

④ (1)

$$S = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}} = \sqrt{\frac{284 - 5 \times 4.33^2}{5}}$$

$$= \sqrt{\frac{12.38}{5}}$$

$$= \sqrt{2.476}$$

$$= 1.573$$

(2)

$$1 - \alpha = 0.9 \quad \alpha = 0.05 \quad n = 5$$

$$\chi^2_{\frac{\alpha}{2}}(n-1) = \chi^2_{0.025}(5) = 11.07$$

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$$\chi^2_{1-\alpha}(n-1) = \chi^2_{0.95}(5) = 1.15$$

$$\sqrt{\frac{(n-1)S^2}{\chi^2_{\frac{\alpha}{2}}(n-1)}} \leq \sqrt{\frac{(n-1)S^2}{\chi^2_{1-\alpha}(n-1)}}$$

$$= \left(\sqrt{\frac{5 \times 10.38}{11.07}}, \sqrt{\frac{5 \times 10.38}{1.15}} \right)$$

$$= (2.17, 6.12)$$

$$\textcircled{50} \quad \left(\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2} \right)^2$$

$$(1) \quad V = \frac{\left(\frac{S_1^2}{n_1} \right)^2}{(n_1-1)} + \frac{\left(\frac{S_2^2}{n_2} \right)^2}{(n_2-1)}$$

$$n_1 = 9 \quad \bar{x} = 7.67 \quad S_1 = 9.27$$

$$n_2 = 9 \quad \bar{y} = 6.78 \quad S_2 = 21.15$$

$$V = \frac{\left(\frac{9.27^2}{9} + \frac{21.15^2}{9} \right)^2}{\frac{9.27^2}{8} + \frac{21.15^2}{8}} = 10.96 \approx 11$$

$$(\bar{x} - \bar{y}) \pm t_{\frac{\alpha}{2}}(v) \sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}$$

$$= 7.67 - 6.78 \pm t_{0.025}(11) \sqrt{\frac{9.27^2}{9} + \frac{21.15^2}{9}}$$

$$= 0.89 \pm 2.201 \times 7.70$$

$$= 0.89 \pm 16.95$$