

Distribución	Parámetros	Función de Probabilidad	Dominio	Media	Varianza	Función Generatriz de Momentos
<i>Bernoulli</i>	$x \sim \text{bernoulli}(p)$	$f(x) = p^x(1-p)^{1-x}$	$x = 0, 1$	p	$p(1-p)$	$(1-p) + e^t p$
<i>Binomial</i>	$x \sim \text{bin}(n, p)$	$f(x) = \binom{n}{x} p^x (1-p)^{n-x}$	$x = 1, 2, \dots, \mathbb{Z}^+$	np	$np(1-p)$	$[(1-p) + e^t p]^n$
<i>Binomial Negativa</i>	$x \sim \text{NB}(r, p)$	$f(x) = \binom{x-1}{r-1} p^r (1-p)^{x-r}$	$x = r, r+1, \dots, \mathbb{Z}^+$	$\frac{r}{p}$	$\frac{r(1-p)}{p^2}$	$\left[\frac{pe^t}{1-e^t(1-p)} \right]^r$
<i>Geométrica</i>	$x \sim \text{geo}(p)$	$f(x) = p(1-p)^{x-1}$	$x = 1, 2, \dots, \mathbb{Z}^+$	$\frac{1}{p}$	$\frac{(1-p)}{p^2}$	$\frac{pe^t}{1-e^t(1-p)}$
<i>Poisson</i>	$x \sim \text{POI}(\lambda)$	$f(x) = \frac{e^{-\lambda} \lambda^x}{x!}$	$x = 0, 1, 2, \dots, \mathbb{Z}^+$	λ	λ	$e^{\lambda(e^t-1)}$
<i>Hipergeométrica</i>	$x \sim \text{hyp}(N, M, K)$	$f(x) = \frac{\binom{M}{x} \binom{N-M}{K-x}}{\binom{N}{K}}$	$x = 0, 1, 2, \dots, \mathbb{Z}^+$	$\frac{KM}{N}$	$\frac{KM}{N} \left[\frac{(N-M)(N-K)}{N(N-1)} \right]$	–
<i>Uniforme Discreta Escalonada</i>	$x \sim \text{DU}(x_1, \dots, x_k)$	$f(x) = \frac{1}{k}$	$x = x_1, x_2, \dots, x_k$	\bar{x}	$\sum_{i=1}^k \frac{(x_i - \bar{x})^2}{k}$	–
<i>Uniforme Discreta Seguida</i>	$x \sim \text{DU}(1, k)$	$f(x) = \frac{1}{k}$	$x = 1, 2, \dots, k$	$\frac{k+1}{2}$	$\frac{k^2-1}{12}$	$\frac{1}{k} \left[\frac{e^t(1-e^{tk})}{1-e^t} \right]$

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Uniforme Continua	$x \sim \text{unif}(a, b)$	$f(x) = \frac{1}{b-a}$	$a < x < b$	$\frac{b+a}{2}$	$\frac{(b-a)^2}{12}$
Gamma	$x \sim \text{gam}(\alpha, \beta)$	$f(x) = \frac{1}{\Gamma(\alpha)\beta^\alpha} x^{\alpha-1} e^{-\frac{x}{\beta}}$	$x > 0$	$\alpha\beta$	$\alpha\beta^2$
Exponencial	$x \sim \text{exp}(\theta)$	$f(x) = \frac{1}{\theta} e^{-\frac{x}{\theta}}$	$x > 0$	θ	θ^2
χ^2	$x \sim \chi_v^2$	$f(x) = \frac{1}{\Gamma\left(\frac{v}{2}\right) 2^{v/2}} x^{v/2-1} e^{-\frac{x}{2}}$	$x > 0$	v	$2v$
T	$x \sim T_v$	$f(x) = \frac{\Gamma\left(\frac{v+1}{2}\right)}{\Gamma\left(\frac{v}{2}\right)} \frac{1}{\sqrt{v\pi}} \left(1 + \frac{x^2}{v}\right)^{-\left(\frac{v+1}{2}\right)}$	$x \in \mathbb{R}$	0	$\frac{v}{v-2}; v > 2$
F	$x \sim F_{v_1, v_2}$	$f(x) = \frac{\Gamma\left(\frac{v_1+v_2}{2}\right)}{\Gamma\left(\frac{v_1}{2}\right)\Gamma\left(\frac{v_2}{2}\right)} \left(\frac{v_1}{v_2}\right)^{\frac{v_1}{2}} x^{\frac{v_1}{2}-1} \left(1 + \frac{v_1}{v_2}x\right)^{-\left(\frac{v_1+v_2}{2}\right)}$	$x > 0$	$\frac{v_2}{v_2-2}$	$\frac{2v_2^2}{v_1} \left[\frac{v_1+v_2-2}{(v_2-2)^2(v_2-4)} \right]$
Normal	$x \sim N(\mu, \sigma^2)$	$f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2\sigma^2}(x-\mu)^2}$	$x \in \mathbb{R}$	μ	σ^2
Lognormal	$x \sim \text{LOGN}(\mu, \sigma^2)$	$f(x) = \frac{1}{\sqrt{2\pi}x\sigma} e^{-\frac{1}{2\sigma^2}(\ln x - \mu)^2}$	$x > 0$	$e^{\mu + \frac{\sigma^2}{2}}$	$(e^{\sigma^2} - 1)e^{2\mu + \sigma^2}$

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Beta	$x \sim \text{beta}(\alpha, \beta)$	$f(x) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} x^{\alpha-1} (1-x)^{\beta-1}$	$0 < x < 1$	$\frac{\alpha}{\alpha + \beta}$	$\frac{\alpha\beta}{(\alpha + \beta)^2(\alpha + \beta + 1)}$
Pareto	$x \sim \text{pareto}(\theta, k)$	$f(x) = \frac{k}{\theta} \left(1 + \frac{x}{\theta}\right)^{-(k+1)}$	$x > 0$	$\frac{\theta}{k-1}$	$\frac{\theta^2 k}{(k-2)(k-1)^2}$
Weibull	$x \sim \text{weibull}(\theta, \beta)$	$f(x) = \frac{\beta}{\theta^\beta} x^{\beta-1} e^{-\left(\frac{x}{\theta}\right)^\beta}$	$x > 0$	$\theta \Gamma\left(1 + \frac{1}{\beta}\right)$	$\theta^2 \left\{ \Gamma\left(1 + \frac{2}{\beta}\right) - \left[\Gamma\left(1 + \frac{1}{\beta}\right) \right]^2 \right\}$
Exponencial de Dos Parámetros	$x \sim \text{exp}(\theta, \eta)$	$f(x) = \frac{1}{\theta} e^{-\left(\frac{x-\eta}{\theta}\right)}$	$x > \eta$	$\theta + \eta$	θ^2
Doble Exponencial	$x \sim \text{DE}(\theta, \eta)$	$f(x) = \frac{1}{2\theta} e^{-\frac{ x-\eta }{\theta}}$	$x \in \mathbb{R}$	η	$2\theta^2$
Cauchy	$x \sim \text{CAU}(\theta, \eta)$	$f(x) = \frac{1}{\theta\pi \left\{ 1 + \left(\frac{x-\eta}{\theta}\right)^2 \right\}}$	$x \in \mathbb{R}$	—	—
Valores Extremos (Gumbel)	$x \sim \text{gumbel}(\theta, \eta)$	$f(x) = \frac{1}{\theta} e^{-\left(\frac{x-\eta}{\theta}\right)} e^{-e^{-\left(\frac{x-\eta}{\theta}\right)}}$	$x \in \mathbb{R}$	$\eta - \gamma\theta$ $\gamma = 0.5772$	$\frac{\pi^2 \theta^2}{6}$
Logística	$x \sim \text{LOG}(\mu, \theta)$	$f(x) = \frac{1}{4\theta} \text{sech}^2\left(\frac{x-\mu}{2\theta}\right)$	$x \in \mathbb{R}$	μ	$\frac{\pi^2}{3} \theta^2$

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<i>Uniforme Continua</i>	$x \sim \text{unif}(a, b)$	$\frac{e^{bt} - e^{at}}{t(b - a)}$	$F(x) = \frac{x - a}{b - a}$
<i>Gamma</i>	$x \sim \text{gam}(\alpha, \beta)$	$\frac{1}{(1 - \beta t)^\alpha}$	–
<i>Exponencial</i>	$x \sim \text{exp}(\theta)$	$\frac{1}{1 - \theta t}$	$F(x) = 1 - e^{-\frac{x}{\theta}}$
χ^2	$x \sim \chi_v^2$	$\frac{1}{(1 - 2t)^{\frac{v}{2}}}$	–
<i>Normal</i>	$x \sim N(\mu, \sigma^2)$	$e^{\mu t + \frac{\sigma^2 t^2}{2}}$	–
<i>Beta</i>	$x \sim \text{beta}(\alpha, \beta)$	$1 + \sum_{k=1}^{\infty} \left(\prod_{r=0}^{k-1} \frac{\alpha + r}{\alpha + \beta + r} \right) \frac{t^k}{k!}$	–
<i>Weibull</i>	$x \sim \text{weibull}(\theta, \beta)$	$\sum_{n=0}^{\infty} \frac{t^n \theta^n}{n!} \Gamma\left(1 + \frac{n}{\beta}\right)$	$F(x) = 1 - e^{-\left(\frac{x}{\theta}\right)^\beta}$

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<i>Cauchy</i>	$x \sim \text{CAU}(\theta, \eta)$	—	$F(x) = \frac{1}{\pi} \tan^{-1} \left(\frac{x - \eta}{\theta} \right) + \frac{1}{2}$
<i>Exponencial de Dos Parámetros</i>	$x \sim \text{exp}(\theta, \eta)$	$\frac{e^{\eta t}}{1 - \theta t}$	$F(x) = 1 - e^{-\frac{(x - \mu)}{\theta}}$
<i>Doble Exponencial</i>	$x \sim \text{DE}(\theta, \eta)$	$\frac{e^{\eta t}}{1 - \theta^2 t^2}$	—
<i>Valores Extremos (Gumbel)</i>	$x \sim \text{EV}(\theta, \eta)$	$e^{\eta t} \Gamma(1 - \theta t)$	$F(x) = e^{-e^{-\left(\frac{x - \eta}{\theta}\right)}}$
<i>Logística</i>	$x \sim \text{LOG}(\mu, \theta)$	$e^{\mu t} \beta(1 - \theta t, 1 + \theta t)$	$F(x) = \frac{1}{2} + \frac{1}{2} \tanh \left(\frac{x - \mu}{2\theta} \right)$
<i>Geométrica</i>	$x \sim \text{geo}(p)$	$\frac{pe^t}{1 - e^t(1 - p)}$	$F(x) = 1 - (1 - p)^x$
<i>Pareto</i>	$x \sim \text{pareto}(\theta, k)$	—	$F(x) = 1 - \left(1 + \frac{x}{\theta} \right)^{-k}$

Distribución	Dominio	Función de Probabilidad	Teoremas
Normal Bivariada	$x \in \mathcal{R}$ $y \in \mathbb{R}$ $\sigma_x > 0$ $\sigma_y > 0$ $-1 \leq \rho \leq 1$	$f(x, y) = \frac{1}{2\pi\sigma_x\sigma_y\sqrt{1-\rho^2}} e^{-\frac{1}{2(1-\rho^2)}\left[\left(\frac{x-\mu_x}{\sigma_x}\right)^2 - 2\rho\left(\frac{x-\mu_x}{\sigma_x}\right)\left(\frac{y-\mu_y}{\sigma_y}\right) + \left(\frac{y-\mu_y}{\sigma_y}\right)^2\right]}$	$x \sim N(\mu_x, \sigma_x^2)$ $y \sim N(\mu_y, \sigma_y^2)$ $corr_{x,y} = \rho$ $corr(x^2, y^2) = \rho^2$ $x y \sim N\left[\mu_x + \rho\frac{\sigma_x}{\sigma_y}(y - \mu_y), \sigma_x^2(1 - \rho^2)\right]$
Multinomial	$\sum_{i=1}^k x_i = n$ $\sum_{i=1}^k p_i = 1$ $x = 0, 1, \dots, \mathbb{Z}^+$	$f(x_1, x_2, \dots, x_k; n; p_1^{x_1}, p_2^{x_2}, \dots, p_k^{x_k}) = \frac{n!}{x_1! x_2! \dots x_k!} p_1^{x_1} p_2^{x_2} \dots p_k^{x_k}$	$x_j \sim bin(m, p_j)$, $m = n$ $cov(x_i, x_j) = -mp_i p_j$ $x_i x_j \sim bin\left(m - x_j, \frac{p_i}{1 - p_j}\right)$
Hipergeométrica Multivariada	$\sum_{i=1}^k x_i = n$ $\sum_{i=1}^k M_i = N$ $x = 0, 1, \dots, \mathbb{Z}^+$	$f(x_1, x_2, \dots, x_k; N; M_1, M_2, \dots, M_K) = \frac{\binom{M_1}{x_1} \binom{M_2}{x_2} \binom{M_3}{x_3} \dots \binom{M_k}{x_k}}{\binom{N}{n}}$	—
Dirichlet Bivariada	$0 < x < 1$ $0 < y < 1$ $0 < y < 1 - x < 1$ $\alpha > 0$ $\beta > 0$ $c > 0$	$f(x, y; \alpha, \beta, c) = \frac{\Gamma(\alpha + \beta + c)}{\Gamma(\alpha)\Gamma(\beta)\Gamma(c)} x^{\alpha-1} y^{\beta-1} (1 - x - y)^{c-1}$	$x \sim beta(\alpha, \beta + c)$ $y \sim beta(\beta, \alpha + c)$ $Y X \sim beta(\beta, c)$ $1 - x \sim beta(\beta + c, \alpha)$