# Radius/Momentum Calculation for S444 Experiment February 2020 - Overview

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## 0.1 The Setup





## 1 Geometry and relative position of the detectors in the beam direction

Here, the positions are given for the s444 and s467 experiments

```
zMW0 = -2520 \text{ mm}
z position of the MWPC0:
z position of the target:
                                 zT = -684.5 \text{ mm}
z position of the MWPC1 in front of the Twin-MUSIC:
                                                                   zM1 = 279 \text{ mm}
z position of the middle of the Twin-MUSIC:
                                                        zTwin = 553 \text{ mm}
z position of the MWPC2 after the Twin-MUSIC:
                                                             zM2 = 854 \text{ mm}
\alpha tilted angle of GLAD (14 degrees):
                                                = 0.244 \text{ rad}
effective length of GLAD:
                                  L_{\text{-eff}} = 2067 \text{ mm}
z middle of GLAD
                           zGm = 2577mm
horizontal of the central path (18 degree)
                                                   \theta_out0 = pi/10 rad
                                                zM3 = 5937 \text{ mm}
z position of the MWPC3 after GLAD
z position of the ToFwall
                                  zToFW = 6660.2 \text{ mm}
```

Correspondence between the GLAD current and the magnetic field: I = 3584 A, B = 2.2 T

Positions of the TOFWPads:

 $1 \Rightarrow \text{Messel}$ 

27⇒ Wixhausen

# $\begin{array}{ll} \mathbf{2} & \mathbf{RUNS} \ \mathbf{used} \ \mathbf{for} \ \mathbf{calibration} = \mathbf{SWEEP} \ \mathbf{RUNS} \ \mathbf{with} \\ \mathbf{out} \ \mathbf{target} \end{array}$

UN	Beam ion	Beam Energy [AmeV]	GLAD current [A]	Comments	
		V/ 100000			
3	36 12C primary	400	1444	before broken motor, here we see that tof is about 5ns faster. So they probably changed the position of the TOFW afterwards	
3	37 12C primary	400	1444	44 it has be seen that motor drive not working	
	88 12C primary	400	1444	1444 tof is back with new gates *magnet sweep 1444A	
3	39 12C primary	400	1498	B	
	10 12C primary	400	1501		
4	11 12C primary	400	1501	stopped with 1558 A	
4	12 12C primary	400	1558		
4	13 12C primary	400	1558	stopped with 1653 A	
4	14 12C primary	400	1653		
4	15 12C primary	400	1653	stopped with 1748 A	
	16 12C primary	400			
	17 12C primary	400	1748	stopped with 1843 A	
4	18 12C primary	400	1843		
4	19 12C primary	400	1843	stopped with 1938 A	
	112C primary	400	1938		
	2 12C primary	400	1938	stopped with 1444 A	
	3 12C primary	400	1444		
	4 12C primary	400	1444	stopped with 1349 A	
	55 12C primary	400	1349		
	6 12C primary	400	1349	stopped with 1254 A	
	7 12C primary	400	1254		
	8 12C primary	400	1254	stopped with 1159	
	9 12C primary	400			
	0 12C primary	400	1159	stopped with 1064	
(	112C primary	400	1064		
	2 12C primary	400	1064	stopped with 1444 A	
	23 12C primary	650		stopped with 1957	
12	24 12C primary	650	1957		
	=	sweeping			
	=	stable GLAD current			

#### 2.0.1 Other RUNS used for various checks:

RUN 70: 2 cm C target

RUN 80: 10.86 mm C target RUN 81: 24.53 mm CH2 target RUN 67: 24 mm CH2 target

RUN 68: 1 cm C target

RUN 79: 12.29 mm CH2 target RUN 75: 21.98mm C target

# 3 Methods for flightpath reconstruction in the (x,z) plane

#### 3.1 The "Kickplane" method

3.1.1 From MW0 to the entrance of GLAD, the ion is following a straight line



The straight line trajectory from MW0 to entrance before glad is defined by:  $\Rightarrow$  one absolute value before GLAD absolute = calibrated position in mm in the laboratory frame To get the position, use the position given by one MWPCs (1 or 2)

⇒ the theta angle (theta\_in) before GLAD

Angle obtained from comining MWPC1 and MWPC2 (to get higher precision the drift time in TWIM MUSIC could be used)

#### 3.1.2 From entrance to the exit of GLAD, the effective trajectory is circular



The circular trajectory is defined by:

- ⇒ one absolute position before GLAD B and angle theta\_in (see: 3.1.1)
- $\Rightarrow$  one absolute position at MWPC3

From this information the angle theta\_out is constructed in follwing steps:

- 1. Extend the line of flight of the ion before the GLAD.
- 2. The point of intersection with the "kickplane" (symmetry axis line of GLAD magnet) is the kickpoint C.
- 3. Draw a straight line between C and the absolute position at MWPC3 = M3.
- 4. theta\_out is the positive angle between the z-beam direction and the line between C and M3.

The curvature radius  $\rho$  is given by 1:

$$\rho = \frac{\text{L-eff}}{2 \cdot \sin\left(\frac{theta-in}{2} + \frac{theta-out}{2}\right) \cdot \cos(\delta)}$$

With  $\delta$ :

$$\delta = \arctan\left(\left|\frac{\frac{\cos(theta\_out) - \cos(theta\_in)}{\sin(theta\_out) + \sin(theta\_in)} + \tan(\alpha)}{1 - \frac{\cos(theta\_out) - \cos(theta\_in)}{\sin(theta\_out) + \sin(theta\_in)} \cdot \tan(\alpha)}\right|\right)$$

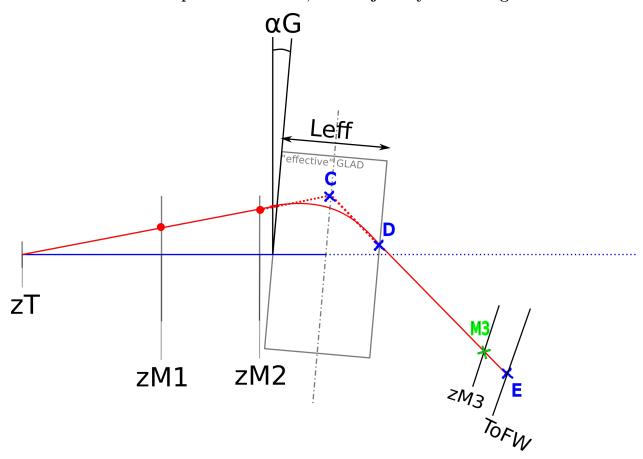
The full derivation can be found in the appendix.

The circular trajectory is then given by:

$$\omega = 2 * \left| \arcsin \left[ \frac{BD}{2 \cdot \rho} \right] \right|$$

with BD = length of the BD segment

#### 3.1.3 After GLAD up to the TOFW, the trajectory is a straight line



The straight line trajectory from D to E is definded by:

 $<sup>^1 \</sup>mathrm{for}$  consistency checks the  $\mathrm{cos}(\delta)$  term can be omitted, as it plays a minor role

- ⇒ the output angle from GLAD theta\_out
- ⇒ one absolute position after GLAD in the laboratory frame M3

With this information the straight line trajectory length after GLAD can be measured. It starts at the exit point of GLAD D and follows the straigh line (characterized by the angle theta\_out and the absolute position at MWPC3) until the intersection with the TofW (middle position of the ToFWall zToFW= 6660.2mm, tilted angle= 18°).

Finally the pathlength in the (x,z) plane from the target position to the ToFW is given by:

$$P = AB + \rho \cdot \omega + DE$$

#### where:

A = (x,z) position at the target point

B = (x,z) position at the GLAD entry point

D = (x,z) position at the GLAD exit point

E = (x,z) position where the constructed trajectory line hits the ToFW

The assumption for the "Kickplane" method is that the kickpoint for each event lies on the predefinded Kickplane, the symmetry axis line of the GLAD magnet.

#### 3.2 The "Fit-Track" method

For the "Fit-Track" method the assumption that the kickpoint C lies on the symmetry axis line of the GLAD magnet is rejected. Instead following algorithm is applied: <sup>2</sup>

- 1. Extend the line of flight of the ion before the GLAD.
- 2. Draw a line from the point MW3 to C (as constructed with the "Kickplane" method).
- 3. Now sweep the straight line after the kickpoint, leaving the position MW3 unchanged but sweeping the intersection point along the inline beam.
- 4. For each sweeping step plot theta\_out versus (d1-d2) where d1 is the distance between B and the point of intersection and d2 the distance between D and the intersection point accordingly.
- 5. 50 sweeping steps are performed.
- 6. Fit the final theta\_out versus (d1-d2) plot with linear least square fit.

<sup>&</sup>lt;sup>2</sup>This algorithm is motivated from https://www.blogs.uni-mainz.de/fb08-kernphysik/files/2018/09/PHDThesis\_OlgaBertini.pdf, section 3.4

7. Find the intersection of the abscissa. The corresponding theta\_out value is now the corrected one which should be used for the calculation of the radius.



### 3.3 The "Theta\_in correction" method

Here the "Kickplane" method is used and subsequently the theta\_out is corrected by theta\_in. That means:

 $theta\_out\_corr = theta\_out - theta\_in.$ 

Consequentely the theta\_in dependence of  $\rho$  vanishes(neglecting the  $\cos(\delta)$  term):

$$\rho = \frac{\text{L_eff}}{2 \cdot \sin\left(\frac{theta \cdot sin}{2} + \frac{theta \cdot out \cdot corr}{2}\right)} = \frac{\text{L_eff}}{2 \cdot \sin\left(\frac{theta \cdot out}{2}\right)}$$

#### 3.4 Final method: "Advanced Fit-Track" method

The same track finding algorithm as for the "Fit-Track" method is used with the only difference that the value for *theta\_in* is calculated from the fit of *theta\_out* vs. xMW3:

The parameters of the linear fit are used for the calculation of theta\_in:

$$theta\_in = \alpha - a \cdot x\_MW3 - b$$

With **a** being the slope and **b** the offset of the fit. This method prevents from adding up the errors from theta\_in measurement.

 $\alpha$  corresponds to the mean value of the theta\_out from the fit of theta\_out vs. xMW3.

## 4 Plots

In this section all the plots for the various track finding algorithms are presented. For the calculation of the theta\_in angle MWPC1 and MWPC2 are used. Alternatively MWPC0 and MWPC2 could be used, to get a longer lever arm (work in progress ...).

### 4.1 MWPC1 vs MWPC2 - x position



Figure 1: MWPC1 vs MPWPC2 - x position for sweep runs 39-61.

## 4.2 MW0 vs MW2- x position



Figure 2: MWPC2 vs MWPC0 - x position for sweep runs 39-61.

## 4.3 MW1 vs MW3 - x position



Figure 3: MWPC3 vs MWPC1 - x position for sweep runs 39-61.

### 4.4 theta\_out vs MW3- x position



Figure 4: Theta\_out vs MWPC3 x position for sweep runs 39-61.

### 4.5 theta\_in vs MW3 - x position



Figure 5: Theta \_in vs MWPC3 x position for sweep runs 39-61.

### 4.6 theta\_in+theta\_out vs MW3- x position



Figure 6: Theta  $\_$ out + theta  $\_$ in vs MWPC3 x position for sweep runs 39-61.

### 4.7 theta\_in vs Radius



Figure 7: Theta in vs GLAD Radius for sweep runs 39-61.

### 4.8 theta\_out vs Radius



Figure 8: Theta \_out vs GLAD Radius for sweep runs 39-61.

#### 4.9 theta\_in vs theta\_out



Figure 9: Theta \_in vs theta \_out for sweep runs 39-61.

## 4.10 MW3 vs Radius - x position



Figure 10: MWPC3 x position vs GLAD Radius for sweep runs 39-61.

## 4.11 MW2 vs Radius - x position



Figure 11: MWPC2 x position vs GLAD Radius for sweep runs 39-61.

## 5 Relative momentum resolution "Advanced Fit-Track-Method"

The momentum resolution is calculated from the radius-calculation as  $\rho \sim p$ . From that follows:

$$\frac{\Delta p}{p} = \frac{\Delta \rho}{\rho}$$

For the evaluation of the resolutions for the various sweep runs the two dimensional plot "MWPC3.fX versus GLAD Radius" is projected on the abscissa. The resulting 1D plot is fitted with a gaussian. The mean value from the fit corresponds to  $\rho$  and the  $\sigma$  to  $\Delta \rho$  respectively.

Runnr.	$\overline{ ho}$	$\sigma$	rel. resolution
39	6.48911e+03	2.13410e+01	3.289e-03
40	6.42396e+03	1.56313e+01	2.433e-03
42	6.20033e+03	1.42716e+01	2.301e-03
44	5.86854e+03	1.29449e+01	2.206e-03
46	5.57125e+03	1.31369e+01	2.358e-03
48	5.30203e+03	1.07044e+01	2.018e-03
51	5.06232e+03	1.07182e+01	2.117e-03
53	6.64556e + 03	1.66141e+01	2.500e-03
55	7.08710e + 03	1.91895e+01	2.708e-03
57	7.57474e + 03	2.16135e+01	2.853e-03
59	8.15089e+03	2.22151e+01	2.725e-03
61	8.81055e+03	2.72038e+01	3.088e-03

With mean relative resolution  $\frac{\Delta \rho}{\rho} = 2.55 \text{e-}03$ .