

A.

$$x + 2y = 11$$

B.

$$4x + y = 2$$

C.

$$5x + 10y = 55$$

D.

$$y = 2 - 4x$$

E.

$$2x + \frac{1}{2}y = 1$$

F.

$$x + 2y - 11 = 0$$

G.

$$\begin{aligned} -x + 4y &= 1 \\ 2x + y &= 7 \end{aligned}$$

H.

$$\begin{aligned} x + y &= 12 \\ 3x - 5y &= 4 \end{aligned}$$

I.

$$\begin{aligned} 4x - 4y &= 44 \\ 6x + 3y &= 12 \end{aligned}$$

J.

$$\begin{aligned} 4y &= 4 - 2x \\ x + 5y &= -7 \end{aligned}$$

K.

$$\begin{aligned} \frac{1}{3}x + 2y &= 4 \\ x + y &= -3 \end{aligned}$$

L.

$$\begin{aligned} 4x + 2y &= 8 \\ 5x &= 5y + 55 \end{aligned}$$

Warm-Up

- Sort the cards A–F into groups of equivalent equations.
- Choose one card. Write a new equivalent equation that would belong in that group.

_____ is equivalent to _____ because . . .

Activity 1: First Steps of Elimination

Caasi and Diego are trying to solve this system of equations.

- What was Caasi's first step?
- Caasi got stuck. Why do you think she got stuck?
- What was Diego's first step?
- Finish Diego's work to solve the system.

<p>Caasi's Work</p> $\begin{array}{r} x + 2y = 11 \\ -(4x + y = 2) \\ \hline -3x + y = 9 \end{array}$
<p>Diego's Work</p> $\begin{array}{l} x + 2y = 11 \\ 4x + y = 2 \end{array} \rightarrow \begin{array}{l} x + 2y = 11 \\ 8x + 2y = 4 \end{array}$

- Diego says: $8x + 2y = 4$ is equivalent to $4x + y = 2$. This means the solution to the system is the same.

Explain what Diego means in your own words.

- What might be Diego's first step in solving this system?

$$\begin{array}{l} -5x + y = 7 \\ x - 4y = -9 \end{array}$$



Unit A1.5, Lesson 3: Process of Elimination

Name _____

Activity 2: More Than One Way?

Caasi and Kwabena started solving this system in different ways.

$$4x - y = 5$$

With a partner, solve the system both ways. Compare your solutions.

$$x + 2y = 8$$

Caasi: *Multiply the first equation by 2.*

Kwabena: *Multiply the second equation by -4 .*

Activity 3: Prepare to Be Eliminated

Instructions for Each Round

1. Select a card from G–L. Discuss two possible first steps you could take to solve the system.
2. Solve your system individually. Choose a different first step from your partner.
3. Compare your solutions and support each other to make adjustments as needed.

Round 1, Card _____

Equation 1: _____

Equation 2: _____

Solution: $x =$ _____ and $y =$ _____

Round 2, Card _____

Equation 1: _____

Equation 2: _____

Solution: $x =$ _____ and $y =$ _____

Round 3, Card _____

Equation 1: _____

Equation 2: _____

Solution: $x =$ _____ and $y =$ _____

Explore

The solution to this system of equations is $x = 5$ and $y = 2$.

What are possible values for A and B ?

$$Ax - By = 24$$

$$Ax + By = 16$$



Unit A1.5, Lesson 3: Process of Elimination

Name _____

Lesson Synthesis

Describe how writing equivalent equations can help you solve systems of equations.

$$x + 3y = 6$$

$$2x + y = 7$$

Use this system if it helps you explain your thinking.

Cool-Down

Solve this system of equations:

$$2x - y = 1$$

$$-x + 5y = -5$$

Line Zapper #1

$$3x + 4y = 3$$

$$-3x + 3y = 18$$

Line Zapper #2

$$y = 2x - 4$$

$$y = 0.5x + 5$$

Line Zapper #3

$$y = 3x + 6$$

$$2x + 2y = 20$$

$$x - y = 10$$



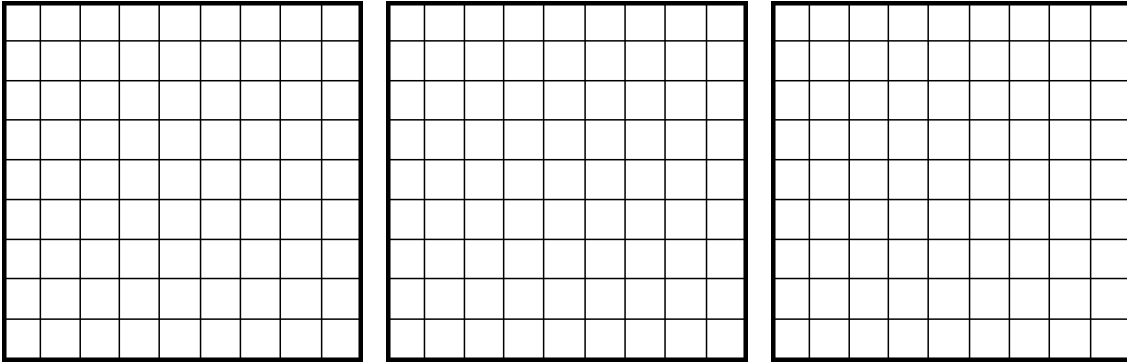
Repeated Challenges

Use additional paper as needed.

Cool-Down

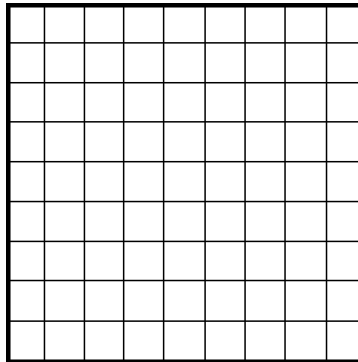
Your Pattern: Part 1

1. Draw your pattern in the space below.



2. Describe what about your pattern is changing and what is staying the same.

3. Draw the pattern for when $s = 4$.



4. How many tiles will there be when $s = 10$? Draw a picture if it helps with your thinking.

Your Pattern: Part 2

1. Write an equation that represents your pattern.
2. Explain how you see each term of your equation represented in the pattern.
3. How many tiles will there be when $s = 15$? Show or explain your thinking.

Gallery Walk

<p>1. What features of your classmates' work helped you understand their thinking?</p>	<p>2. Now that you've seen the work of other groups, what would you have done differently if you had more time?</p>
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Tables

Screens 4 and 5

[illegible]

Screen 6

[illegible]

Screen 9

[illegible]

Screen 10

[illegible]

Screen 11

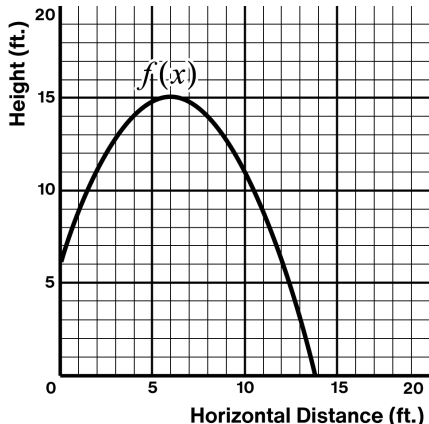
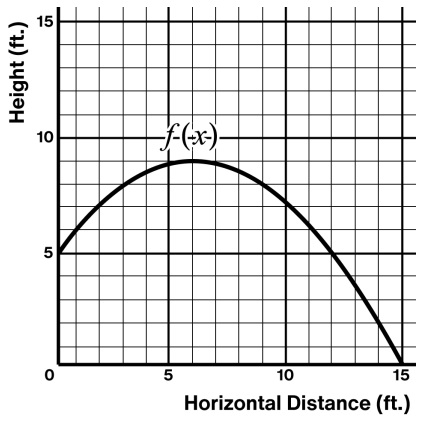
[illegible]

<p>The ball hits the ground 15 feet from where it is launched.</p>	<p>The maximum height of the ball is 15 feet.</p>	<p>Vertex at (3, 13)</p>
<p>The range of this graph is $0 \leq y \leq 15$.</p>	<p>$f(2) = 12$</p>	<p>y-intercept at (0, 15)</p>

<p>The ball hits the ground 15 feet from where it is launched.</p>	<p>The maximum height of the ball is 15 feet.</p>	<p>Vertex at (3, 13)</p>
<p>The range of this graph is $0 \leq y \leq 15$.</p>	<p>$f(2) = 12$</p>	<p>y-intercept at (0, 15)</p>

Activity 1: Ball Launch

1. Match the cards to the graphs and table. One card will not match because it has an error.

Graph or Table	Card #1	Card #2												
														
<table><tr><th>Horizontal Distance (ft.)</th><th>Height (ft.)</th></tr><tr><td>0</td><td>4</td></tr><tr><td>1</td><td>9</td></tr><tr><td>2</td><td>12</td></tr><tr><td>3</td><td>13</td></tr><tr><td>4</td><td>12</td></tr></table>	Horizontal Distance (ft.)	Height (ft.)	0	4	1	9	2	12	3	13	4	12		
Horizontal Distance (ft.)	Height (ft.)													
0	4													
1	9													
2	12													
3	13													
4	12													
														

2. Fix the card with the error so that each table or graph has two matching cards.
Discuss your thinking with a partner.

Activity 2: The Best Robot

Here is information about each robot’s ball launches.

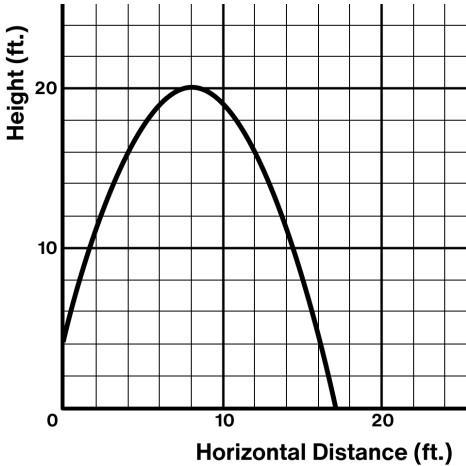
Robot A

Horizontal Distance (ft.)	Height (ft.)
0	5
1	12
2	17
3	20

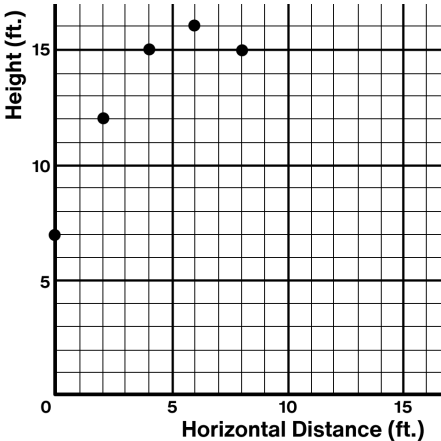
Robot B

The height of the ball can be modeled by $f(x) = 4 - x^2$, where x is the horizontal distance the ball has traveled.

Robot C



Robot D



Workspace for deciding which robots get each award:

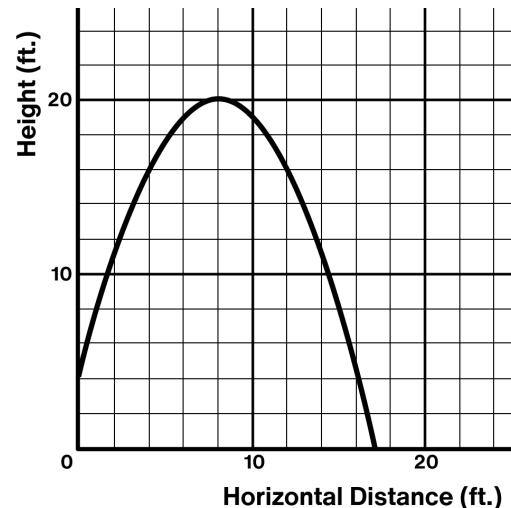
Awards: Give out as many of these awards as you want.

Highest Launch	Farthest Launch	Cutest Robot	Strongest Robot

Lesson Synthesis

How do the features of a parabola help you describe the motion of a ball?

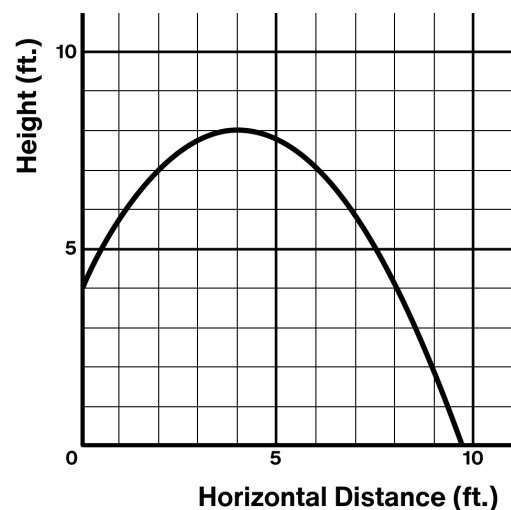
Use this parabola if it helps you to explain your thinking.



Cool-Down

The graph shows the height of a ball after it is launched.

- 1.1 Mark and label the vertex of this parabola.
- 1.2 What does the vertex tell you about the movement of the ball?
- 2.1 Mark and label the x -intercept(s) of this parabola.
- 2.2 What do the x -intercept(s) tell you about the movement of the ball?



Warm-Up

Match each expression in factored form with its equivalent expression in standard form.

Factored Form	Standard Form
1. $(5x + 6)(x - 3)$ _____	A. $5x^2 + 43x - 18$
2. $(5x - 3)(x + 6)$ _____	B. $5x^2 - 9x - 18$
3. $(5x - 2)(x + 9)$ _____	C. $5x^2 - 43x - 18$
4. $(5x + 2)(x - 9)$ _____	D. $5x^2 + 27x - 18$

Activity 1: Diagram Puzzles

Complete each diagram puzzle, standard-form expression, and factored-form expression.

	Diagram	Standard Form	Factored Form
1	<div><div><div>3x</div><div>-5</div></div><div><div>4x</div><div><div></div><div></div></div></div><div><div>-9x</div><div>15</div></div></div>	<div><div>_____</div><div>_____</div><div>+ 15</div></div>	<div><div>$(3x - 5)(4x$</div><div>_____)</div></div>
2	<div><div><div>2x</div><div>3</div></div><div><div>4x²</div><div>6x</div></div></div> <div><div></div><div>-9</div></div>	<div><div>4x²</div><div>_____</div></div>	<div><div>$(2x + 3)($</div><div>_____)</div></div>
3	<div><div><div></div><div>-3</div></div><div><div>2x²</div><div>-3x</div></div></div> <div><div>8x</div><div></div></div>	<div><div>2x² + 5x</div><div>_____</div></div>	

	Diagram	Standard Form	Factored Form						
4	<table><tr><td>$3x^2$</td><td>$4x$</td></tr><tr><td>$15x$</td><td>20</td></tr></table>	$3x^2$	$4x$	$15x$	20				
$3x^2$	$4x$								
$15x$	20								
5	<table><tr><td colspan="2">x</td></tr><tr><td>x</td><td>x^2</td></tr><tr><td></td><td>-10</td></tr></table>	x		x	x^2		-10	$x^2 - 3x - 10$	
x									
x	x^2								
	-10								
6	<table><tr><td>$3x^2$</td><td></td></tr><tr><td></td><td>1</td></tr></table>	$3x^2$			1	$3x^2 + 4x + 1$			
$3x^2$									
	1								
7	<table><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table>					$x^2 + 9x + 20$			
8	<table><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table>					$6x^2 + 7x + 2$			

Activity 2: Next Steps

Tameeka is trying to factor $2x^2 + 9x + 7$.

1. Discuss with a partner:

- How can you tell Tameeka's work is incorrect?
- What did Tameeka do well?
- What could she try next?

	$2x$	1
x	$2x^2$	x
7	$14x$	7

Sneha is trying to factor $2x^2 + 23x - 12$. She started by creating this diagram.

2.1 List pairs of constants Sneha could try in order to complete the outside of the diagram.

	$2x$	$-$
x	$2x^2$	
$-$		-12

Sneha tried the numbers -6 and 2 .

2.2 Discuss with a partner:

- How can you tell Sneha's work is incorrect?
- What did Sneha do well?
- What could she try next?

	$2x$	(2)
x	$2x^2$	$2x$
(-6)	$-12x$	-12

2.3 Rewrite $2x^2 + 23x - 12$ in factored form.

Use the diagram supplement if it helps with your thinking.

Ariana is trying to factor $10x^2 - 7x - 12$. She starts by creating this diagram.

3.1 Ariana says: *I have to use factors of 10. I also need to use factors of -12.*

What do you think she means?

$10x^2$	
	-12

3.2 Rewrite $10x^2 - 7x - 12$ in factored form.

Here are three other expressions with a c -value of -12 . Rewrite each expression in factored form.

4.1 $x^2 + x - 12$

4.2 $3x^2 - 16x - 12$

4.3 $6x^2 - 1x - 12$



Unit A1.8, Lesson 3: X-Factor

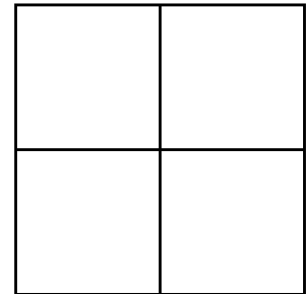
Name _____

Lesson Synthesis

Describe how to rewrite a standard-form expression in factored form.

Use the example if it helps with your thinking.

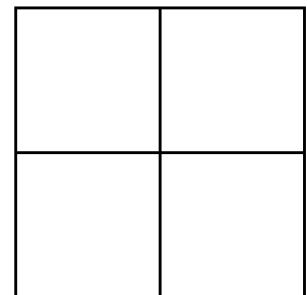
$$5x^2 - 31x - 28$$



Cool-Down

Rewrite $x^2 + 3x - 28$ in factored form.

Use the diagram if it helps with your thinking.



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Unit A1.8, Lesson 4: Form Up

A $x^2 + 5x - 6$	I $x^2 - 15x + 56$	Q $x^2 - 6x - 40$
B $x^2 + 3x - 10$	J $x^2 + 18x + 80$	R $x^2 + 11x + 18$
C $4x^2 - 8x - 5$	K $4x^2 + 13x + 10$	S $3x^2 + 13x + 12$
D $2x^2 - 13x - 24$	L $3x^2 + 8x - 16$	T $2x^2 + 15x + 18$

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Unit A1.8, Lesson 4: Form Up

E

$$100x^2 - 9$$

M

$$25x^2 - 64$$

U

$$x^2 - 36$$

F

$$9x^2 - 1$$

N

$$x^2 - 16$$

V

$$x^2 - 4$$

G

$$-2x^2 + 2x + 4$$

O

$$-6x^2 + 21x$$

W

$$15x^2 - 5x - 20$$

H

$$6x^2 - 6x - 36$$

P

$$5x^2 - 15x - 20$$

X

$$10x^2 - 60x + 80$$

Activity 1: Spotting Similarities

Here are three groups of expressions.

Group 1	Group 2	Group 3
$4x^2 - 25$	$8x^2 + 32x + 24$	$x^2 - 6x - 27$
$x^2 - 36$	$4x^2 - 8x - 32$	$x^2 + 2x - 80$
$x^2 - 100$	$10x^2 + 20x + 10$	$x^2 - 13x + 30$
$25x^2 - 49$	$2x^2 - 22x + 60$	$x^2 + 2x - 63$

1. Explain how the expressions in each group are alike.

Group 1:

Group 2:

Group 3:

2. Factor one expression from each group.

Group 1:

Group 2:

Group 3:

Deiondre factored the expression $7x^2 + 28x + 21$.

3.1 Discuss with a classmate:

- Are $7x^2 + 28x + 21$ and $7(x^2 + 4x + 3)$ equivalent? How do you know?
- Why might Deiondre have written $7(x^2 + 4x + 3)$ as a first step?

Deiondre's Work

$$\begin{aligned} 7x^2 + 28x + 21 \\ 7(x^2 + 4x + 3) \\ 7(x + 3)(x + 1) \end{aligned}$$

3.2 Does Deiondre's expression belong in group 1, 2, or 3? Explain your thinking.

Yasmine factored the expression $9x^2 - 49$.

4.1 Discuss with a classmate: Does Yasmine's expression belong in group 1, 2, or 3? Explain your thinking.

4.2 Write a new expression in standard form that belongs in the same group as Yasmine's.

Yasmine's Work

$$\begin{aligned} 9x^2 - 49 \\ 9x^2 + 0x - 49 \\ (3x - 7)(3x + 7) \end{aligned}$$

4.3 Factor the expression you wrote in problem 4.2.

Factor each expression.

5. $3x^2 - 6x - 105$

6. $16x^2 - 49$

7. $4x^2 + 52x + 120$

Name _____

Activity 2: Solve and Swap

1. Your teacher will give you a card. Factor the expression on your card.
2. Find a partner and swap cards. Factor your new expression and check with your partner.
3. Find a new partner and repeat step 2.

[illegible]



Unit A1.8, Lesson 4: Form Up

Name _____

Lesson Synthesis

What do you think is important to remember when factoring an expression in standard form?

Use the expressions if they help with your thinking.

$$5x^2 - 18x - 8$$

$$9x^2 - 16$$

$$6x^2 - 24x - 30$$

Cool-Down

Factor the expression $2x^2 - 8x - 10$.

Science Mom Lesson 83

STudent worksheet

Activity 2: Solution Search

Use screen 8 to guide your exploration of solutions to quadratic equations.

1.1 Here is an equation that has **two integer solutions**. Find two more equations.

Equation: $1x^2 - 5x + 6 = 0$ Solutions: $x = \frac{5 \pm \sqrt{1}}{2}$	Equation: Solutions:	Equation: Solutions:
--	---	---

1.2 Find three equations that have **one solution**.

Equation: Solutions:	Equation: Solutions:	Equation: Solutions:
---	---	---

1.3 Find three equations that have **no solutions**.

Equation: Solutions:	Equation: Solutions:	Equation: Solutions:
---	---	---

2. Examine the equations and solutions you found.
Discuss with your partner: *What patterns do you notice?*

Activity 1: Form Over Function

Here are four quadratic equations and their solutions.

Use the quadratic formula to show that the solutions are correct.

The Quadratic Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

1.1 $x^2 - 8x + 15 = 0$

$$x = \frac{-(-8) \pm \sqrt{(-8)^2 - 4(1)(15)}}{2(1)}$$

Solutions: $x = 5$ and $x = 3$

1.2 $x^2 + 10x + 18 = 0$

Solutions: $x = -5 \pm \frac{\sqrt{28}}{2}$

1.3 $9x^2 - 6x = -1$

Solution: $x = \frac{1}{3}$

1.4 $2x^2 + 6x + 5 = 0$

No solutions

- Discuss with a partner: *Do you think that the quadratic formula is the best strategy for solving each of these equations? Explain your thinking.*

Activity 2: Error Analysis

Your teacher will give you a supplement with the same equations from the previous activity. Each attempt to solve the equation contains an error.

1. With a partner:
 - Identify the error in each attempt. Then discuss or show how to correct the error.
 - Discuss why someone might make this error.
- 2.1 Solve the following equation using the quadratic formula, **but include an error that you think would be common.**

$$3x^2 - 6x - 1 = 0$$

- 2.2 Swap equations with a classmate. Identify and describe the error in each other's work.
- 3.1 Reflect: *What kinds of errors do you think you are most likely to make when using the quadratic formula?*
- 3.2 Write two pieces of advice that will help your future self correctly use the quadratic formula. Include examples if they help with your thinking.
 -
 -

**Lesson Synthesis**

What are some advantages of using the quadratic formula to solve quadratic equations?

What are some disadvantages?

Use the examples if they help with your thinking.

$$x^2 - 6x + 8 = 0$$

$$x^2 + 4x - 1 = 0$$

$$2x^2 + 7x - 10 = 0$$

Cool-Down**The Quadratic Formula**

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Use the quadratic formula to solve the equation $2x^2 + 5x - 12 = 0$.

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Unit A1.8, Lesson 14: Supplement

Name(s) _____

Error Analysis

1.1

$$x^2 - 8x + 15 = 0$$

$$a = 1, b = -8, c = 15$$

$$x = \frac{-(-8) \pm \sqrt{(-8)^2 - 4(1)(15)}}{2(1)}$$

$$x = \frac{8 \pm \sqrt{-64 - 60}}{2}$$

$$x = \frac{8 \pm \sqrt{-124}}{2}$$

No solutions

1.2

$$x^2 + 10x + 18 = 0$$

$$a = 1, b = 10, c = 18$$

$$x = \frac{-10 \pm \sqrt{10^2 - 4(1)(18)}}{2(1)}$$

$$x = \frac{-10 \pm \sqrt{100 - 72}}{2}$$

$$x = \frac{-10 \pm \sqrt{28}}{2}$$

$$x = -5 \pm \sqrt{14}$$



Unit A1.8, Lesson 14: Supplement

Name(s) _____

Error Analysis

1.3

$$9x^2 - 6x = -1$$

$$a = 9, b = -6, c = -1$$

$$x = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(9)(-1)}}{2(9)}$$

$$x = \frac{6 \pm \sqrt{36 + 36}}{18}$$

$$x = \frac{6 \pm \sqrt{72}}{18}$$

1.4

$$2x^2 + 6x + 5 = 0$$

$$a = 2, b = 6, c = 5$$

$$x = \frac{-6 \pm \sqrt{(6)^2 - 4(2)(5)}}{2(2)}$$

$$x = \frac{-6 \pm \sqrt{36 - 40}}{4}$$

$$x = \frac{-6 \pm \sqrt{-4}}{4}$$

$$x = \frac{-6 \pm 2}{4}$$

$$x = -2 \text{ and } x = -1$$

Shooting Stars #1

$$y = x^2 - 11$$

$$y = 5$$

Shooting Stars #2

$$y = x^2$$

$$y = -4x + 12$$

Shooting Stars #3

$$y = (x - 2)^2$$

$$y = x$$

Repeated Challenges

Use additional paper as needed.

Cool-Down