Radius/Momentum Calculation for S444 Experiment February 2020 - Overview

Tobias Jenegger

0.1 The Setup





1 Geometry and relative position of the detectors in the beam direction

Here, the positions are given for the s444 and s467 experiments

```
zMW0 = -2520 \text{ mm}
z position of the MWPC0:
z position of the target:
                                 zT = -684.5 \text{ mm}
z position of the MWPC1 in front of the Twin-MUSIC:
                                                                   zM1 = 279 \text{ mm}
z position of the middle of the Twin-MUSIC:
                                                        zTwin = 553 \text{ mm}
z position of the MWPC2 after the Twin-MUSIC:
                                                             zM2 = 854 \text{ mm}
\alpha tilted angle of GLAD (14 degrees):
                                                = 0.244 \text{ rad}
effective length of GLAD:
                                  L_{\text{-eff}} = 2067 \text{ mm}
z middle of GLAD
                           zGm = 2577mm
horizontal of the central path (18 degree)
                                                   \theta_out0 = pi/10 rad
                                                zM3 = 5937 \text{ mm}
z position of the MWPC3 after GLAD
z position of the ToFwall
                                  zToFW = 6660.2 \text{ mm}
```

Correspondence between the GLAD current and the magnetic field: I = 3584 A, B = 2.2 T

Positions of the TOFWPads:

 $1 \Rightarrow \text{Messel}$

27⇒ Wixhausen

$\begin{array}{ll} \mathbf{2} & \mathbf{RUNS} \ \mathbf{used} \ \mathbf{for} \ \mathbf{calibration} = \mathbf{SWEEP} \ \mathbf{RUNS} \ \mathbf{with} \\ \mathbf{out} \ \mathbf{target} \end{array}$

UN	Beam ion	Beam Energy [AmeV]	GLAD current [A]	Comments
		V/ 100000		
3	36 12C primary	400	1444	before broken motor, here we see that tof is about 5ns faster. So they probably changed the position of the TOFW afterwards
3	37 12C primary	400	1444	it has be seen that motor drive not working
	88 12C primary	400	1444	tof is back with new gates *magnet sweep 1444A
3	39 12C primary	400	1498	
	10 12C primary	400	1501	
4	11 12C primary	400	1501	stopped with 1558 A
4	12 12C primary	400	1558	
4	13 12C primary	400	1558	stopped with 1653 A
4	14 12C primary	400	1653	
4	15 12C primary	400	1653	stopped with 1748 A
	16 12C primary	400		
	17 12C primary	400	1748	stopped with 1843 A
4	18 12C primary	400	1843	
	19 12C primary	400	1843	stopped with 1938 A
	112C primary	400	1938	
	2 12C primary	400	1938	stopped with 1444 A
	3 12C primary	400	1444	
	4 12C primary	400	1444	stopped with 1349 A
	55 12C primary	400	1349	
	6 12C primary	400	1349	stopped with 1254 A
	7 12C primary	400	1254	
	8 12C primary	400	1254	stopped with 1159
	9 12C primary	400		
(60 12C primary	400	1159	stopped with 1064
(112C primary	400	1064	
	2 12C primary	400	1064	stopped with 1444 A
	23 12C primary	650		stopped with 1957
12	24 12C primary	650	1957	
	=	sweeping		
	=	stable GLAD current		

2.0.1 Other RUNS used for various checks:

RUN 70: 2 cm C target

RUN 80: 10.86 mm C target RUN 81: 24.53 mm CH2 target RUN 67: 24 mm CH2 target

RUN 68: 1 cm C target

RUN 79: 12.29 mm CH2 target RUN 75: 21.98mm C target

3 Methods for flightpath reconstruction in the (x,z) plane

3.1 The "Kickplane" method

3.1.1 From MW0 to the entrance of GLAD, the ion is following a straight line



The straight line trajectory from MW0 to entrance before glad is defined by: \Rightarrow one absolute value before GLAD absolute = calibrated position in mm in the laboratory frame To get the position, use the position given by one MWPCs (1 or 2)

⇒ the theta angle (theta_in) before GLAD

Angle obtained from comining MWPC1 and MWPC2 (to get higher precision the drift time in TWIM MUSIC could be used)

3.1.2 From entrance to the exit of GLAD, the effective trajectory is circular



The circular trajectory is defined by:

- ⇒ one absolute position before GLAD B and angle theta_in (see: 3.1.1)
- \Rightarrow one absolute position at MWPC3

From this information the angle theta_out is constructed in follwing steps:

- 1. Extend the line of flight of the ion before the GLAD.
- 2. The point of intersection with the "kickplane" (symmetry axis line of GLAD magnet) is the kickpoint C.
- 3. Draw a straight line between C and the absolute position at MWPC3 = M3.
- 4. theta_out is the positive angle between the z-beam direction and the line between C and M3.

The curvature radius ρ is given by 1:

$$\rho = \frac{\text{L-eff}}{2 \cdot \sin\left(\frac{theta-in}{2} + \frac{theta-out}{2}\right) \cdot \cos(\delta)}$$

With δ :

$$\delta = \arctan\left(\left|\frac{\frac{\cos(theta_out) - \cos(theta_in)}{\sin(theta_out) + \sin(theta_in)} + \tan(\alpha)}{1 - \frac{\cos(theta_out) - \cos(theta_in)}{\sin(theta_out) + \sin(theta_in)} \cdot \tan(\alpha)}\right|\right)$$

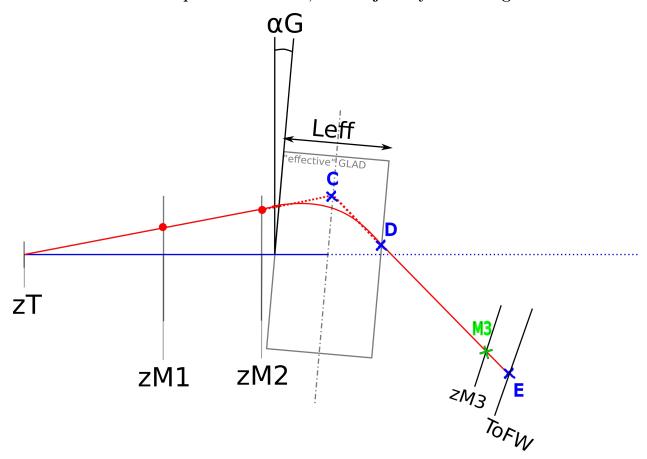
The full derivation can be found in the appendix.

The circular trajectory is then given by:

$$\omega = 2 * \left| \arcsin \left[\frac{BD}{2 \cdot \rho} \right] \right|$$

with BD = length of the BD segment

3.1.3 After GLAD up to the TOFW, the trajectory is a straight line



The straight line trajectory from D to E is definded by:

 $^{^{1}\}text{for consistency checks the} \cos(\delta)$ term can be omitted, as it plays a minor role

- ⇒ the output angle from GLAD theta_out
- ⇒ one absolute position after GLAD in the laboratory frame M3

With this information the straight line trajectory length after GLAD can be measured. It starts at the exit point of GLAD D and follows the straigh line (characterized by the angle theta_out and the absolute position at MWPC3) until the intersection with the TofW (middle position of the ToFWall zToFW= 6660.2mm, tilted angle= 18°).

Finally the pathlength in the (x,z) plane from the target position to the ToFW is given by:

$$P = AB + \rho \cdot \omega + DE$$

where:

A = (x,z) position at the target point

B = (x,z) position at the GLAD entry point

D = (x,z) position at the GLAD exit point

E = (x,z) position where the constructed trajectory line hits the ToFW

The assumption for the "Kickplane" method is that the kickpoint for each event lies on the predefinded Kickplane, the symmetry axis line of the GLAD magnet.

3.2 The "Fit-Track" method

For the "Fit-Track" method the assumption that the kickpoint C lies on the symmetry axis line of the GLAD magnet is rejected. Instead following algorithm is applied: ²

- 1. Extend the line of flight of the ion before the GLAD.
- 2. Draw a line from the point MW3 to C (as constructed with the "Kickplane" method).
- 3. Now sweep the straight line after the kickpoint, leaving the position MW3 unchanged but sweeping the intersection point along the inline beam.
- 4. For each sweeping step plot theta_out versus (d1-d2) where d1 is the distance between B and the point of intersection and d2 the distance between D and the intersection point accordingly.
- 5. 50 sweeping steps are performed.
- 6. Fit the final theta_out versus (d1-d2) plot with linear least square fit.

²This algorithm is motivated from https://www.blogs.uni-mainz.de/fb08-kernphysik/files/2018/09/PHDThesis_OlgaBertini.pdf, section 3.4

7. Find the intersection of the abscissa. The corresponding theta_out value is now the corrected one which should be used for the calculation of the radius.



3.3 The "Theta_in correction" method

Here the "Kickplane" method is used and subsequently the theta_out is corrected by theta_in. That means:

 $theta_out_corr = theta_out - theta_in.$

Consequentely the theta_in dependence of ρ vanishes(neglecting the $\cos(\delta)$ term):

$$\rho = \frac{\text{L_eff}}{2 \cdot \sin\left(\frac{theta \cdot sin}{2} + \frac{theta \cdot out \cdot corr}{2}\right)} = \frac{\text{L_eff}}{2 \cdot \sin\left(\frac{theta \cdot out}{2}\right)}$$

3.4 Final method: "Advanced Fit-Track" method

The same track finding algorithm as for the "Fit-Track" method is used with the only difference that the value for *theta_in* is calculated from the fit of *theta_out* vs. xMW3:

The parameters of the linear fit are used for the calculation of theta_in:

$$theta_in = \alpha - a \cdot x_MW3 - b$$

With **a** being the slope and **b** the offset of the fit. This method prevents from adding up the errors from theta_in measurement.

 α corresponds to the mean value of the theta_out from the fit of theta_out vs. xMW3.

4 Plots

In this section all the plots for the various track finding algorithms are presented. For the calculation of the theta_in angle MWPC1 and MWPC2 are used. Alternatively MWPC0 and MWPC2 could be used, to get a longer lever arm (work in progress ...).

4.1 MWPC1 vs MWPC2 - x position



Figure 1: MWPC1 vs MPWPC2 - x position for sweep runs 39-61.

4.2 MW0 vs MW2- x position



Figure 2: MWPC2 vs MWPC0 - x position for sweep runs 39-61.

4.3 MW1 vs MW3 - x position



Figure 3: MWPC3 vs MWPC1 - x position for sweep runs 39-61.

4.4 theta_out vs MW3- x position



Figure 4: Theta_out vs MWPC3 x position for sweep runs 39-61.

4.5 theta_in vs MW3 - x position



Figure 5: Theta _in vs MWPC3 x position for sweep runs 39-61.

4.6 theta_in+theta_out vs MW3- x position



Figure 6: Theta $_$ out + theta $_$ in vs MWPC3 x position for sweep runs 39-61.

4.7 theta_in vs Radius



Figure 7: Theta in vs GLAD Radius for sweep runs 39-61.

4.8 theta_out vs Radius



Figure 8: Theta _out vs GLAD Radius for sweep runs 39-61.

4.9 theta_in vs theta_out



Figure 9: Theta _in vs theta _out for sweep runs 39-61.

4.10 MW3 vs Radius - x position



Figure 10: MWPC3 x position vs GLAD Radius for sweep runs 39-61.

4.11 MW2 vs Radius - x position



Figure 11: MWPC2 x position vs GLAD Radius for sweep runs 39-61.

5 Relative momentum resolution "Advanced Fit-Track-Method"

The momentum resolution is calculated from the radius-calculation as $\rho \sim p$. From that follows:

$$\frac{\Delta p}{p} = \frac{\Delta \rho}{\rho}$$

For the evaluation of the resolutions for the various sweep runs the two dimensional plot "MWPC3.fX versus GLAD Radius" is projected on the abscissa. The resulting 1D plot is fitted with a gaussian. The mean value from the fit corresponds to ρ and the σ to $\Delta \rho$ respectively.

Runnr.	$\overline{ ho}$	σ	rel. resolution
39	6.48911e+03	2.13410e+01	3.289e-03
40	6.42396e+03	1.56313e+01	2.433e-03
42	6.20033e+03	1.42716e+01	2.301e-03
44	5.86854e+03	1.29449e+01	2.206e-03
46	5.57125e+03	1.31369e+01	2.358e-03
48	5.30203e+03	1.07044e+01	2.018e-03
51	5.06232e+03	1.07182e+01	2.117e-03
53	6.64556e + 03	1.66141e+01	2.500e-03
55	7.08710e + 03	1.91895e+01	2.708e-03
57	7.57474e + 03	2.16135e+01	2.853e-03
59	8.15089e+03	2.22151e+01	2.725e-03
61	8.81055e+03	2.72038e+01	3.088e-03

With mean relative resolution $\frac{\Delta \rho}{\rho} = 2.55\text{e-}03$.

6 Limiting Radius/Momentum resolution factors

The radius/momentum resolution is limited by:

- Energy straggling
- Angular straggling
- Angular resolution of MWPC1/2
- position resolution of MWPC3 (higher order??)

6.1Engergy straggling

For the error calculation the mean energy inside the GLAD was used and the corresponding standard deviation. Generally for a charged particle drifting through a magnetic field the radius of the curved path the particle is following is defined as:

$$\rho = \frac{\gamma \cdot \beta \cdot m}{q \cdot B}$$
(considering c = 1)

Energy straggling has an effect on β and γ respectively. The measurement uncertainty with respect to β can be calculated as follows:

$$\frac{d\rho}{d\beta} = \frac{1}{(\sqrt{1-\beta^2})^3} \cdot \frac{m}{qB}$$

$$\Delta \rho_{\beta} = \frac{d\rho}{d\beta} \cdot \Delta \beta = \frac{\Delta \beta}{(\sqrt{1-\beta^2})^3} \cdot \frac{m}{qB}$$

with relative measurement uncertainty $\frac{\Delta \rho_{\beta}}{\rho} = 5.434e - 04$

6.2Angular straggling

For the error calculation originating from angular straggling it is considered only angular straggling starting from the backend of the MWPC1. That means for this error calculation it is assumed to have a perfect focussed beam undergoes no broadening until it hits the MWPC1 (always at the same x-y-z position). Angular straggling broadens the beam focus and affects therefore both Θ_{-} in and Θ_{-} out.

(angular straggling for Θ_{in} can be neglected, higher order...)

For the calculation of measurement uncertainty with respect to Θ_{-} out we use the simplified geometrical formula of the radius:

$$\rho = \frac{L_{eff}}{2 \cdot \sin(\frac{\Theta in + \Theta out}{2})}^{3}$$
From that follows:

$$\Delta \rho_{\Theta out} = -\rho \cdot \frac{1}{2 \cdot \tan(\frac{\Theta in + \Theta out}{2})} \cdot \Delta \Theta out$$

with $\Delta\Theta_{out} = 3.401e^{-0.04}$. This is the value calculated with LISE++ from MWPC1 to the very center of GLAD. Hence:

$$\left|\frac{\Delta \rho \Theta out}{\rho}\right| = \frac{1}{2 \cdot \tan(\frac{\Theta in + \Theta out}{2})} \cdot \Delta \Theta out = 1.079 e-03$$

Angular resolution of MWPC1/2

$$\begin{split} &\Delta \rho_{\Theta in} = -\rho \cdot \frac{1}{2 \cdot \tan(\frac{\Theta in + \Theta out}{2})} \cdot \Delta \Theta in \\ &\text{with } \Delta \Theta_{in} = \frac{2 \cdot \Delta x^4}{L} \text{ and L the (z-)distance between MWPC1 and MWPC2 (= 575 mm)}. \end{split}$$

³on the following pages I set $\Theta in = 0$ and Θout to the value given by the GLAD field calculator (Mass = 12, Charge = 6, Energy = 400 A/MeV, Current = 1444), see http://web-docs.gsi.de/~land/glad/. ${}^4\Theta_{in} = \frac{x_2 - x1}{L}, \ \Delta\Theta_{in} = \left|\frac{d\Theta_{in}}{dx_2}\right| \cdot \Delta x_2 + \left|\frac{d\Theta_{in}}{dx_1}\right| \cdot \Delta x_1 = \frac{2 \cdot \Delta x}{L}$

With $\Delta x = 0.1mm$ it follows:

$$\left| \frac{\Delta \rho_{\Theta_{in}}}{\rho} \right| = 1.104 \text{e-}03.$$

Adding up the above errors quadratically we get:
$$\left|\frac{\Delta\rho}{\rho}\right| = \sqrt{(5.434 \cdot 10^{-4})^2 + (1.079 \cdot 10^{-3})^2 + (1.104 \cdot 10^{-3})^2} = 1.64 \cdot 10^{-3}$$

Limiting Radius resolution factors on data

For this subsection RUN 53 (with GLAD current = 1444A) is taken in account.

From the table of relative radius resolution we see that for RUN 53 it corresponds to 2.500e-03. The contribution from angular resolution of MWPC1/2 is 1.104e-03 (see previous section). The major limiting factor, the angular straggling can be retrieved from the resolution of theta _out. It has to be considered that the resolution of theta _out is affected by the beam broadening before the MWPC1. To account for that it has to be analyzed the impact of theta _in on theta _out.

Therefore an offset of 1 mrad is added to theta in and the mean values for theta out can be compared:

- theta _out without shift: $3.13257 \cdot 10^{-1}$
- theta out with 1 mrad theta in shift: $3.13912 \cdot 10^{-1}$
- difference: $6.55 \cdot 10^{-1}$ mrad

That means we have a translation factor (for small angles) of 0.655 for theta in to theta

The error calculation in the previous section predicts following angular straggling error:

$$2.5 \cdot 10^{-3} = \sqrt{(1.104 \cdot 10^{-3})^2 + (\left| \frac{\Delta \rho \Theta_{out}}{\rho} \right|)^2}$$
 follows:
$$\left| \frac{\Delta \rho \Theta_{out}}{\rho} \right| = 2.24 \cdot 10^{-3}$$

$$\implies 2.24 \cdot 10^{-3} \cdot \tan(0.15625) \cdot 2 = 7.1 \cdot 10^{-4} = \Delta \theta_{out}$$

The angular resolution of theta _out from data is 1.78045E-03. From this value the angular beam broadening (multiplied by the translation factor) before MWPC1 has to be substracted: $\Delta\theta_{out} = 1.78045 \cdot 10^{-3} - 0.655 \cdot 1.61086 \cdot 10^{-3} = 7.253 \cdot 10^{-4}$

This result coincides well with the predicted one and confirms that the predominant factors for the limiting radius resolution are angular straggling and the angular resolution of MWPC1/2.

Scalability of the field 7

Using the sweep runs (39-61) with different GLAD currents, the scalability of the B-Field can be analyzed. In figure 12 B_{ρ} from GLAD calculator divided by the mean radius is plotted against the according current values.

Taking the assumption that:

Scalability of the field

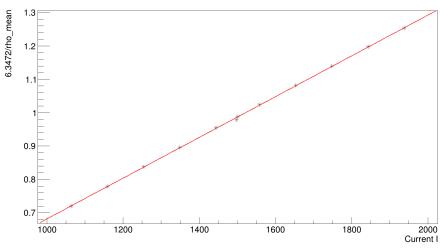


Figure 12

 $B = current \cdot k$ (with k being a constant)

we get from the fit in 12:

slope = 0.000610713

offset = 0.0709244

When plotting the proprotional factor k (which is equal to $\frac{Brho}{I\rho}$, with Brho from GLAD calculator and ρ equal to the mean radius for each run) for each RUN versus the current and adding the proprotional factor from the fit as a straight line, we can see in figure 13 that the factor k from the fit seems to be slightly underestimated.

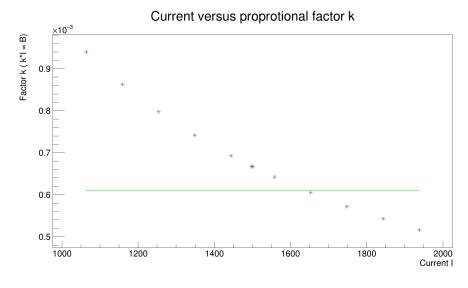


Figure 13

8 Z versus A/q calculations

In this section the target RUNs 82,83,86,88 are analyzed with GLAD current = 1444 A, target = CH2 12.29 mm.

Data is taken for the x-position on MW1,MW2 and MW3, time difference between START and TOFW Detector and charge value from TWIM Music.

The radius of curvature in GLAD is computed using the "Advanced Fit Track" method. The time of flight is calculated using the time difference between START and TOFW with the respective offsets (for the TOF detector pads) and substracting from that the fime of flight between START detector and target. The latter is calculated using $\beta = 0.714549 (\equiv 400 A/MeV)$ and as distance between START and target 1183.25 mm.

Offsets used for RUNs 82 and 83 (using sweep RUNs 39-61) and for RUNs 86 and 88 (using sweep run 36), respectively:

Detnr. TOFW	Time offset 39-61 [ns]	Time offset 36 [ns]
1	114.916	114.4
2	113.592	113.588
3	116.172	116.132
4	114.396	114.358
5	115.279	115.261
6	115.910	115.886
7	116.751	116.734
8	116.002	115.982
9	114.242	114.222
10	115.822	115.801
11	112.410	112.402
12	115.801	115.786
13	113.355	113.347
14	114.925	114.917
15	113.514	118.516
16	112.817	117.823
17	114.214	119.217
18	111.899	116.913
19	113.050	118.063
20	112.578	117.591
21	116.283	121.295
22	116.685	121.690
23	115.884	120.896
24	115.922	120.931
25	114.642	119.649
26	114.207	119.225
27	114.212	119.274

The proceeding for the Z versus A/q calculations are:

- 1. Plot without any cuts/restrictions Z versus Radius using the "Fit-Track" method (see 14).
- 2. From that plot identify the various isotopes and cut on them.
- 3. Plot for each isotope theta_out vs x_3 and make a linear fit (see 17).
- 4. Feed the "Advanced Fit-Track" method with the parameters of the fit for the various isotopes (which you can separate using the previously selected cuts).
- 5. Calculate beta (using the above TOFW offsets) for the various isotopes and plot Z versus A/q.

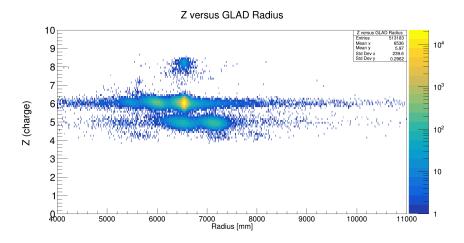


Figure 14: Z versus Radius for RUN 88.

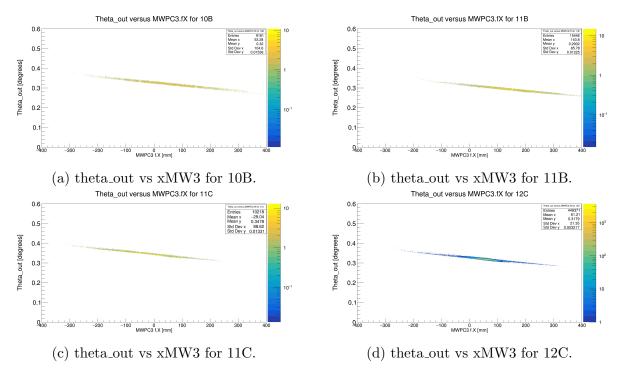


Figure 15: theta_out vs xMW3 for isotopes.

The cuts on the various isotopes in 14 are:

10B: 4.49 < Z < 5.35 and $6131 < \rho < 6786$

11B: 4.34 < Z < 5.48 and $6820 < \rho < 7505$

11C: 5.54 < Z < 6.61 and $5720 < \rho < 6216$

12C: 5.42 < Z < 6.7 and $6247 < \rho < 6850$

Using this cuts we get following fit parameters for the various isotopes:

Isotope	α	a (= slope)	b (=offset)
10B:	0.3202	0.000143964	0.327888
11B:	0.2934	0.000140786	0.313639
11C:	0.3461	0.000146043	0.340846
12C:	0.3178	0.000143976	0.326675

Separating the isotopes by the above charge and radius cuts and using the appropriate α , a and b parameters the Radius gets recalculated via the "Advanced Fit-Track" method. The new value for the radius is now used in the A/q calculation:

$$A/q = \frac{B \cdot \rho \cdot e}{\gamma \cdot \beta \cdot c \cdot u}$$

with:

e: elementary charge = $1.602176634 \cdot 10^{-19}$ C

c: speed of light = 299792458 m/s

u: atomic mass unit = $1.66053906660 \cdot 10^{-27}$ kg

In figure 16 the separated isotopes are shown.

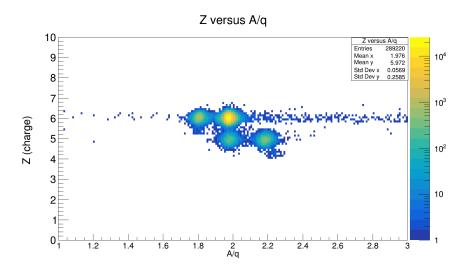


Figure 16: Z versus A/q for run 88 with target CH2 12.29 mm.

Limiting Mass number resolution factors⁵. \Rightarrow REDO! I use 8.1 γ _fixed. Error calculation simplifies...

From the formula:

$$A/q = \frac{B \cdot \rho \cdot e}{\gamma \cdot \beta \cdot c \cdot u}$$

we can see that the determination of A/q is limited by the radius ρ and time measurement and path calculation.

⁵This analysis was done with RUN 88, CH2 target, 12.29mm, GLAD current = 1444 A on the isotope 12C

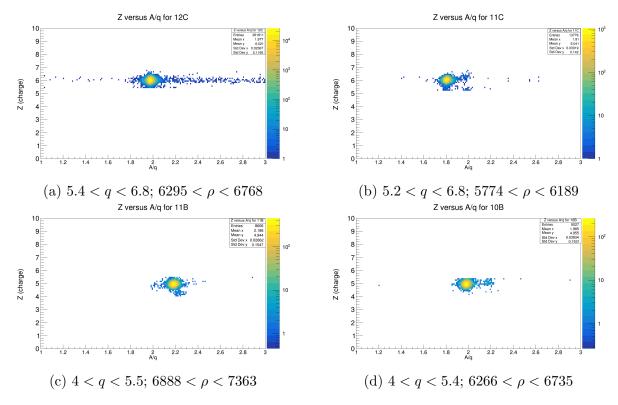


Figure 17: Z versus A/q for runs 82, 83, 86, 88 with target CH2 12.29 mm.

That means:

$$\begin{split} \left|\frac{\Delta A/q}{A/q}\right| &= \sqrt{\left|\frac{\Delta A/q_{\rho}}{A/q}\right|^2 + \left|\frac{\Delta A/q_t}{A/q}\right|^2 + \left|\frac{\Delta A/q_s}{A/q}\right|^2} \\ \text{with:} \\ \left|\frac{\Delta A/q_{\rho}}{A/q}\right| &= \left|\frac{\Delta \rho}{\rho}\right| = 1.64 \cdot 10^{-3} \\ \text{and} \\ \left|\frac{\Delta A/q_t}{A/q}\right| &= \frac{\Delta t}{t} \end{split}$$

 Δt corresponds to the resolution of the time measurement of the TOFW and t the time of flight from target to the TOFW ($\sim 35ns$).

and:

 $|\frac{\Delta A/q_s}{A/q}| = \frac{\Delta s}{s}$ with $\Delta s \sim \Delta \rho$ and s the pathlength from target to TOFW ($\sim 7500mm$). The time resolution is calculated by taking the mean value of σ_t of the most hit TOFW detectors (run 88):

• 10B: most hit detnr: $12,13,14,15,16; \sigma_t = 9.764 \cdot 10^{-2} ns$

• 11B: most hit detnr: 8,9,10,11,12; $\sigma_t = 1.008 \cdot 10^{-1} ns$

• 11C: most hit detnr: 16,17,18,19; $\sigma_t = 1.009 \cdot 10^{-1} ns$

• 12C; most hit detnr: 13,14; $\sigma_t = 9.834 \cdot 10^{-2} ns$

From that follows a relative error due to the time resolution (assuming for all isotopes the same mean time of flight):

- 10B: $2.79 \cdot 10^{-3}$
- 11B: $2.88 \cdot 10^{-3}$
- 11C: $2.88 \cdot 10^{-3}$
- 12C: $2.81 \cdot 10^{-3}$

$$\left|\frac{\Delta A/q_s}{A/a}\right| = \frac{\Delta s}{s} = \frac{\Delta \rho}{s} = 1.421 \cdot 10^{-3}$$

 $|\frac{\Delta A/q_s}{A/q}|=\frac{\Delta s}{s}=\frac{\Delta \rho}{s}=1.421\cdot 10^{-3}$ Summing up all errors quadratically we get for the isotopes:

• 12C:
$$\left| \frac{\Delta A/q}{A/q} \right| = \sqrt{(2.81 \cdot 10^{-3})^2 + (1.64 \cdot 10^{-3})^2 + (1.421 \cdot 10^{-3})^2} = 3.55 \cdot 10^{-3}$$

• 11C:
$$\left| \frac{\Delta A/q}{A/q} \right| = \sqrt{(2.88 \cdot 10^{-3})^2 + (1.64 \cdot 10^{-3})^2 + (1.421 \cdot 10^{-3})^2} = 3.61 \cdot 10^{-3}$$

• 11B:
$$\left| \frac{\Delta A/q}{A/q} \right| = \sqrt{(2.88 \cdot 10^{-3})^2 + (1.64 \cdot 10^{-3})^2 + (1.421 \cdot 10^{-3})^2} = 3.61 \cdot 10^{-3}$$

• 10B:
$$\left| \frac{\Delta A/q}{A/q} \right| = \sqrt{(2.79 \cdot 10^{-3})^2 + (1.64 \cdot 10^{-3})^2 + (1.421 \cdot 10^{-3})^2} = 3.53 \cdot 10^{-3}$$

Revised A/q resolution (with fixed γ)... 9 progress

Looking at the formula:

$$A/q = \frac{B \cdot \rho \cdot e}{\gamma \cdot \beta \cdot c \cdot u}$$

the measured observables are: s,t (which give β) and ρ (from position measurements in MW1,2,3 and Z (from TWIM-Music). On the other side γ remains a fixed parameter as the B-Field is too. The relativistic B-Field is determined once by the GLAD calculator. It contains already a fixed γ value, therefore the formula has to be divided by a fixed γ value too.

In comparison to the non-relativistic formula the above one has an additional factor of γ . While the pathlength and the time of flight are measured in the lab frame (ρ can be neglected, as it is perpendicular to the flight direction and therefore is the same in the patricle and lab frame), the B-Field is calculated in the GLAD calculator in the particle frame. The particle in its own frame is exposed to a higher B-Field by a factor of γ . Hence, if we want to determine the resting mass we need to divide the B-Field by γ .

In figure 18 the calculated A₋q values versus the time of flight are plotted for each isotope and each event. From the plots we get following resolutions for A/q and for ρ (for RUN 88):

Isotope	A/q	$\left \frac{\Delta A/q}{A/q} \right $
10B:	1.96089	0.004735
11B:	2.13816	0.004410
11C:	1.80957	0.004301
12C:	1.96433	0.003220

10 Set by step discrimination of the isotopes

- Plot the charge values of the particles going through TWIM Music and make a gauss fit on them. The intersection of the two gaussians is the charge cut between Z=5 and Z=6.
- Plot A/q versus time of flightfor both charges using the derived formula for ρ
- Project the plot to the A/q axis and make two gaussian fits on both Z = 5 and Z = 6. The intersection between the gaussians give you the mass cuts between 11C and 12C (10B and 11B).
- Now plot for each isotope theta _out vs x_MW3. Make a linear fit on it and extract from it the parameters α , a and b (for the formula: $theta_in = \alpha a \cdot x_MW3 b$)
- Now calculate again A/q for each isotope using the formula for ρ but now with the formula for theta _in from the previous step

Appendices

A Radius resolution with minimal constraints

When using minimal constraints (one single fX entry in MWPC0,1,2,3; instead of requiring also one single entry in fY for MW0,1,2,3) for events in sweep RUN 39-61 the resolution for the radius determination improves:

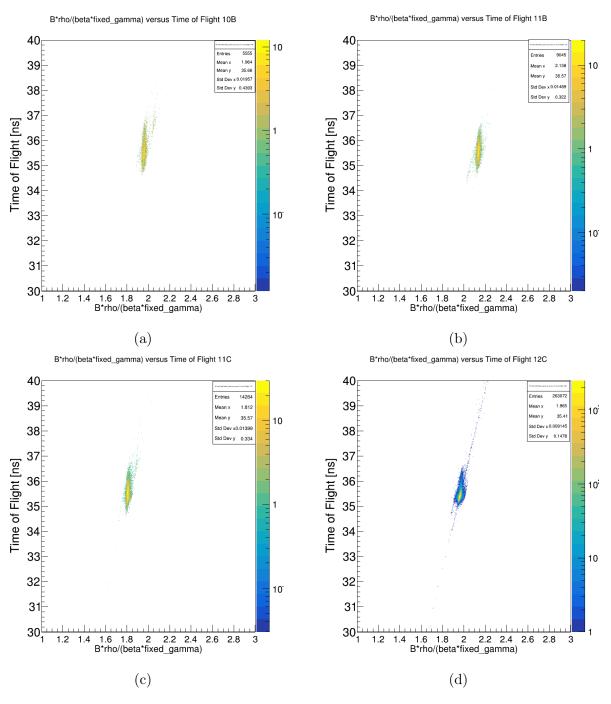


Figure 18: Time of Flight versus A/q with β from time measurement and flightpath reconstruction and fixed γ for RUN 88.

Runnr.	$\overline{ ho}$	σ	rel. resolution
39	6.48993e + 03	2.30085e+01	3.545e-03
40	6.42478e + 03	1.23238e+01	1.918e-03
42	6.20135e+03	1.16977e+01	1.886e-03
44	5.86911e+03	1.05839e+01	1.803e-03
46	5.57055e+03	9.45711e+00	1.697e-03
48	5.30096e+03	8.63127e+00	1.628e-03
51	5.06178e + 03	8.99078e+00	1.776e-03
53	6.64685e+03	1.30785e+01	1.967e-03
55	7.08715e+03	1.56974e+01	2.214e-03
57	7.57535e+03	1.68392e+01	2.222e-03
59	8.15170e + 03	1.93779e+01	2.377e-03
61	8.81023e+03	2.33200e+01	2.646e-03

With the exception of RUN 39 (why??) the resolution improve with low constraints. This could be due to the lower angular straggling inpact when particles don't hit/interact with the y-wires of the MWPCs.

B Time of Flight Calibration

To make the Time of Flight(ToF) calibration, following recipe was used: Calculate the ToF resolution = pathlength(for plastic)/(velocity) where the pathlength is a fixed parameter for each plastic while velocity = pathlength/calibrated time of flight (for each event). As ToF and resolution we get (using sweep RUNS 39-61):

each event). As 101		_ `
Detectornr. TOFV	L J	$Std_{dev}[ns]$
1	4.06321e+01	6.28229e-02
2	4.06324e+01	5.53876e-02
3	4.06304e+01	8.08743e-02
4	4.06301e+01	6.90470e-02
5	4.06281e+01	8.67233e-02
6	4.06272e+01	6.83199e-02
7	4.06262e+01	8.08281e-02
8	4.06264e+01	8.28594e-02
9	4.06242e+01	8.43386e-02
10	4.06240e+01	7.83839e-02
11	4.06224e+01	1.41360e-01
12	4.06236e+01	1.16904e-01
13	4.06194e+01	1.03966e-01
14	4.06205e+01	9.27237e-02
15	4.06174e+01	8.37932e-02
16	4.06166e+01	9.08337e-02
17	4.06155e+01	9.05575e-02
18	4.06131e+01	1.20459e-01
19	4.06106e+01	1.01854e-01
20	4.06130e+01	1.21520e-01
21	4.06119e+01	2.46357e-01
22	4.06103e+01	9.69992e-02
23	4.06092e+01	9.85493e-02
24	4.06069e+01	1.38125e-01
25	4.06062e+01	1.01997e-01
26	4.06065e+01	1.00157e-01
27	4.06030e+01	7.90385e-02

This gives a mean standard deviation of $\sigma_t = 9.907 \cdot 10^{-2}$

C Trigger patterns for S444- February 2020

- tpat 1 = spill on + sofstart
- tpat 2 = spill on + sofstart + califa
- tpat 3 = spill on + sofstart + neuland

- \bullet tpat 4 = spill on + sofstart + califa + neuland
- tpat 9 = spill off + califa
- tpat 10 = spill off + neuland