

# Inter Quartile Range (IQR)

- The Interquartile Range (IQR) is a measure of statistical dispersion, representing the **difference between the 75th and 25th percentiles (Q3 and Q1) of a dataset.**
- It's often used in conjunction with a multiplier of 1.5 to identify potential outliers
- The IQR is calculated as  $Q3 - Q1$ , where Q3 is the median of the upper half of the data and Q1 is the median of the lower half.
- Essentially, it's the range within which the middle 50% of the data falls.

## Why 1.5 multiplier?

- The 1.5 IQR rule **uses 1.5 as a scale to identify outliers.** It's based on the idea that data points significantly different from the rest of the dataset are outliers.
- Specifically, any data point that is more than 1.5 times the IQR below Q1 or above Q3 is considered a potential outlier.
- This rule helps to balance sensitivity (detecting actual outliers) and stringency (avoiding false positives).
- The 1.5 multiplier provides a reasonable compromise for identifying outliers while keeping the boundaries within a reasonable range.

Exercise:

- The interquartile range. Compare the two interquartile ranges.
- Any outliers in either set.

The five number summary for the day and night classes is

	Minimum	$Q_1$	Median	$Q_3$	Maximum
Day	32	56	74.5	82.5	99
Night	25.5	78	81	89	98

<b>IQR value : <math>IQR = Q_3 - Q_1</math></b> <b>Day: <math>IQR = 82.5 - 56 = 26.5</math></b> <b>Night : <math>IQR = 89 - 78 = 11</math></b>	
<b>Lesser : (DAY)</b> Lesser IQR = $Q_1 - 1.5 * IQR$ $= 56 - (1.5) * (26.5)$ $= 16.25$	<b>Greater : (DAY)</b> Greater IQR = $Q_3 + 1.5 * IQR$ $= 82.5 + (1.5) * (26.5)$ $= 122.25$
<b>Lesser : (Night)</b> Lesser IQR = $Q_1 - 1.5 * IQR$ $= 78 - (1.5) * (11)$ $= 61.5$	<b>Greater : (Night)</b> Greater IQR = $Q_3 + 1.5 * IQR$ $= 89 + (1.5) * (11)$ $= 105.5$

DAY: Range: **16.25 to 122.25** → All values (32 to 99) fall inside → So No Outliers

NIGHT: Range: **61.5 to 105.5** → But **25.5 < 61.5** → **Outlier found at 25.5**

**We can replace 25.5 in the place of 61.5 in Night classes.**

### Analyzing IQR values in Placement Dataset

	ssc_p	hsc_p	degree_p	etest_p	mba_p	salary
<b>Mean</b>	67.303395	66.333163	66.370186	72.100558	62.278186	288655.405405
<b>Median</b>	67.0	65.0	66.0	71.0	62.0	265000.0
<b>Mode</b>	62.0	63.0	65.0	60.0	56.7	300000.0
<b>Q1:25%</b>	60.6	60.9	61.0	60.0	57.945	240000.0
<b>Q2:50%</b>	67.0	65.0	66.0	71.0	62.0	265000.0
<b>Q3:75%</b>	75.7	73.0	72.0	83.5	66.255	300000.0
<b>99%</b>	87.0	91.86	83.86	97.0	76.1142	NaN
<b>Q4:100%</b>	89.4	97.7	91.0	98.0	77.89	940000.0
<b>IQR</b>	15.1	12.1	11.0	23.5	8.31	60000.0
<b>1.5rule</b>	22.65	18.15	16.5	35.25	12.465	90000.0
<b>Lesser</b>	37.95	42.75	44.5	24.75	45.48	150000.0
<b>Greater</b>	98.35	91.15	88.5	118.75	78.72	390000.0
<b>Min</b>	40.89	37.0	50.0	50.0	51.21	200000.0
<b>Max</b>	89.4	97.7	91.0	98.0	77.89	940000.0

#### SSC :

IQR = 15.1

Min = 40.89 > Lesser = 37.95

Max = 89.4 < Greater = 98.35

**Conclusion:** No outliers in SSC percentage data.

#### HSC :

IQR = 12.1

Min = 37.0 < Lesser = 42.75

Max = 97.7 > Greater = 91.15

**Conclusion:** Two outlier exists in HSC percentage data.

**Degree Percentage:**

IQR = 11.0

Min = 50.0 > Lesser = 44.5

Max = 91.0 < Greater = 88.5

Conclusion: **One outlier** exists in degree scores.

**E-test Percentage:**

IQR = 23.5

Min = 50.0 > Lesser = 24.75

Max = 98.0 < Greater = 118.75

**Conclusion:** No outliers found in E-test scores.

**MBA Percentage:**

IQR = 8.31

Min = 51.21 > Lesser = 45.48

Max = 77.89 < Greater = 78.72

**Conclusion:** No outliers in MBA scores.

**Salary:**

IQR = ₹60,000

Min = ₹200,000 > Lesser = ₹150,000

**Max = ₹940,000 > Greater = ₹390,000**

**Conclusion:** There is **one outlier** in salary data.