

**M C M C**

# Computer Intensive Statistics in Ecology

Department of Life Science

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**HW 14**

# M C M C

Estimate the posterior distributions of parameters using the method Markov chain Monte Carlo (MCMC).

$\sigma = 0.032$

Prior distributions

$L_{inf} \sim U[40, 100]$

$K \sim U[0.1, 0.6]$

# MCMC



1

**Data Input**



2

**Likelihood**



3

**MCMC**



4

**Results**





1

**Data Input**

```
# female Pacific Hake
```

```
Age = c(1,2,3.3,4.3,5.3,6.3,7.3,8.3,9.3,10.3,11.3,12.3,13.3)
```

```
Length = c(15.4,28.03,41.18,46.2,48.23,50.26,51.82,54.27,56.98,58.93,59,60.91,61.83)
```



2

**Likelihood**

## Template

### # population dynamics model

```
pop_model <- function(r,N0){  
  N = NULL  
  Dev2 = NULL  
  N[1] = N0  
  for(t in 2:33){  
    N[t] = N[t-1]*(1+r)  
    Dev2[t]=(log(obs_N[t]/N[t]))^2  
  }  
}
```

## HW 14

### # von Bertalanffy Growth Function

```
VBGF <-function(x, Linf, K){  
  y = Linf * (1 - exp(- K * (x - 0)))  
  return(y)  
}
```

$$L(t) = L_{\infty} \left( 1 - \exp(-K(t - t_0)) \right) e^{\varepsilon} \quad \varepsilon \sim N(0, \sigma^2)$$

```

Like_1 = 1/obs_N[9]*(1/sqrt(2*pi*sigma[9]*sigma[9]))*exp(-
Dev2[9]/(2*sigma[9]*sigma[9]))
Like_2 = 1/obs_N[16]*(1/sqrt(2*pi*sigma[16]
*sigma[16]))*exp(-Dev2[16]/(2*sigma[16]*sigma[16]))
Like_3 = 1/obs_N[26]*(1/sqrt(2*pi*sigma[26]
*sigma[26]))*exp(-Dev2[26]/(2*sigma[26]*sigma[26]))
neg_likelihood = -(log(Like_1)+log(Like_2)+log(Like_3))

```

```

if (is.na(neg_likelihood)) neg_likelihood = 100000

```

---

```

totoal_like = exp(-neg_likelihood)

```

```

Outs <- NULL
Outs$totoal_like <- totoal_like
Outs$neg_likelihood <- neg_likelihood
Outs$r <- r
Outs$N0 <- N0
Outs$N_lastyr <- N[33]

```

```

return(Outs)

```

```

}

```

Template

## lognormal\_like = function(Linf, K){

```

Like = numeric(length(Length))
neg_likelihood = numeric(length(Length))
ypred = VBGF(Age, Linf, K)
Dev2 =(log(Length) - log(ypred)) ^ 2
sigma = 0.032
for (i in 1:length(Length)){
  Like[i] = (1 / (Age[i] * sqrt(2 * pi) * sigma)) * exp(-Dev2[i] / (2 * sigma
^ 2))
  neg_likelihood[i] = -log(Like[i])
}

```

---

```

totoal_Like = exp(-sum(neg_likelihood))

```

```

Outs <- NULL
Outs$totoal_Like <- totoal_Like
Outs$neg_likelihood <- sum(neg_likelihood)
Outs$ypred <- ypred
Outs$Linf <- Linf
Outs$K <- K

```

```

return(Outs)

```

```

}

```

HW 14





3

**MCMC**

DoMCMC



Function

for

# simulation

# jump function

if

# evaluate the ratio

if

# thinning

if

# burn in

# DoMCMC ←

```
function(Xinit,Ndim,Nsim=1000,Nburn=0,Nthin=1)
```

```
{           # Step size
```

```
Linf_jump_max = 100
```

```
Linf_jump_min = -100
```

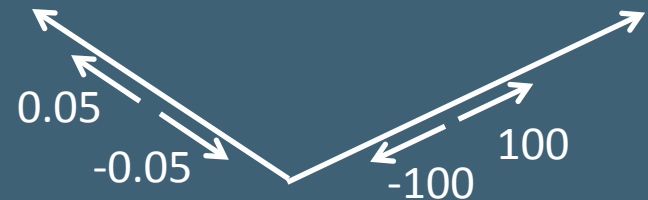
```
K_jump_max = 0.05
```

```
K_jump_min = -0.05
```

## MLE results

Linf = 61.09

K = 0.30



```
Xcurr <- Xinit
```

```
Fcurr <- -1* lognormal_like (r=Xcurr[1],N0=Xcurr[2])$neg_likelihood
```

```
Outs2 <- matrix(-9999,  
                nrow=(Nsim-Nburn),  
                ncol=(Ndim+1))
```

```
lpnt <- 0; lcnt <- 0
```

```
for (lsim in 1:Nsim)
```

```
{  # jump function
```

```
  Xnext = NULL
```

```
  Xnext[1] = Xcurr[1]  
             + runif(1, 0, 1) * (Linf_jump_max - Linf_jump_min)  
             + Linf_jump_min
```

```
  Xnext[2] = Xcurr[2]  
             + runif(1, 0, 1) * (K_jump_max - K_jump_min)  
             + K_jump_min
```

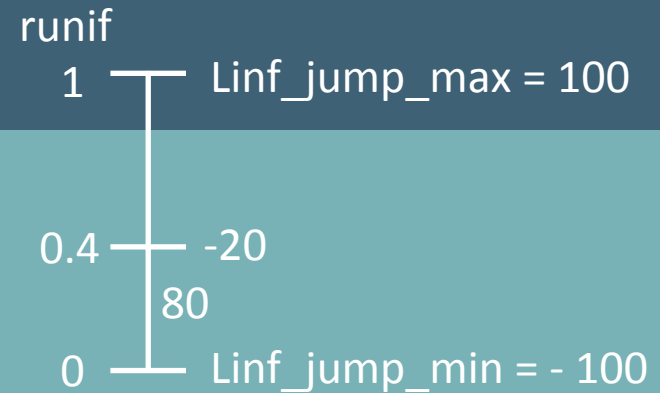
```
for (lsim in 1:Nsim)
```

```
{ # jump function
```

```
  Xnext = NULL
```

```
  Xnext[1] = Xcurr[1]  
            + runif(1, 0, 1) * (Linf_jump_max - Linf_jump_min)  
            + Linf_jump_min
```

```
  Xnext[2] = Xcurr[2]  
            + runif(1, 0, 1) * (K_jump_max - K_jump_min)  
            + K_jump_min
```



```
for (lsim in 1:Nsim)
```

```
{  # jump function
    Xnext = NULL

    # Linf prior:  $L_{inf} \sim U [40, 100]$ 
    Xnext[1] =      Xcurr[1]
               + runif(1, 0, 1) * (Linf_jump_max - Linf_jump_min)
               + Linf_jump_min

    # K prior:  $K \sim U [0.1, 0.6]$ 
    Xnext[2] =      Xcurr[2]
               + runif(1, 0, 1) * (K_jump_max - K_jump_min)
               + K_jump_min
```

# for (Isim in 1:Nsim)

```
{ # jump function
  Xnext = NULL

  repeat{ # Linf prior:  $Linf \sim U[40, 100]$ 
    Xnext[1] =      Xcurr[1]
              + runif(1, 0, 1) * (Linf_jump_max - Linf_jump_min)
              + Linf_jump_min
    if(100>=Xnext[1] && Xnext[1]>=40){
      break}
  }

  repeat{ # K prior:  $K \sim U[0.1, 0.6]$ 
    Xnext[2] =      Xcurr[2]
              + runif(1, 0, 1) * (K_jump_max - K_jump_min)
              + K_jump_min
    if(0.6>=Xnext[2] && Xnext[2]>=0.1){
      break}
  }
```



# evaluate the ratio

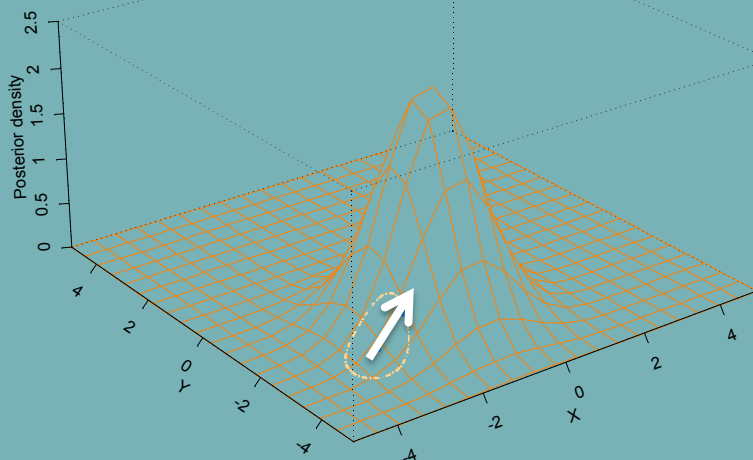
```
Fnext <- -1 * lognormal_like(Linf = Xnext[1], K = Xnext[2])$neg_likelihood
```

```
Rand1 <- log(runif(1,0,1))
```

```
if (Fnext > Fcurr+Rand1)
```

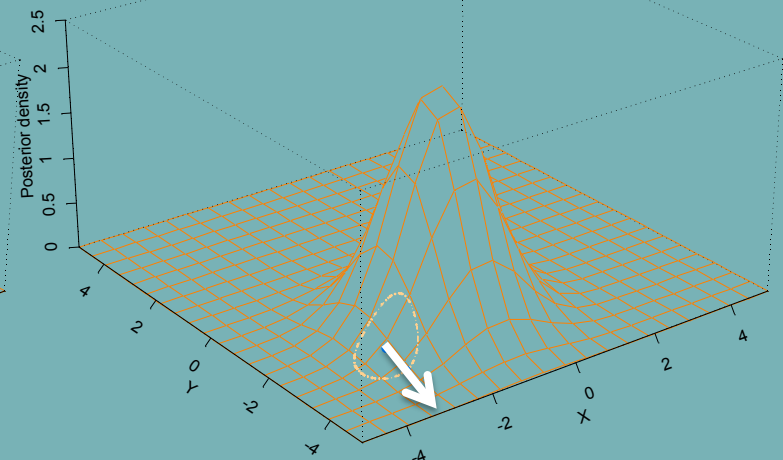
```
{Fcurr <- Fnext; Xcurr <- Xnext}
```

$$F_{\text{next}} / F_{\text{curr}} = r$$



$$r \geq 1$$

Accept the new point



$$r < 1$$

Accept the new point  
with probability  $r$

```

if (lsim %% Nthin == 0)  # thinning
{
  lpnt <- lpnt + 1

  if (lpnt > Nburn)  # burn in
  {
    lcnt <- lcnt + 1
    Outs2[lcnt, ] <- c(Xcurr, Fcurr)
  }
}

```

```

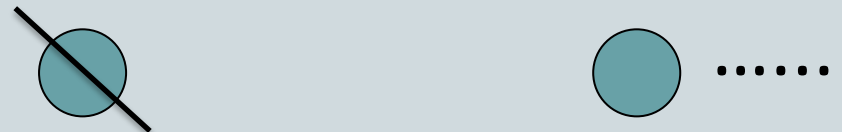
}
return(Outs2[1:lcnt,])
}

```

Nthin = 5



Nburn = 1





4

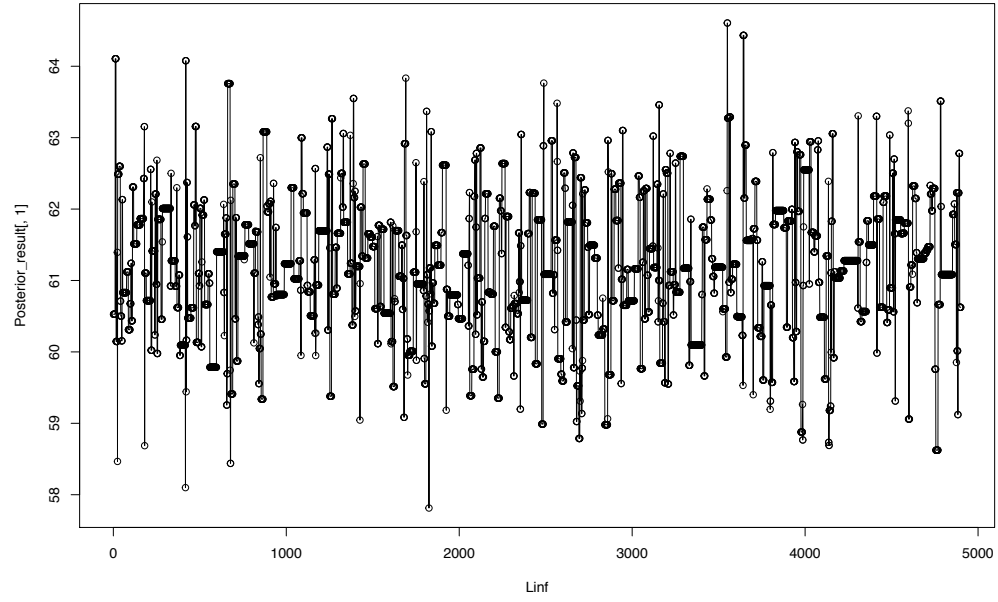
**Results**

```
Posterior_result <- DoMCMC( Xinit = c(100, 0.1),  
                             Ndim = 2,  
                             Nsim = 50000,  
                             Nburn = 100,  
                             Nthin = 10)
```

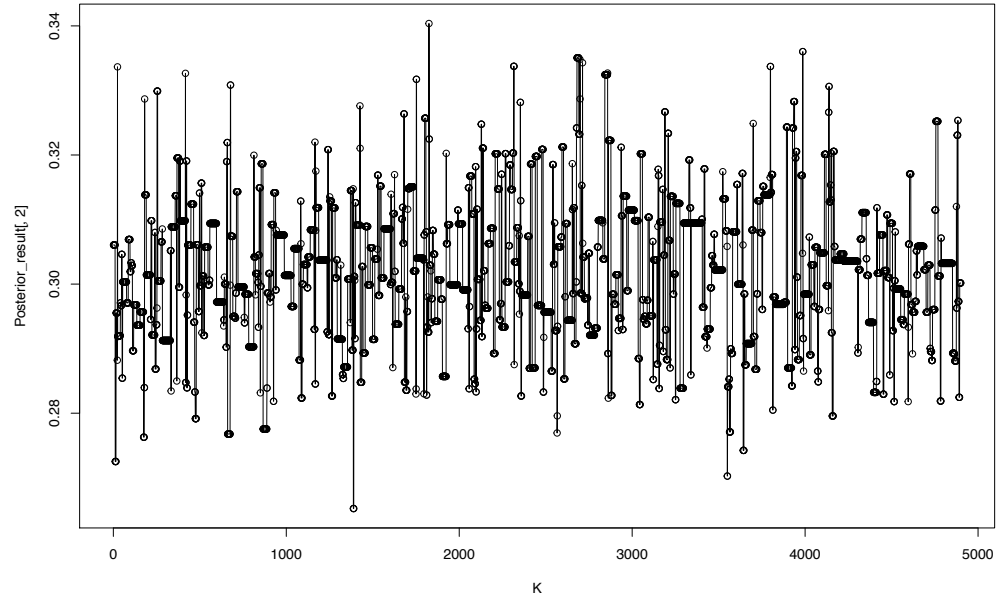
```
plot(Posterior_result[,1],main="",xlab="Linf",type="o")
```

```
hist(Posterior_result[,1], main="", xlab="Linf", col="gray",  
     breaks = seq(min(Posterior_result[,1]), max(Posterior_result[,1]),  
                   length.out = 1000))  
abline(v=median(Posterior_result[,1]), col = "red")
```

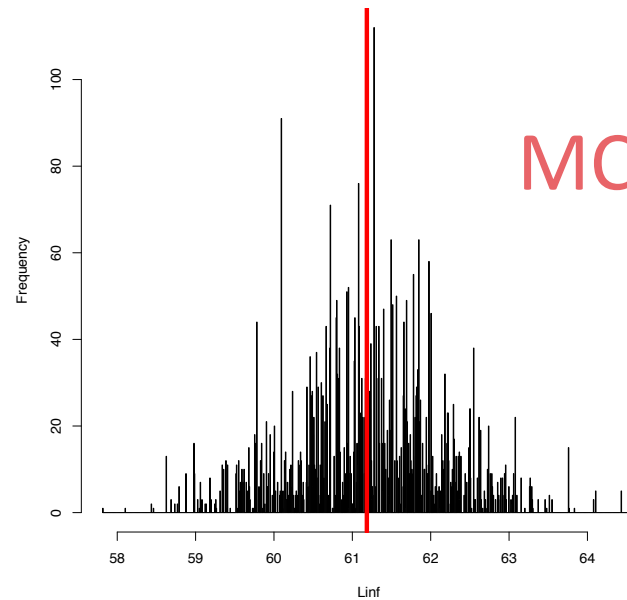
# Linf



# K



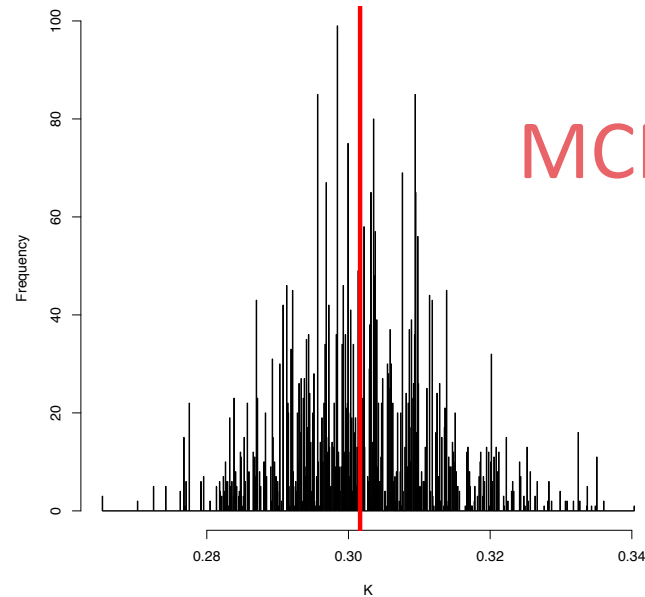
# Linf



MCMC Medium = 61.13

MLE results = 61.09

# K



MCMC Medium = 0.30

MLE results = 0.30

M C M C

Thank you