

1 Math

$$e^{i\theta} = \cos(\theta) + i\sin(\theta) \text{ Euler's Law}$$

$$\int \frac{1}{(R^2+x^2)^{3/2}} = \frac{x}{R^2(R^2+x^2)^{1/2}} \text{ A Common Integral}$$

2 Constants

$$\text{Electron/Proton Charge} = -1.6\text{E-}19 \text{ [C]}$$

$$\text{Electron Mass} = 9.11\text{E-}31 \text{ [kg]}$$

$$\text{Proton/Neutron Mass} = 1.67\text{E-}27 \text{ [kg]}$$

$$\varepsilon_o = 8.85 \text{ E-}12 \text{ [C}^2/\text{N} \cdot \text{m}^2]$$

$$k = 9\text{E}9 = 1/4\pi\varepsilon_o \text{ [N} \cdot \text{m}^2/\text{C}^2]$$

$$\mu_o = 4\pi\text{E-}7 \text{ [T} \cdot \text{m/A]}$$

$$c = 3\text{E-}8 \text{ [m/s]}$$

3 Electricity

$$E = \frac{kq}{r^2} \text{ [N/C]}$$

$$F = \frac{k|q_1q_2|}{r^2} \text{ [N]}$$

$$V = \frac{kq}{r} \text{ [V]}$$

$$W = -Vq \text{ [V} \cdot \text{C]}$$

4 Resistors

Use power

$$\rho = \frac{E}{J} = \frac{RA}{L} \text{ [\Omega} \cdot \text{m}] \text{ Resistivity}$$

5 Capacitors

Store charge

$$C = \kappa\varepsilon_o A/d \text{ Parallel Plates}$$

$$Q = VC \text{ Charge}$$

$$U_E = QV/C \text{ Potential Energy Stored}$$

6 Inductors

Slow changes in current

$M_{21} = N_2 \Phi_{B2} / I_1 = N_1 \Phi_{B1} / I_2$ Mutual Inductance, proportionality of EMF in coil 2 to change in current in coil 1

$M = \mu_o A N_1 N_2 / l$ Mutual Inductance

$\varepsilon_2 = -M \frac{\partial i_1}{\partial t}$ EMF from Mutual Inductance

$L = N \Phi_B / I$ Self Inductance

$V = -L \frac{\partial i}{\partial t}$ Voltage in inductor

$U_B = \frac{LI^2}{2C}$ Potential Energy Stored

7 Magnetism

$F = qv \times B$ [N] Force on charge

$F = Il \times B$ [N] Force on conductor

$\frac{F}{l} = \frac{\mu_o I_1 I_2}{2\pi d}$ [F/m] Force between parallel conductors

$\vec{B} = \frac{\mu_o qv \times \hat{r}}{4\pi r^2}$ [T]

$\partial \vec{B} = \frac{\mu_o I \partial \vec{l} \times \hat{r}}{4\pi r^2}$ [∂ T]

$r = \frac{mv}{qB}$ [m] Circling Charge

$\tau = NBI A \sin(\theta)$ [N·m] Spinning Rectangular Loop

$B = \frac{\mu_o I}{2\pi d}$ [T] Infinitely Long Wire

$B = \mu_o n I$ [T] Inside Solenoid, $n=N/l$

$B = \frac{\mu_o I a^2}{2(x^2+a^2)^{3/2}}$ [T] Axis of Circular Loop

$\mu = NIA$ [$A \cdot m^2$], [N·m/T] Magnetic Moment

$\Phi_B = BA \sin(\theta)$ [$T \cdot m^2$] Flux in constant field

$\Phi_B = \iint B \cdot dA$ [$T \cdot m^2$] Flux in varying field

$\varepsilon = -N \frac{\partial \Phi_E}{\partial t}$ [V] Induced EMF

$\varepsilon = Blv$ [V] Motional EMF

8 Maxwell's Equations

$\oiint_S J dA = \frac{q_{enclosed}}{\varepsilon_o}$ Gauss's Law for Electricity

$\oiint_S B dA = 0$ Gauss's Law for Magnetism

$\oint E dl = \frac{\partial \Phi_B}{\partial t}$ Faraday's Law

$\oint B dl = \mu_o (I_{enclosed} + \epsilon_o \frac{\partial \Phi_E}{\partial t})$ Ampere's Law Modified

9 Transformers

Step up transformer increases output voltage

$V_2/V_1 = N_2/N_1$ Voltage proportional to loops

$V_1 I_1 = V_2 I_2$ Power is conserved

10 Circuits

$$I_{RMS} = \frac{I_{max}}{\sqrt{2}}$$

$$I_{RAV} = \frac{2}{\pi} I_{max}$$

Time Constant

$$\tau = RC \text{ RC Circuit}$$

$$\tau = L/R \text{ LR Circuit}$$

$$I = I_o e^{\frac{-t}{\tau}} \text{ Discharging}$$

$$I = I_o (1 - e^{\frac{-t}{\tau}}) \text{ Charging}$$

11 Series Circuits

R_{eff}, L_{eff} are the sum of their sub-components

C_{eff}, Q_{eff} are the inverse of the sum of inversed sub-components

Resonance when voltage to resistor is max and capacitor/inductor impedance is zero

$$V_s^2 = V_R^2 + (V_L - V_C)^2$$

$$I_s = I_R = I_L = I_C$$

$$Z^2 = R^2 + (X_L - X_C)^2 \text{ Reactance Geometric Format}$$

$$\tilde{Z} = R + (X_L - X_C)i \text{ Reactance Complex Format}$$

$$\cos(\theta) = R/Z$$

12 Parallel Circuits

Q_{eff}, C_{eff} are the sum of their sub-components

R_{eff}, L_{eff} are the inverse of the sum of inversed sub-components

Resonance when current to resistor is max and capacitor/inductor impedance is infinite

$$I_s^2 = I_R^2 + (I_L - I_C)^2$$

$$V_s = V_R = V_L = V_C$$

$$\frac{1}{Z} = \sqrt{\left(\frac{1}{R}\right)^2 + \left(\frac{1}{X_L} - \frac{1}{X_C}\right)^2} \text{ Reactance Geometric Format}$$

$$\frac{1}{Z} = \frac{1}{R} + \left(\frac{1}{X_L} - \frac{1}{X_C}\right)i \text{ Reactance Complex Format}$$

$$Y = \frac{1}{Z} \text{ Admittance}$$

$$\cos(\theta) = Z/R$$

13 Both Circuits

Leading means current is ahead of voltage in phase diagram

$$\omega = \frac{1}{\sqrt{LC}} \text{ Resonance Frequency when Net Reactance is 0}$$

$$X_L = \omega L$$

$$\widetilde{Z}_L = iX_L \text{ Inductor Reactance}$$

$$X_C = \frac{1}{\omega C}$$

$$\widetilde{Z}_C = -iX_C \text{ Capacitor Reactance}$$

$$P = \frac{1}{2} V_{max} I_{max} \cos(\theta) \text{ Power}$$

14 With Damping

$$\omega' = \sqrt{\omega^2 - (R/2L)^2}$$