

Prep Course

Module 2

Numpy Broadcasting

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Broadcasting Rules: *compatible or not?!*

Given two input arrays A and B to a numpy operation or function that performs broadcasting:


- Moving backwards from the last dimension of each array, we check if their dimensions are compatible.
- Dimensions are compatible if they are equal or either of them is one.
- If all of A 's dimensions are compatible with B 's dimensions, or vice versa, they are compatible arrays.
- The size of the output array is the size that is not 1 along each dimension of the inputs.

Example 1:


Step 1: Compatible?
Yes

$$\begin{array}{l}
 \text{A: } (3, 4) \\
 \text{B: } (3, 1)
 \end{array}
 \quad
 \begin{array}{c}
 \text{A} \\
 \begin{bmatrix} 4 & 7 & 6 & 5 \\ 9 & 2 & 8 & 7 \\ 9 & 1 & 6 & 1 \end{bmatrix}
 \end{array}
 +
 \begin{array}{c}
 \text{B} \\
 \begin{bmatrix} 7 \\ 3 \\ 1 \end{bmatrix}
 \end{array}$$


Step 2: Match last
dimension

$$\begin{array}{l}
 \text{A: } (3, 4) \\
 \text{B: } (3, 4)
 \end{array}
 \quad
 \begin{array}{c}
 \text{A} \\
 \begin{bmatrix} 4 & 7 & 6 & 5 \\ 9 & 2 & 8 & 7 \\ 9 & 1 & 6 & 1 \end{bmatrix}
 \end{array}
 +
 \begin{array}{c}
 \text{B} \\
 \begin{bmatrix} 7 & 7 & 7 & 7 \\ 3 & 3 & 3 & 3 \\ 1 & 1 & 1 & 1 \end{bmatrix}
 \end{array}$$


Step 3: Match 2nd last
dimension

$$\begin{array}{l}
 \text{A: } (3, 4) \\
 \text{B: } (3, 4)
 \end{array}
 \quad
 \begin{array}{c}
 \text{A} \\
 \begin{bmatrix} 4 & 7 & 6 & 5 \\ 9 & 2 & 8 & 7 \\ 9 & 1 & 6 & 1 \end{bmatrix}
 \end{array}
 +
 \begin{array}{c}
 \text{B} \\
 \begin{bmatrix} 7 & 7 & 7 & 7 \\ 3 & 3 & 3 & 3 \\ 1 & 1 & 1 & 1 \end{bmatrix}
 \end{array}
 =
 \begin{array}{c}
 \begin{bmatrix} 11 & 14 & 13 & 12 \\ 12 & 5 & 11 & 10 \\ 10 & 2 & 7 & 2 \end{bmatrix}
 \end{array}$$


Example 2:

Step 1: Compatible?
No

| | | | |
|-----------|--|---|--|
| | A | | B |
| A: (4, 4) | $\begin{bmatrix} 3 & 9 & 3 & 2 \\ 8 & 6 & 3 & 5 \\ 7 & 1 & 9 & 7 \\ 6 & 4 & 2 & 2 \end{bmatrix}$ | + | $\begin{bmatrix} 7 \\ 2 \end{bmatrix}$ |
| B: (2, 1) | | | |

Step 2: Even if we can match the last dimension, there is no rule to match the 2nd last dimensions as those dimensions are not equal and both are not one. Thus, a Value Error is thrown out.

| | | | | |
|-----------|--|---|--|---|
| | A | | B | |
| A: (4, 4) | $\begin{bmatrix} 3 & 9 & 3 & 2 \\ 8 & 6 & 3 & 5 \\ 7 & 1 & 9 & 7 \\ 6 & 4 & 2 & 2 \end{bmatrix}$ | + | $\begin{bmatrix} 7 & 7 & 7 & 7 \\ 2 & 2 & 2 & 2 \end{bmatrix}$ | ValueError: operands could not be broadcast together with shapes (4,4) (2,1) |
| B: (2, 4) | | | | |

↑

Example 3:

```

1 x = np.arange(4)
2 print(x)
3 print()
4
5 y = np.ones(5)
6 print(y)
7 print()
8
9 print(x.shape)
10 print(y.shape)
11 print()
12
13 print(x + y)

```

```
[0 1 2 3]
```

```
[1. 1. 1. 1. 1.]
```

```
(4,)
```

```
(5,)
```

Step 1: Compatible?
No

Step 2:, a Value Error
is thrown out.

```

-----
-----
ValueError                                Traceback
(most recent call last)
<ipython-input-14-c4bc8c28d366> in <module>
      11 print()
      12
----> 13 print(x + y)

ValueError: operands could not be broadcast together
with shapes (4,) (5,)

```

Example 4:

```

1 x = np.arange(4)
2 X = x.reshape(4, 1)
3 print(X)
4 print()
5
6 y = np.ones(5)
7 print(y)
8 print()
9
10 print(X.shape)
11 print(f' ( , {y.shape[0]}) ')
12 print()
13
14 print(X + y)

```

```

[[0]
 [1]
 [2]
 [3]]

```

```
[1. 1. 1. 1. 1.]
```

```

(4, 1)
( , 5)

```

```

[[1. 1. 1. 1. 1.]
 [2. 2. 2. 2. 2.]
 [3. 3. 3. 3. 3.]
 [4. 4. 4. 4. 4.]]

```

Step 1: Compatible?
Yes.

Step 2: Match both
dimensions.