

## 1 Math

$$Ae^{i\theta} = A\cos(\theta) + iA\sin(\theta)$$

$$Ae^{-i\theta} = A\cos(\theta) - iA\sin(\theta)$$

$$\int \frac{1}{(R^2+x^2)^{3/2}} = \frac{x}{R^2(R^2+x^2)^{1/2}}$$

## 2 Constants

$$\text{Electron/Proton Charge} = -1.6\text{E-}19 \text{ [C]}$$

$$\text{Electron Mass} = 9.11\text{E-}31 \text{ [kg]}$$

$$\text{Proton/Neutron Mass} = 1.67\text{E-}27 \text{ [kg]}$$

$$\epsilon_o = 8.85 \text{ E-}12 \text{ [C}^2/\text{N} \cdot \text{m}^2\text{]}$$

$$k = 9\text{E}9 = 1/4\pi\epsilon_o \text{ [N} \cdot \text{m}^2/\text{C}^2\text{]}$$

$$\mu_o = 4\pi\text{E-}7 \text{ [T} \cdot \text{m/A]}$$

$$c = 3\text{E-}8 \text{ [m/s]}$$

## 3 Electricity

$$E = \frac{kq}{r^2} \text{ [N/C]}$$

$$F = \frac{k|q_1q_2|}{r^2} \text{ [N]}$$

$$V = \frac{kq}{r} \text{ [V]}$$

$$W = -Vq \text{ [V} \cdot \text{C]}$$

## 4 Resistors

Use power

$$\rho = \frac{E}{J} = \frac{RA}{L} \text{ [\Omega} \cdot \text{m}] \text{ Resistivity}$$

## 5 Capacitors

Store charge

$$C = \kappa\epsilon_o A/d \text{ Parallel Plates}$$

$$Q = VC \text{ Charge}$$

$$U_E = QV/C \text{ Potential Energy Stored}$$

## 6 Inductors

Slow changes in current

$M_{21} = N_2 \Phi_{B2} / I_1 = N_1 \Phi_{B1} / I_2$  Mutual Inductance, proportionality of EMF in coil 2 to change in current in coil 1

$M = \mu_o A N_1 N_2 / l$  Mutual Inductance

$\varepsilon_2 = -M \frac{\partial i_1}{\partial t}$  EMF from Mutual Inductance

$L = N \Phi_B / I$  Self Inductance

$V = -L \frac{\partial i}{\partial t}$  Voltage in inductor

$U_B = \frac{LI^2}{2C}$  Potential Energy Stored

## 7 Magnetism

$F = qv \times B$  [N] Force on charge

$F = Il \times B$  [N] Force on conductor

$\frac{F}{l} = \frac{\mu_o I_1 I_2}{2\pi d}$  [F/m] Force between parallel conductors

$\vec{B} = \frac{\mu_o qv \times \hat{r}}{4\pi r^2}$  [T]

$\partial \vec{B} = \frac{\mu_o I \partial \vec{l} \times \hat{r}}{4\pi r^2}$  [ $\partial$ T]

$r = \frac{mv}{qB}$  [m] Circling Charge

$\tau = NBIAsin(\theta)$  [N·m] Spinning Rectangular Loop

$B = \frac{\mu_o I}{2\pi d}$  [T] Infinitely Long Wire

$B = \mu_o nI$  [T] Inside Solenoid,  $n=N/l$

$B = \frac{\mu_o I a^2}{2(x^2 + a^2)^{3/2}}$  [T] Axis of Circular Loop

$\mu = NIA$  [ $A \cdot m^2$ ], [N·m/T] Magnetic Moment

$\Phi_B = BAsin(\theta)$  [ $T \cdot m^2$ ] Flux in constant field

$\Phi_B = \iint B \cdot dA$  [ $T \cdot m^2$ ] Flux in varying field

$\varepsilon = -N \frac{\partial \Phi_E}{\partial t}$  [V] Induced EMF

$\varepsilon = Blv$  [V] Motional EMF

## 8 Maxwell's Equations

$\oiint_S J dA = \frac{q_{enclosed}}{\varepsilon_o}$  Gauss's Law for Electricity

$\oiint_S B dA = 0$  Gauss's Law for Magnetism

$\oint E dl = \frac{\partial \Phi_B}{\partial t}$  Faraday's Law

$$\oint B \, dl = \mu_o(I_{enclosed} + \epsilon_o \frac{-\partial \Phi_E}{\partial t}) \text{ Ampere's Law Modified}$$

## 9 Transformers

Step up transformer increases output voltage

$V_2/V_1 = N_2/N_1$  Voltage proportional to loops

$V_1 I_1 = V_2 I_2$  Power is conserved

## 10 Circuits

$$I_{RMS} = \frac{I_{max}}{\sqrt{2}}$$

$$I_{RAV} = \frac{2}{\pi} I_{max}$$

Time Constant

$$\tau = RC \text{ RC Circuit}$$

$$\tau = L/R \text{ LR Circuit}$$

$$I = I_o e^{\frac{-t}{\tau}} \text{ Discharging}$$

$$I = I_o(1 - e^{\frac{-t}{\tau}}) \text{ Charging}$$

## 11 Series Circuits

$R_{eff}, L_{eff}$  are the sum of their sub-components

$C_{eff}, Q_{eff}$  are the inverse of the sum of inversed sub-components

$$V_s^2 = V_R^2 + (V_L - V_C)^2$$

$$I_s = I_R = I_L = I_C$$

$$Z^2 = R^2 + (X_L - X_C)^2$$

$$\cos(\theta) = R/Z$$

## 12 Parallel Circuits

$Q_{eff}, C_{eff}$  are the sum of their sub-components

$R_{eff}, L_{eff}$  are the inverse of the sum of inversed sub-components

$$I_s^2 = I_R^2 + (I_L - I_C)^2$$

$$V_s = V_R = V_L = V_C$$

$$\frac{1}{Z} = \sqrt{\left(\frac{1}{R}\right)^2 + \left(\frac{1}{X_L} - \frac{1}{X_C}\right)^2}$$

$$Y = \frac{1}{Z} \text{ Admittance}$$

$$\cos(\theta) = Z/R$$

### 13 Both Circuits

Leading means current is ahead of voltage in phase diagram

$$\omega = \frac{1}{\sqrt{LC}} \text{ Resonance Frequency}$$

$$X_L = \omega L \text{ Inductor Reactance}$$

$$X_C = \frac{1}{\omega C} \text{ Capacitor Reactance}$$

$$P = \frac{1}{2} V_{max} I_{max} \cos(\theta) \text{ Power}$$

### 14 With Damping

$$\omega' = \sqrt{\omega^2 - (R/2L)^2}$$