

FAKULTETA ZA ELEKTROTEHNIKO

MASTERS THESIS

Msc Disposition

Author:
Jakob JENKO

Supervisor:
Dr. Marko MEŽA

*A thesis submitted in fulfillment of the requirements
for the degree of Masters of electrical engineering*

in the

?
IKT

March 14, 2022

Declaration of Authorship

I, Jakob JENKO, declare that this thesis titled, “Msc Disposition” and the work presented in it are my own. I confirm that:

- This work was done wholly or mainly while in candidature for a research degree at this University.
- Where any part of this thesis has previously been submitted for a degree or any other qualification at this University or any other institution, this has been clearly stated.
- Where I have consulted the published work of others, this is always clearly attributed.
- Where I have quoted from the work of others, the source is always given. With the exception of such quotations, this thesis is entirely my own work.
- I have acknowledged all main sources of help.
- Where the thesis is based on work done by myself jointly with others, I have made clear exactly what was done by others and what I have contributed myself.

Signed:

Date:

Load profiling of home appliances using load classification

0.1 Introduction

Climate change calls to shift to renewable energy and restructuring of electricity sector. Sources Eurostat, 2022 show as of time of reading this paper, 44 % of produced in Europe was from combustible sources such as gas, fuel and coal. Even thorough that is significant decrease of 10 % in last 10 years, it is a significant Co2 emitter. Same source Eurostat, 2022 also states that, third of energy is consumed by residential sector. It is estimated, that human population will reach 10 billion inhabitants in next 10 years, and ever-increasing ownership of electrical appliances such as smartphones, HVACs, and EVs will further increase energy consumption. (elevate this issue) Acknowledging that, Reducing consumption in that sector could leave a significant impact on human footprint.

The EU aims to be climate neutral by 2050, therefore it seeks to improve efficiency of every part of pollution contributors through The European Green Deal. Large part of these contributors is the Energy sector. Sub part of energy sector is residential sector, where many advancements could be made to help to reach the goal.

This could be achieved trough various applications and methods that use load profiling and load monitoring as their core technology. Authors in Chuan, Rao, and Ukil, 2014 proposed method to reduce peak loads by studying consumer appliance usage patterns. Paper Csoknyai et al., 2019 studied consumer usage patterns, and returned feedback that contributed to reducing consumption. Another notable way is a use of distributed energy resources and manage them in such a way to decrease net output of energy flow such as authors describe in Moreno Jaramillo et al., 2021. All described methods would reduce and alleviate the load off the power grid.

Load profiling and load monitoring and anomaly detection in building energy consumption are not a novelty and had been in research since 1980s. While aggregated load profiles of households, are relatively predictable, recent data obtained using smart meter data showed large deviance from user to user due to different lifestyles, as author states in Proedrou, 2021. In recent years load profiles have changed due to renewable energy accelerated development of distributed energy resources such as residential photovoltaic power plants, home wind energy and using EVs and home batteries. Goal of these systems is to mitigate net energy flow to be as local as possible. Socioeconomic changes such as (work-from-home), also drastically reshaped the load profile curve.

Technology advancements in load monitoring and non-intrusive load monitoring and increased adoption of smart energy meters offer a new way of load profiling, that is NILM load profiling. Besides consumption reduction there are many applications of load profiling which I will later describe.

0.2 Structure

M.Sc. degree will be composed of the following parts. In the first part I will define what is load profiling, appliance level load profiling, non-intrusive load monitoring, intrusive load monitoring and anomaly detection. Then I will review related research work done to date. Next, I will elaborate on existing ideas where load profiling is being used to-date and what are its possible applications. Then, I will present used datasets and finally, I will present a working demo using appliance classification and simple load profiling. Demo will present possible use of one of previously mentioned applications.

0.3 Definitions

Author Proedrou, 2021 defines terms as following

- Residential: private residences, with no commercial usage, occupied by one or more persons either full-time or part-time during a calendar year.
- Load: the electricity that all the electricity-powered devices in the household consume in unit time.
- Profile: a graph representing the significant features of the electricity load over time.
- Model: "a formal system that represents the combined processes" Kavousian, Rajagopal, and Fischer, 2013 of electricity consumption by all the electricity powered devices in a private residence/number of residences.

Besides above pre-defined terms I have defined few of my own:

- activation or use frequency profile or (AFP): frequency of use of certain appliance per given unit time
- appliance level load (ALL) - the electricity that the electricity-powered devices in the household consume in unit time.

0.4 Related work

Work relating to load profiling can be found in two research verticals or topics. First one is load profiling and load profile models, that in most cases study the load profile curve of the building. There are few exceptions that study load profiles on appliance-level. Second vertical is anomaly detection in building energy consumption data. While first topic is closer, there are quite few connections with the latter. If one wants to do anomaly detection, in some cases, one must first build some kind of "normal consumption profile"

0.4.1 Load profiling

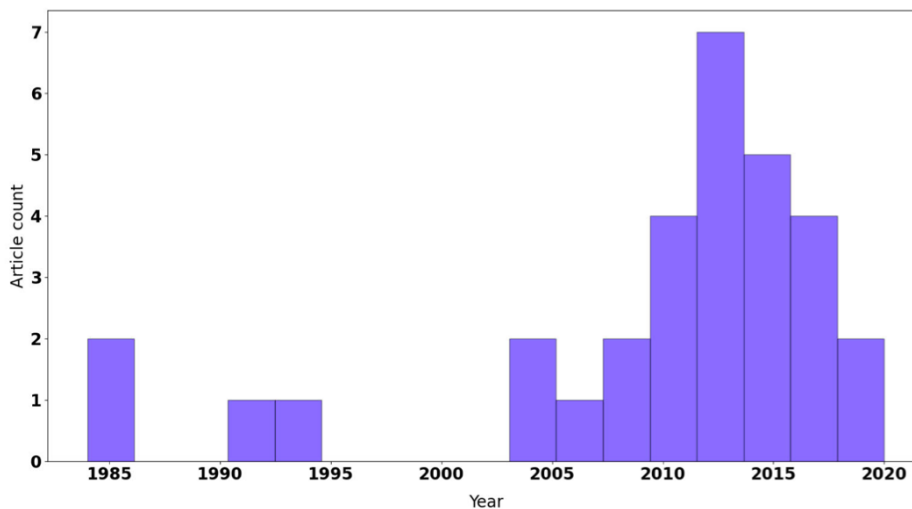
Load profiling has been researched since 1980. Load-profiling can be performed in two ways. Bottom-up and top-down.

With Bottom-up approach as Swan and Ugursal, 2009 state "calculates the individual dwelling energy or electricity consumption and extrapolate these results

over a target area or region" Whereas with Top-down approach as Swan and Ugursal, 2009 state "uses the total energy or electricity consumption estimates to assign them to the characteristics of the building stock" In other words, Bottom-up sub-meter data, Top-down uses aggregated data. In our case we take a deeper dive into bottom-up approach, since it is more relatable.

Proedrou, 2021 did a comprehensive review on load profiling. Author defined various load-profile application subgroups such as demand side management, planning and control design of energy systems and residential load profiles. She also grouped modeling technique as probabilistic models, Markov chains and Monte Carlo. Author first disclosed current state of load progress and issues with past work. They made a review of existing load profile models, and asses the-state-of-the art. Review was structured by different methods. Next, they pointed out at future research directions and applications of load profile models. Finally, author exposes changes that researchers face and addresses possible solutions with conclusions.

FIGURE 1: "Distribution of publications on load profiling from 1985 to 2020. The graph was published by Proedrou, 2021"



Early years

One of the first publications on load profiling were published by Train, Herriges, and Windle, 1985. They used bottom-up approach using sub-meter data and other socioeconomic and demographic characteristics to create a load profile or statistically adjusted engineering (SAE) as they call it. They are able to adjust the curve based on weather, dwelling size and income. In same year Walker and Pokoski, 1985 published paper where they used bottom-up approach with psychological factors to create probability models of when will individual use an appliance.

Since then there were two more in 1995. Research picked up the pace in 2005 with 7 publications in 2013 as figure 1 shows.

0.4.2 Main load profiles

Gerbec et al., 2005 tried to assign typical load profiles to a particular group of consumers based on their activity. To achieve that, they used probabilistic neural networks as a way of classification. Their methodology was tested in real use scenario.

Gao, Liu, and Zhu, 2018 makes use of bottom-up method to build a forecasting framework for household load profile considering consumption behavior of residents. Model falls into demand side management subgroup. They developed a "similar day extraction model", that is formulated to select similar days by comparing external environmental factors and household internal influence factors on energy consumption in order to enhance prediction accuracy of residents consumption behavior. This method falls into probabilistic method subgroup. Results show that their method successfully modeled daily usage.

Chuan, Rao, and Ukil, 2014 uses load profiling in order to optimize energy consumption distribution during the day. This reduces peaks usage and alleviates load off the grid. Author used bottom-up method, that is, using sum-meter data. Using this data, he made daily usage analysis on one hour basis. Using this information he optimized daily activation of appliances so that peaks usage were not as high. Results show that peak shedding was successful.

Csoknyai et al., 2019 analyze energy consumption habits, trends and intervention strategies in residential buildings. This is mainly done through the serious game approach, with a combination of direct consumer feedback through smart metering. Application or serious game as they call also offers advices, comparisons, savings, reductions goals and monitoring. They measure almost all dimensions of electricity usage as well as heating. Their results show that their serious game was not able to induce energy saving behavior.

Jeong et al., 2021 used extreme points in appliance usage curve. Usually, the first usage peak is in morning, and the second one in the evening. Besides that, they used demographic characteristics that are: region, area, age, salary, etc. Using collected data to find usage profile clusters. They had discovered 6 different usage profiles, where every cluster had a physical meaning such as energy saving, morning heavy, evening heavy, etc.

Another clustering methodology was proposed by Park and Son, 2019, using load image profiles and image processing. They represented time series data as image. Image is a grid of squares where y-axis contains monthly data with resolution of one day, x-axis contains daily data with resolution of one hour. Grid if color filled with algorithm that authors developed, where red means more activity and blue less. Using digital image filters they transform type-1 image to type-2 and from there used a threshold to obtain type-3. Using that information they clustered data based on image similarly. They used three different clustering methods: k-means, FCM and EM algorithm. Using Davies-Bouldin index, they were able to prove that image based clustering performs better than non-image.

Abreu, Câmara Pereira, and Ferrão, 2012 clustered different load profiles using electricity consumption data and surveys. They profiled residential homes. They used PCA for k-means resulting 5 clusters. Similar to other load profiling papers.

Whereas most of above-mentioned papers focused on aggregated consumption of building to build a load profile, authors Issi and Kaplan, 2018 focused on appliance-level load profiling. Their main contribution is to create a realistic per appliance load profile. They developed wireless measurement system with smart-plugs that enabled them to obtain power signatures for each appliance. They evaluated the data and based on observations they determined working cycles for each appliance.

Maybe more usefull at use case Moreno Jaramillo et al., 2021 present the first systematic review of load modeling and identification technique applied to distributed energy resources on distribution networks.

0.4.3 Anomaly detection in building energy consumption data

Review on Anomaly detection in building energy consumption data was written by Himeur et al., 2021. Here, authors took a deep dive into detecting anomalies in energy consumption in buildings. Author first makes an overview of existing anomaly detection schemes and applications. Second they perform a critical analysis and an in-depth discussion of the state-of-the-art. Next, they describe current trends such as NILM anomaly detection, and finally they derive a set of future research directions.

Both reviews pointed out that NILM anomaly detection or NILM load profiling is a possible future research direction. Only one paper was published on NILM anomaly detection Rashid et al., 2019b. Here, authors propose an algorithm that functions on top of existing state-of-the-art NILM algorithms Hidden Markov model, combinatorial optimization, Latent Bayesian Modeling and Graph-based Signal Processing. They focus on three appliances, fridge, freezer and heater. Their metric was a Number of cycles taken by appliance and energy used in those cycles. They implemented sigma variables to represent standard deviation and used rule based anomaly detection. So if energy or counts are significantly larger than mean then day is considered anomalous. Their rule had only one manual setting and that was a number of standard deviations before sample was considered anomalous. Their results show that sub meter anomaly detection works decently whereas NILM based anomaly does not work at all. Rashid et al., 2019a published another paper in the same year, where they took similar approach, except that they used only compressor based appliances such as fridge and air conditioner. They also added additional rule to their anomaly detection algorithm, but results still showed that NILM algorithms are not there yet.

Another anomaly detection paper was by Azizi, Beheshti, and Bolouki, 2021... insert descriptions

Castangia et al., 2021 used disaggregated sub meter data to detect anomalies in use consumption. They used private dataset of 20 homes from northern Italy with no synthetic anomalies. Dataset included data from 2018 to 2020 meaning it included covid induced anomalies. Authors first pre-processed the data by aggregating input load into Hourly energy consumption, second derived additional features, which are Time of use and duration of the activation. They use that data to detect single-point deviations for which they implemented Isolation Forest algorithm and anomalous trends for which to detect, they implemented Change Point Detection.

0.4.4 Possible use cases

Load profiling method has a lot of different use cases across different fields.

Energy saving

As mentioned before many applications for load profiling could be used in order to reduce energy use and increase energy efficiency. With emerging EV-market and ever-increasing installation of heat pumps, more and more energy is being used in form of electricity. Meaning, most of the current power grids would have to be upgraded in order to keep up with demand.

On the other side more and more photovoltaic systems are being installed which is slowly shifting energy production towards end-users. Slowly energy grid is starting to shift towards so-called distributed energy resources or "DER" Moreno Jaramillo et al., 2021. DERs includes all kinds of micro-energy sources such as PV, wind-power,

water power and all kinds of energy accumulators that can store and release energy when needed such as heat pumps with hot water storage, home batteries and EVs that can be used as a battery.

These appliances above, with smart management could be used in a way that would reduce net flow off energy and alleviate the load on power grid. A way to achieve this is via load profiling and load modeling. In order to manage the appliances, a control system would have to be put in place. It would be enough to control the devices that using the most of the energy.

An actual use case would be EV owner with installed PV system and heat pump, who works from home on occasions. In this case two profiles would be developed. Normal work day and work from home day. Additional information would be obtained from users calendar. On normal work day, system would use PV energy to heat up the water and store it, based on user profile. On work from home day, system would start charging the car with the morning sun, using only the PV energy. In the evening hours, when consumption rises and production falls, EV could inject the power back to the house, again using appliance load profiles to mitigate net energy flow as close to zero as possible. With ever-increasing power capacity and increasing range of EVs, more and more of battery capacity could be used for mitigation. In case of grid batteries, similar steps could be taken.

One other way to use user load profiles it to optimally distribute load by studying users usage patterns as Chuan, Rao, and Ukil, 2014 proposed in his paper. This could be further extended to neighborhood connected into p2p energy distribution network. As mentioned earlier, way to save energy consumption is to distribute it as locally as possible. Knowing usage patterns of all peers, system could optimally distribute the energy using DERs across all homes without dwellers even noticing.

Another use case could be using heat pump and heat storage, where besides users use profile system would also obtain weather forecast from the internet. Heat pumps that extract heat from air are more efficient when temperature differences are smaller. Heat pump could store energy when warm and release the energy when cold. Based on user usage profile, energy could be optimal distributed.

Many papers have been published, where authors explored ways to reduce energy consumption of users by studying their user load profiles. Energy saving is done through instant feedback, reduction goals, rewards and by comparing their use profile to the average user.

Grid management

Increasing percentage of PV systems is causing troubles to energy distributors, due to increased energy flow. In prior chapter it was mentioned how energy saving measures would benefit users and their peers. One other use case would be cooperation between end-user and energy distribution company. Joint actions between them would benefit both.

If electricity provider could control the use of main appliances so that load on power grid is as uniform as possible, with as little peaks as possible. For this to function, user would have to allow the installation of energy meters and controllers on appliances that use most electricity and their use can be allocated, fridge cannot be allocated, whereas heat pump can be. This would introduce a statistical multiplex, similar to what is done with internet traffic, alleviating load off the grid.

Benefit of user would be lower cost of charging and heating the building. This is already done through so-called small and high tariffs. More detailed user load profiles would enable electricity provider to introduce real-time tariffs.

User would have three options. First one would be that user can use the appliances as freely as one desires, this would result a normal tariff. Second option would be to use the appliances as regularly as possible, this would lead to lower tariffs. Third option would be to leave the management of main electricity consumption appliances to electricity provider. Provider would combine the user appliance load-profile and real time market price of energy to optimize the cost. This would lead to free or even negative price of electricity, since distribution companies have to keep the frequency of the grid as stable as possible.

In order for them to stabilize the frequency, they sometimes have to resort to load shedding. Load shedding is a process where a load is disconnected from the grid in order to keep the grid in sync. Commonly whole neighborhoods are being disconnected, affecting their daily lives. Using user load profiles distribution companies could disconnect the load in a way that would minimally affect end-user. When they would need load the grid due to low of a demand, they could charge EVs for free of charge or even pay to do so. This benefits the company as well, since they do not need to lower energy production, which can be expensive.

Elderly care

Demographic changes i.e. aging population is an increasing socioeconomic issue. Elderly are facing many issues when staying at home alone for extended periods of time. Accidents such as falls or in-ability to do chores due to health related issues or even dementia induced issues such as leaving appliances on for long periods of time could all be detected using user load profiling.

To detect falls or other issues a normal daily appliance use profile would be developed. It would involve routine behavior of users such as turning on coffee machine, turning on stove, oven and kitchen vent in the noon or using kettle and toaster in the evening. All these routines could be measured and tracked. Using this data, a profile would be developed. Probability of an anomaly and a threshold would enable system to detect an issue.

Example would be: coffee machine not turning on in the morning or stove and kitchen vent not being used at the noon. Another issue could be detected if appliance would be used more frequently or for extended periods of time. This could indicate that user forgot to turn off stove, oven or even a light. Same system could detect that fridge or freezer was left open since duty cycles would be longer and more frequent. As soon as issue would be detected it would notify caregiver to check on caretaker. (find source)

Anomaly detection

One use case of anomaly detection was already mentioned in prior chapter. One more thing that could be detected, using load profiling, would be altered operation of appliances. In case of fridge, system would detect that duty cycles are too long. Increased duty cycle can be caused by cooling liquid leakage, fridge being open or compressor motor malfunction. Heat pumps work on same basis as fridges, meaning same anomalies could be detected. Malfunction could also be detected in heating element appliances such as toaster or boiler. Since mentioned appliances are one of the largest consumers in a household, early enough detection could lead to large energy saving benefits. (source)

Other

Load profiling could also be used as feedback to the manufacturer, of how a certain device is being used and if it is being used as designed. This would enable the manufacturers to improve their products according to users needs, without unnecessary features.

One other use case could be occupancy detection of buildings. Information about occupancy could be used as part of elderly care monitoring or in case of building automation, to run certain tasks when user enters or leaves the room or a building.

0.5 Structure

- - Abstract?
- - Introduction
-
- - Define load profiling
- - Anomaly detection (how it fits in) maybe?
- - Related work
- - Define contributions and goals
-
- - Present "Demo"
- - Methodology
- - Datasets (used)
- - Load classification
- - Mention my work on images?
- - Machine learning
- - Load profiling method
- - Results
-
- - Use cases
- - Privacy
- - Concerns
- - Sharing and transparency
- - Solutions
- - Datasets
- - Issues

- - Load profiling
- - Papers not sharing their datasets
- - Solutions
-
- - Future research directions
- - Map of current work
- - Where does NILM load profiling lay on the Map
-
- - Discussion
- - Conclusions

Bibliography

- Abreu, Joana M., Francisco Câmara Pereira, and Paulo Ferrão (2012). "Using pattern recognition to identify habitual behavior in residential electricity consumption". In: *Energy and Buildings* 49, pp. 479–487. ISSN: 0378-7788. DOI: <https://doi.org/10.1016/j.enbuild.2012.02.044>. URL: <https://www.sciencedirect.com/science/article/pii/S0378778812001363>.
- Azizi, Elnaz, Mohammad T. H. Beheshti, and Sadegh Bolouki (2021). "Appliance-Level Anomaly Detection in Nonintrusive Load Monitoring via Power Consumption-Based Feature Analysis". In: *IEEE Transactions on Consumer Electronics* 67.4, pp. 363–371. ISSN: 1558-4127. DOI: [10.1109/TCE.2021.3129356](https://doi.org/10.1109/TCE.2021.3129356).
- Castangia, Marco et al. (2021). "Detection of Anomalies in Household Appliances from Disaggregated Load Consumption". In: *2021 International Conference on Smart Energy Systems and Technologies (SEST)*, pp. 1–6. DOI: [10.1109/SEST50973.2021.9543232](https://doi.org/10.1109/SEST50973.2021.9543232).
- Chuan, Luo, D. M. K. K. Venkateswara Rao, and Abhisek Ukil (2014). "Load profiling of Singapore buildings for peak shaving". In: *2014 IEEE PES Asia-Pacific Power and Energy Engineering Conference (APPEEC)*, pp. 1–6. DOI: [10.1109/APPEEC.2014.7065998](https://doi.org/10.1109/APPEEC.2014.7065998).
- Csoknyai, Tamás et al. (2019). "Analysis of energy consumption profiles in residential buildings and impact assessment of a serious game on occupants' behavior". In: *Energy and Buildings* 196, pp. 1–20. ISSN: 0378-7788. DOI: <https://doi.org/10.1016/j.enbuild.2019.05.009>. URL: <https://www.sciencedirect.com/science/article/pii/S0378778818334790>.
- Eurostat (2022). "Gross and net production of electricity and derived heat by type of plant and operator". In: 62. URL: https://ec.europa.eu/eurostat/databrowser/view/nrg_ind_peh/default/table?lang=en.
- Gao, Bingtuan, Xiaofeng Liu, and Zhenyu Zhu (2018). "A Bottom-Up Model for Household Load Profile Based on the Consumption Behavior of Residents". In: *Energies* 11.8. ISSN: 1996-1073. DOI: [10.3390/en11082112](https://doi.org/10.3390/en11082112). URL: <https://www.mdpi.com/1996-1073/11/8/2112>.
- Gerbec, D. et al. (2005). "Allocation of the load profiles to consumers using probabilistic neural networks". In: *IEEE Transactions on Power Systems* 20.2, pp. 548–555. ISSN: 1558-0679. DOI: [10.1109/TPWRS.2005.846236](https://doi.org/10.1109/TPWRS.2005.846236).
- Himeur, Yassine et al. (2021). "Artificial intelligence based anomaly detection of energy consumption in buildings: A review, current trends and new perspectives". In: *Applied Energy* 287, p. 116601. ISSN: 0306-2619. DOI: <https://doi.org/10.1016/j.apenergy.2021.116601>. URL: <https://www.sciencedirect.com/science/article/pii/S0306261921001409>.
- Issi, Fatih and Orhan Kaplan (2018). "The Determination of Load Profiles and Power Consumptions of Home Appliances". In: *Energies* 11.3. ISSN: 1996-1073. DOI: [10.3390/en11030607](https://doi.org/10.3390/en11030607). URL: <https://www.mdpi.com/1996-1073/11/3/607>.
- Jeong, Hyun Cheol et al. (2021). "Clustering of Load Profiles of Residential Customers Using Extreme Points and Demographic Characteristics". In: *Electronics*

- 10.3. ISSN: 2079-9292. DOI: [10.3390/electronics10030290](https://doi.org/10.3390/electronics10030290). URL: <https://www.mdpi.com/2079-9292/10/3/290>.
- Kavousian, Amir, Ram Rajagopal, and Martin Fischer (2013). "Determinants of residential electricity consumption: Using smart meter data to examine the effect of climate, building characteristics, appliance stock, and occupants' behavior". In: *Energy* 55, pp. 184–194. ISSN: 0360-5442. DOI: <https://doi.org/10.1016/j.energy.2013.03.086>. URL: <https://www.sciencedirect.com/science/article/pii/S0360544213002831>.
- Moreno Jaramillo, Andres F. et al. (2021). "Load modelling and non-intrusive load monitoring to integrate distributed energy resources in low and medium voltage networks". In: *Renewable Energy* 179, pp. 445–466. ISSN: 0960-1481. DOI: <https://doi.org/10.1016/j.renene.2021.07.056>. URL: <https://www.sciencedirect.com/science/article/pii/S0960148121010612>.
- Park, Keon-Jun and Sung-Yong Son (2019). "A Novel Load Image Profile-Based Electricity Load Clustering Methodology". In: *IEEE Access* 7, pp. 59048–59058. ISSN: 2169-3536. DOI: [10.1109/ACCESS.2019.2914216](https://doi.org/10.1109/ACCESS.2019.2914216).
- Proedrou, Elisavet (2021). "A Comprehensive Review of Residential Electricity Load Profile Models". In: *IEEE Access* 9, pp. 12114–12133. ISSN: 2169-3536. DOI: [10.1109/ACCESS.2021.3050074](https://doi.org/10.1109/ACCESS.2021.3050074).
- Rashid, Haroon et al. (2019a). "Can non-intrusive load monitoring be used for identifying an appliances anomalous behaviour?" In: *Applied Energy* 238, pp. 796–805. ISSN: 0306-2619. DOI: <https://doi.org/10.1016/j.apenergy.2019.01.061>. URL: <https://www.sciencedirect.com/science/article/pii/S0306261919300613>.
- Rashid, Haroon et al. (2019b). "Evaluation of Non-intrusive Load Monitoring Algorithms for Appliance-level Anomaly Detection". In: *ICASSP 2019 - 2019 IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)*, pp. 8325–8329. DOI: [10.1109/ICASSP.2019.8683792](https://doi.org/10.1109/ICASSP.2019.8683792).
- Swan, Lukas G. and V. Ismet Ugursal (2009). "Modeling of end-use energy consumption in the residential sector: A review of modeling techniques". In: *Renewable and Sustainable Energy Reviews* 13.8, pp. 1819–1835. ISSN: 1364-0321. DOI: <https://doi.org/10.1016/j.rser.2008.09.033>. URL: <https://www.sciencedirect.com/science/article/pii/S1364032108001949>.
- Train, Kenneth, Joseph Herriges, and Robert Windle (1985). "Statistically adjusted engineering (SAE) models of end-use load curves". In: *Energy* 10.10, pp. 1103–1111. ISSN: 0360-5442. DOI: [https://doi.org/10.1016/0360-5442\(85\)90025-8](https://doi.org/10.1016/0360-5442(85)90025-8). URL: <https://www.sciencedirect.com/science/article/pii/0360544285900258>.
- Walker, C.F. and J.L. Pokoski (1985). "Residential Load Shape Modelling Based on Customer Behavior". In: *IEEE Transactions on Power Apparatus and Systems* PAS-104.7, pp. 1703–1711. DOI: [10.1109/TPAS.1985.319202](https://doi.org/10.1109/TPAS.1985.319202).