

Algorithms Lab HS21
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cadmo.ethz.ch/education/lectures/HS21/algolab

Exercise - From Russia with Love

On the way from Istanbul to Trieste, the evil SPECTRE agent Grant has infiltrated the train. His goal is brutal: he has orders to assassinate James Bond. Fortunately, our hero is not an easy target. The two have clashed in one of the sleeping cars, and during their fight Bond used his suitcase to fend off Grant. Now the suitcase is broken and all its contents are scattered on the floor. The fight continues in the restaurant car...

In the meantime, passengers p_0, \ldots, p_{m-1} have come to the sleeping car to see what all the noise is about. They find traces of a fight and, interestingly, n coins on the floor. Quickly they realize that these coins are old British sovereigns, which are quite valuable. (Probably Bond brought them to use as a bribe.) The passengers decide to split the sovereigns among them before Bond and Grant return. They plan to use the following splitting procedure.

All sovereigns are placed on a straight line so that they appear as s_0, \ldots, s_{n-1} from left to right. For every sovereign s_i they know its value x_i in pounds. Now p_0 starts and picks either the leftmost (s_0) or the rightmost sovereign (s_{n-1}) and adds it to her pile. Then p_1 does the same on the remaining line of sovereigns. If p_0 picked s_0 , then p_1 has the choice between s_1 and s_{n-1} . Otherwise, p_0 picked s_{n-1} , which leaves p_1 the choice between s_0 and s_{n-2} . Then p_2, \ldots, p_{m-1} continue in the same fashion. After p_{m-1} takes a sovereign, it is again p_0 's turn and the whole procedure repeats until there are no more sovereigns left. The winnings of a passenger are the sum of values of all sovereigns in her pile at the end of the procedure.

Given an integer $k \in \{0, ..., m-1\}$, you have to find the largest possible winnings that passenger p_k can collect regardless of how other passengers play. Notice that the word 'regardless' implies that you cannot make any assumption of what the other passengers do. In particular, they may not play to maximise their own winnings.

Input The first line of the input contains the number $t \le 30$ of test cases. Each of the t test cases is described as follows.

- It starts with a line that contains three integers n m k, separated by a space. They denote
 - n, the number of sovereigns $(1 \le n \le 10^3)$;
 - m, the number of passengers $(1 \le m \le 5 \cdot 10^2)$;
 - k, the index of the passenger whose winnings you are interested in $(0 \le k \le m-1)$.
- The following line defines the value of the sovereigns in pounds. It contains n integers $x_0 \ldots x_{n-1}$, separated by a space, and such that $0 \le x_i \le 2^{10}$, for $i \in \{0, \ldots, n-1\}$.

Output For each test case the corresponding output appears on a separate line. It consists of one integer w which denotes the largest winnings that passenger p_k can collect, regardless of how other passengers play.

Points There are three groups of test sets, worth 100 points in total.

- 1. For the first group of test sets, worth 20 points, and the corresponding hidden test sets, worth 5 points, you may assume that there are exactly two passengers p_0 and p_1 and you are interested in the winnings of p_1 (m = 2 and k = 1).
- 2. For the second group of test sets, worth 40 points, and the corresponding hidden test sets, worth 10 points, you may assume that there are no more than three passengers and you are interested in the winnings of the last passenger ($m \le 3$ and k = m 1).
- 3. For the third group of test sets, worth 20 points, and the corresponding hidden test sets, worth 5 points, there are no additional assumptions.

Corresponding sample test sets are contained in testi.in/out, for $i \in \{1, 2, 3\}$.

Sample Input 3 5 2 1

3 5 2 1 1 3 2 5 4 5 3 2 1 1 8 5 5 7 3 1 100 100 1 1 8 5 5 8 5 105

Sample Output