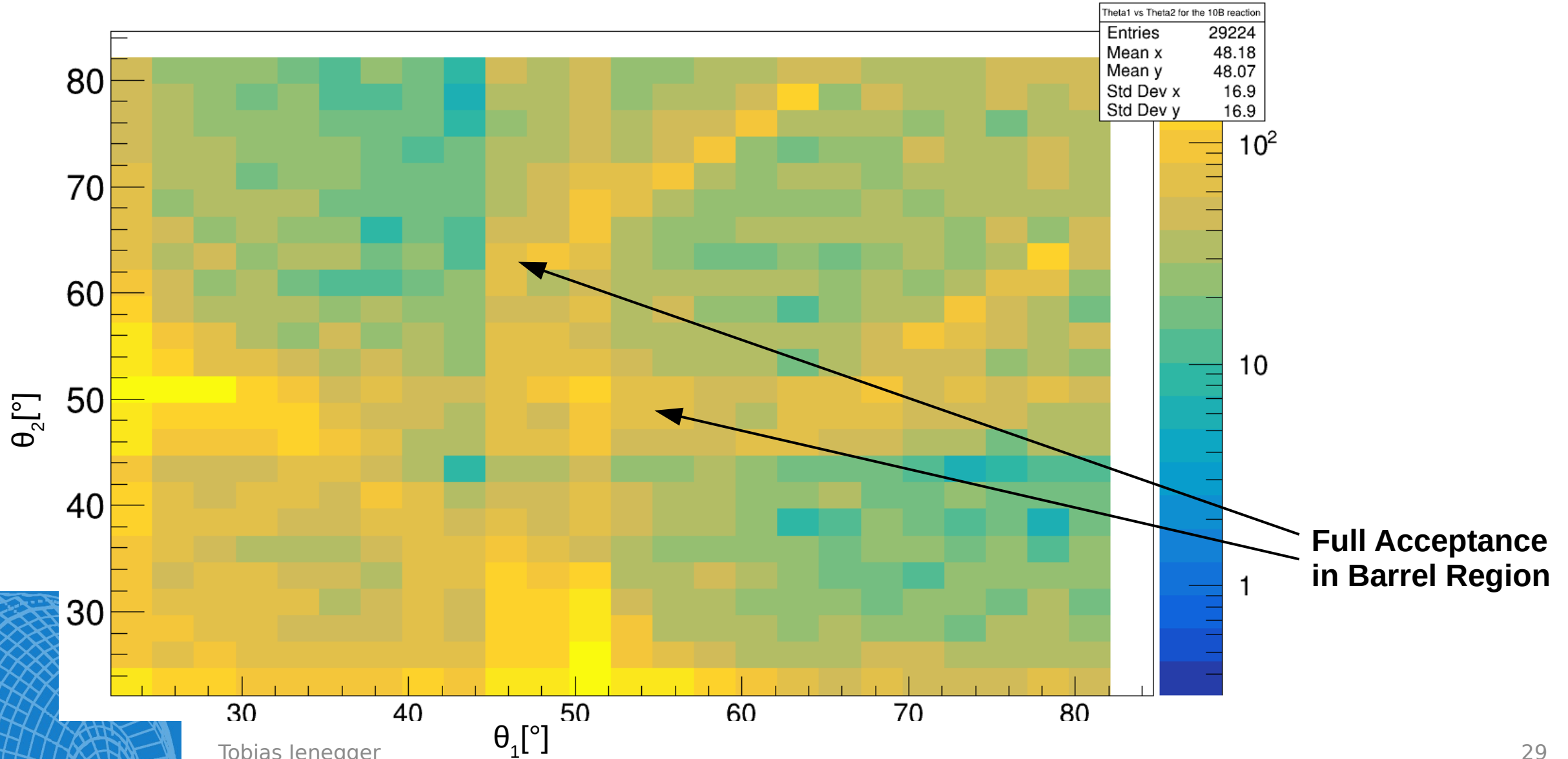
# First (Polar) Angular Plots ...

$\theta_1$ (proton 1) vs.  $\theta_2$  (proton2) without any angular restrictions:



# First (Polar) Angular Plots ...

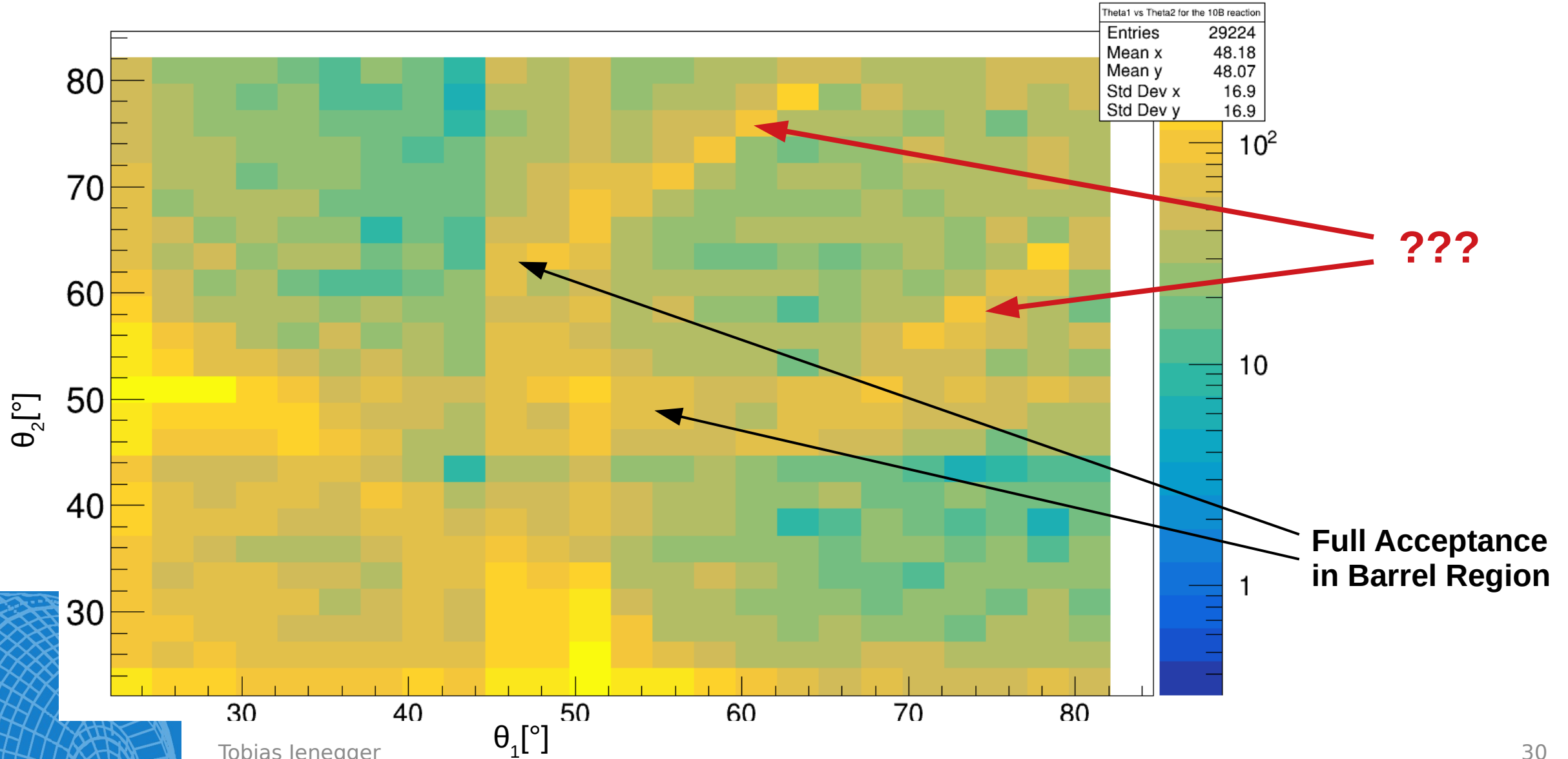
$\theta_1$ (proton 1) vs  $\theta_2$ (proton2) without any angular restrictions:





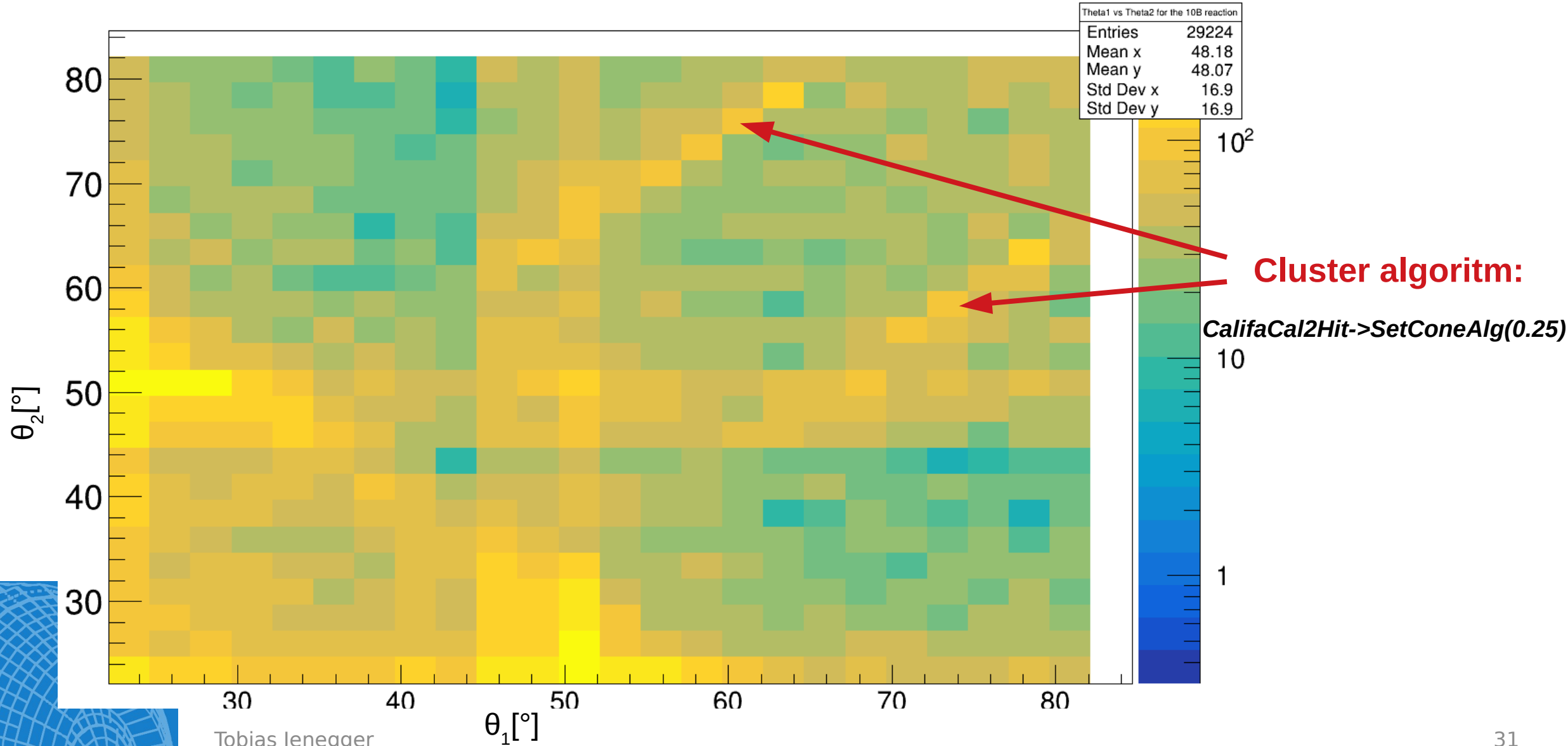
# First (Polar) Angular Plots ...

$\theta_1$ (proton 1) vs  $\theta_2$ (proton2) without any angular restrictions:



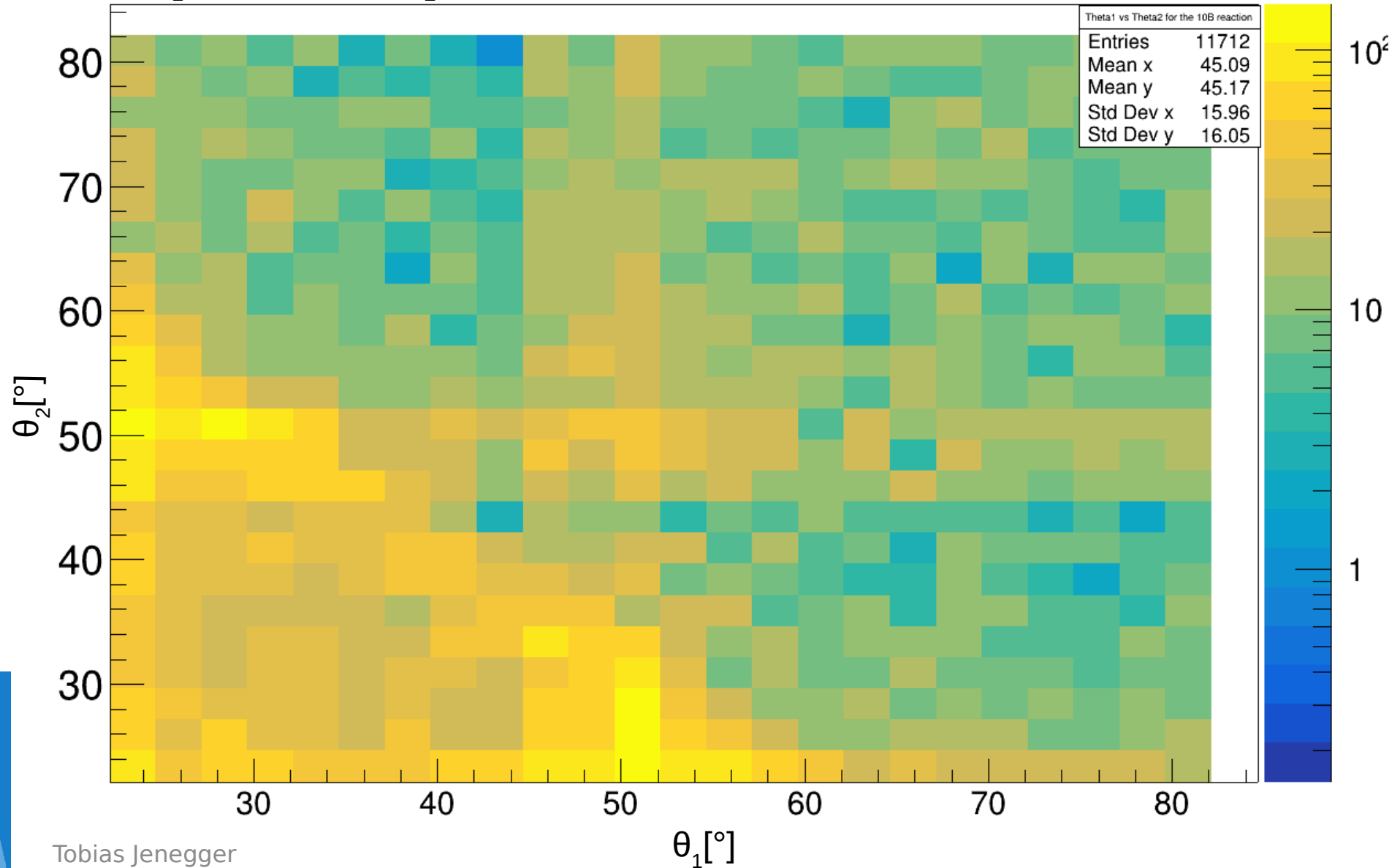
# First (Polar) Angular Plots ...

$\theta_1$ (proton 1) vs  $\theta_2$ (proton2) without any angular restrictions:



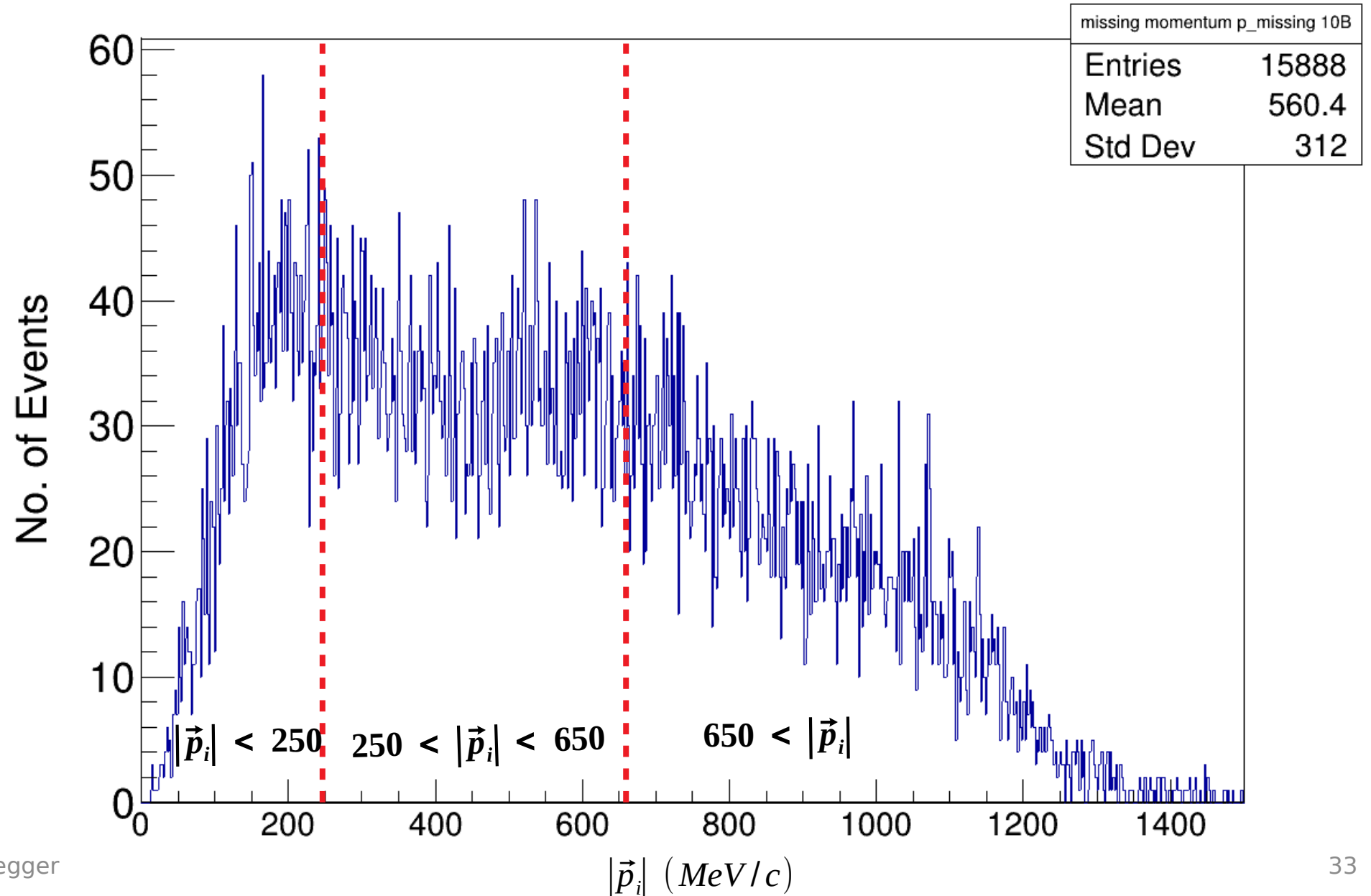
# First (Polar) Angular Plots ...

$\theta_1$ (proton 1) vs  $\theta_2$ (proton2) **with** angular cut:  $\Delta\phi > 100^\circ$



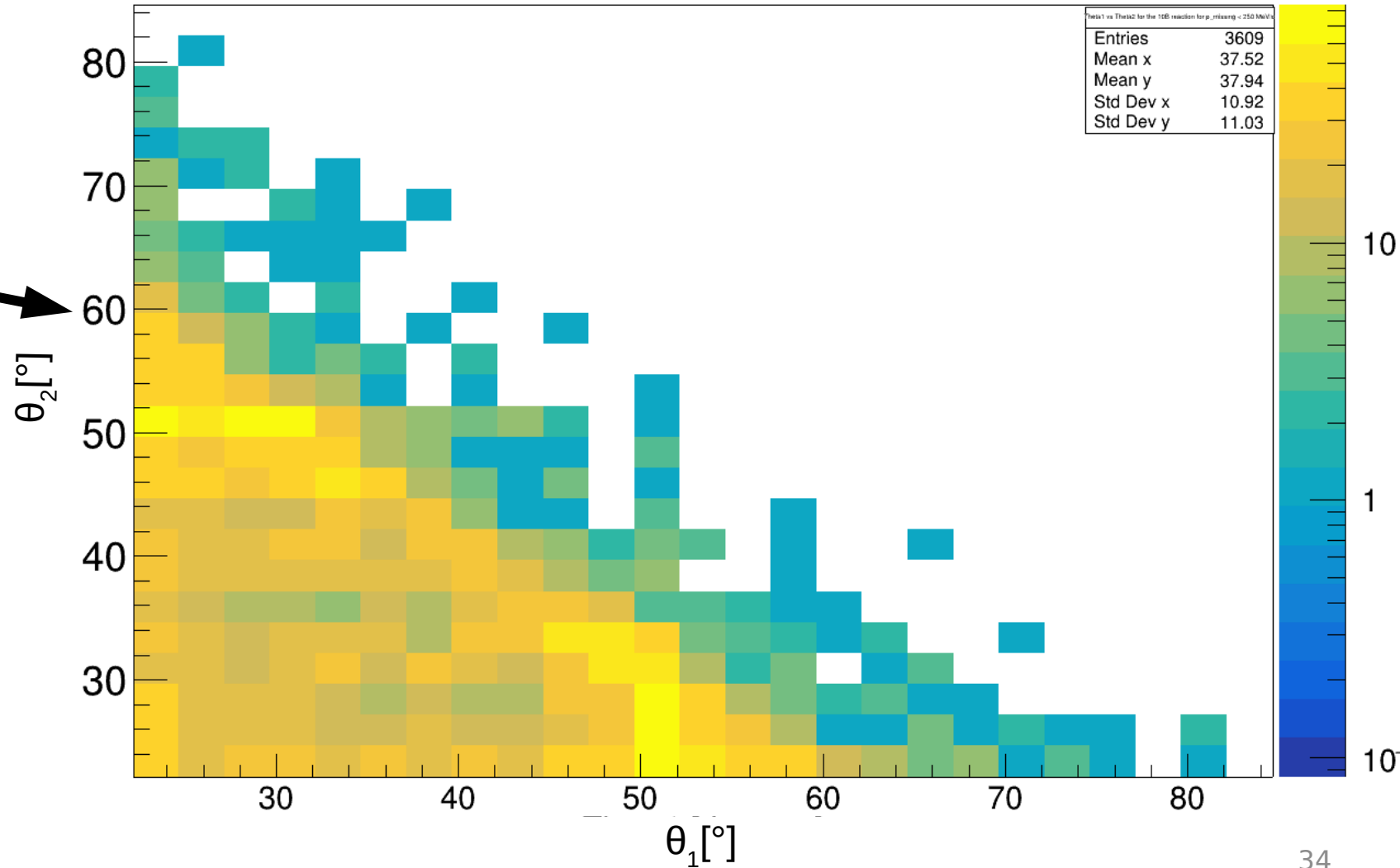
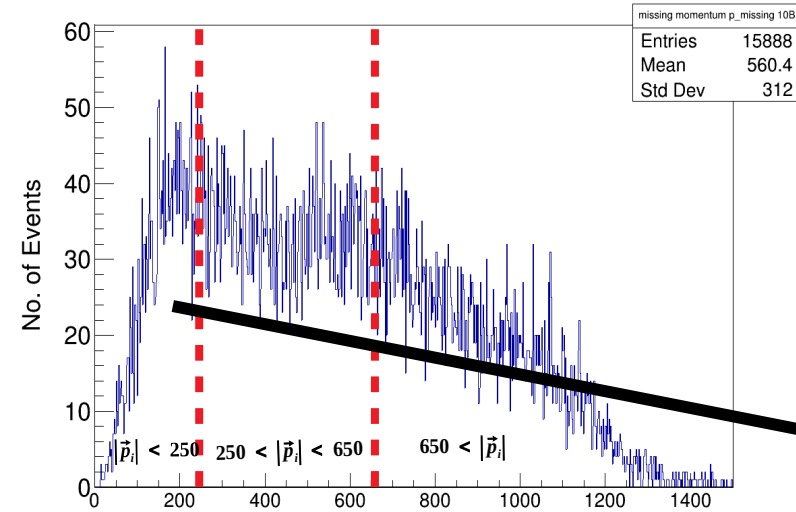
# Reconstruction of inner momentum $\vec{p}_i$

$$\vec{p}_i = \vec{p}_1 + \vec{p}_2 - \vec{p}_{tg}$$



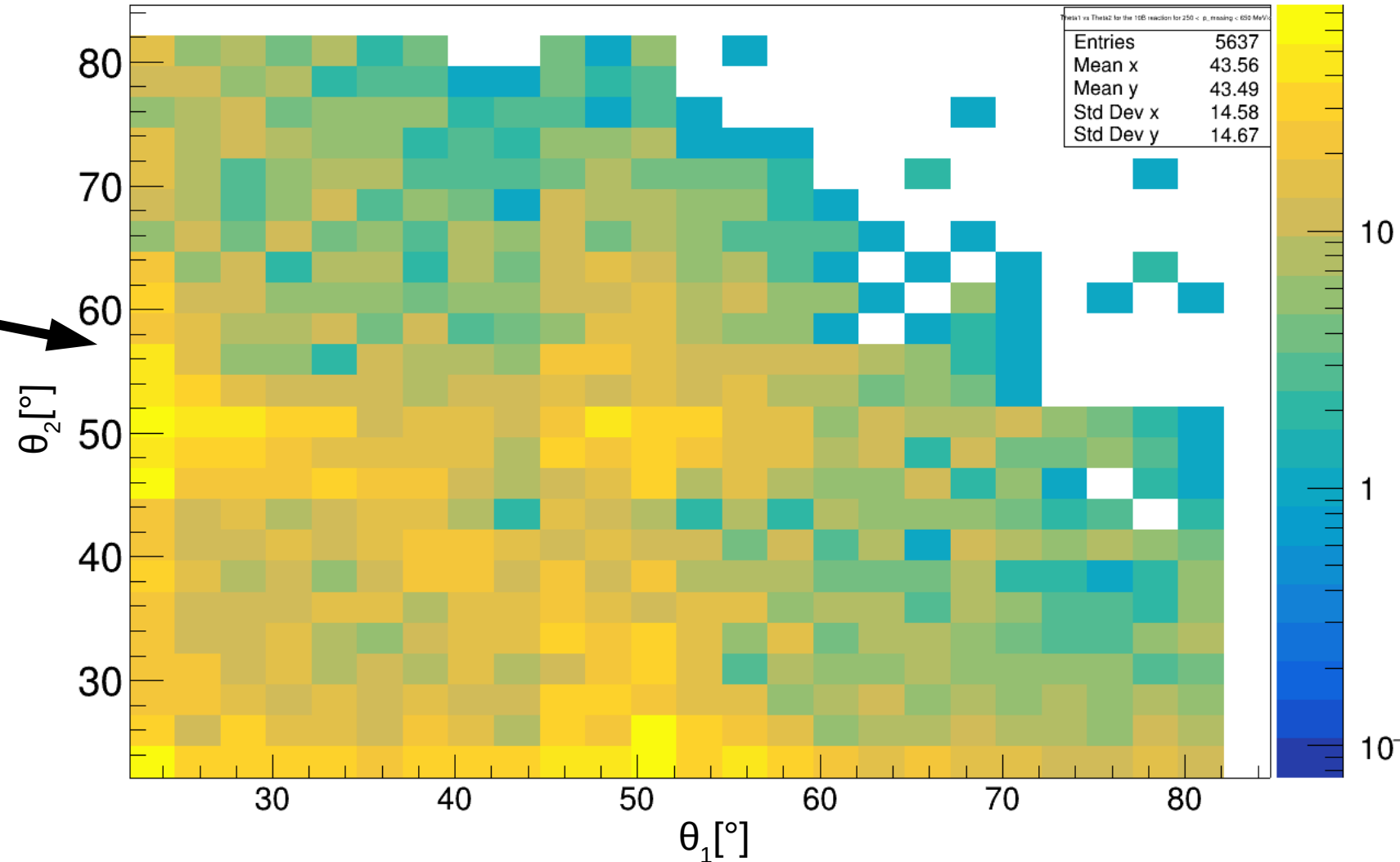
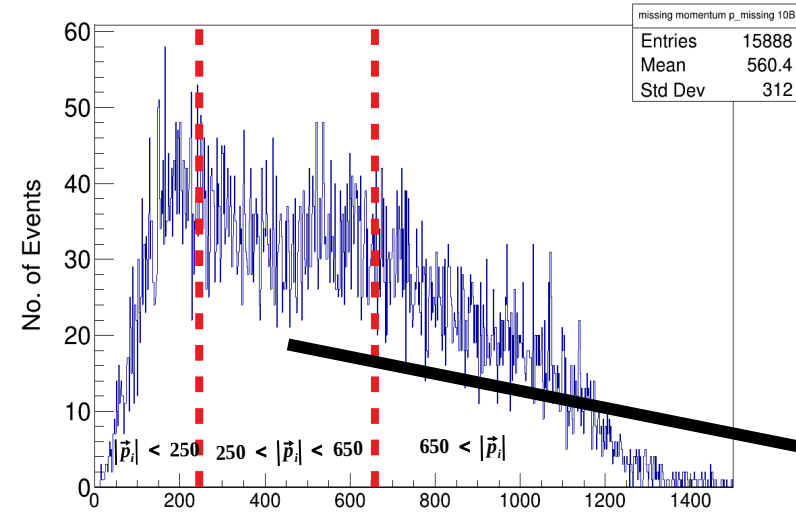


# Angular Distribution for $|\vec{p}_i| < 250$



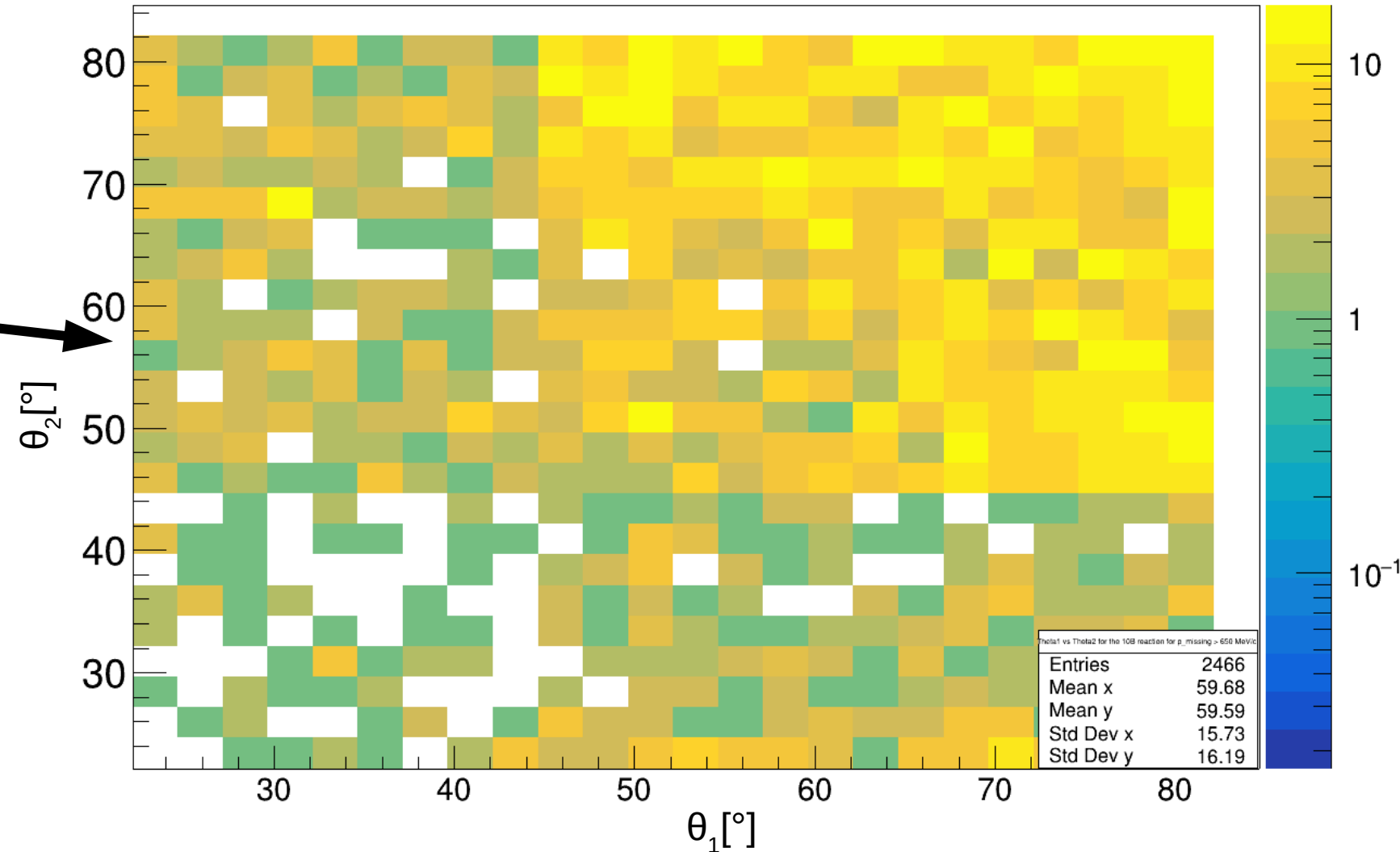
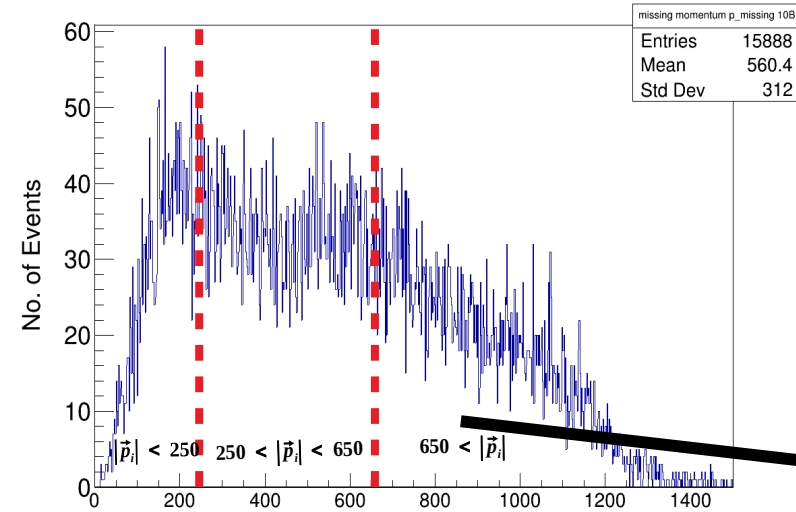


# Angular Distribution for $250 \text{ MeV}/c < |\vec{p}_i| < 650 \text{ MeV}/c$





# Angular Distribution for $|\vec{p}_i| > 650 \text{ MeV}/c$





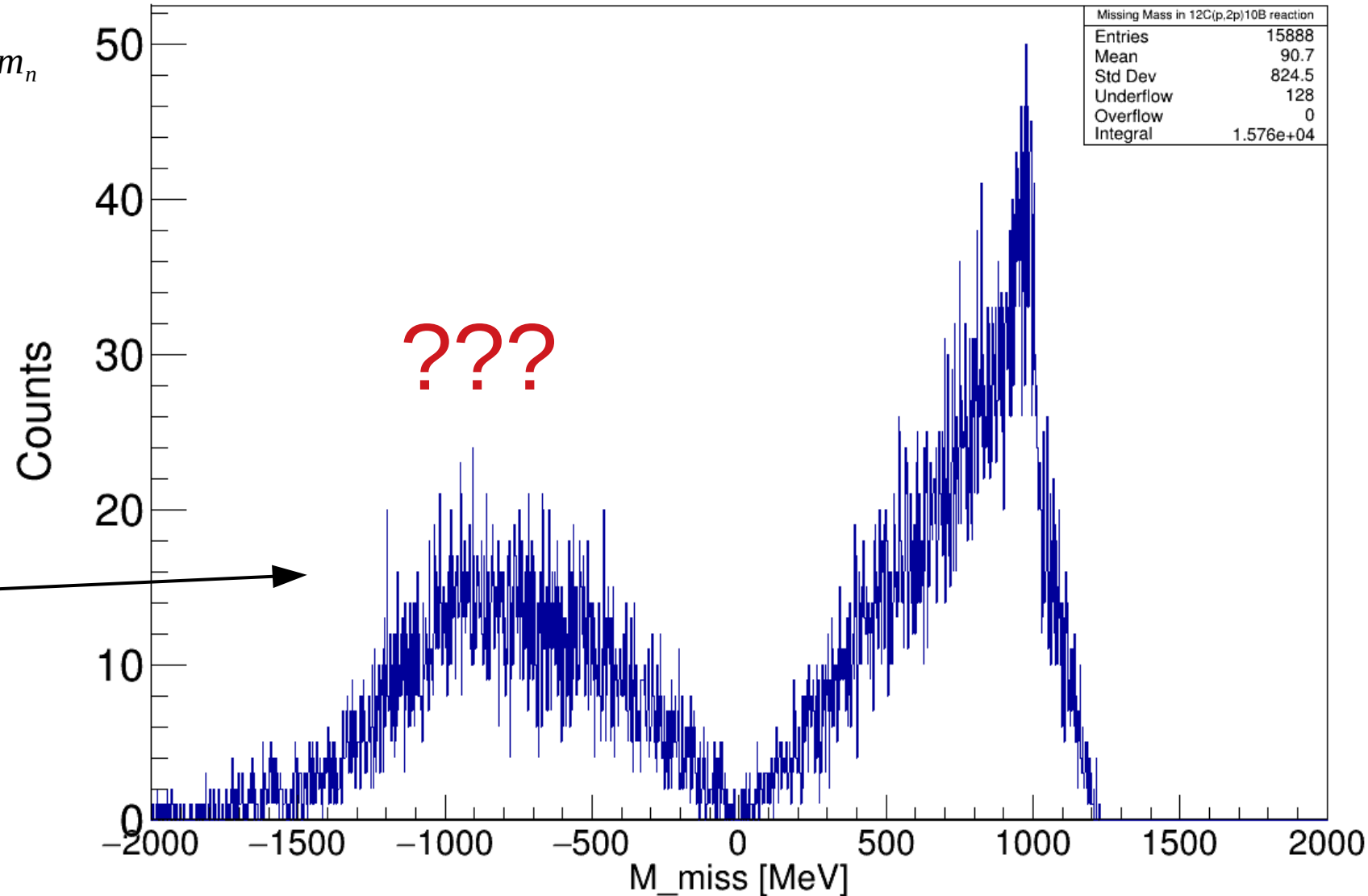
$$M_{\text{missing}}^2 = (\underbrace{p_{12C} + p_{tg}}_{\text{before reaction}} - \underbrace{p_1 + p_2 + p_{10B}}_{\text{after reaction}})^2 \approx m_n^2$$

before  
reaction

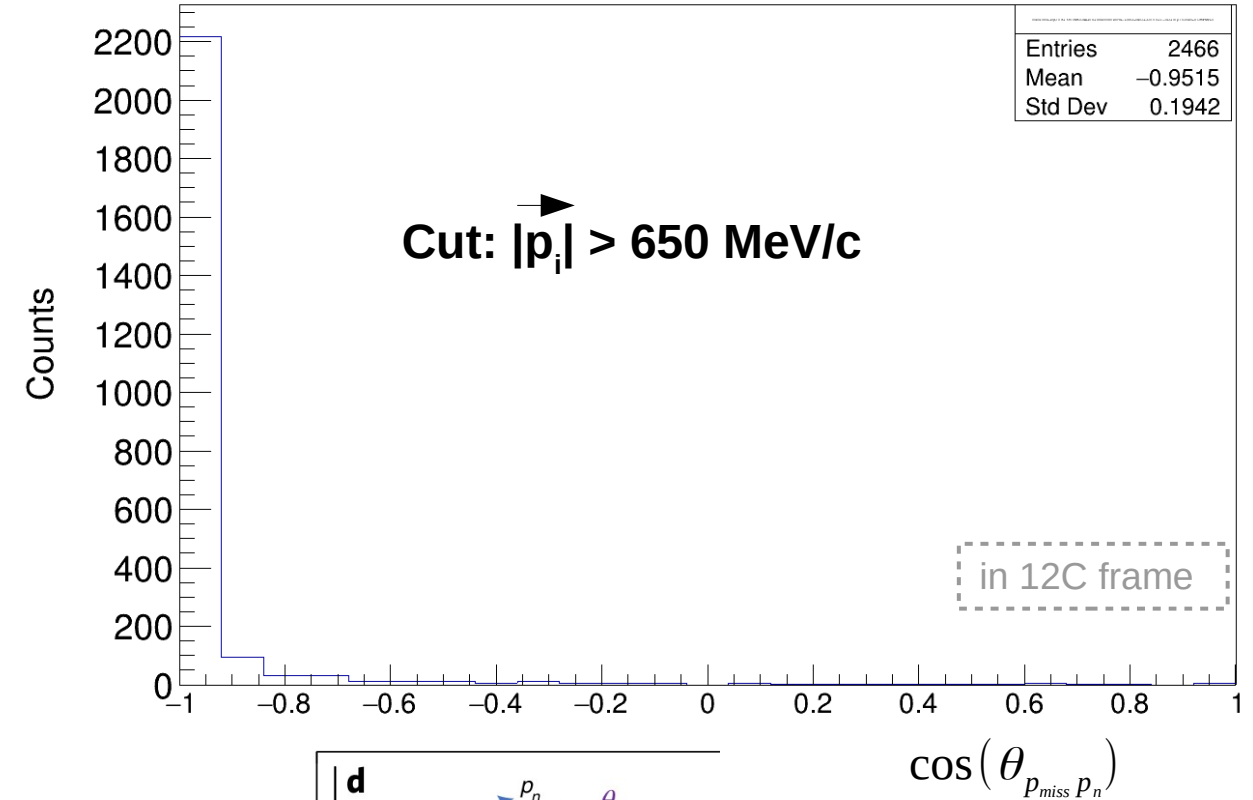
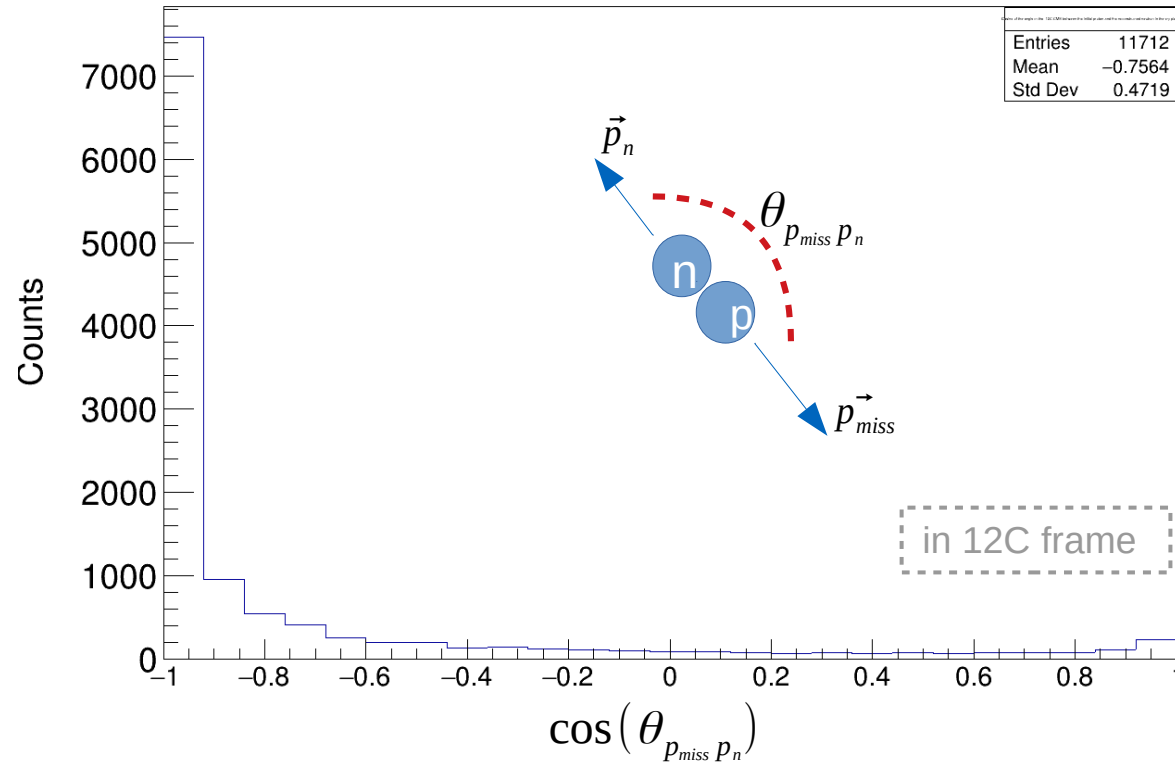
after  
reaction

## Possible Explanations:

- boosting effects / z-shift
- further checks needed

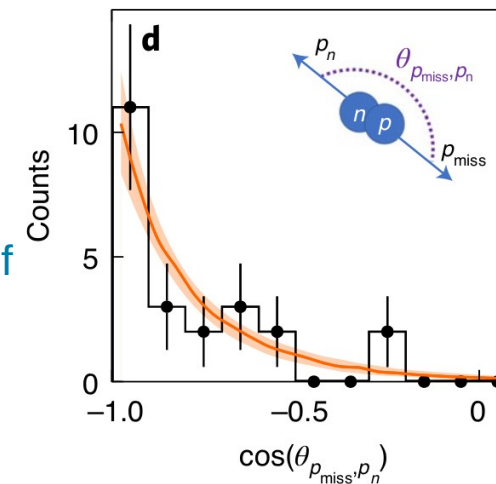


# Angular Correlations for $^{12}\text{C}(\text{p},\text{ppn}/\text{pd})^{10}\text{B}$ in the x-y plane

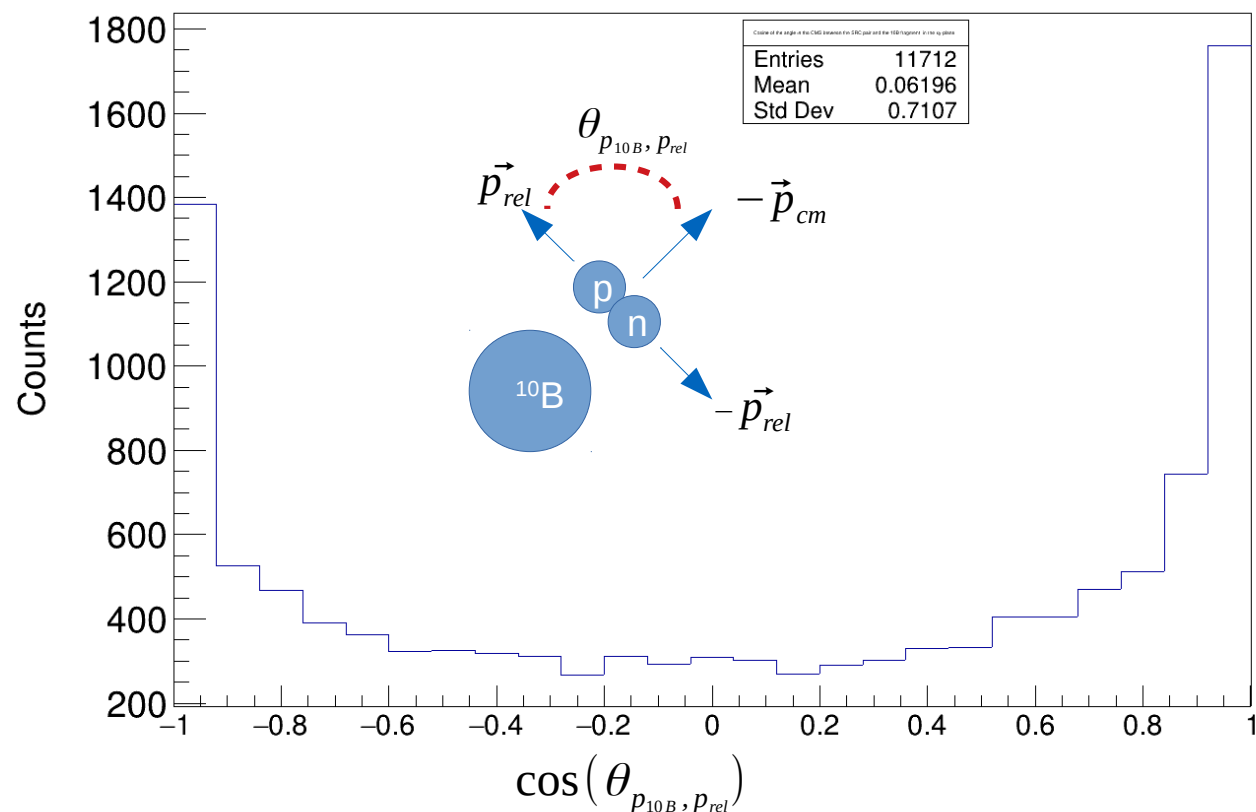


Compare to:

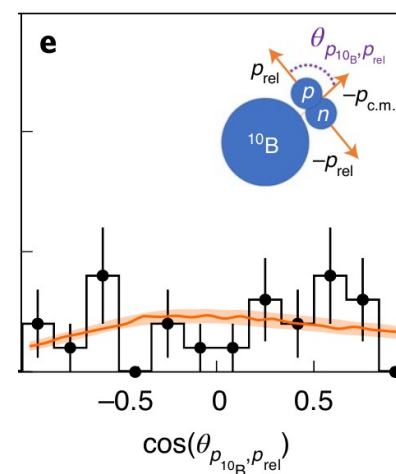
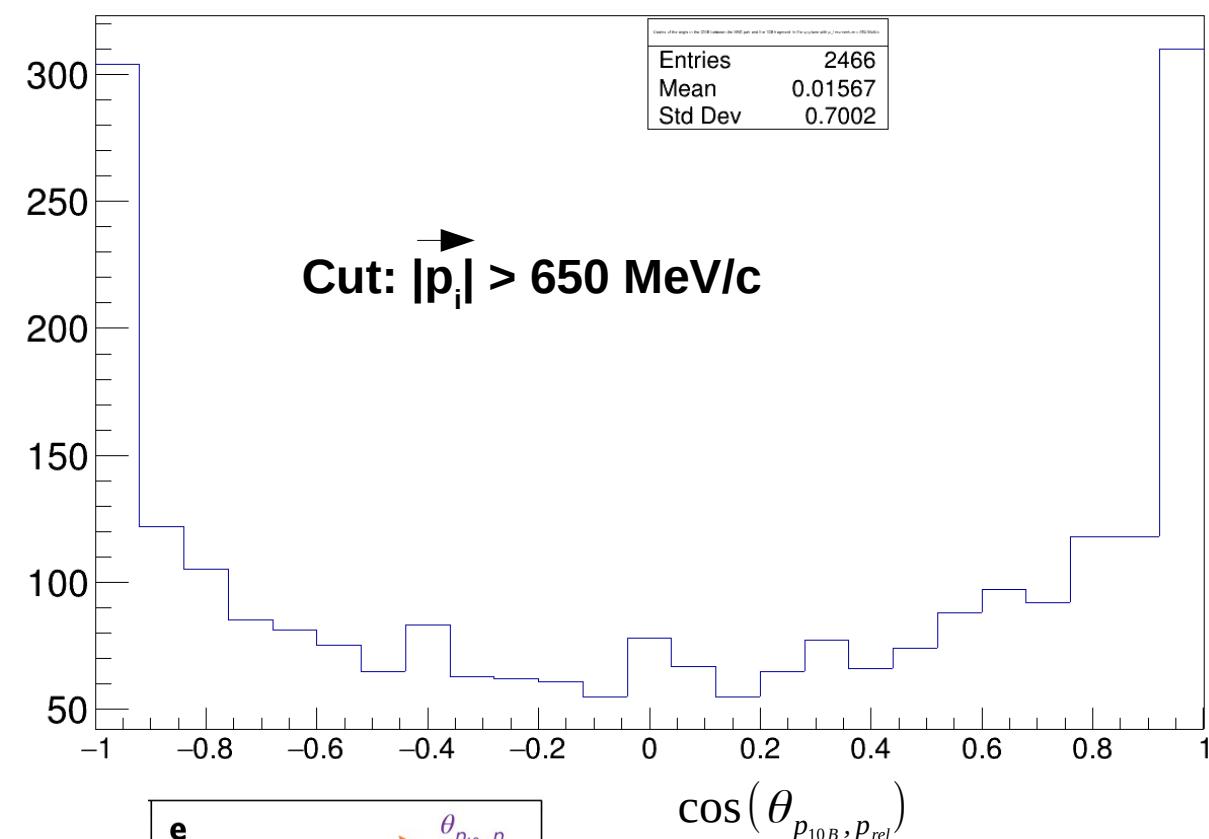
<https://www.nature.com/articles/s41567-021-01193-4.pdf>



# Angular Correlations for $^{12}\text{C}(\text{p},\text{ppn}/\text{pd})^{10}\text{B}$ in the x-y plane



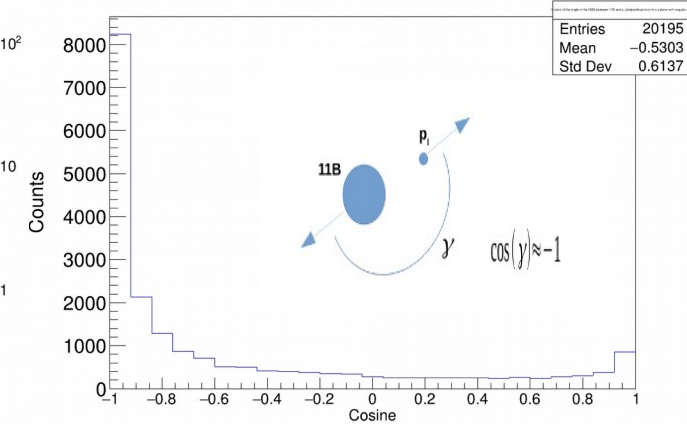
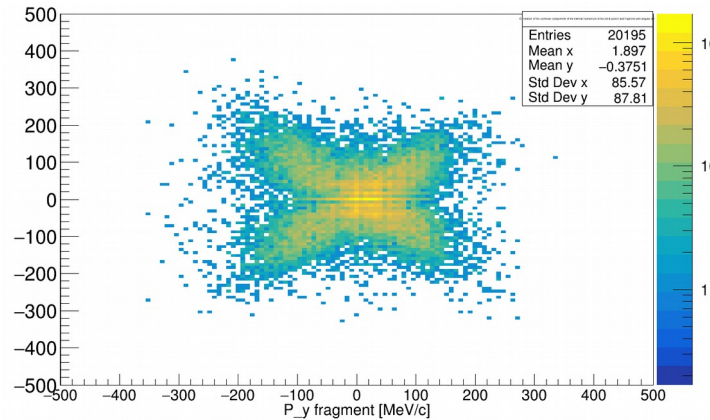
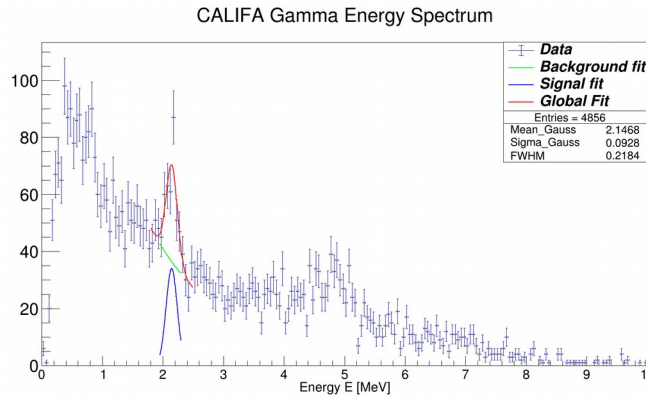
with:  $\vec{p}_{rel} = (p_{miss} - p_n)/2$



Compare to:

<https://www.nature.com/articles/s41567-021-01193-4.pdf>

## ➤ $^{12}\text{C}(p,2p)^{11}\text{B}$ Quasi Free Scattering looks promising

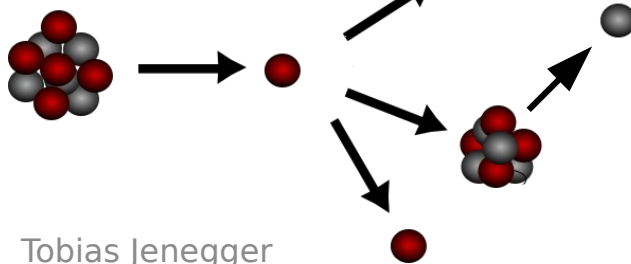


➤ But: Momentum shift in z-direction has to be further analyzed

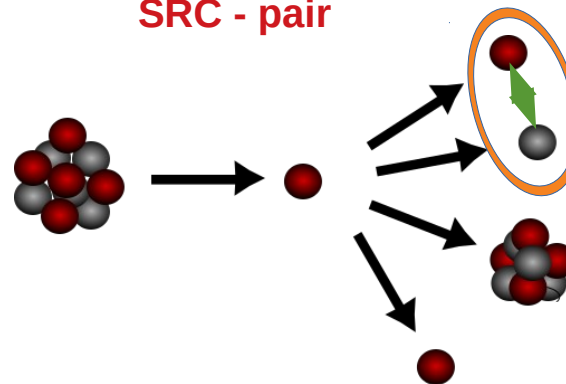
## ➤ For $^{12}\text{C}(p,ppn/pd)^{10}\text{B}$ already first results

➤ How to distinguish between the three reaction types? (Deuteron detection with  $N_f-N_s$  information from CALIFA? Reasonable cuts?)

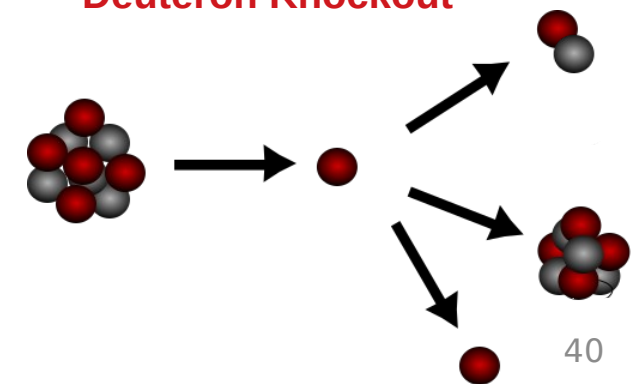
Neutron Evaporation



SRC - pair



Deuteron Knockout





# Thank you!



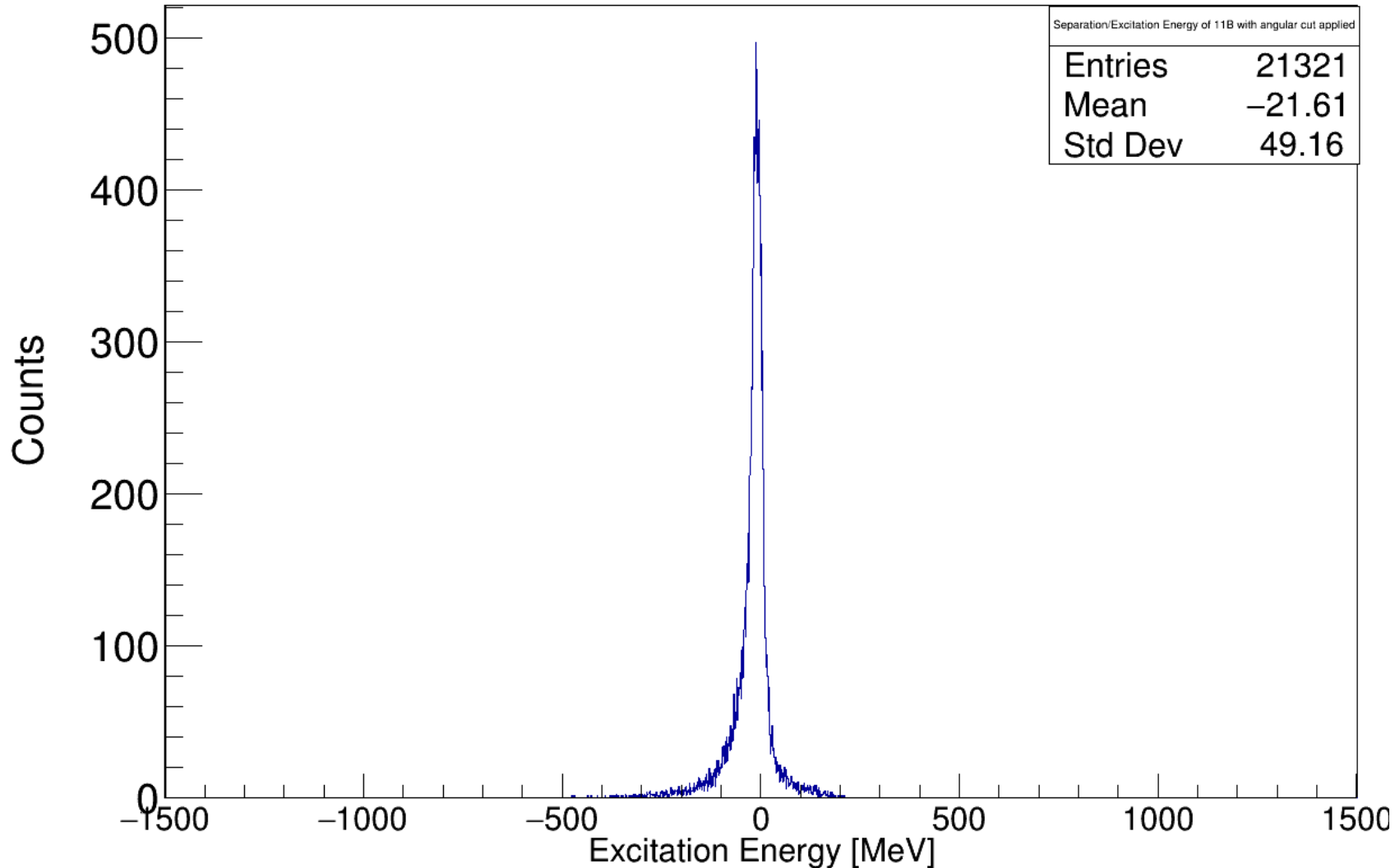


# Backup



# Excitation Energy of $^{11}\text{B}$

$$E_{exc} = \left( \underbrace{P_{^{12}\text{C}} + p_{tg} - p_1 - p_2}_{-p_i} \right) \cdot M - M_{^{11}\text{B}}$$



Is this formula valid?



# Excitation Energy vs. E\_miss

